Sorting and Searching

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Administrative Notes

Now, let’s talk about sorting lists of elements

All of our examples tonight use integers, but it all works the same way. As long as all elements in the list are of the same type, you can sort them into an order.

An easy one to understand - bubble sort.

Suppose you have a list of integers:

[4, -2, 19, 944, 27, 3]

You can go through the list and compare each pair of numbers. If the first one is larger than the second one, swap them.

When you have gone through the list one time, you will have “bubbled” the largest

Element up to the end of the list.

An example - first, on the slide; then some coding

Original list :[4, -2, 19, 944, 27, 3]

Bubble sort - “bubble” the largest number left each time to the end of the list

-2, 4, 19, 944, 27, 3

-2, 4, 19, 27, 944, 3

-2, 4, 19, 27, 3, 944

-2, 4, 19, 3, 27, 944

We can write bubble sort as an iterative function, or as a recursive one

```
def iterative_bubble_sort (numbers):
# go through the entire list of numbers
  for i in range(len(numbers)-1,0, -1):
    for j in range(i):
      if (numbers[j]>numbers[j+1]):
        #swap the numbers - we'll use a
temp
        temp = numbers[j]
        numbers[j] = numbers [j+1]
        numbers[j+1] = temp
  return(numbers)
```

Recursive Bubble Sort

```
def recursive_bubble_sort (numbers):
   if len(numbers) == 1:
      return(numbers)
   else:
      #bubble the largest number to the end
      for j in range(len(numbers)-1):
         if numbers[j] > numbers[j+1]:
            temp = numbers[j]
            numbers[j] = numbers[j+1]
            numbers[j+1] = temp
      #then recursively call the function with
      #all but the last element of the list
      new_nums = recursive_bubble_sort(numbers[:-1])
      #add the last element back on
      sorted_list = new_nums + numbers[-1:]
      return(sorted_list)
```

Stopping the sort

The list is sorted if there are no swaps made during a pass through the list

- Think about why

The previous code continues through even after the list is sorted.

We can be more efficient by converting the outer “for” loop into a “while” loop and using a boolean flag

- Let’s look at the code

Selection Sort

Now, a different type of sorting.

This time, we’re going to search through the entire list to find the smallest element, and then swap it with the first element in the list.

We then go through the rest of the list and select the smallest remaining element. We put this into the next available slot, and repeat until the list is sorted

We “select” the smallest element from the list, and thus this called a

...selection sort

Selection sort, on paper and as an iterative function

Original list :[4, -2, 19, 944, 27, 3]

-2, 4, 19, 944, 27, 3

-2, 3, 19, 944, 27, 4

-2, 3, 4, 944, 27, 19

-2, 3, 4, 19, 27, 944

```
def iterative_selection_sort(numbers):
  for i in range(len(numbers)):

  #find the smallest element remaining in the
  #unsorted list. Start by presuming it's the
  #first element
    smallest = i
    for j in range(i + 1, len(numbers)):
      if numbers[smallest] > numbers[j]:
        smallest = j

    # When the loop is done, we know that smallest is
    # the index of the smallest value. Swap it
    # with the first element
    temp = numbers[smallest]
    numbers[smallest] = numbers[i]
    numbers[i] = temp
```

Can we implement *this* as a recursive function?

```
def recursive_selection_sort (nums):
  #The base case is: a list of length 0 or 1 is sorted
  if len(nums) <= 1:
     return nums
  else:
     #the core of the algorithm is the same
     #as the iterative routine
     index_of_smallest = 0
     for j in range(1, len(nums)):
        if nums[j] < nums[index_of_smallest]:
           index_of_smallest = j
```

```
# now swap the smallest element found with the first
     temp = nums[0]
     nums[0] = nums[index_of_smallest]
     nums[index_of_smallest] = temp
    #now make the recursive call with the first
    #element stripped out
     r = recursive_selection_sort(nums[1:])
     results = nums[:1] + r
     return results
```

One more sorting algorithm: QuickSort

The idea here: pick an element in the list. Call this the “pivot”

Sort the list so that every item less than the pivot is before the pivot - “to the left of” the pivot, if you will

Every item greater than the pivot will be to the right - after the pivot in the list.

Note that there is no guarantee the items to the left and to the right of the pivot will be in any order at all.

So you have to recursively call the quicksort routine on the left side of the pivot, and then on the right.

Spoiler alert: this is called quicksort because it works faster than the other algorithms

A paper example before the code

Original list :[4, -2, 19, 944, 27, 3]

Less: -2, 3

Equal: 4

Greater: 19, 944, 27

Recursive call: Less; Greater

Quicksort code - this works best as a recursive function

```
def quicksort(list_of_nums):
   #base case - a list of length one is sorted
   if len(list_of_nums) <= 1:
      return(list_of_nums)
   #recursive case
   else:
      #pick a pivot - the first element
      pivot = list_of_nums[0]
      #define three empty lists, for elements greater than the pivot, less than the pivot, and equal to the pivot
      less = []
      equal = []
      greater =[]
```

Quicksort (continued)

```
# go through the list and put each element in the proper list
    for i in range(len(list_of_nums)):
        if list_of_nums[i] > pivot:
            greater.append(list_of_nums[i])
        elif list_of_nums[i] == pivot:
            equal.append(list_of_nums[i])
        else:
            less.append(list_of_nums[i])
    results = quicksort(less) + equal + quicksort(greater)
    return(results)
```

Searching - linear and binary

Linear search is what python uses as a default

Go through the list, one item at a time, in order from first element to last

Stop when you find the right element, or return failure if you never find it

It works, but it’s not efficient

Binary Search

If the list is already sorted, we can search much more efficiently.

Go to the middle element of the list. List [len(list)//2]

Is this greater than the element we're searching for? If it is, just look at the first half of the original list. If not, just look at the right half. If this element is exactly what we're looking for, stop.

So now we have a recursive call to a list half the size of the original list

We'll look at the code in a minute, but we'll find the element we're looking for, or find it isn't there, in log(base2) of the length of the original list operations.

Code for binary search

```
def binary_search (numbers, target):
    if len(numbers)//2 == 0:
        return -1
    if numbers[len(numbers)//2] == target:
        return len(numbers)//2
    elif numbers[len(numbers)//2] > target:
        return binary_search(numbers[:len(numbers)//2], target)
    else:
        return binary_search(numbers[len(numbers)//2:], target)
```