- ciphart ——

memory-hard key derivation with easier measurable security caveman¹ January 10, 2021

 $argon2^2$ is mostly nice, but trying to interpret its contribution to the protection against password brute-forcing attacks remains more difficult than it should be. this vagueness is a problem that is not limited to argon2, but also shared with every other key derivation function that i've known so far.

when one uses argon2, his derived key will surely have superior protection against password brute-forcing attacks, but by how much? to answer this, one would need to survey the industry that manufactures application-specific integrated circuits to obtain a map between time and money. the centre of my thesis is that this part is not nice, because i found that life can be easier.

resolving this vagueness is not a mere luxury to have, but a necessity for maximising survival, because it hinders the process of studying the cost-value of memory-hard key derivation functions, which, effectively, increases the risk of having a false sense of security.

so i propose *ciphart* — a memory-hard key derivation function with a security contribution that is measured in a unit that i call *relative entropy bits*. this unit is measured objectively and is guaranteed to be true irrespective of whatever alien technology that the adversary might have.

libciphart³ is a library that implements *ciphart* very closely to this paper, without much fluff. this should make integrating *ciphart* into other systems more convenient.

ciphart⁴ is an application for encrypting and decrypting files that makes use of libciphart. this application is intended for use by end-users or scripts, henceforth it has some fluff to treat mankind with dignity.

1 ciphart

1.1 parameters

enc encryption function.

p password.

s salt.

L number of memory lanes for concurrency.

M total memory in bytes.

T number of tasks per lane segment.

R number of rounds per task.

B added security in relative entropy bits.

 K_{out} output key size in bytes.

1.2 internal variables

$$C \qquad \leftarrow \begin{cases} 64 \text{ bytes} & \text{if enc is } xchacha20\\ 16 \text{ bytes} & \text{if enc is } aes\\ \dots \end{cases}$$

this to reflect the block size of the encryption algorithm that's going to use *ciphart*'s generated key to encrypt data.

$$K_{\rm in} \leftarrow \begin{cases} 32 \text{ bytes} & \text{if enc is } xchacha20\\ 16 \text{ bytes} & \text{if enc is } aes-128\\ \dots \end{cases}$$

this is the size of the encryption key that's used to solve *ciphart*'s tasks.

- \hat{T} $\leftarrow T (T \mod 2) + 2$. this is to ensure that it is in multiples of 2. why? because we need a buffer for storing the clear-text and another for storing the output cipher-text.
- $\hat{M} \leftarrow M (M \mod C\hat{T}L) + C\hat{T}L$. this is to ensure that it is in multiples of $C\hat{T}L$. why? so that all segments are of equal lengths in order to simplify *ciphart*'s logic. e.g. it wouldn't be nice if the last segments were of unequal sizes.
- $G \leftarrow \hat{M}/C/\hat{T}/L$; total number of segments per lane.
- \hat{B} $\leftarrow \max(\log_2(GL\hat{T}R), B)$. this is to ensure that \hat{B} is large enough to have at least one pass over the \hat{M} -bytes memory.
- \hat{B} $\leftarrow \log_2(2^{\hat{B}} (2^{\hat{B}} \mod L\hat{T}R) + L\hat{T}R)$. this is just to reflect the reality with ciphart that segments must complete. i.e. when the user asks for B relative entropy bits, he gets \hat{B} instead, where $\hat{B} \geq B$. more details on this later.
- m_i C-bytes memory for i^{th} task in the \hat{M} -bytes pad.
- $n_l \leftarrow l\hat{T}R$; nonce variable for l^{th} lane with at least
- $f \leftarrow \mathbf{false}$; a flag indicating whether the \hat{M} -bytes pad is filled.

1.3 output

k K-bytes key with > B relative entropy bits.

1.4 steps

shown in algorithm 1.

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²https://github.com/P-H-C/phc-winner-argon2

³https://github.com/Al-Caveman/libciphart

⁴https://github.com/Al-Caveman/ciphart

algorithm 1: ciphart version 6

```
_{1} while true do
         for g = 0, 1, ..., G - 1 do
 2
             for l = 0, 1, ..., L - 1 do
 3
                  for t = 0, 1, ..., T - 1 do
 4
                       for r = 0, 1, ..., R - 1 do
  5
                           i \leftarrow gT + t;
  6
                           if t = 0 then
  7
                              j \leftarrow i + T - 1;
  8
                           else if t = T - 1 then
  9
                                j \leftarrow i + 1 - T;
10
                           \mathbf{else}
11
                             j \leftarrow i+1;
\bf 12
                           m_i \leftarrow \text{enc}(m_i, n_l, k);
13
                           n_l \leftarrow n_l + 1;
14
                           k \leftarrow f(m_j, p, l, s, t);
15
             if f = \mathbf{true} and \log_2(n_1L) \geq B then
16
               go to line 19;
17
         f \leftarrow \text{true};
18
    while true do
19
         for l = 1, 2, ..., L do
20
             if len(k) \ge K then return k[0:K];
21
             n \leftarrow n + 1;
\mathbf{22}
             k \leftarrow k \parallel \operatorname{enc}(m_{l,S,T}[1], n, k);
23
```

- 2 parallelism
- 3 memory-hardness
- 4 security interpretation
- 5 comparison
- 6 summary