

# Crying Wolf in the Lab

Arya Gaduh, Peter McGee, Alexander Ugarov\*

April 6, 2023

## **Abstract**

Abstract is here —

Keywords: alarms, value of information, information economics, information design, —

# 1 Introduction

The 2010 gas blowout on Deep Horizon oil rig has killed 11 workers and caused one of the largest oil spills in history. The death toll was possibly aggravated by switching off a general safety alarm because its sirens interfered with workers' sleep.<sup>1</sup> This illustrates the trade-off between false-positive and false-negative test results with false-positive rates leading to higher false alarm costs and false-negative resulting in missed events.

Many real-life situations involve choosing binary tests to discover and prevent a negative outcome. Most binary tests transform continuous signals about the likelihood of an adverse state into simple yes/no prediction. This transformation relies on choosing a threshold for positive classification. Holding a continuous signal constant, a decrease in probability of no alarm in an adverse state (false-negative rate) corresponds to an increase in probability of alarm in a non-adverse state (false-positive rate). This trade-off motivates multiple discussions in medical diagnostics, alarm systems and extreme weather alerts. Despite ubiquity of binary alarms, there is little empirical evidence on how users evaluate alarms with different false-positive and false-negative rates.

In order to understand preferences over these trade-offs, we study the demand for information in the framework with a potential protection action. The subject, first, receives a signal about the probability of an adverse event. Then she decides to protect or not. This environment describes several practically important scenarios including extreme weather alerts, medical testing and safety alarms.

Some recent studies observe that many people put non-zero value on information about ego-relevant beliefs or future utility even if it has no apparent effect on subsequent decisions (all the citations). These preferences is not the focus of our study and hence we use relatively low stakes and ego-neutral information. As a result, our findings might not apply to settings with changing identity beliefs or to settings with delayed resolution of uncertainty and large potential payoffs.

We find that the value of information in our setup weakly correlates with the willingness-to-pay. First, subjects on average underreact to quality of the signal, resulting in overpaying for low-quality signal and underpaying for high-quality signals. Second, subjects tend to overreact to false-negative rates when the prior probability is low and overreact to false-positive rates when priors are high. We show that this pattern is most consistent with failure to estimate the effect of frequencies of false-positive and false-negative outcomes on the costs of using the signal. Xu (2020) similarly finds that individuals(?) do not properly account for priors and often choose tests not affecting optimal decisions even then more instrumental tests are available.

Our work is one of a few experimental studies measuring demand for information used for decision-making (instrumental information). Previous experimental studies studies the demand for signals in the prediction game in which subjects have to choose an optimal state under

---

<sup>1</sup><https://www.nytimes.com/2010/07/24/us/24hearings.html>

uncertainty. The field experiment conducted by (Hoffman, 2016) finds that the demand for information increases with initial uncertainty, but decreases with the signal’s accuracy. However, the decrease in accuracy is more modest than expected for a Bayesian decision-maker resulting in subjects underpaying for high-quality signals. The laboratory experiment of Ambuehl and Li (2018) finds that subjects tend to underreact to the accuracy of the binary signal about state of the world, but put a premium on completely certain signals. The paper of ? similarly employs a prediction game but varies priors on top of signal characteristics. reducing prior uncertainty makes more signals non-instrumental in the sense that there should be no effect from a signal to optimal decisions. She find that many subjects choose non-instrumental over instrumental signals which is consistent with

Our setup differs in two important aspects from (Ambuehl and Li, 2018; ?), because we study alerts and not prediction tasks. The subject faces a costly protection decision and not a prediction decision, resulting in three distinct payoffs: full payoff, full payoff minus protection costs and full payoff minus losses. It means that risk preferences affect the value of information and can change sensitivities to false-positive and false-negative rates. Our findings however are similar to prediction game findings. Consistent with Ambuehl and Li (2018) we also find that subjects undervalue accurate signals, but we do not find a premium for certain signals. And similar to ? we find that subjects do not properly account for interaction between prior probabilities and signal characteristics.

Due to its applicability for studying preferences over expectations, there is a larger stream of literature on the demand for non-instrumental information. Eliaz and Schotter (2010) find that subjects are willing to pay for signals even when these signals are excessive for making optimal choices. Their design involves subjects choosing between two boxes with one box containing a prize of \$20. Most subjects pay just to know the probability of finding \$20 in box A even if this box is more likely to contain a prize in all the possible states. This finding is inconsistent with expected utility maximization but indicates instead having preferences for certainty before making choices. Similar to this paper, Masatlioglu et al. (2017) also study preferences over information structures differing which differ in false-positive and false-negative rates but in their setup allows for a larger role of expectations. They find that for a positive potential outcome, most subjects prefer facing high false-negative rates rather than high false-positive rates. In other words, they tolerate uncertainty after negative signals better than uncertainty after positive signals. These preferences are salient: subjects require an average payment of 18-35 cents to switch to their least preferred information structure.

There is some mixed evidence that people update beliefs differently when these beliefs are ego-relevant or concern future gains and losses. Eil and Rao (2011) find asymmetry in updating ego-relevant beliefs such as beauty and IQ. Subjects update more after receiving positive signals and do not update enough after negative signals. Additionally, subjects with high posterior ego-relevant beliefs are willing to pay to receive a more precise signals, but require a compensation for learning when their beliefs are low. In contrast, Coutts (2019) does not find any updating

asymmetry with respect to either ego-relevant beliefs or beliefs about future payoffs.

Our paper is the first to measure value of information in the experimental setting of diagnostic tests or alarms. Previous work studies the use of alarms in context of medical testing, medical monitoring, safety alarms and extreme weather. Early literature on decision-making of medical professionals finds that doctors suffer from multiple biases when ordering testing, including inaccurate posterior probability estimation due to availability heuristics, hindsight bias and regret (Bornstein and Emler, 2001). Gigerenzer et al. (2007) find that very few mammologists understand mamogram results and tend to overestimate probability of cancer based on a positive result. Providing practitioners with natural frequencies instead of probabilities tends to reduce this bias.

Patients' willingness-to-pay for medical tests is large and largely responsive to test accuracy (Liang et al., 2003; Howard and Salkeld, 2009; Neumann et al., 2012). But there are several apparent violations of rationality. First, users are willing to pay for tests having little or zero diagnostic value (Schwartz et al., 2004; Neumann et al., 2012). For example, Schwartz et al. (2004) find that 73% of Americans in their survey prefer a free full-body CT scan versus one thousand USD cash. However, medical professional do not recommend full-body CT scans for healthy people due to extreme likelihood of false-positive findings. Second, the framing of test accuracy seems to matter a lot. Howard and Salkeld (2009) conduct a discrete-choice experiment to measure willingness-to-pay for the colorectal cancer screening. Their subjects agree to get 23 unnecessary colonoscopies in order to find one additional true cancer, but only 10.4 for reducing the number of cancers missed by one even though these descriptions are equivalent. Surprisingly, the perceived risk of cancer (prior) did not significantly affect the WTP in their study though the effect may come from its relatively low variation in the population.

This work also relates to the vast literature on demand for insurance and protection. Similar to our findings, several studies observe that the demand for insurance goes up after the recent experience with low-probability events. Field evidence indicates that people underinsure with respect to rare natural disasters (Friedl et al., 2014). Laury et al. (2009) find no under-insurance for low-probability events in the laboratory setting. One offered explanation (Volkman-Wise, 2015) is that subjects overweight recent evidence leading to underinsurance when there were no negative events in the recent past and to overinsurance after the fact. It is consistent with underweighting prior probabilities relative to more recent signals.

The bias we are finding is similar to the base-rate and signal neglect phenomena. Psychology researchers Hammerton (1973) and Kahneman and Tversky (1973) first observed that subjects underweighted prior probabilities (base rates) when calculating posteriors. This phenomenon had received the name of *base-rate neglect*. Multiple studies in economics then confirmed (Grether, 1992; Holt and Smith, 2009) this phenomenon in incentivized laboratory experiments. Most of these studies find that subjects also underweight signals on top of priors. We observe both phenomena in responses to our belief elicitation task, but the calculation

of signals' values differs substantially from the calculation of posterior probabilities. While the calculation of posterior probabilities would require using a Bayes formula, signal's value depends only on products of prior probabilities. However, we observe that subjects underestimate the effect of priors compared to theoretical predictions for an expected-utility decision-maker.

## 2 Model

**Environment.** The model describes a decision-maker considering a purchase of threat-assessment information. Let  $\omega \in \{0, 1\}$  denote the state of world, where 1 corresponds to some adverse event happening with probability  $\pi$ . The decision-maker has a lower utility in the adverse state, but only if she does not take the protective action. Denote actions by  $a \in \{0, 1\}$  with 1 meaning taking the protective action. The protection technology is perfect: protected agents bear no losses but pay protection costs  $c$  regardless of the state  $\omega$ . Decision-maker preferences are described by the utility function which depends on wealth  $Y$ , protective action  $a$  and potential damage in the adverse state  $\omega(1 - a)$ . Utility is separable in wealth, protection costs  $c > 0$  and potential loss in the adverse state  $L > c$ <sup>2</sup>:

$$U = U(Y, a, \omega(1 - a)) = u(Y - ac - \omega(1 - a)L) \quad (1)$$

The decision-maker can purchase a binary informative signal  $s \in \{0, 1\}$  about the state of the world before making a decision. Let  $P_{ij} \equiv P(s = i | \omega = j)$  be the probability of a signal taking value  $i$  conditional on the state of the world being  $j$ . After receiving the signal, the decision-maker updates her belief on the likelihood of the bad state to  $\mu(s)$ . Unless specified otherwise, we assume that the decision-maker forms her posterior beliefs by using the Bayes rule. Hence the posterior belief equals:

$$\mu(s) = \frac{\pi P_{s1}}{\pi P_{s1} + (1 - \pi)P_{s0}} \quad (2)$$

We also assume without loss of generality that a higher signal means a higher posterior probability of an adverse event  $\mu(1) \geq \mu(0)$ . Otherwise we can always re-label the signals.

**Preferences.** If there is no signal, the decision-maker protects if and only if it increases their expected utility:

$$EU_0 = \max[u(Y - c), \pi u(Y - L) + (1 - \pi)u(Y)] \quad (3)$$

---

<sup>2</sup>Separability condition does not impose additional restrictions on the utility function  $U$  as long as the variation in wealth has limited range. More specifically, if  $Y \in [Y_{min}, Y_{max}]$  and  $c < Y_{max} - Y_{min}$ ,  $L < c + (Y_{max} - Y_{min})$ , then the function  $u(\cdot)$  can be constructed from segments of  $U(\cdot, 0, 0)$ ,  $U(\cdot, 1, 0)$ ,  $U(\cdot, 0, 1)$ . While the resulting function  $u(\cdot)$  is not necessarily monotonic, it is likely to be monotonic if protective actions and potential damages are relatively high.

