

1. Convert 892.035 into octal

$$\begin{array}{r} 8 \overline{) 892} \\ 8 \overline{) 111} - 4 \\ 8 \overline{) 13} - 7 \\ 1 - 5 \end{array}$$

$$0.035 \times 8 = 0.28 \quad 0$$

$$0.28 \times 8 = 2.24 \quad 2$$

$$0.24 \times 8 = 1.92 \quad 1$$

$$0.92 \times 8 = 7.36 \quad 7$$

$$(892.035)_{10} = (1574.0217)_8$$

2. Convert $A092$ into binary

$$\begin{array}{cccc} 10 & 0 & 9 & 2 \\ 1010 & 0000 & 1001 & 0010 \end{array}$$

$$(A092)_{16} = (1010000010010010)_2$$

3. Find 15's complement of $F9E7$

$$\begin{array}{cccc} 15 & 15 & 15 & 15 \\ 15 & 9 & 14 & 7 \\ \hline 0 & 6 & 1 & 8 \end{array}$$

$$15's \text{ complement of } F9E7 = (0618)_{16}$$

4. Find 6's complement of $(362)_7$

$$\begin{array}{ccc} 6 & 6 & 6 \\ 3 & 6 & 2 \\ \hline 3 & 0 & 4 \end{array}$$

$$6's \text{ complement of } (362)_7 = (304)_7$$

5. Subtract 25 and 37 using 2's complement

$$A: 25 \Rightarrow 010101$$

$$B: 37 \Rightarrow 100111 \Rightarrow 011000 \text{ (1's)}$$

$$\begin{array}{r} 1 \\ 011000 \\ \hline 011001 \text{ (2's)} \end{array}$$

$$0 \ 1 \ 0 \ 1 \ 0 \ 1$$

$$0 \ 1 \ 1 \ 0 \ 0 \ 1$$

$$1 \ 0 \ 1 \ 1 \ 1 \ 0 \Rightarrow 0 \ 1 \ 0 \ 0 \ 0 \ 1 \ (1'A)$$

$$\begin{array}{r} 1 \\ \hline 0 \ 1 \ 0 \ 0 \ 1 \ 0 \Rightarrow -22 \end{array}$$

