GSERM - **St. Gallen 2019**Generalized Estimating Equations

June 19, 2019 (morning session)

Quick GLM review

Linear-normal model is:

$$Y_i = \mu_i + u_i$$

with:

$$\mu_i = \mathbf{X}_i \boldsymbol{\beta}.$$

Generalize:

$$g(\mu_i) = \mathbf{X}_i \boldsymbol{\beta}$$

and:

$$Y_i \sim \text{i.i.d. } F[\mu_i, \mathbf{V}_i].$$

GLM Estimation

"Score" equations:

$$\mathbf{U}(\beta) = \sum_{i=1}^{N} \mathbf{D}'_{i} \mathbf{V}_{i}^{-1} [Y_{i} - \mu_{i}] = \mathbf{0}.$$

with:

- $\mathbf{D}_i = \frac{\partial \mu_i}{\partial \beta}$,
- ullet ${f V}_i=rac{h(\mu_i)}{\phi}$, and
- $(Y_i \mu_i) \approx$ a "residual."
- Known as "quasi-likelihood" (e.g. Wedderburn 1974 Biometrika).

Now suppose:

$$Y_{it} = \mu_{it} + u_{it}$$

where

- $i \in \{1, ...N\}$ are i.i.d. "units,"
- $t \in \{1, ... T\}$, T > 1 are "time points,"
- we want $g(\mu_{it}) = \mathbf{X}_{it}\beta$.

Key issue: Accounting for (conditional) dependence in Y over time.

GEE Basics

Full joint distributions over T are hard. But...

Define:

$$\mathbf{R}_{i}(\boldsymbol{\alpha}) = \begin{pmatrix} 1.0 & \alpha_{12} & \cdots & \alpha_{1,T} \\ \alpha_{21} & 1.0 & \cdots & \alpha_{2,T} \\ \vdots & \vdots & \ddots & \vdots \\ \alpha_{T,1} & \cdots & \alpha_{T,T-1} & 1.0 \end{pmatrix},$$

- \rightarrow "working correlation" matrix.
 - Completely defined by α ,
 - Structure specified by the analyst.

GEE Origins

Liang and Zeger (1986): We can decompose the variance of Y_{it} as:

$$\mathbf{V}_i = \mathsf{diag}(\mathbf{V}_i^{rac{1}{2}})\,\mathbf{R}_i(lpha)\,\mathsf{diag}(\mathbf{V}_i^{rac{1}{2}})$$

With a standard GLM assumption about the mean and variance, this is:

$$\mathbf{V}_{i} = \frac{\left(\mathbf{A}_{i}^{\frac{1}{2}}\right) \mathbf{R}_{i}(\alpha) \left(\mathbf{A}_{i}^{\frac{1}{2}}\right)}{\phi}$$

where

$$\mathbf{A}_i = egin{pmatrix} h(\mu_{i1}) & 0 & \cdots & 0 \ 0 & h(\mu_{i2}) & \cdots & 0 \ dots & dots & \ddots & dots \ 0 & \cdots & 0 & h(\mu_{iT}) \end{pmatrix}$$

What does that mean?

$$V_i = Var(Y_{it}|X_{it}, \beta)$$
 has two parts:

- $\mathbf{A}_i = unit$ -level variation,
- $\mathbf{R}_i(\alpha)$ = within-unit *temporal* variation.

Specifying $\mathbf{R}_i(\alpha)$

Independent:
$$\mathbf{R}_i(\alpha) = \begin{pmatrix} 1.0 & 0 & \cdots & 0 \\ 0 & 1.0 & \cdots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & \cdots & 0 & 1.0 \end{pmatrix}$$

- Assumes no within-unit temporal correlation.
- Equivalent to GLM on pooled data.

Exchangeable:
$$\mathbf{R}_i(\alpha) = \begin{pmatrix} 1.0 & \alpha & \cdots & \alpha \\ \alpha & 1.0 & \cdots & \alpha \\ \vdots & \vdots & \ddots & \vdots \\ \alpha & \cdots & \alpha & 1.0 \end{pmatrix}$$

- One free parameter in $\mathbf{R}_i(\alpha)$ ($\alpha_{ts} = \alpha \ \forall \ t \neq s$)
- Temporal correlation within units is constant across time points.
- Akin (in some respects) to a random-effects model...