The signal can increase expected utility if the decision-maker reacts differently to positive and negative signals. Under these assumptions, her expected utility with a signal is:

$$EU_s = \pi P_{11}u(Y - c) + \pi P_{01}u(Y - L) + (1 - \pi)P_{10}u(Y - c) + (1 - \pi)P_{00}u(Y) \quad (4)$$

We consider the maximum amount  $b$  which the decision-maker is willing to pay for the signal. In our framework, it is a price paid with a signal such that a decision-maker is indifferent between having a signal and paying  $b$  and not having a signal. Because the decision-maker can always ignore a useless signal, the signal's value is bounded from below by zero. Hence it equals to the maximum between zero and the solution to the following equation:

$$\begin{aligned} P(s = 1)u(Y - b - c) + \pi P_{01}u(Y - b - L) + (1 - \pi)P_{00}u(Y - b) = \\ = \max[u(Y - c), \pi u(Y - L) + (1 - \pi)u(Y)] \end{aligned} \quad (5)$$

The left-hand side expression of this equation is a strictly decreasing function of  $b$ . Additionally, for  $b \rightarrow \infty$  the left-hand side is smaller than the right-hand side. It implies that the equation (5) above has at most one positive solution.

Obviously, perfectly accurate signals always have positive value  $b > 0$  because the payoff distribution with the signal first-order stochastically dominates the distribution without the signal. If the decision-maker protects without a signal, a perfect signal reduces the protection costs and if she takes chances, then it reduces losses in the adverse outcome from  $L$  to  $c < L$ . However, it is harder to determine the value of the imperfect signal without imposing more restrictions on preferences as it requires weighing  $u(Y - L)$  against  $u(Y - c)$ .

**Risk-neutral agent.** If the decision-maker is risk-neutral, the expression above collapses to:

$$b + P(s = 1)c + \pi P_{01}L = \min[c, \pi L]$$

The signal's value is just:

$$b = \max[0, \min[c, \pi L] - P(s = 1)c - \pi P_{01}L] \quad (6)$$

We can express WTP  $b$  as a function of priors, false-positive and false-negative rates. This is the equation we use in our empirical work:

$$b = \max[0, \min[c, \pi L] - \pi(1 - P_{01})c - (1 - \pi)P_{10}c - \pi P_{01}L] \quad (7)$$

The sensitivity of (positive) value  $b$  with respect to false-positive and false-negative rates is given by:

$$\frac{db}{dP_{10}} = -(1 - \pi)c \quad (8)$$

$$\frac{db}{dP_{10}} = -\pi(L - c) \quad (9)$$

Both false-positive and false-negative rates decrease the (positive) signal's value. The effect is proportional to the adverse state probability for the false-negative rate and to the non-adverse state probability for the false-positive rates.

**Risk Aversion Effects.** In a more general expected utility framework, risk aversion can both increase and decrease the signal's value. More specifically, risk aversion decreases the value when the protection costs are low:

**Proposition 1.** *If protection costs are low  $c < \pi L$ , then the strictly risk-averse decision-maker pays less than a risk-neutral one.*

*Proof.* See the Appendix. □

It is harder to make definite statements for lower risks or higher protection costs. For example, risk aversion increases value of a perfect signal as long as risk-averse decision-maker still chooses to not protect without a signal. This follows from the standard argument of increasing demand for insurance with risk aversion and the fact that the protection problem with a perfect signal is isomorphic to the insurance problem with deductible  $c$ .

Next, we study the effect of false-positive and false-negative rates on the signal's value  $b$ . Assuming a differentiable utility function  $u()$  we use implicit differentiation to derive sensitivities of WTP  $b$  to false-positive and false-negative rates:

$$\begin{aligned} \frac{db}{dP_{10}} &= -\frac{(1 - \pi)(u(Y - b) - u(Y - c - b))}{D(\pi, P_{01}, P_{10}, b)} \\ \frac{db}{dP_{01}} &= -\frac{\pi(u(Y - c - b) - u(Y - L - b))}{D(\pi, P_{01}, P_{10}, b)} \end{aligned}$$

With the denominator equal to the expected marginal utility:

$$\begin{aligned} D(\pi, P_{01}, P_{10}, b) &\equiv P(S = 1)u'(Y - c - b) + \pi P_{01}u'(Y - L - b) + \\ &+ (1 - \pi)P_{00}u'(Y - b) = E[MU] > 0 \end{aligned}$$

It is clear that the signal's value decreases with false-positive and false-negative rates  $\frac{db}{dP_{10}}, \frac{db}{dP_{01}} < 0$ . We can also say a bit more about the sensitivity to false-negative rates:

**Proposition 2.** *Risk-averse and imprudent decision-maker has higher sensitivity to false-negative rates as compared to a risk-neutral one.*

*Proof.* Use the mean value theorem to rewrite the sensitivity as:

$$\frac{db}{dP_{01}} = -\frac{\pi u'(\zeta)(L - c)}{E[MU]}, \zeta \in (Y - c - b, Y - L - b)$$

Now let  $X$  denote a random payoff of the decision-maker with a signal. A risk-averse decision-maker puts a positive value on the signal only if its expected payoff is higher than the payoff with full protection:  $EX > Y - c - b$ . If a decision-maker is imprudent ( $u''' < 0$ ) then  $E[MU] \equiv E[u'(X)] < u'(EX)$ . Next, because  $u'$  is a strictly increasing function and  $EX > Y - c - b$ :  $u'(\zeta) > u'(Y - c - b) > u'(EX)$ . Hence  $\frac{u'(\zeta)}{E[MU]} > 1$  and  $\frac{db}{dP_{01}} < -\pi(L - c)$ .  $\square$

However, risk aversion can both increase and decrease subject's sensitivity to false-positive rates depending on the utility function curvature and signal's characteristics. Intuitively, an expected marginal utility of a strongly risk-averse subject with a bad signal can be lower than the average slope of the utility function between  $Y - c - b$  and  $Y - b$  reducing sensitivity to false-positive rates. It can also be higher if either the signal is good or the curvature is small.

### 3 Experimental Design

In each session, subjects received a USD 5 show-up fee and were endowed with USD 25 that they might lose in the experiment. Subjects must then make a series of decisions in four sets of tasks: (i) Blind Protection; (ii) Informed Protection; (iii) Belief Elicitation; and (iv) Willingness to Pay Elicitation. To verify that subjects understand these tasks, they must answer a quiz before each task. If a subject gets any answer wrong, they read correct answers and explanations for each wrong answer. Additionally, subjects receive extra questions if they give wrong answers in a 5-question quiz given before the Informed Protection task. We do this because we consider Informed Protection as a first challenging task in the sequence which understanding is essential for the rest of the tasks. Each set of tasks has 6 rounds, for a total of 24 rounds. One of these rounds is selected at random as the payment round. A copy of the instruction is included in Appendix XX.

**Blind Protection (BP).** In each BP round, subjects must decide whether to insure (or “protect”) against an adverse event (i.e., drawing a black ball from a box). Subjects were informed of the prior probability of drawing a black ball before making their decision. The cost to protect is USD 5. If a black ball is drawn, an unprotected subject will lose USD 20. Subjects then played six rounds, where the probability of drawing a black ball was varied between XX and XX percent in each round. During the BP task, subjects did not receive any feedback on how that round would have been realized were it chosen as the payment round.

**Informed Protection (IP).** For the IP task, subjects make a protection decision as in BP. However, before each decision, subjects are given a signal that was generated with varying



degrees of inaccuracy. Following Coutts (2019), we present the signal-generation process using groups of “gremlins” that represent three types of signals: accurate (an honest gremlin), false positive (a black-swamp gremlin that always announces that the ball is black), and false negative (a white-swamp gremlin that always announces that the ball is white). Figure XX illustrates how the different gremlin types were presented to the subjects. Subjects knew the composition of the group from which the hint came from, but did not know which gremlin provided the hint. We vary the proportion of black balls in the box (prior probability of a black ball) and the composition of gremlins (signal quality) between rounds.

**Belief Elicitation (BE).** We use the BE task to elicit subjects’ beliefs about the likelihood of an adverse event and an adverse signal conditional on prior and signal characteristics in an incentive-compatible way. Similar to the IP task, subjects were informed of the prior probability of a black ball and the composition of the group of gremlins that would provide an additional signal. However, instead of asking subjects to make a protection decision, we asked them to estimate the probability of two events, to wit: (i) the ball is black ball when a randomly drawn gremlin says that it is white; (ii) the ball is black when a randomly drawn gremlin says that it is black.

We follow the stochastic version of the Becker-DeGroot-Marshak mechanism developed by Grether (1992) and Holt and Smith (2009) to elicit incentive-compatible responses: the subject submits their belief of the probability of the event  $\mu \in [0, 1]$ . If this belief is above some uniform random number  $r \in [0, 1]$ , they receive the payoff  $x$  only if the stated event happens. Otherwise their payoff is determined by an independent lottery which pays  $x$  with probability  $r$  and 0 otherwise.<sup>3</sup> To help subjects understand this complex mechanism, we prefaced our explanation of it with the fact that under this mechanism, truthful reporting of beliefs is the dominant strategy.

**Willingness to Pay Elicitation (WTPE).** The WTPE task measures subjects’ willingness to pay (WTP) for signals. Subjects know the prior probability of a black ball and the group composition of the gremlins that will determine signal quality. We then ask subjects for their WTP to receive a hint from a randomly drawn gremlin. Subjects can choose a value from USD 0 to 5 with USD 50-cent increments. Their decisions are incentive compatible: if a WTPE round is selected as the payment round, a random price of a hint will be drawn. If that price exceeded the subjects’ WTP, they will play a BP round. Otherwise, the subject would pay for the hint and play an IP round. After completing the WTPE task, subjects were asked a few demographic questions. The session concluded with the random selection and realization of the payment round, after which subjects were paid and dismissed.

---

<sup>3</sup>The benefit of this mechanism versus other probability elicitation mechanism (for example, quadratic scoring) is that reporting truthfully is a dominant strategy regardless of risk preferences (Karni, 2009). The only requirements a subject needs to satisfy are probabilistic sophistication and dominance: they rank lotteries based on their probabilities only and prefer higher probabilities of higher payoffs.