$$25 - 37 = -22$$

6. Represent the following in POS and SOP form

$$Y = y + xz' \quad Z = (x+y') \cdot z \cdot (y+z)$$

$$Y = y(x+x')(z+z') + xz'(y+y')$$

$$Y = yx + yx'(z+z') + xyz' + xy'z'$$

$$Y = xyz + xyz' + x'yz + x'y'z' + xyz' + xy'z'$$

$$Y = xyz + xyz' + x'yz + x'y'z' + xy'z'$$

$$Y = \sum (2, 3, 4, 6, 7)$$

$$Y = \pi (0, 1, 5)$$

$$Z = (xz + xy'z)(y+z)$$

$$Z = xyz + xz + y'z$$

$$Z = xyz + xz(y+y') + y'z(x+x')$$

$$Z = xyz + xyz + xy'z + xy'z + x'y'z$$

$$Z = xyz + xy'z + x'y'z$$

$$Z = \sum (1, 5, 7)$$

$$Z = \pi (0, 2, 3, 4, 6)$$

7. Simplify the following Boolean expressions in algebraic form

$$M = abc + abc' + ab'c + a + bc' + a'b$$

$$M = ab(c + c') + ab'c + a + bc' + a'b$$

$$M = ab + ab'c + a + bc' + a'b$$

$$M = a(b + 1) + ab'c + bc' + a'b$$

$$M = a + ab'c + bc' + a'b$$

$$M = a(1 + b'c) + bc' + a'b$$

$$M = a + bc' + a'b$$

$$M = a + b + bc'$$

$$M = a + b(1 + c')$$

$$M = a + b$$

$$N = (a + d)(c' + a)(a' + b)$$

$$N = (ac' + a + c'd + ad)(a' + b)$$

$$N = (a(c' + 1) + c'd + ad)(a' + b)$$

$$N = (a + c'd + ad)(a' + b)$$

$$N = (a(1 + d) + c'd)(a' + b)$$

$$N = (a + c'd)(a + b)$$

$$N = ab + a'c'd + bc'd$$

9. Find dual and complement of $F = xy + z'w$

$$\text{dual of } F = (x + y)(z' + w)$$

$$F' = \overline{xy + z'w}$$

$$= (xy)' \cdot (z'w)'$$

$$F' = (x' + y')(z + w')$$

10. Represent the complement of the following Boolean expression in sum of min terms and product of maxterms form: $y'z' + x'$

$$F = y'z' + x'$$

$$F' = \overline{y'z' + x'}$$

$$= (y'z')' \cdot (x')'$$

$$F' = (y+z)(x)$$

$$F' = xy + xz$$

$$= xy(z+z') + xz(y+y')$$

$$F' = xyz + xyz' + xyz + xy'z$$

$$F' = xyz + xyz' + xy'z$$

$$F' = \sum (5, 6, 7)$$

$$F' = \pi (0, 1, 2, 3, 4)$$

$$F' = (x' + y' + z')(x' + y' + z)(x' + y + z')(x' + y + z)(x + y' + z')$$

8. Simplify using K-map

i) $F = \pi(0, 2, 3)$ and $d = \pi(1)$

		B	
A	\bar{B}	B	
\bar{A}	0	x	
	0	1	
A	0	0	
	2	3	

$$F =$$

ii) $Y = \pi(1, 3, 4, 5, 7)$ and $Y = \sum(0, 2, 6)$

		BC		
A	$\bar{B}\bar{C}$	$\bar{B}C$	BC	$B\bar{C}$
\bar{A}	1			1
	0	1	3	4
A				
	6	5	7	2

$$Y = \bar{A}\bar{C} + B\bar{C}$$

$$Y = \bar{C}(\bar{A} + B)$$

$$iii) \Sigma = \Pi(0, 1, 5, 7, 9, 10, 14, 15), d = \Pi(2, 8)$$

$$Y = \Sigma(2, 3, 4, 6, 8, 11, 12, 13), d = \Pi(2, 8)$$

AB \ CD				
	$\bar{C}\bar{D}$	$\bar{C}D$	CD	$C\bar{D}$
$\bar{A}\bar{B}$		1	1 ₃	X ₂
$\bar{A}B$	1 ₄	5	7	1 ₆
AB	1 ₁₂	1 ₁₃	15	14
$A\bar{B}$	X ₈	9	1 ₁₁	10

$$Y = \bar{B}C\bar{D} + \bar{A}C\bar{D} + B\bar{C}\bar{D} + AB\bar{C}$$

$$iv) M = \Sigma(1, 3)$$

A \ B	\bar{B}	B
\bar{A}	0	1 ₁
A	2	1 ₃

$$M = B$$

$$v) N = \Sigma(0, 2, 3, 7)$$

A \ B	$\bar{B}\bar{C}$	$\bar{B}C$	BC	$B\bar{C}$
\bar{A}	1 ₀	1	1 ₃	1 ₂
A		5	1 ₇	6

$$N = \bar{A}\bar{C} + BC$$

$$vi) T = \Sigma(0, 2, 3, 5, 9, 10, 12, 13, 15), d = \Sigma(7, 8)$$

AB \ CD				
	$\bar{C}\bar{D}$	$\bar{C}D$	CD	$C\bar{D}$
$\bar{A}\bar{B}$	1 ₀	1	1 ₃	1 ₂
$\bar{A}B$		1 ₅	X ₇	6
AB	1 ₁₂	1 ₁₃	1 ₁₅	14
$A\bar{B}$	X ₈	1 ₉	11	1 ₁₀

$$T = \bar{D}\bar{B} + BD + A\bar{C} + \bar{A}\bar{B}C$$