Specifying $\mathbf{R}_i(\alpha)$

$$AR(p) \text{ (e.g., } AR(1)): \qquad \mathbf{R}_i(\alpha) = \begin{pmatrix} 1.0 & \alpha & \alpha^2 & \cdots & \alpha^{T-1} \\ \alpha & 1.0 & \alpha & \cdots & \alpha^{T-2} \\ \vdots & \vdots & \ddots & \vdots & \vdots \\ \alpha^{T-1} & \cdots & \alpha^2 & \alpha & 1.0 \end{pmatrix}$$

- One free parameter in $\mathbf{R}_i(\alpha)$ ($\alpha_{ts} = \alpha^{|t-s|} \ \forall \ t \neq s$).
- Conditional within-unit correlation an exponential function of the lag.

$$Stationary(p): \qquad \mathbf{R}_i(\alpha) = \begin{pmatrix} 1.0 & \alpha_1 & \cdots & \alpha_p & 0 & \cdots & 0 \\ \alpha_1 & 1.0 & \alpha_1 & \cdots & \cdots & \cdots & 0 \\ \vdots & \vdots & \vdots & \ddots & \vdots & \vdots & \vdots \\ 0 & \cdots & 0 & \alpha_p & \cdots & \alpha_1 & 1.0 \end{pmatrix}$$

- AKA "banded," or "p-dependent."
- $p \leq T 1$ free parameters in $\mathbf{R}_i(\alpha)$.
- Conditional within-unit correlation an exponential function of the lag, up to lag p, and zero thereafter.

Specifying $\mathbf{R}_i(\alpha)$

Unstructured:
$$\mathbf{R}_{i}(\alpha) = \begin{pmatrix} 1.0 & \alpha_{12} & \alpha_{13} & \cdots & \alpha_{1,T-1} \\ \alpha_{12} & 1.0 & \alpha_{23} & \cdots & \alpha_{2,T-1} \\ \vdots & \vdots & \ddots & \vdots & \vdots \\ \alpha_{1,T-1} & \alpha_{2,T-1} & \cdots & \alpha_{T-1,T-1} & 1.0 \end{pmatrix}$$

- $\frac{T(T-1)}{2}$ free parameters in $\mathbf{R}_i(\alpha)$.
- Conditional within-unit correlation is completely data-dependent.

Estimation

Score equations:

$$\boldsymbol{U}_{GEE}(\boldsymbol{\beta}_{GEE}) = \sum_{i=1}^{N} \mathbf{D}_{i}^{\prime} \left[\frac{(\mathbf{A}_{i}^{\frac{1}{2}}) \, \mathbf{R}_{i}(\boldsymbol{\alpha}) \, (\mathbf{A}_{i}^{\frac{1}{2}})}{\phi} \right]^{-1} \left[Y_{i} - \mu_{i} \right] = \mathbf{0}$$

Two-step estimation:

- For fixed values of α_s and ϕ_s at iteration s, use Newton scoring to estimate $\hat{\beta}_s$,
- Use $\hat{\beta}_s$ to calculate standardized residuals $(Y_i \hat{\mu}_i)_s$, from which consistent estimates of α_{s+1} and ϕ_{s+1} can be estimated.

Inference

Liang & Zeger (1986):

$$\hat{oldsymbol{eta}}_{ extit{GEE}} \ \mathop{\sim}\limits_{N o \infty} \ oldsymbol{N}(oldsymbol{eta}, oldsymbol{\Sigma}).$$

For $\hat{\Sigma}$, two options:

$$\hat{\mathbf{\Sigma}}_{\mathsf{Model}} = N \left(\sum_{i=1}^{N} \hat{\mathbf{\mathcal{D}}}_{i}' \hat{\mathbf{\mathcal{V}}}_{i}^{-1} \hat{\mathbf{\mathcal{D}}}_{i} \right)$$

$$\hat{\boldsymbol{\Sigma}}_{\mathsf{Robust}} = N \left(\sum_{i=1}^{N} \hat{\boldsymbol{D}}_{i}^{\prime} \hat{\boldsymbol{V}}_{i}^{-1} \hat{\boldsymbol{D}}_{i} \right)^{-1} \left(\sum_{i=1}^{N} \hat{\boldsymbol{D}}_{i}^{\prime} \hat{\boldsymbol{V}}_{i}^{-1} \hat{\boldsymbol{S}}_{i} \hat{\boldsymbol{V}}_{i}^{-1} \hat{\boldsymbol{D}}_{i} \right) \left(\sum_{i=1}^{N} \hat{\boldsymbol{D}}_{i}^{\prime} \hat{\boldsymbol{V}}_{i}^{-1} \hat{\boldsymbol{D}}_{i} \right)^{-1}$$

where $\hat{\boldsymbol{S}}_i = (Y_i - \hat{\mu}_i)(Y_i - \hat{\mu}_i)'$.

