ciphart —

memory-hard key derivation with easier measurable security

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 $argon2^2$ is mostly nice, but trying to interpret its contribution to the protection against password brute-forcing attacks remains more difficult than it should be. this vagueness is a problem that is not limited to argon2, but also shared with every other key derivation function that i've known so far.

when one uses argon2, his derived key will surely have superior protection against password brute-forcing attacks, but by how much? to answer this, one would need to survey the industry that manufactures application-specific integrated circuits to obtain a map between time and money, in order to get an estimation on how much would it cost the adversary to discover the password in a given time window.

resolving this vagueness is not a mere luxury to have, but a necessity for maximising survival, because it hinders the process of studying the cost-value of memory-hard key derivation functions, which, effectively, increases the risk of having a false sense of security.

so i propose *ciphart* — a memory-hard key derivation function with a security contribution that is measured in a unit that i call *relative entropy bits*. this unit is measured objectively and is guaranteed to be true irrespective of whatever alien technology that the adversary might have.

libciphart³ is a library that implements *ciphart* very closely to this paper, without much fluff. this should make integrating *ciphart* into other systems more convenient.

ciphart⁴ is an application for encrypting and decrypting files that makes use of libciphart. this application is intended for use by end-users or scripts, henceforth it has some fluff to treat mankind with dignity.

1 ciphart

1.1 parameters

enc encryption function.

p password.

s salt.

L number of memory lanes for concurrency.

M total memory in bytes.

T number of tasks per lane segment.

R number of rounds per task.

B added security in relative entropy bits.

 K_{out} output key size in bytes.

1.2 internal variables

 $C \qquad \leftarrow \begin{cases} 64 \text{ bytes} & \text{if enc is } xchacha20\\ 16 \text{ bytes} & \text{if enc is } aes\\ \dots \end{cases}$

this to reflect the block size of the encryption algorithm that's going to use *ciphart*'s generated key to encrypt data.

$$K_{\rm in} \leftarrow \begin{cases} 32 \text{ bytes} & \text{if enc is } xchacha20\\ 16 \text{ bytes} & \text{if enc is } aes-128\\ \dots \end{cases}$$

this is the size of the encryption key that's used to solve ciphart's tasks. this is different than the enc-independent K_{out} which is possibly used by other encryption algorithms in later stages⁵.

 \hat{T} $\leftarrow T - (T \mod 2) + 2$. this is to ensure that it is in multiples of 2. why? because we need a buffer for storing the clear-text and another for storing the output cipher-text.

 $\hat{M} \leftarrow M - (M \mod C\hat{T}L) + C\hat{T}L$. this is to ensure that it is in multiples of $C\hat{T}L$. why? so that all segments are of equal lengths in order to simplify *ciphart*'s logic. e.g. it wouldn't be nice if the last segments were of unequal sizes.

 $G \leftarrow \hat{M}C^{-1}\hat{T}^{-1}L^{-1}$. total number of segments per

 \hat{B} $\leftarrow \max(\log_2(\hat{M}C^{-1}R), B)$. this is to ensure that \hat{B} is large enough to have at least one pass over the \hat{M} -bytes memory.

 \hat{B} $\leftarrow \log_2(2^{\hat{B}} - (2^{\hat{B}} \mod L\hat{T}R) + L\hat{T}R)$. this is just to reflect the reality with *ciphart* that segments must complete. i.e. when the user asks for B relative entropy bits, he gets \hat{B} instead, where $\hat{B} > B$. more details on this later.

 m_i C-bytes memory for i^{th} task in the \hat{M} -bytes pad.

 $n_l \leftarrow l\hat{T}R$. nonce variable for l^{th} lane with at least 64 bits.

 $f \leftarrow 0$. a flag indicating whether the \hat{M} -bytes pad is filled.

1.3 output

k K-bytes key with $\geq B$ relative entropy bits.

1.4 steps

shown in algorithm 1.

2 parallelism

since iterations of the loop in line 3 in algorithm 1 are fully independent of one other, they can quite happily utilise L cpu cores, specially when segment sizes, T, are larger.

other lines are not easily independent, so i didn't even bother to try to parallelise them. specially since this is

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²https://github.com/P-H-C/phc-winner-argon2

³https://github.com/Al-Caveman/libciphart

⁴https://github.com/Al-Caveman/ciphart

⁵at the expense of losing the meaning of relative entropy bits.

algorithm 1: ciphart version 6

```
1 while 1 do
        for q = 0, 1, ..., G - 1 do
 2
             for l = 0, 1, ..., L - 1 do
 3
                  for t = 0, 1, ..., T - 1 do
 4
                      for r = 0, 1, ..., R - 1 do
 5
                           i \leftarrow qT + t;
  6
                           if t = 0 then
                               j \leftarrow i + T - 1;
  8
                           else if t = T - 1 then
  9
                                j \leftarrow i + 1 - T;
10
                           else
11
                             j \leftarrow i+1;
12
                           m_i \leftarrow \text{enc}(m_i, n_l, k);
13
                           n_l \leftarrow n_l + 1;
14
                           k \leftarrow f(m_j, p, l, s, t);
15
             if f and \log_2(n_1L) \geq B then
16
                 go to line 19;
17
        f \leftarrow 1;
18
    while 1 do
19
        for l = 1, 2, ..., L do
20
             if len(k) \ge K then return k[0:K];
21
             n \leftarrow n + 1;
\mathbf{22}
             k \leftarrow k \parallel \operatorname{enc}(m_{l,S,T}[1], n, k);
23
```

- 3 memory-hardness
- 4 security interpretation
- 5 comparison
- 6 summary

not a problem, since the cpu-heavy part is in in the easilyparalleliseable part.

with argon2, if one wants to increase the cpu load without increasing memory pad's use, one can increase the number of passes over the pad. this feature is supported by ciphart via the relative entropy bits parameter B.

but, simply increasing number of passes on the pad may not be the best option for all cases. e.g. what if someone has a small pad, and small segments? in such case, a higher percentage of the cpu will be wasted in the nonparalleliseable steps, which is a waste.

this is why *ciphart* has an additional parameter R. this parameter can allow to increase the load on the cpu without even requiring to go through the non-paralleliseable steps. argon2 lacks this parameter. this is not the main reason *ciphart* was made, but it's one of the incremental improvements.

one could philosophically argue that argon2 has the R parameter, except that it always assumes that R = 1. i don't agree with this assumption, which is why i made ciphart to allows the user to set R more flexibly.