Day5 exercise solutions

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Problem 1

skim(salary)

Table 1: Data summary

Name	salary
Number of rows	325
Number of columns	5
Column type frequency:	
V 1	
character	1
factor	1

 $\begin{array}{ccc} \text{numeric} & & 3 \\ \hline \\ \text{Group variables} & & \text{None} \end{array}$

Variable type: character

skim_variable	n_missing	$complete_rate$	min	max	empty	n_unique	whitespace
District	0	1	3	24	0	325	0

Variable type: factor

skim_variable	$n_{missing}$	$complete_rate$	ordered	n _unique	top_counts
size	0	1	FALSE	3	1: 223, 2: 68, 3: 34

Variable type: numeric

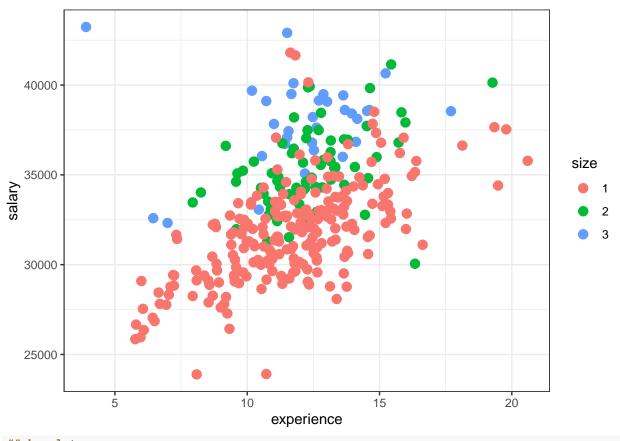
skim_variable_	_missingcom	plete_ra	te mean	sd	p0	p25	p50	p75	p100	hist
districtSize	0	1	1.42	0.67	1.00	1.00	1.00	2.00	3.0	
salary	0	1	33168.33	3412.77	23889.50	30847.70	32867.50	35296.70	43232.6	
experience	0	1	11.86	2.55	3.91	10.44	11.97	13.33	20.6	

The average salary in USD is 3.3168327×10^4 and in CHF is 2.8856445×10^4 !

• Graphical summary

```
# visualize the dataset

## scatter plot
salary %>%
    ggplot(aes(x = experience, y = salary, color = size)) +
    geom_point(size = 3) +
    theme_bw()
```

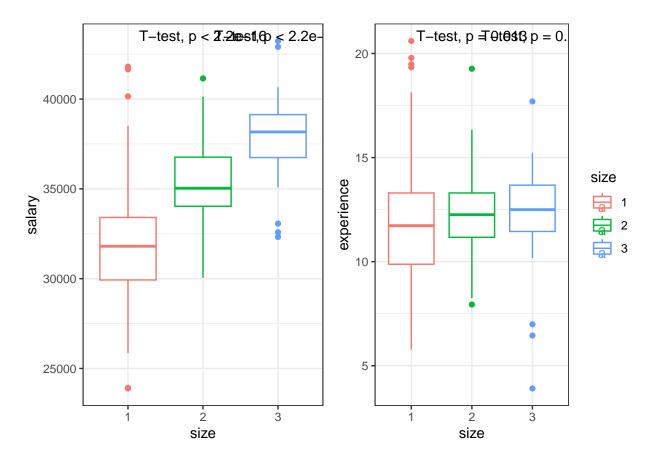


```
## boxplots

bxp1 <- salary %>%
    ggplot(aes(x = size, y = salary, color = size)) +
    geom_boxplot() +
    stat_compare_means(ref.group = "1", method = "t.test") +
    theme_bw() +
    theme(legend.position = "none")

bxp2 <- salary %>%
    ggplot(aes(x = size, y = experience, color = size)) +
    geom_boxplot() +
    stat_compare_means(ref.group = "1", method = "t.test") +
    theme_bw()

# Arrange the plots side by side
grid.arrange(bxp1, bxp2, ncol = 2)
```



1.C)

```
# fit models
model_a <- lm(salary ~ 1 + experience + districtSize, data = salary)</pre>
model_b <- lm(salary ~ 1 + experience + size, data = salary)</pre>
## model A
summary(model_a)
##
## lm(formula = salary ~ 1 + experience + districtSize, data = salary)
## Residuals:
       Min
               1Q Median
                               3Q
## -7446.0 -1307.9 -180.7 1142.7 10099.5
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 22065.55
                         622.14
                                     35.47
                                             <2e-16 ***
                                     12.02
                                             <2e-16 ***
## experience
                 586.42
                             48.79
                                             <2e-16 ***
## districtSize 2924.90
                            184.47
                                     15.86
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
```

```
## Residual standard error: 2225 on 322 degrees of freedom
## Multiple R-squared: 0.5775, Adjusted R-squared: 0.5748
## F-statistic:
                 220 on 2 and 322 DF, p-value: < 2.2e-16
## model A
summary(model_b)
##
## Call:
## lm(formula = salary ~ 1 + experience + size, data = salary)
## Residuals:
##
      Min
               1Q Median
                                30
                                      Max
                   -108.9 1141.3 10220.8
## -7577.1 -1283.9
##
## Coefficients:
##
              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 24995.49
                            589.35
                                   42.412
                                             <2e-16 ***
                                             <2e-16 ***
## experience
                584.15
                            48.96
                                   11.932
## size2
                3088.00
                            310.73
                                     9.938
                                             <2e-16 ***
               5732.28
## size3
                            410.84 13.952
                                             <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 2227 on 321 degrees of freedom
## Multiple R-squared: 0.578, Adjusted R-squared: 0.5741
## F-statistic: 146.6 on 3 and 321 DF, p-value: < 2.2e-16
```