Inference (aka, magic!)

- ullet $\hat{\Sigma}_{\mathsf{Model}}$
 - Requires that $R_i(\alpha)$ be "correct" for consistency.
 - Is slightly more efficient than $\hat{\Sigma}_{\text{Robust}}$ if so.
- $\bullet \ \ \hat{\Sigma}_{\mathsf{Robust}}$
 - Is consistent even if $R_i(\alpha)$ is misspecified.
 - Is slightly less efficient than $\hat{\Sigma}_{\mathsf{Model}}$ if $\mathsf{R}_i(lpha)$ is correct.

Use $\hat{\Sigma}_{\mathsf{Robust}}$.

Summary

GFFs:

- Are a straightforward variation on GLMs, and so
- Can be applied to a range of data types (continuous, binary, count, proportions, etc.),
- Yield robustly consistent point estimates of β s,
- Account for within-unit correlation in an informed way, but also
- Provide consistent inferences even if that correlation is misspecified.

Practical Issues: Model Interpretation

- In general, GEEs = GLMs.
- GEEs are marginal models, so:
 - $\hat{\beta}$ s have an interpretation as average / total effects.
 - Estimates / effect sizes generally be smaller than conditional (e.g. fixed/random) effects models.
 - E.g., for logit, $\hat{\beta}_M \approx \frac{\hat{\beta}_C}{\sqrt{1+0.35\sigma_{\eta}^2}}$, where $\sigma_{\eta}^2 > 0$ is the variance of the unit effects.

Practical Issues: Specifying $\mathbf{R}_i(\alpha)$

- Has been called "more art than science."
- Pointers:
 - Choose based on *substance* of the problem.
 - Remember that $\mathbf{R}_i(\alpha)$ is conditional on \mathbf{X} , $\hat{\boldsymbol{\beta}}$.
 - Consider unstructured when T is small and N large.
 - Try different ones, and compare.
- In general, it shouldn't matter terribly much...

Substantive interest in $\mathbf{R}_i(\alpha)$ (e.g., Prentice 1988)?

Add:

$$\mathbf{U}_{GEE}(lpha) = \sum_{i=1}^{N} \mathbf{E}_i' \mathbf{W}_i^{-1} (\mathbf{Z}_i - \eta_i)$$

where

- $\mathbf{E}_i = \frac{\partial \eta_i}{\partial \alpha}$,
- **W**_i is the "working" VCV matrix for the **Z**s,
- $\mathbf{Z}'_i = (Z_{i12}, Z_{i13}, ... Z_{iT-1, T-1})$ are the $\frac{T(T-1)}{2}$ observed sample pairwise correlations for i, and
- η_i is a vector of expected values for \mathbf{Z}_i which may include covariates.

GEE2: Estimation

Independently from $U_{GEE}(\beta)$:

$$\mathbf{U}_{\textit{GEE}}(\alpha, \boldsymbol{\beta}) = \sum_{i=1}^{N} \begin{pmatrix} \mathbf{D}_{i}^{\prime} & \mathbf{0} \\ \mathbf{0} & \mathbf{E}_{i}^{\prime} \end{pmatrix} \begin{pmatrix} \mathbf{V}_{i}^{-1} & \mathbf{0} \\ \mathbf{0} & \mathbf{W}_{i}^{-1} \end{pmatrix} \begin{pmatrix} \mathbf{Y}_{i} - \mu_{i} \\ \mathbf{Z}_{i} - \eta_{i} \end{pmatrix}$$

or allowing the two to covary:

$$\boldsymbol{U}_{GEE}(\alpha, \boldsymbol{\beta}) = \sum_{i=1}^{N} \begin{pmatrix} \mathbf{D}_{i}^{\prime} & \mathbf{0} \\ \mathbf{F}_{i}^{\prime} & \mathbf{E}_{i}^{\prime} \end{pmatrix} \begin{pmatrix} \mathbf{V}_{i}^{-1} & \mathsf{Cov}(\mathbf{Y}_{i}, \mathbf{W}_{i}) \\ \mathsf{Cov}(\mathbf{W}_{i}, \mathbf{Y}_{i}) & \mathbf{W}_{i}^{-1} \end{pmatrix} \begin{pmatrix} \mathbf{Y}_{i} - \mu_{i} \\ \mathbf{Z}_{i} - \eta_{i} \end{pmatrix}$$

where $\mathbf{F}_i = \frac{\partial \alpha_i}{\partial \boldsymbol{\beta}}$.

