Crying Wolf in the Lab

Arya Gaduh, Peter McGee, Alexander Ugarov*

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Abstract

Designing multiple kinds of signals involves trade-offs between false-positive and false-negative costs. We conduct a laboratory experiment to evaluate preferences over these trade-offs in a controlled environment. We find that the choices significantly diverge from the predictions of the model with a risk-neutral model expected utility maximizers as well as from some predictions of expected utility frameworks. Subjects' willingness-to-pay for signals exhibits excessive sensitivity to false-negative rates for low priors, but lower sensitivity for high priors. Subjects preferences demonstrate a reverse bias for false-positive rates. We find that this pattern is not consistent with the EU framework, but most consistent with decision-making heuristic in which subjects do not differentiate between false-positive and false-negative rates when choosing signals.

Keywords: alarms, value of information, information economics, information design, medical tests, —

1 Introduction

The 2010 gas blowout on Deep Horizon oil rig has killed 11 workers and caused one of the largest oil spills in history. The death toll was possibly aggravated by switching off a general safety alarm because its sirens interfered with workers' sleep.[1] This illustrates the trade-off between false-positive and false-negative test results with false-positive rates leading to higher false alarm costs and false-negative resulting in missed events.

Many real-life situations involve choosing binary tests to discover and prevent a negative outcome. Most binary tests transform continuous signals about the likelihood of an adverse state into simple yes/no prediction. This transformation relies on choosing a threshold for positive classification. Holding a continuous signal constant, a decrease in probability of no alarm in an adverse state (false-negative rate) corresponds to an increase in probability of alarm in a non-adverse state (false-positive rate). This trade-off motivates multiple discussions in medical diagnostics, alarm systems and extreme weather alerts. Despite ubiquity of binary alarms, there is little empirical evidence on how users evaluate alarms with different false-positive and false-negative rates.

In order to understand preferences over these trade-offs, we study the demand for information in the framework with a potential protection action. The subject, first, receives a signal about the probability of an adverse event. Then she decides to protect or not. This environment describes several practically important scenarios including extreme weather alerts, medical testing and safety alarms.

We find that the value of information in our setup weakly correlates with the willingness-to-pay. First, subjects on average underreact to quality of the signal, resulting in overpaying for low-quality signal and underpaying for high-quaity signals. Second, subjects tend to overreact to false-negative rates when the prior probability is low and overreact to false-positive positive rates when priors are high. We show that this pattern is most consistent with failure to estimate the effect of frequencies of false-positive and false-negative outcomes on the costs of using the signal. (**?**) similarly finds that individuals do not properly account for priors and often choose tests not affecting optimal decisions even when more useful tests are available.

Our work is one of a few experimental studies measuring demand for information used for decision-making (instrumental information). Previous experimental studies studies the demand for signals in the prediction game in which subjects have to choose an optimal state under uncertainty. The field experiment conducted by (**?**) finds that the demand for information increases with initial uncertainty, but decreases with the signal's accuracy. However, the decrease in accuracy is more modest than expected for a Bayesian decision-maker resulting in subjects underpaying for high-quality signals. The laboratory experiment of **?** finds that subjects tend to underreact to the accuracy of the binary signal about state of the world, but put a premium on completely certain signals. The paper of **?** also employs a prediction game setup

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[1]https://www.nytimes.com/2010/07/24/us/24hearings.html

to measure information preferences but varies priors on top of signal characteristics. She finds that many subjects choose non-instrumental over instrumental signals which is most consistent with failures of contingent reasoning on future value of information.

Our setup differs in two important aspects from (**??**), because we study alerts and not prediction tasks. The subject faces a costly protection decision and not a prediction decision, resulting in three distinct payoffs: full payoff, full payoff minus protection costs and full payoff minus losses. It means that risk preferences affect the value of information and can change sensitivities to false-positive and false-negative rates. Our findings however are similar to prediction game findings. Consistent with **?** we also find that subjects overvalue inaccurate signals, but we do not find a premium for certain signals. And similar to **?** we find that subjects commit reasoning errors leading to lower correlation between preferences and signal's usefulness in terms of cost reduction.

