key derivation with easier measurable security

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January 8, 2021

 ${\rm hi-i}$ propose ciphart, a memory-hard key derivation function that has a security gain that's measurable more objectively and more conveniently than anything in class known to date.

to nail this goal, ciphart's security gain is measured in the unit of relative entropy bits. relative to what? relative to the encryption algorithm that's used later on. therefore, this relative entropy bits measure is guaranteed to be true when the encryption algorithm that's used with ciphart is also the same one that's used to encrypt the data afterwards.

my reference implementation is available here¹.

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1 ciphart

parameters:

W each task's size, at least 32 bytes. M total memory in multiples of 2W.

R number of rounds per task.

B added security in relative entropy bits.

enc encryption function.

k initial key.

input:

 $\begin{array}{ll} T & \leftarrow M/W \\ P & \leftarrow \max(2, \lceil 2^B/(TR) \rceil) \\ m_{l,s,t} & \text{memory for t^{th} task, in s^{th} segment, in l^{th}} \\ & \text{lane to work on.} \end{array}$

 $n \leftarrow 0$, a variable with enough bytes to store nonces in. n[0] means first 64 bits. n[1] means second 64 bits.

output:

 \hat{k} better key, with B, or more, relative entropy bits.

steps:

1

 $\mathbf{2}$

 $\mathbf{2}$

 $\mathbf{2}$

 $\mathbf{2}$

 $\mathbf{2}$

1 while true do

```
for s = 1, 2, ..., S do
              for l = 1, 2, ..., L do
 3
                   for t = 1, 2, ..., T do
 4
                        for r = 1, 2, ..., R do
 5
                             if t = 1 then
 6
                                 m_{l,s,t} \leftarrow \operatorname{enc}(m_{l,s,T}, n, k);
 8
                              m_{l,s,t} \leftarrow \operatorname{enc}(m_{l,s,t-1}, n, k);
                             n[1] \leftarrow n[1] + 1;
10
                             k \leftarrow f(m_{l,s,t}[-64:], p, l, s, t);
11
              if \log_2(n[0] \times SLTR + n[1]) \ge B then
12
               go to step 15;
13
        n[0] \leftarrow n[0] + 1;
14
15 while true do
         n[0] \leftarrow n[0] + 1;
16
         for l = 1, 2, ..., L do
17
              if len(\hat{k}) \geq K then
18
               return \hat{k}[0:K]
19
              \hat{k} \leftarrow \hat{k} \parallel \operatorname{enc}(m_{l,S,T}[1], n, k);
20
              n[1] \leftarrow n[1] + 1;
```

 $^{^{1} \}verb|https://github.com/Al-Caveman/ciphart|$

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