The first three tasks were designed to provide measures of the different components of WTP described in Section XX and use them to examine the extent to which they explain subjects’ WTP measured in the WTPE task. We use the BP task both to measure subjects’ responses to the prior and their risk aversion. Next, we use the IP task to examine how signals affect protection decisions. Finally, we use the BE task as a measure of subjects’ ability to estimate the probability of a signal for a given quality and to perform Bayesian updating. To construct these measures, we presented our subjects with 6 different priors for the BP task, and 3 priors and 2 gremlin groupings for the IP, BE, and WTPE tasks. Table reftab:treatments XX shows the values of the different priors in our treatments, as well as the gremlin groupings (along with the associated false positive and false positive rates) that we used for the different tasks.

We conducted this experiment in the Behavioral Business Research Lab (BBRL) at the University of Arkansas between October and November 2021. The experiment was implemented using Qualtrics. There were a total of 105 subjects. 84 percent of the subjects were university students and 41 percent were male. About 60 percent of the subjects had taken at least one statistics course. On average, including the show-up fee, subjects received around USD 26 for a session lasting around 45 minutes.

I think we need to have panels for parameter values in BP to help understand BP in Fig.1

Table 1: List of Treatments

Prop. of black balls ( $p$ )	Gremlins composition			FP rate	FN rate
	Honest	Black-eyed	White-eyed		
0.1, 0.2, 0.3, 0.5	2	0	0	0	0
0.1, 0.2, 0.3, 0.5	3	1	0	0.33	0
0.1, 0.2, 0.3, 0.5	3	0	1	0	0.33
0.1, 0.2, 0.3, 0.5	3	1	1	0.33	0.33
0.1, 0.2, 0.3, 0.5	5	1	0	0.2	0
0.1, 0.2, 0.3, 0.5	5	0	1	0	0.2
0.1, 0.2, 0.3, 0.5	5	1	1	0.2	0.2

## 4 Results

I’m not going to futz with the sections right now, but I would make section 4 Subject Decisions, then have various subsections ~~We begin with a brief overview of subject behavior in the different tasks.~~

Overall, we find that subject behavior across our tasks is largely “sensible,” i.e., subjects respond to increases in risk by protecting more, but deviates from the risk-neutral theoretical benchmark. Below we investigate several standard possible explanations, including risk preferences and failures of Bayesian updating, before exploring how the characteristics of the signal influences protection decisions, beliefs, and WTP.

We follow that discussion with a regression analysis to explain subjects' WTP for signals of different qualities. Our regression results suggest that subjects' WTP deviated from those of a risk-neutral utility maximizing subject which was driven by their failure to fully account for signal quality when calculating their WTP. Furthermore, we find that these deviations remained after controlling for risk aversion or subjects' ability to perform Bayesian updating.

#### 4.1 Blind Protection

**Blind Protection.** ~~Subjects' responses in the BP task are generally consistent with the expected utility framework.~~ Figure 1 plots the probability of protection decision against ~~prior~~posterior probability of a black ball for the BP task, where the posterior is equivalent to the prior, and the IP task. On aggregate, subjects protect more with a higher probability of a negative outcome: only 13% subjects protect when the probability of a black ball is 10% in contrast to 70% protecting when the probability is 30%.

At the individual level, BP responses are also largely sensible but indicate significant heterogeneity in terms of risk aversion. For approximately 70% of subjects (X/Y), the probability of choosing protection increases monotonically in posterior probability. The remaining 30% make at least one switch from protecting to not protecting and back, which is inconsistent with EU maximization. Among these switchers, however, 83% (24/39) skip only a single increment of the presented probability scale, suggesting an inattention error.<sup>4</sup> Risk-neutral subjects maximize their expected utility by protecting whenever the prior probability exceeds 0.25, which is the ratio of the protection cost (\$5) to the potential loss (\$20). In contrast, many of our subjects start protecting for lower probabilities of 0.1 or 0.2 indicating strict risk aversion. As a point of reference, switching at the probability 0.1 corresponds to CRRA risk aversion of  $\theta = 2$ , while switching at 0.2 corresponds to  $\theta = 0.573$  (see ?? in Appendix). ~~I need to review the literature here to compare.~~ A smaller group of subjects makes choices consistent with risk loving by never protecting or protecting for the probability of 0.3. We use the total number of protection choices as a measure of subjects' risk aversion, but following Holt and Laury (2002) exclude subjects switching more than once. Most of our results do not condition on risk aversion and hence are not affected by this calculation. ~~I don't understand exactly what you mean by using the total to "calculate" risk preferences. In HL, the total corresponds to a range for the parameter of a CRRA utility function, but I think we are just using the total as a relative metric in our sample? Also, we probably need to make sure that everything doesn't go totally bananas if we include the multiple switchers, then offer in a footnote to send those results to anyone who cares.~~

---

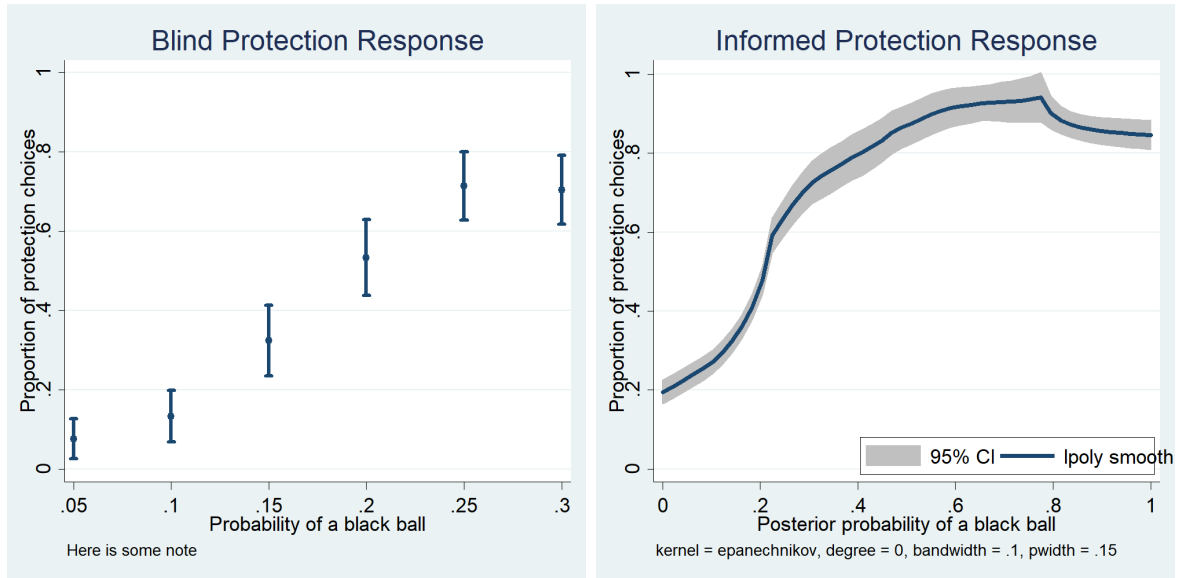
<sup>4</sup>For comparison, this reference on the Holt and Laury (2002) instrument suggests the XX% (YY%) of subjects switch at least (at most) once.

## 4.2 Informed Protection

Protection decisions are also positively correlated across tasks for a given individual. Subjects receive more information in the IP task than in the BP task, though using that information requires that subjects engage in Bayesian updating. Figure 1 shows that, consistent with their behavior in the BP task, the share of subjects protecting in the IP task is increasing in the posterior probabilities. Roughly 28% of subjects break monotonicity in their protection responses with respect to posterior probabilities<sup>5</sup> which roughly equals the percentage of non-monotonic responses for the BP task. At the individual level, we also observe that the total number of times subjects choose protection in the BP task significantly correlates with their likelihood to protect in the IP task conditional on posteriors, but this explains only a very small part ( $<1\%$ ) of variation in the IP decisions<sup>6</sup>

Subjects' responses in the first two tasks suggest that conditional on the true probabilities, subjects protected more in the IP task compared to the BP task at low probabilities, **even though the difference is not statistically significant** What is the test? Proportion of protection decisions for probabilities less than X or something?. These choices suggest that subjects' updated beliefs overshoot the true posterior at low probabilities. Unfortunately, we cannot compare their decisions for higher probabilities because we do not present choices with higher prior in the BP task.

Figure 1: Average Protection Response



Eventually we need to add notes to the figures

<sup>5</sup>They do not protect for some treatments with posterior probability  $P$  while protecting for a posterior probability  $P' < P$ .

<sup>6</sup>We use a LPM to estimate this relationship, and while the coefficient on the total number of protection choices is significant at 99%,  $R^2$  increases from 0.295 to 0.3.

### 4.3 Belief Elicitation

While the IP task gives us a sense for how subjects utilize signals in making protection decisions, we observe only whether or not they choose to protect, which conflates preferences with potential errors in updating posteriors. The BP task gives provides insight into subjects' risk preferences, while the BE task allows us to better understand to what extent updating errors influence decisions.

We define updating errors as the difference between the posterior and subjects' elicited belief on the posterior probability of a black ball for a given signal. We plot the distribution of the updating errors in the left hand column of Figure 2, while the right hand column provides a scatter plot of the elicited beliefs against the true posterior with a fitted line. I would prefer to take the r-squared out of this figure and put it in the table note with the correlations for each panel. Duly noted, will be incorporated.. Panel A of Figure 2 uses all elicited beliefs and suggests that, while errors occur, beliefs are still sensible. The distribution of updating errors is centered at 0, with roughly one-half (51%) concentrated within  $\pm 0.1$  interval around zero. Overall, the correlation between the elicited beliefs and the true posteriors was 0.653.

Using all the observations, however, obscures an important distinction: in many cases the ball color is completely certain based on priors and signals and so the updating should be trivial. Panel B of Figure 2 includes only those 44% beliefs elicited for an uncertain posterior. The median error is now -0.12, with with 90% of errors between -0.48 and 0.3, suggesting that subjects tend to overestimate the likelihood of adverse events for uncertain posteriors, which is consistent with what we see in Figure 1. The correlation between beliefs and posteriors in this subset of observations is only 0.571. Panel C of Figure 2 plots the distribution of updating errors with certain posteriors, which includes: (i) treatments with all-honest gremlins; and (ii) treatments with obviously irrelevant dishonest gremlins (e.g., a group with honest and white-eyed gremlins with a hint that the ball is black — or vice versa). Reassuringly, 69% of reported beliefs are correct, but subjects still err in about 30% of cases. About half of these errors involve reporting a probability of between one and zero, with the other half reporting a probability of one when it should have been zero. There is little evidence of these drastic errors (0 instead of 1) being strongly correlated with randomness in other treatments. It depends a bit. Are some guys doing everything right here and others doing everything wrong? Is there any relationship between errors here and inconsistencies in BP or a lower correlation between BP and IP tasks?