Due to its applicability for studying preferences over expectations, there is a larger stream of literature on the demand for non-instrumental information. **?** find that subjects are willing to pay for signals even when these signals are excessive for making optimal choices. Their design involves subjects choosing between two boxes with one box containing a prize of $20. Most subjects pay just to know the probability of finding $20 in box A even if this box is more likely to contain a prize in all the possible states. This finding is inconsistent with expected utility maximization but indicates instead having preferences for certainty before making choices. Similar to this paper, **?** also study preferences over information structures differing in false-positive and false-negative rates but their setup allows for a larger role of expectations. They find that for a positive potential outcome, most subjects prefer facing high false-negative rates rather than high false-positive rates. In other words, they tolerate uncertainty after negative signals better than uncertainty after positive signals. These preferences are salient: subjects require an average payment of 18-35 cents to switch to their least preferred information structure.

There is some mixed evidence that people update beliefs differently when these beliefs are ego-relevant or concern future gains and losses. **?** find asymmetry in updating ego-relevant beliefs such as beauty and IQ. Subjects update more after receiving positive signals and do not update enough after negative signals. Additionally, subjects with high posterior ego-relevant beliefs are willing to pay to receive a more precise signals, but require a compensation for learning when their beliefs are low. In contrast, **?** does not find any updating asymmetry with respect to either ego-relevant beliefs or beliefs about future payoffs.

Our paper is the first to measure value of information in the experimental setting of diagnostic tests or alarms. Previous work studies the use of alarms in context of medical testing, medical monitoring, safety alarms and extreme weather. Early literature on decision-making of medical professionals finds that doctors suffer from multiple biases when ordering testing, including inaccurate posterior probability estimation due to availability heuristics, hindsight bias and regret (**?**). **?** find that most mammologists tend to overestimate the probability of cancer based on a positive result. Providing practitioners with natural frequencies instead of

probabilities tends to reduce this bias.

Patients' willingness-to-pay for medical tests is large and sensitive to test accuracy (**???**). But test preferences also exhibit several abnormalities. First, users are willing to pay for tests having little or zero diagnostic value (**??**). For example, **?** find that 73% of Americans in their survey prefer a free full-body CT scan versus one thousand USD cash. However, medical professional do not recommend full-body CT scans for healthy people due to extreme likelihood of false-positive findings. Second, the framing of test accuracy seems to matter a lot. **?** conduct a discrete-choice experiment to measure willingness-to-pay for the colorectal cancer screening. Their subjects agree to get 23 unnecessary colonoscopies in order to find one additional true cancer, but only 10.4 for reducing the number of cancers missed by one even though these descriptions are equivalent. Surprisingly, the perceived risk of cancer (prior) did not significantly affect the WTP in their study.

Our work also relates to the vast literature on demand for insurance and protection. Similar to our findings, several studies observe that the demand for insurance goes up after the recent experience with low probability events. Field evidence indicates that people under-insure with respect to rare natural disasters (Friedl et al, 2014). **?** find no under-insurance for low-probability events in the laboratory setting. One offered explanation (**?**) is that subjects overweight recent evidence leading to under-insurance when there were no negative events in the recent past and to overinsurance after the fact. It is consistent with underweighting prior probabilities relative to more recent signals.

The bias we are finding is similar to the base-rate and signal neglect phenomenons. Psychology researchers **?** and **?** first observed that subjects underweighted prior probabilities (base rates) when calculating posteriors. This phenomenon had received the name of *base-rate neglect*. Multiple studies in economics then confirmed (**??**) this phenomenon in incentivized laboratory experiments. Most of these studies find that subjects also underweight signals on top of priors. We observe both phenomenons in responses to our belief elicitation task, but the calculation of signals' values differs substantially from the calculation of posterior probabilities. While the calculation of posterior probabilities would require using a Bayes formula, signal's value depends only on products of prior probabilities. However, we observe that subjects underestimate the effect of priors compared to theoretical predictions for an expected-utility decision-maker.

