

$$1) \frac{x}{4} + 3 - \frac{x+3}{2} = 1$$

$$\frac{x}{4} + \frac{12}{4} - \frac{2x+6}{4} = \frac{4}{4}$$

$$x + 12 - 2x - 6 = 4$$

$$x + 2x = 4 - 12 + 6$$

$$3x = -2$$

$$\boxed{x = -\frac{2}{3}}$$

$$2) \frac{1}{8} (2x+4) - \frac{2}{3} (2x+6) + x = -4$$

$$\frac{2x+4}{8} - \frac{4x+12}{3} + x = 4$$

$$\frac{6x+12}{24} - \frac{12x+96}{24} + \frac{24x}{24} = \frac{96}{24}$$

$$6x + 12 - 12x - 96 + 24x = 96$$

$$6x - 12x + 24x = 96 + 96 - 12$$

$$18x = 180$$

$$x = \frac{180}{18}$$

$$\boxed{x = 10}$$

$$3) \frac{x-2}{3} - \frac{x-3}{2} = \frac{4-2x}{5}$$

$$\frac{10x-20}{30} - \frac{15x-45}{30} = \frac{24-12x}{30}$$

$$10x - 20 - 15x + 45 = 24 - 12x$$

$$10x - 15x + 12x = 24 + 20 - 45$$

$$7x = -3$$

$$\boxed{x = -\frac{3}{7}}$$

$$4) \quad \frac{3x+7}{2} - \frac{1-4x}{4} = \frac{1-x}{6} - \frac{9+x}{3}$$

$$m.c.m(2, 4, 6, 3) = 2^2 \cdot 3 = \underline{12}$$

$\downarrow \quad \downarrow$
 $2^2 \quad 2 \cdot 3$

$$\frac{18x+42}{12} - \frac{3-12x}{12} = \frac{2-x}{12} - \frac{36+4x}{12}$$

$$18x+42-3+12x = 2-x-36-4x$$

$$18x+12x+4x+x = 2-36-42+3$$

$$35x = -73$$

$$\boxed{x = -\frac{73}{35}}$$