Overall, the pattern of belief updating is consistent with previous literature which finds that while humans usually update beliefs in a correct direction, they tend to underreact both to priors and the signals. The effect of underweighting priors, first noted in the psychology literature (Phillips and Edwards, 1966; Tversky and Kahneman, 1971; Kahneman and Tversky, 1972), and is known under the names of representativeness bias or base rate neglect. Subjects sensitivity both to priors and signals is easy to measure through estimating the following equation ((first introduced by Grether (1980)) which links the posterior probabilities  $\mu(B|S)$  of the state  $B$

conditional on signal  $S$  with the prior log-odds  $\log\left(\frac{P(S|B)}{P(S|W)}\right)$  of the signal and signal log-odds  $\log\left(\frac{P(B)}{P(W)}\right)$ :

$$\log\left(\frac{\mu(B|S)}{1 - \mu(B|S)}\right) = \alpha \log\left(\frac{P(S|B)}{P(S|W)}\right) + \beta \log\left(\frac{P(B)}{P(W)}\right) \quad (10)$$

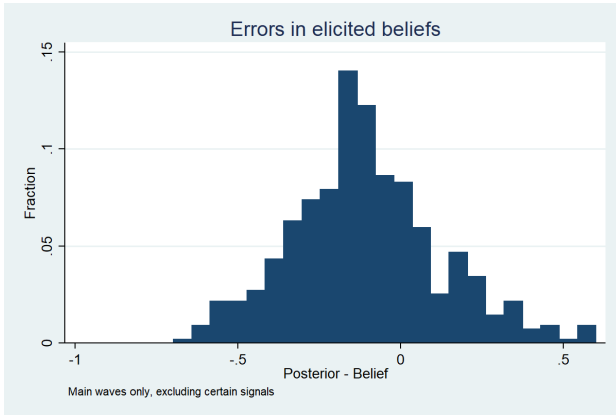
Coefficients  $\alpha$  and  $\beta$  should equal one if subjects perfectly follow Bayesian updating. Our estimates of these parameters are significantly below one with  $\hat{\alpha} = 0.43$   $\hat{\beta} = 0.25$  (see Column 1 in A). This is consistent with the meta-analysis in Benjamin (2019) which calculates the average  $\hat{\alpha}$  estimate to be around 0.22 (0.4 for incentivized studies only) and the average  $\hat{\beta}$  to be 0.6 (0.43 for incentivized) for studies presenting signals simultaneously (consistent with this study)<sup>7</sup>. Hence our subjects also demonstrate both the base-rate neglect and the signals underweighting. These effects lower the correlation between posteriors and reported beliefs and reduce sensitivity of beliefs to signal characteristics.

---

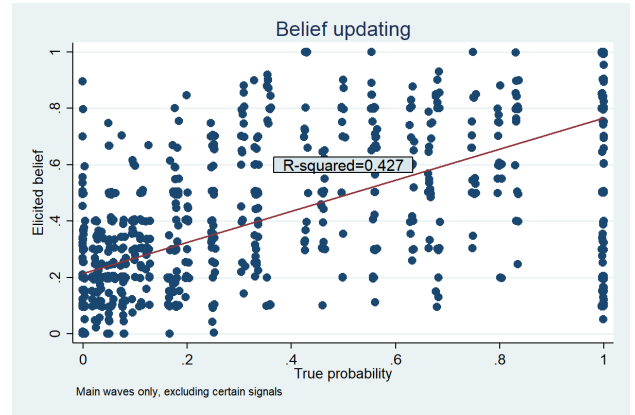
<sup>7</sup>The common name for this kinds of experiments is *bookbag-and-poker-chip experiments*

Figure 2: Errors in Bayesian Updating

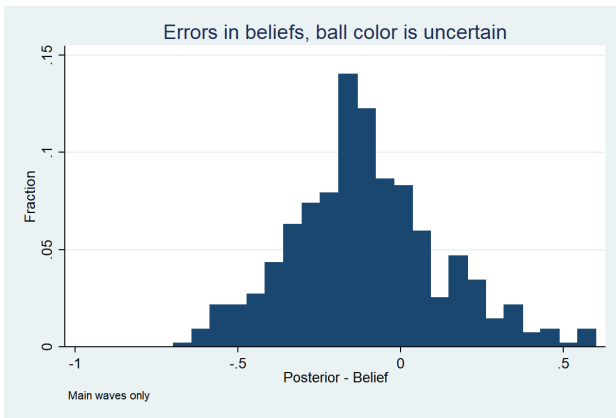
(a) Error Distribution



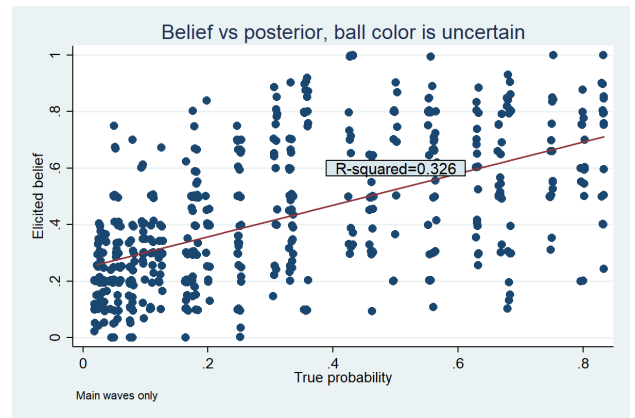
(b) Error v. Posterior



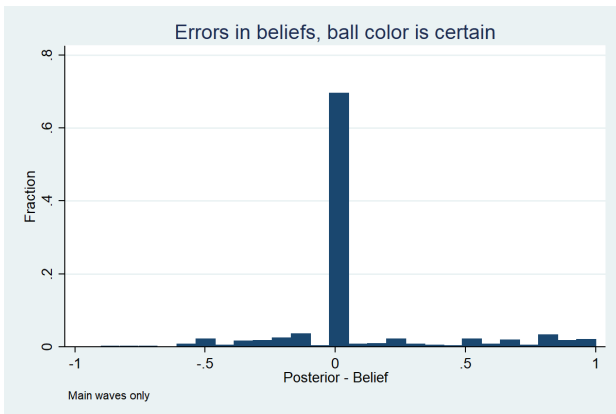
(c) Error Distribution, Uncertain Color



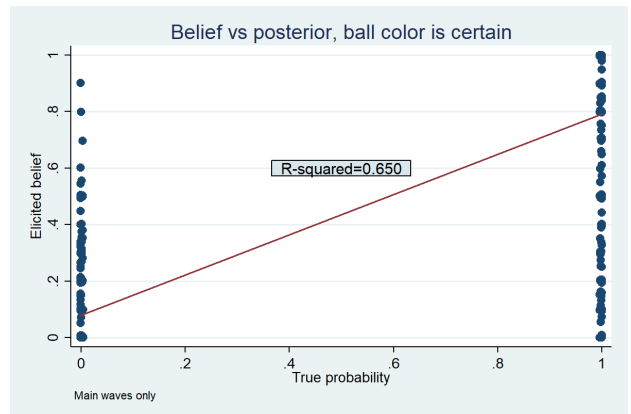
(d) Error v. Posterior, Uncertain Color



(e) Error Distribution, Certain Color



(f) Error v. Posterior, Certain Color



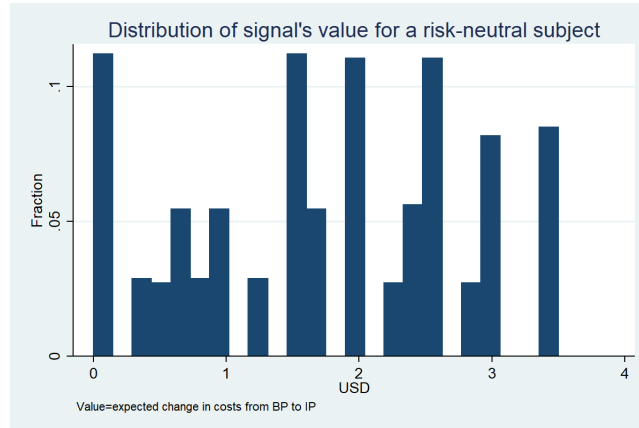
#### 4.4 Willingness-to-Pay Elicitation

The BP, IP, and BE tasks allow us to discern how individuals use freely provided information to make protection decisions, but signals are not necessarily provided freely. To better understand how subjects value the signals, we elicit their Willingness-to-Pay for signals of differing degrees of informativeness. Figure XX plots the distributions of the theoretically optimal WTP (Panel A), the distribution of actual WTP (Panel B), and the distribution of the discrepancies between the theoretical and actual WTP that we observe. WTP is bounded between \$0 and \$5, where the latter is because protection can be purchased for \$5 so if information were that valuable, an individual would just choose to protect. Reported WTP is centered around the theoretical WTP, suggesting that it is a useful benchmark. However, the variation is very substantial. Only 25% of actual WTP are within \$0.50 of the theoretical one, and subjects overvalue the signal by at least \$1.5 in 22% of cases and undervalue it by at least \$1.5 in 19% of cases.