2   Model

Environment.   Consider an agent's purchase of threat assessment information. Let $\omega \in \{0, 1\}$ denote the state of world, where 1 corresponds to an adverse event happening with probability π. Without a protective action, the agent has a lower utility in the adverse state. The protective action $a \in \{0, 1\}$ employs a perfect technology: agents bear no losses when protected. Its cost is c. Preferences are described by the utility function which depends on the state of the world ω, wealth Y, protective action a, and the potential loss in an adverse state $L > c$. Utility is

separable in wealth, protection cost and the potential loss in the adverse state:[2]

$$U = U(Y, a, \omega(1 - a)) = u(Y - ac - \omega(1 - a)L) \tag{1}$$

The agent can purchase a binary informative signal $s \in \{0, 1\}$ about the state of the world before making a decision. Let $P_{ij} \equiv P(s = i | \omega = j)$ be the probability of a signal s taking value i conditional on the state of the world being j. After receiving the signal, the agent updates her belief on the likelihood of the bad state to $\mu(s)$. Unless specified otherwise, we assume that she is Bayesian and her posterior belief equals:

$$\mu(s) = \frac{\pi P_{s1}}{\pi P_{s1} + (1 - \pi)P_{s0}} \tag{2}$$

Without loss of generality, we also assume that a higher signal means a higher posterior probability of an adverse event $\mu(1) \geq \mu(0)$. Otherwise we can always re-label the signals.

Preferences. If there is no signal, the agent protects if and only if it increases her expected utility:

$$EU_0 = \max[u(Y - c), \pi u(Y - L) + (1 - \pi)u(Y)] \tag{3}$$

The signal can increase expected utility if the agent reacts differently to positive and negative signals. Under these assumptions, her expected utility with a signal is:

$$EU_s = \pi P_{11}u(Y - c) + \pi P_{01}u(Y - L) + (1 - \pi)P_{10}u(Y - c) + (1 - \pi)P_{00}u(Y) \tag{4}$$

We consider the maximum amount b which the agent is willing to pay for the signal. In our framework, b is the price such that an agent is indifferent between paying b to have the signal and not having a signal. Because the agent can always ignore a useless signal, the signal's value is bounded from below by zero. Hence it equals to the maximum between zero and the solution to the following equation:

$$
\begin{aligned}
P(s = 1)u(Y - b - c) + \pi P_{01}u(Y - b - L) + (1 - \pi)P_{00}u(Y - b) = \\
= \max[u(Y - c), \pi u(Y - L) + (1 - \pi)u(Y)]
\end{aligned} \tag{5}
$$

Here we use $P(s = 1) \equiv \pi P_{11} + (1 - \pi)P_{10}$ to denote the probability of a positive signal (alert). The left-hand side expression of this equation is a strictly decreasing function of b. Additionally, for $b \to \infty$ the left-hand side is smaller than the right-hand side. It implies that

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[2]Separability condition does not impose additional restrictions on the utility function U as long as the variation in wealth has limited range. More specifically, if $Y \in [Y_{min}, Y_{max}]$ and $c < Y_{max} - Y_{min}, L < c + (Y_{max} - Y_{min})$, then the function $u(\cdot)$ can be constructed from segments of $U(\cdot, 0, 0), U(\cdot, 1, 0), U(\cdot, 0, 1)$. While the resulting function $u(\cdot)$ is not necessarily monotonic, it is likely to be monotonic if protective actions and potential damages are relatively high.

the equation (5) above has a at most one positive solution.

Obviously, perfectly accurate signals always have positive value $b > 0$ because the payoff distribution with the signal first-order stochastically dominates the distribution without the signal. However, it is harder to determine the value of the imperfect signal without imposing more restrictions on preferences as it requires weighing $u(Y - L)$ against $u(Y - c)$.

