1 Semantics

1.1 Grammar and definitions

Value expressions

$$V \to C^{\gamma}$$
 Typed contants
$$| \text{ () Unit constructor}$$

$$| \lambda x : \tau.M \text{ term lambda expressions}$$

$$| x \text{ Variables}$$

$$| \Lambda \phi.V \text{ Effect lambda expressions}$$

$$| V \epsilon \text{ Effect specialisation}$$

Computation expressions

$$M \to V \ V$$
Application
 $\mid do \ x \leftarrow M \ in \ M \ Sequencing$
 $\mid return \ V \ Unit \ computation$ (2)
 $\mid Cons^{\tau_1 \to T_{\xi}\tau_2}(V) \ Computation \ Constructors$
 $\mid Op^{T_{\xi}\tau_1 \to T_{\xi}\tau_2}(M) \ Computation \ Combinators$

Value types

$$\begin{split} \tau &\to \gamma \text{ Ground Types} \\ \mid \tau &\to \Theta \text{ Functions are kleisli arrows} \\ \mid \forall \phi. \tau \text{ Effect quantification} \end{split} \tag{3}$$

Computation (Monad) types

$$\Theta \to T_{\epsilon} \tau$$
 Monad type constructor (4)

Effects

 $\epsilon \rightarrow \phi \mid \xi..$ Effect variables or ground effects

1.2 typing

Value typing rules

$$(\operatorname{Const}) \frac{\Gamma \ OK}{\Gamma \vdash C^{\gamma} : \gamma}$$

$$(\operatorname{Unit}) \frac{\Gamma \ OK}{\Gamma \vdash () : unit}$$

$$(\operatorname{Weaken}) \frac{\Gamma \vdash x : A}{\Gamma, x' : A' \vdash x : A} (x \neq x')$$

$$(\operatorname{Var}) \frac{\Gamma \ OK}{\Gamma, x : A \vdash x : A}$$

$$(\operatorname{Eff-Gen}) \frac{\Gamma \vdash V : A}{\Gamma \vdash \Lambda \phi . V : \forall \phi . A} \phi \not\in fev(\Gamma)$$

$$(\operatorname{Eff-Spec}) \frac{\Gamma \vdash V : A}{\Gamma \vdash V : A[\epsilon \phi]}$$

$$(\operatorname{Lambda}) \frac{\Gamma, x : A \vdash M : \Theta}{\Gamma \vdash \lambda x : A . M : A \to \Theta} x \not\in fv(\Gamma)$$

$$(\operatorname{SubType}) \frac{\Gamma \vdash V : A}{\Gamma \vdash V : A} A \leq B$$

Computation Typing Rules

$$(\text{Application}) \frac{\Gamma \vdash V_1 \colon A \to \Theta \ \Gamma \vdash V_2 \colon A}{\Gamma \vdash V_1 V_2 \colon \Theta} \\ (\text{Sequencing}) \frac{\Gamma \vdash M_1 \colon T_{\epsilon_1} A \ \Gamma, x \colon A \vdash M_2 \colon T_{\epsilon_2} B}{\Gamma \vdash do \ x \leftarrow M_1 \ in \ M_2 \colon T_{\epsilon_1 \circ \epsilon_2} B} \\ (\text{Unit Computation}) \frac{\Gamma \vdash V \colon A}{\Gamma \vdash return(V) \colon T_1 A} \\ (\text{Constructor}) \frac{\Gamma \vdash V \colon \tau_1}{\Gamma \vdash Cons^{\tau_1 \to T_\xi \tau_2}(V) \colon T_\xi \tau_2} \\ (\text{Combinator}) \frac{\Gamma \vdash C \colon T_{\xi_1} \tau_1}{\Gamma \vdash Op^{T_\xi \tau_1 \to T_\xi \tau_2}(M) \colon T_{\xi_2} \tau_2}$$