GEE2: Costs and Benefits

- Allows simultaneous modeling of first and second moments.
- Conditional on proper specification, $\hat{\beta}_{GEE2}$ s are somewhat more efficient than $\hat{\beta}_{GEE}$ s.
- Model (1) requires specification of third and fourth moments.
- Many (e.g. Diggle et al.) suggest using $W_i = \prod_{m \times m}$.
- Biggest drawback: Requires correct specification of R_i(α) for consistent estimates of β̂.
- Software is somewhat limited (EE, MAREG/WinMAREG, geepack, orth, possibly SASTM).

GEEs: Software

Command(s)/Package(s)
<pre>xtgee / xtlogit / xtprobit / xtpois / etc.</pre>
<pre>gee / geepack / multgeeB / orth / repolr</pre>
${\tt genmod} \; \big({\tt w/ \; repeated} \big)$

GEEs: Software Tips

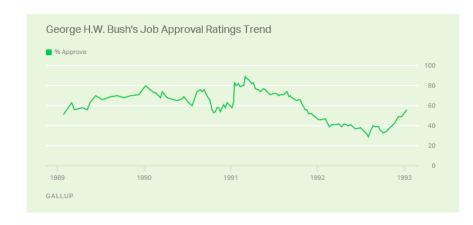
- Generally follow GLMs (specify "family" + "link")
- Certain combinations not possible/recommended
- Estimation: Fisher scoring, MLE, etc. (MCMC?)

From the geepack manual:

Warning

Use "unstructured" correlation structure only with great care. (It may cause R to crash).

Example: President Bush (41) Approval



ANES Data: President Bush (41) Approval

```
> url <- getURL("https://raw.githubusercontent.com/PrisonRodeo/GSERM-2019-git/master/Data/BushApproval.csv")
> Bush <- read.csv(text = url)
> summary(Bush)
     idno
                      year
                                   approval
                                                     partyid
                                                                        perfin
 Min. : 1.0
                 Min.
                        :1990
                                Min.
                                      :-2.0000
                                                  Min. :-3.0000
                                                                    Min. :-2.00000
 1st Qu.:156.8
                1st Qu.:1990
                               1st Qu.:-1.2500
                                                  1st Qu.:-2.0000
                                                                    1st Qu.:-1.00000
 Median :312.5
                Median:1991
                                Median : 1.0000
                                                  Median : 1.0000
                                                                    Median: 0.00000
 Mean
       :312.5
                Mean
                       :1991
                                Mean
                                     : 0.2302
                                                  Mean
                                                        : 0.3793
                                                                    Mean
                                                                          : 0.02724
                                                  3rd Qu.: 2.0000
 3rd Qu.:468.2
                3rd Qu.:1992
                                3rd Qu.: 2.0000
                                                                    3rd Qu.: 1.00000
       :624.0
                Max.
                        :1992
                                      : 2.0000
                                                         : 3.0000
                                                                           : 2.00000
 Max.
                               Max.
                                                  Max.
                                                                    Max.
     nateco
                        age
                                        educ
                                                       class
                                                                      nonwhite
                        :18.00
 Min.
     :-2.0000
                   Min.
                                  Min.
                                          :1.000
                                                   Min.
                                                          :1.000
                                                                   Min.
                                                                          :0.0000
 1st Qu.:-2.0000
                   1st Qu.:32.00
                                  1st Qu.:3.000
                                                   1st Qu.:1.000
                                                                   1st Qu.:0.0000
 Median :-1.0000
                   Median :41.00
                                 Median :4.000
                                                   Median :4.000
                                                                   Median :0.0000
       :-0.9797
                         :45.34
                                        :4.048
                                                   Mean :3.002
                                                                          :0.1378
 Mean
                   Mean
                                  Mean
                                                                   Mean
 3rd Qu.: 0.0000
                   3rd Qu.:59.00
                                  3rd Qu.:6.000
                                                   3rd Qu.:4.000
                                                                   3rd Qu.:0.0000
 Max.
        : 2,0000
                   Max.
                          :85.00
                                   Max.
                                          :7,000
                                                   Max.
                                                          :6.000
                                                                          :1.0000
                                                                   Max.
     female
Min.
       :0.0000
 1st Qu.:0.0000
 Median :1.0000
       :0.5192
 Mean
 3rd Qu.:1.0000
 Max.
        :1.0000
 > pdim(Bush)
Balanced Panel: n=624, T=3, N=1872
```