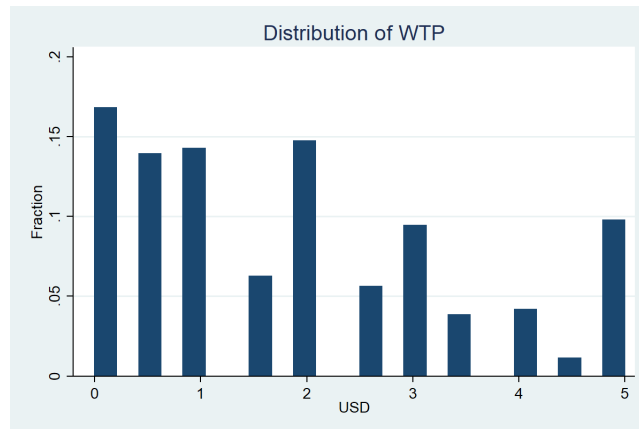


Figure 3: Willingness-to-Pay Distribution

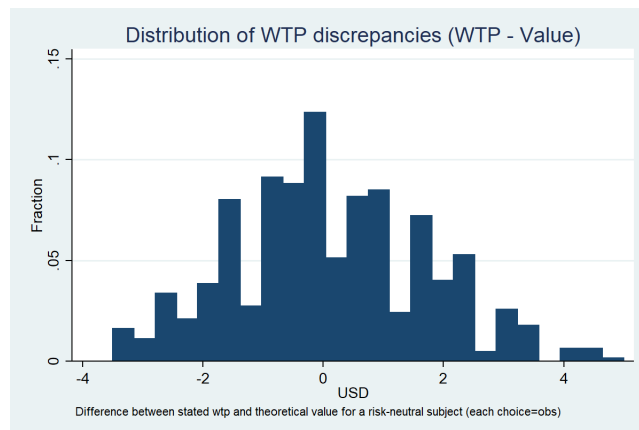
(a) Value Distribution



(b) WTP distribution



(c) Discrepancy (WTP-Value)



## 5 Signal characteristics and protection decisions

I like this structure, but eventually I think we want to put the hypotheses in an earlier section (e.g., with the model)

**Hypothesis 1.** *Conditional on posterior probability of a black ball, signal characteristics do not affect protection decisions.*

**Result 1.** *Conditional on posterior probability of a black ball, subjects' protection decisions still respond to the signals' false positive and false negative rates.*

In Table 2 we break out average protection decisions by signal characteristics. The first three columns summarize the information available to the subject, i.e., the signal as well as whether the signal might be either a false positive or false negative. Column 4 shows the posterior probability of a black ball averaged across all the treatments within a group, Column 5 the share protection among actual IP responses, Column 6 the share of protection under the RN optimum, and Column 7 the p-value of a t-test that actual and optimal choices use the same probability of protection.

First, we note that regardless of FP and FN rates, a hint that the ball is black substantially increases the share of protection decisions. **Second, subjects' protection decisions in the majority of treatments significantly deviate from what is optimal for risk-neutral subjects.** In general, subjects tend to overprotect when facing white signals (rows 1–4) and underprotect when facing black signals (rows 5–8). The exceptions are treatments with black signals and positive FP rates in which we cannot reject the hypothesis that the protection responses matches the response of a risk-neutral subject.

**In light of BP decisions it is not surprising that subjects do not behave as risk-neutral agents, but some biases cannot be explained by the expected utility maximization for any degree of risk aversion.** For example, consider the change in the protection rates between rows 1 and 3: the signal is white, so an increase in the signal's FP rate does not change the posterior, but the protection rate increases by 6 percentage points (pp.). Similarly, row 4 shows that when both FP and FN are positive, the protection rate increases to 56 percent — even though the average (maximum) posterior probability for the signal characteristics is just 13 percent. As a benchmark, with no signal in the BP task, only 13 (32) percent of subjects chose to protect when the probability is 10 (15) percent.

Table 2: Average Protection by Signal Type

Row	Signal Characteristics			Posterior	Share Protect	Share Optimal	P-val ( $H_0 : ShProt = ShOptimal$ )
	Signal	False Positive	False Negative				
	(1)	(2)	(3)	(4)	(5)	(6)	(7)
(1)	White	No	No	0.000	0.067	0.000	0.000
(2)	White	No	Yes	0.100	0.333	0.000	0.000
(3)	White	Yes	No	0.000	0.130	0.000	0.000
(4)	White	Yes	Yes	0.131	0.564	0.121	0.000
(5)	Black	No	No	1.000	0.846	1.000	0.000
(6)	Black	No	Yes	1.000	0.841	1.000	0.000
(7)	Black	Yes	No	0.550	0.833	0.870	0.355
(8)	Black	Yes	Yes	0.483	0.886	0.871	0.685

Notes:

**Hypothesis 2.** *Subjects’ Bayesian-updating errors explain IP decisions.*

Should this be something like “updating errors explain IP decisions, and updating errors are influenced by signal characteristics?”

**Result 2.** *When subjects received a signal that the ball is white, the signal’s false positive and false negative rates biased their belief upward. When subjects received a signal that the ball is black, the signal’s false positive (negative) rates biased their belief upward (downward). Updating errors provide partial explanation for subjects’ IP decisions conditional on posterior.*

We observe that many IP responses cannot be reconciled with expected utility maximization given posterior probability, but these EU violations can also emerge if subjects incorrectly estimate posteriors. Table 3 summarizes how the updating errors vary with signal characteristics. We find that subjects overestimate the probability of a black ball with a white signal. Introducing FP rates to the signal exacerbated their upward bias. To illustrate, consider the change between rows 1 and 3, where introducing a FP rate would not change the posterior because the signal is white. Yet, subjects update their posterior upward, magnifying their updating error. The FN rates also have a similar effect of exacerbating this upward bias for a white signal.

The updating bias for black signals, however, varies by information structure. When there is no risk of a false-positive signal (rows 5-6), subjects underestimate the probability of a black ball after receiving a black signal. **Not sure we need it here: This observation contrasts with the case of the white signal, for which introducing FP rates led subjects to overestimate the posterior instead.** Subjects slightly underestimate the probability even when the signal is honest, but introducing FN rates lead subjects to underestimate it further. To illustrate, the introduction of a FN rate given a black signal does not change the posterior rows 5 and 6, but subjects decrease their beliefs. When there is a risk of a false-positive (i.e.,  $FP > 0$ ), subjects again

overestimate the probability of a black ball with little difference in errors between treatments with FP events only and with both FP and FN events. It seems that, because the false-positive rate negatively affects the posterior, subjects fail to adjust their beliefs enough in response to FP rates.

Table 5 formalizes our analysis using a regression which allows to implicitly control for risk aversion with subject fixed effects. This also controls for a general inability to update though, right? Unlikely, because poor updating should reflect in slope heterogeneity not in intercepts. We estimate a linear regression of updating error (actual posterior - reported belief) on FP and FN rates by signal color. It provides support for the conclusions from Table 3: (i) subjects make positive (negative) updating errors for white (black) signals; (ii) FP rates induce an upward bias in subjects' estimates of the posterior; and (iii) FN rates induce an upward (downward) bias when the signal is white (black). This pattern can explain overprotection in the IP task with white signals when the FP rate is positive.

Table 3: Average Updating Error by Signal Type

Row	Signal Characteristics			Posterior	Updating Error*	P-val ( $H_0 : Error = 0$ )
	False Positive	False Negative	Signal			
	(1)	(2)	(3)	(4)	(5)	
(1)	No	No	White	0.000	0.050	0.000
(3)	No	Yes	White	0.100	0.122	0.000
(5)	Yes	No	White	0.000	0.122	0.000
(7)	Yes	Yes	White	0.131	0.218	0.000
(2)	No	No	Black	1.000	-0.163	0.000
(4)	No	Yes	Black	1.000	-0.279	0.000
(6)	Yes	No	Black	0.550	0.039	0.130
(8)	Yes	Yes	Black	0.483	0.048	0.021

Notes: \*Updating error = *Posterior* - *Belief*.

So far, errors in the posterior estimation seem to be consistent with biases observed in the Informed Protection task. It begs the questions of how much bias in the IP task remains after accounting for biases in beliefs. In Table 6, we regress informed protection decisions on FP and FN rates and flexible controls of both posteriors and reported beliefs:

$$Prob(s_{ij} = 1) = \text{Logit}(\alpha_i + \beta_1 FP + \beta_2 FN + Z(p_{ij}) + Z(\mu_{ij}) + \epsilon_{ij})$$

where  $s_{ij}$  is the protection decision of subject  $i$  in treatment  $j$ ,  $\alpha_i$  - subject FE,  $P_{10}$ ,  $P_{01}$  are FP and FN false positive and false negative rates and  $Z(p_{ij})$ ,  $Z(\mu_{ij})$  are the splines of corresponding variables  $P_{ij}$ ,  $\mu_{ij}$  to control for these variables in the flexible way. Each spline is a function  $Z(x)$  which is just linear  $x + C$  within one interval, and constant everywhere else. The splines are

Table 4: Belief Elicitation: When Mistakes Happen

	(1) All	(2) S=White	(3) S=Black
FP rate	.6*** (0.1)	.292*** (0.1)	.908*** (0.1)
FN rate	.0108 (0.1)	.273*** (0.1)	-.251*** (0.1)
Constant	-.0784*** (0.0)	.314*** (0.0)	-.47*** (0.0)
Subject FE	Yes	Yes	Yes
Observations	1248	624	624
Adjusted $R^2$	0.15	0.41	0.52

Standard errors in parentheses

Dep. variable: reported belief - posterior probability

\*  $p < 0.10$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$ 

Table 5: Updating Errors in BE Task

	All	Signal Received	
		White	Black
	(1)	(2)	(3)
FP rate	.6*** (0.1)	.292*** (0.1)	.908*** (0.1)
FN rate	.0108 (0.1)	.273*** (0.1)	-.251*** (0.1)
Constant	-.0784*** (0.0)	.314*** (0.0)	-.47*** (0.0)
Subject FE	Yes	Yes	Yes
Observations	1248	624	624
Adjusted $R^2$	0.15	0.41	0.52
Subject FE	Yes	Yes	Yes

Notes: Standard errors in parentheses. \*  $p < 0.10$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$ .

constructed so that their linear intervals cover the whole domain of probabilities and beliefs  $[0, 1]$ .<sup>8</sup> of posteriors and reported beliefs  $\mu_{ij}$  for corresponding treatments. Columns 1 and 2 include only the flexible controls of the true posteriors. Columns 3 and 4 add further flexible controls to account for subjects' (often incorrect) estimates of the posterior, inferred from their BE responses. The model is estimated using Maximum Likelihood Estimation, with standard errors clustered at the subject level. The table presents the average marginal effect coefficients.

Columns 1 and 2 confirmed Result 1, to wit, conditional on posterior and subject FE, IP responses are affected by FP and FN rates. For a white signal, FP and FN rates increased the tendency to overprotect; while for a black signal, FP rate had an opposite effect with comparable magnitude but without statistical significance. Column 3 suggests, however, that once we control for both the posterior and subjects' updated belief, only the effect of the FP rate for white signals remains positive and statistically significant at  $p < 0.1$ . **These results provide evidence that subjects' failure to protect optimally is largely — albeit not entirely — driven by their failure to correctly update their posterior given a signal.**

XXX DO WE NEED COLUMNS 2 and 4? XXX NOT SURE...