Risk-neutral agent. If the agent is risk-neutral, the expression above collapses to:

$$b + P(s = 1)c + \pi P_{01} L = \min[c, \pi L]$$

The signal's value is just:

$$b = \max[0, \min[c, \pi L] - P(s = 1)c - \pi P_{01} L] \tag{6}$$

We can express the WTP b as a function of priors, false-positive, and false-negative rates. This is the equation we use in our empirical work:

$$b = \max[0, \min[c, \pi L] - \pi(1 - P_{01})c - (1 - \pi)P_{10}c - \pi P_{01} L] \tag{7}$$

The sensitivity of (positive) value b with respect to false-positive P_{10} and false-negative P_{01} rates is given by:

$$\frac{db}{dP_{10}} = -(1 - \pi)c \tag{8}$$

$$\frac{db}{dP_{01}} = -\pi(L - c) \tag{9}$$

Both false-positive and false-negative rates decrease the (positive) signal's value. The effect is proportional to the adverse state probability for the false-negative rate and to the non-adverse state probability for the false-positive rates.

Risk Aversion Effects. In a more general expected utility framework, risk aversion can both increase and decrease the signal's value. More specifically, risk aversion decreases the value when the protection costs are low:

Proposition 1. *If protection costs are low $c < \pi L$, then a strictly risk-averse decision-maker pays less than a risk-neutral one.*

Proof. If protection costs are low enough $c < \pi L$ than the risk-neutral decision-maker should

always protect without a signal:

$$U = \max[\pi(Y - L) + (1 - \pi)Y, Y - c] = Y - c$$

It means that a strictly risk-averse decision-maker with a utility function $u()$ should also protect:

$$\pi u(Y - L) + (1 - \pi)u(Y) < u(\pi(Y - L) + (1 - \pi)Y) = u(Y - c)$$

Then denote stochastic payoff with a signal as X so that expected utility with a signal is $Eu(X - b)$ where b is the willingness-to-pay solving:

$$Eu(X - b) = u(Y - c)$$

Let b_0 be the willingness-to-pay for a risk-neutral decision-maker. By Jensen's inequality:

$$Eu(X - b_0) < u(EX - b_0) = u(Y - c) = Eu(X - b)$$

Because expected utility with a signal is a decreasing function of b_0 we obtain $b > b_0$. $\qquad\square$

It is harder to make definite statements for lower risks or higher protection costs. For example, risk aversion increases value of a perfect signal as long as risk-averse decision-maker still chooses to not protect without a signal. This follows from the standard argument of increasing demand for insurance with risk aversion and the fact that the protection problem with a perfect signal is isomorphic to the insurance problem with deductible c.

Next, we study the effect of false-positive and false-negative rates on the signal's value b. Assuming a differentiable utility function $u()$ we use implicit differentiation to derive sensitivities of WTP b to false-positive and false-negative rates:

$$\frac{db}{dP_{10}} = -\frac{(1 - \pi)(u(Y - b) - u(Y - c - b))}{D(\pi, P_{01}, P_{10}, b)}$$

$$\frac{db}{dP_{01}} = -\frac{\pi(u(Y - c - b) - u(Y - L - b))}{D(\pi, P_{01}, P_{10}, b)}$$

With the denominator equal to the expected marginal utility:

$$D(\pi, P_{01}, P_{10}, b) \equiv P(S = 1)u'(Y - c - b) + \pi P_{01}u'(Y - L - b)+$$

$$+(1 - \pi)P_{00}u'(Y - b) = E[MU] > 0$$

It is clear that the signal's value decreases with false-positive and false-negative rates $\frac{db}{dP_{10}}, \frac{db}{dP_{01}} < 0$. We can also say a bit more about the sensitivity to false-negative rates:

Proposition 2. *Risk-averse and imprudent decision-maker has higher sensitivity to false-negative rates as compared to a risk-neutral one.*

Proof. Use the mean value theorem to rewrite the sensitivity as:

$$\frac{db}{dP_{01}} = -\frac{\pi u'(\zeta)(L-c)}{E[MU]}, \zeta \in (Y-c-b, Y-L-b)$$

Now let X denote a random payoff of the agent with a signal. A risk-averse decision-maker puts a positive value on the signal only if its expected payoff is higher than the payoff with full protection: $EX > Y - c - b$. If an agent is imprudent ($u''' < 0$) then $E[MU] \equiv E[u'(X)] < u'(EX)$. Next, u' being a strictly increasing function and $EX > Y-c-b$: $u'(\zeta) > u'(Y-c-b) > u'(EX)$. Hence $\frac{u'(\zeta)}{E[MU]} > 1$ and $\frac{db}{dP_{01}} < -\pi(L-c)$. □