The two models are similar in terms of their goodness-of-fit values. Model A has one degree of freedom lower as it treats districtSize as one independent variable, while model B treats factorized size variable as 2.

1.D)

```
# save model summary in an object
summary_b <- summary(model_b)</pre>
```

« comments »

« comments »

The adjusted coefficient of determination for model B is 0.5740808. Therefore, 57.4080767% of variability in the response variable salary can be explained by the proposed linear regression model.

Given p-values < 0.05, it indicates that all predictors has a significant effect on the dependent variable. Therefore, it is not advisable to drop any of the predictor variables.

The parameter estimate for variable "experience" is 584.1517062. That means for 1 year additional experience, given the district is the same, the salary will be increase by 584.1517062.

The parameter estimate for variable "district 2" is 3087.9955923. That means for the same level of experience, teachers in district size 2, earn 3087.9955923 USD more than teachers in the reference district of size 1.

The parameter estimate for variable "district 3" is 5732.2815637. That means for the same level of experience, teachers in district size 3, earn 5732.2815637 USD more than teachers in the reference district of size 1.

1.E)

```
model_b_transformed <- lm(salary ~ I(experience - 13) + size, data = salary)</pre>
summary(model_b_transformed)
##
## Call:
## lm(formula = salary ~ I(experience - 13) + size, data = salary)
##
## Residuals:
##
      Min
                1Q
                   Median
                                       Max
  -7577.1 -1283.9 -108.9
                           1141.3 10220.8
##
##
## Coefficients:
##
                      Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                      32589.46
                                   163.20 199.691
                                                    <2e-16 ***
## I(experience - 13)
                        584.15
                                    48.96 11.932
                                                    <2e-16 ***
## size2
                       3088.00
                                   310.73
                                            9.938
                                                    <2e-16 ***
## size3
                       5732.28
                                   410.84 13.952
                                                    <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2227 on 321 degrees of freedom
## Multiple R-squared: 0.578, Adjusted R-squared: 0.5741
## F-statistic: 146.6 on 3 and 321 DF, p-value: < 2.2e-16
```

When we modify the model by using "experience - 13" instead of experience, the interpretation of the coefficient for intercept and experience will change, but the overall fit and statistical properties of the model (likeR^2, adjusted R^2, p-values) will remain unchanged.

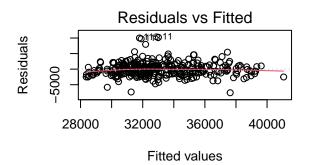
The coefficient for I(experience - 13) will now represent the change in salary for each year of experience compared to 13 years, and the intercept will reflect the average salary when the experience is 13 years, rather than 0 years.

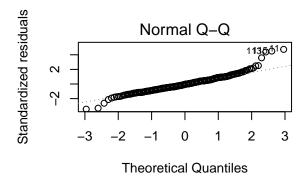
Intercept: In the original model, the intercept represents the expected salary when experience = 0. This can be less meaningful if no teachers in the dataset have exactly 0 years of experience. By shifting the experience to center it around 13 years, the intercept will now represent the expected salary for a teacher with 13 years of experience.

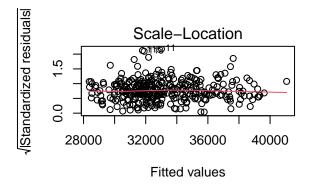
1.F)

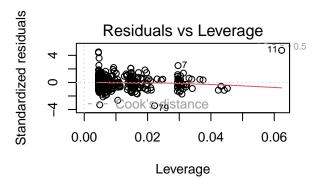
« comments »

```
# Plot diagnostic plots
par(mfrow = c(2, 2)) # Arrange 4 diagnostic plots
plot(model_b)
```









« comments »

- based on the residuals vs fitted plot we can confirm linear relationship between the response and predictor variables
- based on Q-Q Plot for Residuals we can confirm normality of error term of our linear regression model
- based on scale-location plot we can confirm homoscedasticity of the residuals across all levels of the independent variables

1.G)

```
new_data_a <- data.frame(experience = c(10), districtSize = c(3))
new_data_b <- data.frame(experience = c(10), size = c("3"))</pre>
```

« comments »

According to model A the predicted salary will be 3.6704423×10^4 and according to model B 3.6569287×10^4

Problem 2

- 2.A)
- 2.B)
- 2.C)
- 2.D)
- 2.E)