---

<sup>8</sup>We use Stata mkspline command to create 5 splines  $z_1(x), z_2(x), \dots, z_5(x)$  of initial variable  $x$  over the range  $[0, 1]$  such that  $z_k(x) = \min[0, x - x_{k-1}, x_k - x_{k-1}]$  with  $x_k$  being equally spaced knot values. Splines account for potential nonlinear effects of posteriors and beliefs on protection decision with limited effect on degrees of freedom.

Table 6: Informed Protection Response

	(1)	(2)	(3)	(4)
FP rate x (S=White)	.461*** (3.3)	.494** (2.4)	.282** (2.0)	.286 (1.4)
FN rate x (S=White)	.544*** (2.9)	.474** (2.1)	.195 (1.0)	.125 (0.5)
S=Black	.42*** (2.7)	.429*** (2.7)	.316** (2.0)	.336** (2.1)
FP rate x (S=Black)	-.256 (-0.5)	-.225 (-0.4)	-.379 (-0.8)	-.389 (-0.7)
FN rate x (S=Black)	.0494 (0.5)	-.027 (-0.2)	-.00394 (-0.0)	-.0879 (-0.6)
p=0.2	.113*** (4.2)	.101*** (2.8)	.09*** (3.6)	.0723** (2.1)
FP rate x (p=0.2)		-.0363 (-0.2)		.00218 (0.0)
FN rate x (p=0.2)		.122 (0.9)		.127 (0.9)
N	1224	1224	1224	1224
Pseudo R-squared	.551	.552	.578	.578
Log-likelihood	-379	-378	-356	-356
Subject FE	Yes	Yes	Yes	Yes
Flexible controls for:				
Posterior	Yes	Yes	Yes	Yes
Beliefs	No	No	Yes	Yes

*Notes:* Coefficients are average marginal effects. *t*-statistics in parentheses. Standard errors are clustered at the subject level. \*  $p < 0.10$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$ .

We have shown that signal characteristics both indirectly (through beliefs) and directly (white signals and false positives) influence protection decisions when signals are exogenously provided. It is far from clear which signal how signal characteristics should affect WTP decisions, however, where the theoretical benchmark had more limited explanatory power, and where any self-awareness of one’s inability to update might limit the value of information.

I do not see any significant evidence of bias in this table, except the last row, but then we do multiple testing too. Would rather write just that. Table 7 provides some preliminary evidence that, not only do signal characteristics influence WTP, they do so systematically in a way that suggests subjects are not aware of their own biases. When there is no possibility of a false positive, subjects underestimate the value of signal relative to the theoretical benchmark. Regardless of the possibility of a false negative, this difference is not statistically significant at conventional significance levels, though it is both 55% larger in magnitude and closer to significant ( $p = 0.152$ ) when there are false negatives. When there are both false positives and false negatives, however, subjects significantly overvalue signals relative to the theoretical benchmark. Can we plot the distributions of deviations for these 4 cases?

WE NEED A GOOD SEGUE TO REGRESSION AND DISCUSSION OF RESULTS, BUT I HAVE STOPPED HERE IN THIS SECTION

Table 7: Average WTP discrepancy (WTP-Value) by Signal Type

False-positive	False-negative	Mean WTP discrepancy	P(= 0)
No	No	-0.106	0.433
No	Yes	0.143	0.250
Yes	No	0.081	0.502
Yes	Yes	0.492	0.000

In Table ??, we use a regression analysis to investigate how and why subjects deviate from the risk-neutral subjects’ theoretical WTP for a signal of a given quality (conditional on prior). We first estimate how individual deviations from the theoretical benchmark  $b_s^*$  for a given signal  $s$  are correlated with signal’s characteristics:

$$b_{is} - b_s^* = \beta_0 + \beta_1 FalsePositive + \beta_2 FalseNegative + \epsilon_{is}$$

where  $b_{is}$  is the reported WTP of individual  $i$  for treatment  $s$  and  $b_s^*$  is the signal’s value for a risk-neutral subject, and FalsePositive (FalseNegative) is the false positive (false negative) costs variables that captures signal quality. We calculate false positive costs as the product of prior probability of a white ball multiplied by the conditional probability of getting a black signal (“The ball is black!”) from a randomly chosen gremlin:  $FalsePositive = (1 - \pi)P_{10}c$ . Similarly we calculate false negative costs as the probability of an adverse state multiplied by a conditional probability of getting a white signal conditional on the ball being black and multiplied by potential loss  $FalseNegative = \pi P_{01}L$ . Note that these costs already account



for expected frequency of receiving different incorrect signals as consistent with their base rate. If our subjects were risk neutral expected utility maximizers, we expect  $\beta_1$  and  $\beta_2$  to be zero.

Table 8: WTP for Information (tobit)

	(1)	(2)	(3)	(4)	(5)	(6)
	All	p=0.1	p=0.2	All	All	All
model						
FN costs	-.261*** (0.1)	-1.24** (0.5)	-.682*** (0.3)	-.407*** (0.1)	-.332*** (0.1)	-.316*** (0.1)
FP costs	-1.04*** (0.2)	-.647*** (0.2)	-.519** (0.3)	-.917*** (0.2)	-.754*** (0.2)	-.713*** (0.2)
BP costs				.362*** (0.1)	.353*** (0.1)	.373*** (0.1)
Belief change					.512** (0.2)	
Certainty						1.2** (0.5)
Constant	2.39*** (0.1)	1.79*** (0.2)	2.33*** (0.2)	.983*** (0.3)	.636** (0.3)	-.14 (0.6)
sigma						
Constant	1.94*** (0.1)	1.83*** (0.1)	1.7*** (0.1)	1.89*** (0.1)	1.88*** (0.1)	1.88*** (0.1)
Observations	624	159	153	624	624	624
Adjusted $R^2$						

Standard errors in parentheses

\*  $p < 0.10$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$

Column 1 of Table XX confirms that subjects' WTP deviated from the theoretical benchmark. Subjects did not fully account for signal quality, resulting in overpaying for signals with either high false-positive and false-negative costs. Naturally, two potential sources of deviations from this theoretical benchmark based on a risk-neutral Bayesian updater are subjects' risk-preferences and their ability to perform Bayesian updating. To test for these mechanisms, we interacted the false positive (FP) and false negative (FN) variables with individual risk aversion, whether individuals have accurate belief (as measured by our BE task), and the different priors.

Column 2 shows the results of the regression where the signal quality variables were interacted with the subject's risk preference.<sup>9</sup> This premium doesn't seem to come from risk aversion, as the coefficient on the interaction of risk aversion with FP and FN rates is relatively small and insignificant. Belief accuracy measured in the belief elicitation task apparently explains away the excess sensitivity to the FP rate but this finding should be taken with caution because the coefficient is not statistically significant despite its large absolute magnitude.

<sup>9</sup>Our risk preference estimates come from blind protection choice: subjects switching from no protection to protection at exactly the cost-loss ratio  $\pi = 0.2$  are considered risk-neutral, while switching at lower (higher) levels indicates risk aversion (risk-loving).

Table 9: WTP minus Value of Information (OLS)

	(1)	(2)	(3)	(4)	(5)
FP costs	.237*	.231*	.204	.448***	.412***
	(0.1)	(0.1)	(0.3)	(0.2)	(0.1)
FN costs	.353***	.319***	.232	.337***	-.635***
	(0.1)	(0.1)	(0.3)	(0.1)	(0.2)
Risk-loving			0		
			(.)		
Risk-averse			0		
			(.)		
No risk av. measure			0		
			(.)		
Risk-loving $\times$ FP costs			.165		
			(0.4)		
Risk-averse $\times$ FP costs			-.0197		
			(0.4)		
No risk av. measure $\times$ FP costs			.0244		
			(0.5)		
Risk-loving $\times$ FN costs			.177		
			(0.3)		
Risk-averse $\times$ FN costs			.0608		
			(0.3)		
No risk av. measure $\times$ FN costs			.114		
			(0.3)		
Inaccurate beliefs				.293**	
				(0.1)	
Inaccurate beliefs $\times$ FP costs				-.197	
				(0.5)	
Inaccurate beliefs $\times$ FN costs				.309	
				(0.2)	
plevel=200					-1.39***
					(0.2)
plevel=300					-1.37***
					(0.1)
plevel=500					0
					(.)
plevel=200 $\times$ FP costs					.162
					(0.2)
plevel=300 $\times$ FP costs					-.417***
					(0.2)
plevel=500 $\times$ FP costs					-.755*
					(0.4)
plevel=200 $\times$ FN costs					.828***
					(0.2)
plevel=300 $\times$ FN costs					.886***
					(0.2)
plevel=500 $\times$ FN costs					1.02***
					(0.2)
Constant	-.267	-.182**	-.184**	-.409***	.575***
	(0.2)	(0.1)	(0.1)	(0.1)	(0.1)
Observations	624	624	624	624	624
Adjusted R <sup>2</sup>	0.05	0.03	0.05	0.03	0.53

These results suggest that, on average, subjects failed to fully account for signal quality, resulting in overpaying for signals with high false-positive and false-negative costs. FP/FN significantly impact the deviation from the theoretical value no matter what else is included.

## 5.1 Summary

Table 10: Comparing Findings across the Tasks

Design	Beliefs	IP	WTP
White, FN only	>	<	<> *
Black, FN only	<	>	<>
White, FP only	>	<	<>
Black, FP only	<>	<>	<>
White, FN and FP	>>	<	>
Black, FN and FP	<>	<>	>

\*-WTP estimates do not depend on signals.