GEE: Independence

```
data=Bush.id=idno.familv=gaussian.corstr="independence")
> summary(GEE.IND)
Coefficients:
           Estimate Std.err
                                Wald Pr(>|W|)
(Intercept) 1.118752 0.165415 45.742 1.35e-11 ***
partyid
           -0.317251 0.017570 326.032 < 2e-16 ***
perfin 0.118223 0.032527 13.211 0.000278 ***
nateco
      0.360036 0.039828 81.719 < 2e-16 ***
         -0.001526 0.002270
                               0.452 0.501292
age
educ
         -0.048732 0.026603
                               3.355 0.066982 .
class
       -0.035451 0.024571
                               2.082 0.149078
nonwhite -0.287660 0.112827
                               6.500 0.010786 *
female
      -0.011875 0.076408
                               0.024 0.876493
---
Signif. codes: 0 *** 0.001 ** 0.01 * 0.05 . 0.1
Estimated Scale Parameters:
           Estimate Std.err
(Intercept)
             1.839 0.05423
Correlation: Structure = independenceNumber of clusters: 624 Maximum cluster size: 3
```

> GEE.IND<-geeglm(approval~partyid+perfin+nateco+age+educ+class+nonwhite+female,

> library(geepack)

Identical to GLM

```
> GLM <- glm(approval~partyid+perfin+nateco+age+educ+class+nonwhite+female,
           data=Bush.familv=gaussian)
> # Coefficients:
> cbind(GEE.IND$coefficients,GLM$coefficients)
              [,1]
                      [,2]
(Intercept) 1.11875 1.11875
partyid
       -0.31725 -0.31725
perfin 0.11822 0.11822
nateco
          0.36004 0.36004
        -0.00153 -0.00153
age
educ -0.04873 -0.04873
class -0.03545 -0.03545
nonwhite -0.28766 -0.28766
female
       -0.01188 -0.01188
> # Standard Errors:
> cbind(sgrt(diag(GEE.IND$geese$vbeta.naiv)).sgrt(diag(vcov(GLM))))
             [.1] [.2]
(Intercept) 0.13827 0.13861
partyid
          0.01615 0.01619
perfin
      0.02963 0.02970
nateco
      0.03857 0.03866
        0.00193 0.00194
age
educ
        0.02148 0.02153
class 0.02066 0.02071
nonwhite 0.09477 0.09500
female
      0.06356 0.06371
```

\equiv Identical to OLS

```
> OLS <- lm(approval~partyid+perfin+nateco+age+educ+class+
             nonwhite+female.data=Bush)
> summary(OLS)
Coefficients:
          Estimate Std. Error t value Pr(>|t|)
(Intercept) 1.11875 0.13861
                               8.07 1.2e-15 ***
partyid -0.31725 0.01619 -19.59 < 2e-16 ***
perfin 0.11822 0.02970 3.98 7.1e-05 ***
nateco
      0.36004 0.03866 9.31 < 2e-16 ***
         -0.00153 0.00194
                              -0.79 0.4304
age
         -0.04873 0.02153 -2.26 0.0237 *
educ
class
        -0.03545 0.02071 -1.71 0.0871 .
nonwhite -0.28766 0.09500
                              -3.03 0.0025 **
female -0.01188 0.06371
                              -0.19
                                     0.8522
---
Signif. codes: 0 *** 0.001 ** 0.01 * 0.05 . 0.1 1
Residual standard error: 1.36 on 1863 degrees of freedom
Multiple R-squared: 0.28, Adjusted R-squared: 0.277
F-statistic: 90.6 on 8 and 1863 DF, p-value: <2e-16
> 1.36^2
[1] 1.85
```

