1 Semantics

1.1 Grammar and definitions

Value expressions

$$V \to C^{\gamma}$$
 Typed contants
| () Unit constructor
| $\lambda x : \tau.M$ term lambda expressions
| x Variables
| $\Lambda \phi.V$ Effect lambda expressions
| $V \epsilon$ Effect specialisation

Computation expressions todo: is the if rule necessary?

$$M \to V$$
 VApplication
 $\mid do \ x \leftarrow M \ in \ M$ Sequencing
 $\mid return \ V$ Unit computation
 $\mid if \ V \ then \ C \ else \ C$ Conditional
 $\mid Cons^{\tau_1 \to T_{\xi}\tau_2}(V)$ Computation Constructors
 $\mid Op^{T_{\xi}\tau_1 \to T_{\xi}\tau_2}(M)$ Computation Combinators

Value types

Computation (Monad) types

$$\Theta \to T_{\epsilon} \tau$$
 Monad type constructor (4)

Effects

 $\epsilon \rightarrow \phi \mid \xi..$ Effect variables or ground effects

1.2 typing

Value typing rules

$$(\operatorname{Const}) \frac{\Gamma \ OK}{\Gamma \vdash C^{\gamma} : \gamma}$$

$$(\operatorname{Unit}) \frac{\Gamma \ OK}{\Gamma \vdash () : unit}$$

$$(\operatorname{Weaken}) \frac{\Gamma \vdash x : A}{\Gamma, x' : A' \vdash x : A} (x \neq x')$$

$$(\operatorname{Var}) \frac{\Gamma \ OK}{\Gamma, x : A \vdash x : A}$$

$$(\operatorname{Eff-Gen}) \frac{\Gamma \vdash V : A}{\Gamma \vdash \Lambda \phi . V : \forall \phi . A} \phi \not\in fev(\Gamma)$$

$$(\operatorname{Eff-Spec}) \frac{\Gamma \vdash V : \forall \phi . A}{\Gamma \vdash V : A \vdash (\phi)}$$

$$(\operatorname{Lambda}) \frac{\Gamma, x : A \vdash M : \Theta}{\Gamma \vdash \lambda x : A . M : A \to \Theta} x \not\in fv(\Gamma)$$

$$(\operatorname{SubType}) \frac{\Gamma \vdash V : A}{\Gamma \vdash V : B} A \leq B$$

Computation Typing Rules

$$(\text{Application}) \frac{\Gamma \vdash V_1 \colon A \to \Theta \ \Gamma \vdash V_2 \colon A}{\Gamma \vdash V_1 V_2 \colon \Theta}$$

$$(\text{Sequencing}) \frac{\Gamma \vdash M_1 \colon T_{\epsilon_1} A \ \Gamma, x \colon A \vdash M_2 \colon T_{\epsilon_2} B}{\Gamma \vdash do \ x \leftarrow M_1 \ in \ M_2 \colon T_{\epsilon_1 \circ \epsilon_2} B}$$

$$(\text{Unit Computation}) \frac{\Gamma \vdash V \colon A}{\Gamma \vdash V \colon A}$$

$$(\text{Constructor}) \frac{\Gamma \vdash V \colon \tau_1}{\Gamma \vdash Cons^{\tau_1 \to T_\xi \tau_2}(V) \colon T_\xi \tau_2}$$

$$(\text{Combinator}) \frac{\Gamma \vdash M \colon T_{\xi_1} \tau_1}{\Gamma \vdash Op^{T_\xi \tau_1 \to T_\xi \tau_2}(M) \colon T_{\xi_2} \tau_2}$$

$$(\text{if}) \frac{\Gamma \vdash V \colon Bool \ \Gamma \vdash C_1 \colon \Theta \ \Gamma \vdash C_2 \colon \Theta}{\Gamma \vdash if \ V \ then \ C_1 \ else \ C_2 \colon \Theta}$$

$$(\text{SubTypeC}) \frac{\Gamma \vdash M \colon \Theta_1}{\Gamma \vdash M \colon \Theta_2} \Theta_2 \le \Theta_1$$

Subtyping Rules A ranges over value types

$$(\text{Reflexive})_{\overline{A \le A}}$$

$$(\text{Transitive}) \frac{A \leq B \ B \leq C}{A \leq C}$$

$$(\text{Function}) \frac{A' \leq A \ \Theta \leq \Theta'}{A \to \Theta \leq A' \to \Theta'}$$

$$(\text{Quantification}) \frac{\tau_1 \leq \tau_2}{\Lambda \phi. \tau_1 \leq \Lambda \phi. \tau_2}$$

$$(\text{Computation}) \frac{\epsilon_1 \sqsubseteq \epsilon_2 \quad A \leq B}{T_{\epsilon_1} A \leq T_{\epsilon_2} B}$$