## 6 Subject Heterogeneity

Through out the foregoing results, we have seen both that signal characteristics influence behavior, but also substantial heterogeneity in choices. To better understand the interplay between these two forces, we estimate a latent class multinomial choice model of the following sort [includes the hint, FP and FN rates, and the interaction between the two](#)[We need a footnote here about model selection.](#)

Table 11: Latent Class Multinomial Choice Model Estimates (FP and FN rates by hint)

lc.results		Class	Alt	Hint	FN0	FN1	FP0	FP1	Class share
Model									
r1	1	1	-2.86694	4.392251	4.834518	-.1919326	4.35168	-.8676941	1
r2	2	1	-2.91958	1.881626	7.980388	-.3599557	1.725487	6.632253	.2198715
r3	2	2	-2.91958	6.699559	3.838407	.4707898	5.285504	-8.229022	.7801285

Table 12: IP response by class

	(1)	(2)
	Honesty Seekers	Cautious Bayesians
S=Black	.337***	.0245
	(3.4)	(0.4)
Prop. of lying gremlins	.664***	.277***
	(4.6)	(4.3)
Posterior prob.	-.198*	.788***
	(-1.7)	(4.9)
N	138	486
Pseudo R-squared	.183	.541
Log-likelihood	-67.2	-154

*t* statistics in parentheses

Errors are clustered by subject, average marginal treatment effects

\*  $p < 0.10$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$

## 7 Conclusion

Table 13: Belief Elicitation by Class

	(1) Simpletons	(2) Cautious Bayesians
Posterior prob.	.477*** (0.1)	.587*** (0.0)
S=Black	.0306 (0.1)	.126*** (0.0)
Prop. of lying gremlins	.175** (0.1)	.159*** (0.0)
Constant	.123*** (0.0)	.098*** (0.0)
Observations	276	972
Adjusted $R^2$	0.38	0.64

Standard errors in parentheses

Dep. variable: beliefs, errors clustered by subject

\*  $p < 0.10$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$

Table 14: Expected IP losses by strategy

	p=0.1,0.2			p>0.2		
	Mean loss	% of optimal	Loss prob.	Mean loss	% of optimal	Loss prob.
Baseline (all)	1.166304	156.7689	.0190281	2.11717	140.6088	.0508233
Honesty seekers	1.526998	205.2517	.0435806	3.095308	205.5705	.1163925
Bayesians	1.050706	141.2308	.0112388	1.806053	119.9464	.0300237
Optimal	.7439637	1	.0136432	1.505716	1	.0190598

Table 15: Belief Elicitation: When Mistakes Happen

	(1) All	(2) S=White	(3) S=Black
Simpletons	.0993*** (0.0)	-.258*** (0.0)	.457*** (0.0)
FN rate	.0437 (0.0)	.279*** (0.1)	-.192** (0.1)
Simpletons $\times$ FN rate	-.13 (0.2)	-.0124 (0.2)	-.248 (0.2)
FP rate	.562*** (0.1)	.258*** (0.1)	.866*** (0.1)
Simpletons $\times$ FP rate	.171 (0.2)	.171 (0.2)	.17 (0.3)
Constant	-.0802*** (0.0)	.315*** (0.0)	-.475*** (0.0)
Subject FE	Yes	Yes	Yes
Observations	1248	624	624
Adjusted $R^2$	0.15	0.42	0.52

Standard errors in parentheses

Dep. variable: reported belief - posterior probability

\*  $p < 0.10$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$

## References

- Ambuehl, Sandro and Shengwu Li (2018) “Belief updating and the demand for information,” *Games and Economic Behavior*, 109, 21–39, 10.1016/j.geb.2017.11.009.
- Benjamin, Daniel J. (2019) “Chapter 2 - Errors in probabilistic reasoning and judgment biases,” in Bernheim, B. Douglas, Stefano DellaVigna, and David Laibson eds. *Handbook of Behavioral Economics: Applications and Foundations 1*, 2 of Handbook of Behavioral Economics - Foundations and Applications 2, 69–186: North-Holland, 10.1016/bs.hesbe.2018.11.002.
- Bornstein, B. H. and A. C. Emler (2001) “Rationality in medical decision making: a review of the literature on doctors’ decision-making biases,” *Journal of Evaluation in Clinical Practice*, 7 (2), 97–107, 10.1046/j.1365-2753.2001.00284.x, Number: 2.
- Coutts, Alexander (2019) “Good news and bad news are still news: experimental evidence on belief updating,” *Experimental Economics*, 22 (2), 369–395, 10.1007/s10683-018-9572-5, Number: 2.
- Eil, David and Justin M. Rao (2011) “The Good News-Bad News Effect: Asymmetric Processing of Objective Information about Yourself,” *American Economic Journal: Microeconomics*, 3 (2), 114–138, 10.1257/mic.3.2.114, Number: 2.
- Eliaz, Kfir and Andrew Schotter (2010) “Paying for confidence: An experimental study of the demand for non-instrumental information,” *Games and Economic Behavior*, 70 (2), 304–324, 10.1016/j.geb.2010.01.006, Number: 2.
- Gigerenzer, Gerd, Wolfgang Gaissmaier, Elke Kurz-Milcke, Lisa M. Schwartz, and Steven Woloshin (2007) “Helping Doctors and Patients Make Sense of Health Statistics,” *Psychological Science in the Public Interest: A Journal of the American Psychological Society*, 8 (2), 53–96, 10.1111/j.1539-6053.2008.00033.x, Number: 2.
- Grether, David M. (1980) “Bayes Rule as a Descriptive Model: The Representativeness Heuristic,” *The Quarterly Journal of Economics*, 95 (3), 537–557, 10.2307/1885092, Publisher: Oxford University Press.
- (1992) “Testing bayes rule and the representativeness heuristic: Some experimental evidence,” *Journal of Economic Behavior & Organization*, 17 (1), 31–57, 10.1016/0167-2681(92)90078-P, Number: 1.
- Hammerton, M. (1973) “A case of radical probability estimation,” *Journal of Experimental Psychology*, 101 (2), 252–254, 10.1037/h0035224, Number: 2 Place: US Publisher: American Psychological Association.
- Hoffman, Mitchell (2016) “How is Information Valued? Evidence from Framed Field Experiments,” *The Economic Journal*, 126 (595), 1884–1911, 10.1111/eoj.12401, Number: 595.
- Holt, Charles A. and Angela M. Smith (2009) “An update on Bayesian updating,” *Journal of Economic Behavior & Organization*, 69 (2), 125–134, 10.1016/j.jebo.2007.08.013, Number: 2.
- Howard, Kirsten and Glenn Salkeld (2009) “Does Attribute Framing in Discrete Choice Experiments Influence Willingness to Pay? Results from a Discrete Choice Experiment in Screening for Colorectal Cancer,” *Value in Health*, 12 (2), 354–363, 10.1111/j.1524-4733.2008.00417.x, Number: 2.
- Kahneman, Daniel and Amos Tversky (1972) “Subjective probability: A judgment of representativeness,” *Cognitive Psychology*, 3 (3), 430–454, 10.1016/0010-0285(72)90016-3.

- (1973) “On the psychology of prediction,” *Psychological Review*, 80 (4), 237–251, 10.1037/h0034747, Number: 4 Place: US Publisher: American Psychological Association.
- Karni, Edi (2009) “A Mechanism for Eliciting Probabilities,” *Econometrica*, 77 (2), 603–606, <https://ideas.repec.org/a/ecm/emetrp/v77y2009i2p603-606.html>, Number: 2 Publisher: Econometric Society.
- Laury, Susan K., Melayne Morgan McInnes, and J. Todd Swarthout (2009) “Insurance decisions for low-probability losses,” *Journal of Risk and Uncertainty*, 39 (1), 17–44, 10.1007/s11166-009-9072-2, Number: 1.
- Liang, Wenchi, William F. Lawrence, Caroline B. Burnett, Yi-Ting Hwang, Matthew Freedman, Bruce J. Trock, Jeanne S. Mandelblatt, and Marc E. Lippman (2003) “Acceptability of diagnostic tests for breast cancer,” *Breast Cancer Research and Treatment*, 79 (2), 199–206, 10.1023/a:1023914612152, Number: 2.
- Masatlioglu, Yusufcan, A. Yesim Orhun, and Collin Raymond (2017) “Intrinsic Information Preferences and Skewness,” September, 10.2139/ssrn.3232350, Issue: 3232350.
- Neumann, Peter J., Joshua T. Cohen, James K. Hammitt, Thomas W. Concannon, Hannah R. Auerbach, Chihui Fang, and David M. Kent (2012) “Willingness-to-pay for predictive tests with no immediate treatment implications: a survey of US residents,” *Health Economics*, 21 (3), 238–251, 10.1002/hec.1704, Number: 3.
- Phillips, Lawrence D. and Ward Edwards (1966) “Conservatism in a Simple Probability Inference Task,” *Journal of Experimental Psychology*, 72 (3), 346, 10.1037/h0023653.
- Schwartz, Lisa M., Steven Woloshin, Floyd J. Fowler, and H. Gilbert Welch (2004) “Enthusiasm for cancer screening in the United States,” *JAMA*, 291 (1), 71–78, 10.1001/jama.291.1.71, Number: 1.
- Tversky, Amos and Daniel Kahneman (1971) “Belief in the law of small numbers,” *Psychological Bulletin*, 76, 105–110, 10.1037/h0031322, Place: US Publisher: American Psychological Association.
- Volkman-Wise, Jacqueline (2015) “Representativeness and managing catastrophe risk,” *Journal of Risk and Uncertainty*, 51 (3), 267–290, 10.1007/s11166-015-9230-7, Number: 3.



## A Tables

Table 16: Demographic Characteristics of Subjects

	All		$p \in \{0.1, 0.3\}$		$p \in \{0.2, 0.5\}$	
	N	%	N	%	N	%
Male	43	41	22	41	21	41
Age>23yrs old	14	13	6	11	8	16
Students	88	84	46	85	42	82
Had statistics classes	63	60	37	69	26	51
Total	105	100	54	100	51	100

Table 17: Risk Aversion Measurement

Switching Probability ( $\pi^*$ )	$\theta$	$N$
Always protect	$>2$	1
0.1	2	10
0.15	1.216	13
0.2	0.573	29
0.25	0	16
0.3	-0.539	15
Never protect	$<-0.539$	14

	(1)	(2)	(3)	(4)	(5)	(6)
	OLS	FE	OLS	FE	OLS	FE
Prior	.246*** (5.5)	.202*** (4.0)	.175*** (3.1)	.191** (2.5)	.14** (2.3)	.0403 (0.6)
Signal	.43*** (6.3)	.43*** (6.3)	.327*** (3.2)	.327*** (3.2)	.539*** (5.3)	.539*** (5.3)
Good quiz $\times$ Prior			.143* (1.7)	.0207 (0.2)		
Good quiz $\times$ Signal			.193 (1.4)	.193 (1.4)		
Stat. class $\times$ Prior					.162* (1.9)	.264*** (2.8)
Stat. class $\times$ Signal					-.166 (-1.2)	-.166 (-1.2)
Observations	280	280	280	280	280	280
Adjusted $R^2$	0.31	0.31	0.33	0.32	0.32	0.32