GEE: Exchangeable

```
> GEE.EXC<-geeglm(approval~partyid+perfin+nateco+age+educ+class+nonwhite+female,
  data=Bush.id=idno.familv=gaussian.corstr="exchangeable")
> summary(GEE.EXC)
Coefficients:
          Estimate Std.err Wald Pr(>|W|)
(Intercept) 1.14375 0.16592 47.52 5.4e-12 ***
partyid
      -0.31881 0.01738 336.60 < 2e-16 ***
perfin 0.10193 0.03195 10.18 0.0014 **
         0.32912 0.03964 68.94 < 2e-16 ***
nateco
age -0.00262 0.00228 1.32 0.2512
educ -0.05096 0.02669 3.65 0.0562 .
class -0.03311 0.02471 1.80 0.1803
nonwhite -0.29156 0.11374 6.57 0.0104 *
female
        -0.01596 0.07687 0.04 0.8356
Signif. codes: 0 *** 0.001 ** 0.01 * 0.05 .
Estimated Scale Parameters:
          Estimate Std.err
(Intercept)
              1.84 0.0542
Correlation: Structure = exchangeable Link = identity
Estimated Correlation Parameters:
     Estimate Std.err
        0.232 0.0275
alpha
Number of clusters:
                   624 Maximum cluster size: 3
```

GEE: AR(1)

```
> GEE.AR1<-geeglm(approval~partyid+perfin+nateco+age+educ+class+nonwhite+female,
  data=Bush.id=idno.familv=gaussian.corstr="ar1")
> summary(GEE.AR1)
Coefficients:
          Estimate Std.err Wald Pr(>|W|)
(Intercept) 1.03609 0.16610 38.91 4.4e-10 ***
partyid
       -0.32297 0.01736 346.07 < 2e-16 ***
perfin 0.09890 0.03186 9.64 0.0019 **
          0.34337 0.03967 74.94 < 2e-16 ***
nateco
age -0.00191 0.00229 0.70 0.4038
educ -0.04255 0.02658 2.56 0.1094
class -0.03270 0.02488 1.73 0.1888
nonwhite -0.28120 0.11208 6.29 0.0121 *
female
        -0.01873 0.07690 0.06 0.8075
Signif. codes: 0 *** 0.001 ** 0.01 * 0.05 .
Estimated Scale Parameters:
          Estimate Std.err
(Intercept)
              1.84 0.0543
Correlation: Structure = ar1 Link = identity
Estimated Correlation Parameters:
     Estimate Std.err
        0.285 0.0303
alpha
Number of clusters:
                   624 Maximum cluster size: 3
```

GEE: Unstructured

- > GEE.UNSTR<-geeglm(approval~partyid+perfin+nateco+age+educ+class+nonwhite+female, data=Bush,id=idno,family=gaussian,corstr="unstructured")
- > summary(GEE.UNSTR)

Coefficients:

Estimated Scale Parameters:

Estimate Std.err

(Intercept) 1.85 0.0542

Correlation: Structure = unstructured Link = identity

Signif. codes: 0 *** 0.001 ** 0.01 * 0.05 . 0.1

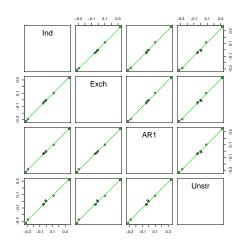
Estimated Correlation Parameters:

```
Estimate Std.err alpha.1:2 0.51573 0.0371 alpha.1:3 0.18614 0.0407 alpha.2:3 0.00277 0.0400
```

Number of clusters: 624 Maximum cluster size: 3

Comparing $\hat{\beta}$ s

- > betas<-cbind(GEE.IND\$coefficients,GEE.EXC\$coefficients,GEE.AR1\$coefficients,
 GEE.UNSTR\$coefficients)</pre>
- > library(car)
- > scatterplotMatrix(betas[-1,],smooth=FALSE,var.labels=c("Ind","Exch","AR1","Unstr"),
 diagonal="none")



Comparing s.e.s

> ses<-cbind(sqrt(diag(GEE.IND\$geese\$vbeta)), sqrt(diag(GEE.EXC\$geese\$vbeta)),
 sqrt(diag(GEE.AR1\$geese\$vbeta)), sqrt(diag(GEE.UNSTR\$geese\$vbeta)))
> scatterplotMatrix(ses[-1,],smooth=FALSE,var.labels=c("Ind","Exch","AR1","Unstr"),
 diagonal="none")

0.00 0.04 0.08

Unstr

Ind Ind Exch AR1

0.04 0.08

GEEs: Wrap-Up

GEEs are:

- Robust
- Flexible
- Extensible beyond panel/TSCS context