

For each instance of the typing relation, define a denotation morphism: $\llbracket \Phi \mid \Gamma \vdash v : A \rrbracket_M : \mathbb{C}(I)(\Gamma_I, A_I)$. Writing Γ_I and A_I for $\llbracket \Phi \vdash \Gamma \text{Ok} \rrbracket_M$ and $\llbracket \Phi \vdash A : \text{Type} \rrbracket_M$.

For each ground constant, \mathbb{C}^A , there exists $c : 1 \rightarrow A_I$ in $\mathbb{C}(I)$.

- (Unit) $\frac{\Phi \vdash \Gamma \text{Ok}}{\llbracket \Phi \mid \Gamma \vdash () : \text{Unit} \rrbracket_M = \langle \rangle_{\Gamma} : \Gamma_I \rightarrow 1}$
- (Const) $\frac{\Phi \vdash \Gamma \text{Ok}}{\llbracket \Phi \mid \Gamma \vdash \mathbb{C}^A : A \rrbracket_M = \llbracket \mathbb{C}^A \rrbracket_M \circ \langle \rangle_{\Gamma} : \Gamma \rightarrow \llbracket A \rrbracket_M}$
- (True) $\frac{\Phi \vdash \Gamma \text{Ok}}{\llbracket \Phi \mid \Gamma \vdash \text{true} : \text{Bool} \rrbracket_M = \text{inl} \circ \langle \rangle_{\Gamma} : \Gamma \rightarrow \llbracket \text{Bool} \rrbracket_M = 1 + 1}$
- (False) $\frac{\Phi \vdash \Gamma \text{Ok}}{\llbracket \Phi \mid \Gamma \vdash \text{false} : \text{Bool} \rrbracket_M = \text{inr} \circ \langle \rangle_{\Gamma} : \Gamma \rightarrow \llbracket \text{Bool} \rrbracket_M = 1 + 1}$
- (Var) $\frac{\Phi \vdash \Gamma \text{Ok}}{\llbracket \Phi \mid \Gamma, x : A \vdash x : A \rrbracket_M = \pi_2 : \Gamma \times A \rightarrow A}$
- (Weaken) $\frac{f = \llbracket \Phi \mid \Gamma \vdash x : A \rrbracket_M : \Gamma \rightarrow A}{\llbracket \Phi \mid \Gamma, y : B \vdash x : A \rrbracket_M = f \circ \pi_1 : \Gamma \times B \rightarrow A}$
- (Lambda) $\frac{f = \llbracket \Phi \mid \Gamma, x : A \vdash v : B \rrbracket_M : \Gamma \times A \rightarrow B}{\llbracket \Phi \mid \Gamma \vdash \lambda x : A. v : A \rightarrow B \rrbracket_M = \text{cur}(f) : \Gamma \rightarrow (B)^A}$
- (Subtype) $\frac{f = \llbracket \Phi \mid \Gamma \vdash v : A \rrbracket_M : \Gamma \rightarrow A \quad g = \llbracket A \leq : \Phi B \rrbracket_M}{\llbracket \Phi \mid \Gamma \vdash v : B \rrbracket_M = g \circ f : \Gamma \rightarrow B}$
- (Return) $\frac{f = \llbracket \Phi \mid \Gamma \vdash v : A \rrbracket_M}{\llbracket \Phi \mid \Gamma \vdash \text{return } v : M_1 A \rrbracket_M = \eta_A \circ f}$
- (If) $\frac{f = \llbracket \Phi \mid \Gamma \vdash v : \text{Bool} \rrbracket_M : \Gamma \rightarrow 1 + 1 \quad g = \llbracket \Phi \mid \Gamma \vdash v_1 : M_{\epsilon} A \rrbracket_M \quad h = \llbracket \Phi \mid \Gamma \vdash v_2 : M_{\epsilon} A \rrbracket_M}{\llbracket \Phi \mid \Gamma \vdash \text{if}_{\epsilon, A} v \text{ then } v_1 \text{ else } v_2 : M_{\epsilon} A \rrbracket_M = \text{app} \circ ((\text{cur}(g \circ \pi_2), \text{cur}(h \circ \pi_2)) \circ f) \times \text{Id}_{\Gamma}) \circ \delta_{\Gamma} : \Gamma \rightarrow T_{\epsilon} A}$
- (Bind) $\frac{f = \llbracket \Phi \mid \Gamma \vdash v_1 : M_{\epsilon_1} A : \Gamma \rightarrow T_{\epsilon_1} A \quad g = \llbracket \Phi \mid \Gamma, x : A \vdash v_2 : M_{\epsilon_2} B \rrbracket_M : \Gamma \times A \rightarrow T_{\epsilon_2} B}{\llbracket \Phi \mid \Gamma \vdash \text{do } x \leftarrow v_1 \text{ in } v_2 : M_{\epsilon_1, \epsilon_2} B \rrbracket_M = \mu_{\epsilon_1, \epsilon_2, B} \circ T_{\epsilon_1} g \circ \text{t}_{\Gamma, A, \epsilon_1} \circ \langle \text{Id}_{\Gamma}, f \rangle : \Gamma \rightarrow T_{\epsilon_1, \epsilon_2} B}$
- (Apply) $\frac{f = \llbracket \Phi \mid \Gamma \vdash v_1 : A \rightarrow B \rrbracket_M : \Gamma \rightarrow (B)^A \quad g = \llbracket \Phi \mid \Gamma \vdash v_2 : A \rrbracket_M : \Gamma \rightarrow A}{\llbracket \Phi \mid \Gamma \vdash v_1 v_2 : B \rrbracket_M = \text{app} \circ \langle f, g \rangle : \Gamma \rightarrow B}$
- (Effect-Lambda) $\frac{f = \llbracket \Phi, \alpha \mid \Gamma \vdash v : A \rrbracket_M : \mathbb{C}(I \times U, W)(\Gamma, A)}{\llbracket \Phi \mid \Gamma \vdash \Lambda \alpha. A : \forall \epsilon. A \rrbracket_M = \bar{f} : \mathbb{C}(I)(\Gamma, \forall_I(A))}$
- (Effect-App) $\frac{g = \llbracket \Phi \mid \Gamma \vdash v : \forall \alpha. A \rrbracket_M : \mathbb{C}(I)(\Gamma, \forall_I(A)) \quad h = \llbracket \Phi \vdash \epsilon : \text{Effect} \rrbracket_M : \mathbb{C}(I, U)}{\llbracket \Phi \mid \Gamma \vdash v \epsilon : A[\epsilon/\alpha] \rrbracket_M = \langle \text{Id}_I, h \rangle^* (\epsilon_{\llbracket \Phi, \beta \vdash A[\beta/\alpha] : \text{Type} \rrbracket_M}) \circ g : \mathbb{C}(I)(\Gamma, A[\epsilon/\alpha])}$