Decomposition works only for imperfect signals

\*  $p < 0.10$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$

Table 18: Informed protection response: logistical regression

	(1) All	(2) S=White	(3) S=Black	(4) All	(5) S=White	(6) W=Black	(7) S=White	(8) W=Black
FP rate	.276*** (3.0)	.473*** (4.1)	.0276 (0.2)	.297*** (3.1)	.726*** (4.0)	.161 (0.5)	.915*** (3.9)	.447*** (0.6)
FN rate	.612*** (7.7)	1.02*** (11.4)	.00397 (0.0)	.596*** (7.7)	1.31*** (16.7)	-.0491 (-0.2)	1.53*** (8.2)	-.0001 (-0.0)
S=Black	.456*** (60.6)			.469*** (61.1)				
plevel=200	.106*** (2.8)	.0911* (1.9)	.121** (2.2)	0 (.)	0 (.)	0 (.)	0 (.)	0 (.)
plevel=300	.167*** (6.7)	.163*** (6.2)	.17*** (4.0)	0 (.)	0 (.)	0 (.)	0 (.)	0 (.)
plevel=500	.174*** (4.5)	.202*** (4.1)	.147*** (2.7)	0 (.)	0 (.)	0 (.)	0 (.)	0 (.)
FP rate x FN rate							-1.37 (-1.3)	.447*** (0.6)
Subject FE	No	No	No	Yes	Yes	Yes	Yes	Yes
P(FP rate $\neq$ FN rate)	.004	.00138	.891	.00714	.01	.6	.00861	.500
N	1248	624	624	1224	450	252	450	252
Pseudo R-squared	.356	.22	.0383	.497	.516	.204	.521	.204
Log-likelihood	-553	-275	-253	-424	-137	-132	-135	-135

*t* statistics in parentheses

Errors are clustered by subject, average marginal treatment effects

\*  $p < 0.10$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$

Table 19: Informed Protection Response: logit with flexible control for posteriors

	(1)	(2)	(3)	(4)
FP rate	.365*** (3.3)	.461*** (3.3)	.583*** (3.1)	.494** (2.4)
FN rate	.169* (1.8)	.544*** (2.9)	.126 (1.0)	.474** (2.1)
p=0.2	.0637** (2.1)	.113*** (4.2)	.0946*** (2.7)	.101*** (2.8)
S=Black	.0421 (0.7)	.42*** (2.7)	.0141 (0.2)	.429*** (2.7)
FP rate x (S=Black)		-.716 (-1.5)		-.719 (-1.5)
FN rate x (S=Black)		-.495** (-2.2)		-.501** (-2.1)
FP rate x (p=0.2)			-.185 (-1.1)	-.0363 (-0.2)
FN rate x (p=0.2)			.0806 (0.5)	.122 (0.9)
Observations	1248	1224	1224	1224
Adjusted $R^2$				

$t$  statistics in parentheses

Reporting average marginal effects, subject FE, errors are clustered by subject.

With flexible controls of posterior probability

\*  $p < 0.10$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$

Table 20: WTP for Information (tobit)

	(1)	(2)	(3)	(4)	(5)	(6)
	All	p=0.1	p=0.2	All	All	All
model						
FN costs	-.261*** (0.1)	-1.24** (0.5)	-.682*** (0.3)	-.407*** (0.1)	-.332*** (0.1)	-.316*** (0.1)
FP costs	-1.04*** (0.2)	-.647*** (0.2)	-.519** (0.3)	-.917*** (0.2)	-.754*** (0.2)	-.713*** (0.2)
BP costs				.362*** (0.1)	.353*** (0.1)	.373*** (0.1)
Belief change					.512** (0.2)	
Certainty						1.2** (0.5)
Constant	2.39*** (0.1)	1.79*** (0.2)	2.33*** (0.2)	.983*** (0.3)	.636** (0.3)	-.14 (0.6)
sigma						
Constant	1.94*** (0.1)	1.83*** (0.1)	1.7*** (0.1)	1.89*** (0.1)	1.88*** (0.1)	1.88*** (0.1)
Observations	624	159	153	624	624	624
Adjusted $R^2$						

Standard errors in parentheses

\*  $p < 0.10$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$

	(1)	(2)	(3)	(4)
model				
FP rate	-4.43 (2.8)	-5.88* (3.3)	-4.76* (2.8)	-6.17* (3.3)
FN rate	-2.35** (1.2)	-1 (1.6)	-2.7* (1.4)	-1.46 (1.8)
Stat. class			-.441* (0.2)	-.436* (0.2)
Stat. class $\times$ FP rate			.809 (1.1)	.762 (1.1)
Stat. class $\times$ FN rate			.568 (1.1)	.609 (1.1)
Constant	1.46*** (0.2)	1.25*** (0.4)	1.77*** (0.3)	1.55*** (0.4)
sigma				
Constant	1.88*** (0.1)	1.88*** (0.1)	1.87*** (0.1)	1.87*** (0.1)
With squares	No	Yes	No	Yes
Observations	630	630	630	630
Adjusted $R^2$				

Controlling for priors and total probabilities of false-positive and false-negative outcomes. Standard errors in parentheses

\*  $p < 0.10$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$

	(1)	(2)	(3)	(4)	(5)	(6)
	OLS	FE	OLS	FE	OLS	FE
Prior	.246*** (5.5)	.202*** (4.0)	.175*** (3.1)	.191** (2.5)	.14** (2.3)	.0403 (0.6)
Signal	.43*** (6.3)	.43*** (6.3)	.327*** (3.2)	.327*** (3.2)	.539*** (5.3)	.539*** (5.3)
Good quiz $\times$ Prior			.143* (1.7)	.0207 (0.2)		
Good quiz $\times$ Signal			.193 (1.4)	.193 (1.4)		
Stat. class $\times$ Prior					.162* (1.9)	.264*** (2.8)
Stat. class $\times$ Signal					-.166 (-1.2)	-.166 (-1.2)
Observations	280	280	280	280	280	280
Adjusted $R^2$	0.31	0.31	0.33	0.32	0.32	0.32

Decomposition works only for imperfect signals

\*  $p < 0.10$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$

Table 21: Informed Protection Response: flexible control for posteriors and beliefs

	(1)	(2)	(3)	(4)	(5)	(6)
		FE			S=White	S=Black
FP rate	.226** (2.0)	.252* (1.8)	.383** (2.0)	.256* (1.8)	.273** (2.3)	.129 (0.3)
FN rate	.0783 (0.8)	.014 (0.2)	-.037 (-0.3)	.0677 (0.4)	.0615 (0.4)	.0738 (0.6)
p=0.2			.07** (2.1)			
FP rate x (p=0.2)			-.128 (-0.8)			
FN rate x (p=0.2)			.0907 (0.7)			
S=Black				.164 (1.1)		
FP rate x (S=Black)				-.481 (-1.0)		
FN rate x (S=Black)				-.0587 (-0.3)		
Observations	1248	1224	1224	1224	624	624
Adjusted $R^2$						

$t$  statistics in parentheses

With flexible controls of posterior probability and beliefs

Errors are clustered by subject, average marginal treatment effects

\*  $p < 0.10$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$

Table 22: Informed protection response: semiparametric control for posteriors

	(1)	(2)	(3)	(4)
FP rate	.414*** (4.2)	.463*** (2.8)	.449*** (4.2)	.322** (2.4)
FN rate	.0152 (0.1)	-.0509 (-0.3)	-.0771 (-0.3)	.0573 (0.4)
p=0.2		.0471 (1.3)		
FP rate x (p $\geq$ 0.2)		-.0368 (-0.2)		
FN rate x (p $\geq$ 0.2)		.0969 (0.5)		
S=Black			.0801 (0.5)	
FP rate x (S=Black)			-.41 (-1.0)	
FN rate x (S=Black)			.12 (0.5)	
Stat. class				-.0101 (-0.3)
FP rate x Stat. class				.163 (1.1)
FN rate x Stat. class				-.0696 (-0.5)
Observations	1248	1248	1248	1248
Adjusted $R^2$	0.01	0.01	0.01	0.01

*t* statistics in parentheses\*  $p < 0.10$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$ 

Table 23: WTP - Value of Information, by prior

	(1)	(2)	(3)	(4)	(5)
	All	0.1	0.2	0.3	0.5
FP rate	.822* (0.5)	1.96*** (0.7)	2.3*** (0.7)	-.121 (0.9)	-.865 (0.9)
FN rate	1.2*** (0.4)	-1.24*** (0.4)	.783 (0.5)	1.57*** (0.6)	3.79*** (0.7)
Constant	-.134 (0.1)	.435*** (0.1)	-.713*** (0.1)	-.921*** (0.1)	.677*** (0.2)
Observations	630	162	153	162	153
Adjusted $R^2$	0.36	0.64	0.49	0.42	0.48

Standard errors in parentheses

\*  $p < 0.10$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$

B Figures

Figure 4: Theoretical vs actual WTP

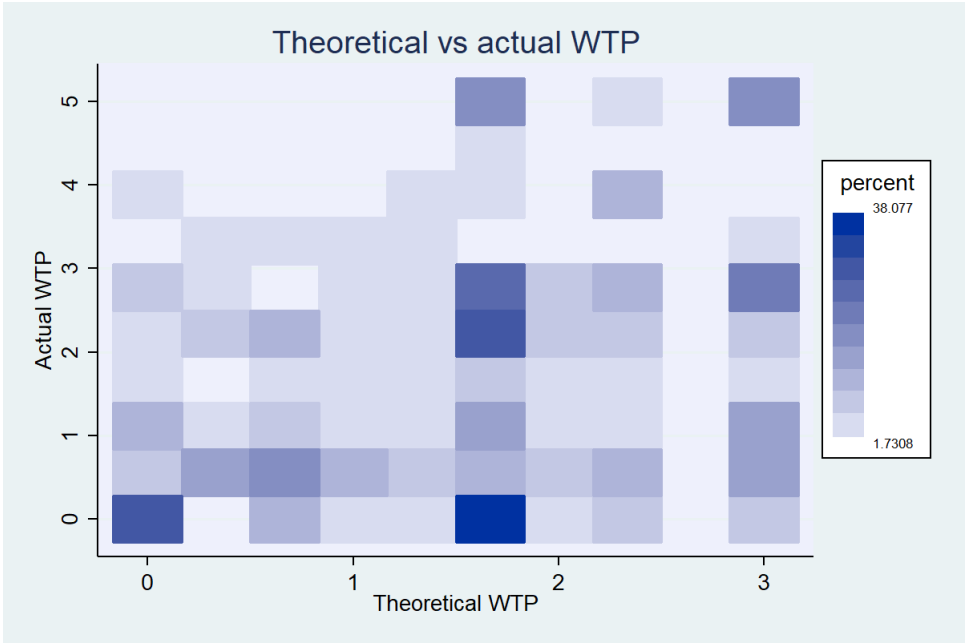


Figure 5: WTP discrepancy