However, risk aversion can both increase and decrease subject's sensitivity to false-positive rates depending on the utility function curvature and signal's characteristics. Intuitively, an expected marginal utility of a strongly risk-averse subject with a bad signal can be lower than the average slope of the utility function between $(Y-c-b)$ and $(Y-b)$ reducing sensitivity to false-positive rates. It can also be higher if either the signal is good or the curvature is small.

If both protection costs c and risks π are low enough (leading to small WTP b) then we can use Taylor expansion to provide an approximate argument on the effect of risk aversion on sensitivities to false-positive and false-egative rates. For this case, risk aversion decreases sensitivity to false-positive rates and increases the ratio of false-negative to false-positive rates. Risk-loving individuals respond in the opposite way.

Start by rewriting the equilibrium condition for willingness-to-pay as the expected sum of utility differences:

$$P(0,0)(u(Y-b)-u(Y)) + p(0,1)(u(Y-b-L)-u(Y-L)) + P(1,0)(u(Y-c-b)-u(Y)) +$$
$$+P(1,1)(u(Y-b-c)-u(Y-L)) = 0$$
(10)

Here, $P(x,y)$ is a shorthand for the probability of an event that the signal equals x and the state equals y. Next, we expand the utility differences of $u(Y-b)-u(Y), u(Y-c-b)-u(Y)$ as Taylor series around Y and $u(Y-L-b)-u(Y-L)$ difference around $Y-L$ to get the following equation:

$$P(0,0)[u'(Y)(-b)+o(b)] + p(0,1)[u'(Y-L)(-b)+o(b)] + P(1,0)[u'(Y)(-c-b)+o(c+b)] +$$
$$+P(1,1)[u(Y)-u'(Y)(b+c)+o(b+c)-u(Y-L)] = 0$$
(11)

Then we drop the terms $o(b), o(b+c)$ which we expect to be small enough to neglect to obtain:

$$P(0,0)u'(Y)b + P(0,1)(u'(Y)+[u'(Y-L)-u'(Y)])b + P(1,0)u'(Y)(c+b) +$$
$$+P(1,1)(-u'(Y)(b+c)-(u(Y-L)-u(Y))) = 0$$
(12)

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Now we can express the equilibrium (approximate) WTP b as:

$$b = \frac{P(1,1)\frac{(u(Y)-u(Y-L))}{u'(Y)} - P(S=1)c}{D}$$

Where the denominator $D \equiv 1 - P(0,1)\left(\frac{(u'(Y)-u'(Y-L))}{u'(Y)}\right)$. Now we remember that $P(1,1) \equiv \pi P_{11} = \pi(1-P_{01}), P(S=1) = \pi(1-P_{01}) + (1-\pi)P_{10}$ and take derivatives of equilibrium (approximate) WTP b with respect to false-positive and false-negative rates:

$$\frac{db}{dP_{10}} = -\frac{(1-\pi)c}{D}$$

$$\frac{db}{dP_{10}} = -\pi \left[\frac{\frac{(u(Y)-u(Y-L))}{u'(Y)} - c}{D} - \left(\frac{P(1,1)\frac{(u(Y)-u(Y-L))}{u'(Y)} - P(s=1)c}{D^2}\right) \frac{(u'(Y)-u'(Y-L))}{u'(Y)} \right]$$

For a strictly risk-averse subject the sensitivity to false-positive rates should be lower than for a risk-neutral one because $u'(Y)-u'(Y-L) < 0$ by decreasing marginal utility leading to $D > 1$. The opposite is true for strictly risk-loving subjects. It is hard to say something more specific about the sensitivity to false-negative rates.

Dividing the sensitivity to FN rate to the sensitivities of FP rate, we also obtain that this ratio is greater than 1 for strictly risk-averse subjects and less than one for strictly risk-loving ones.

$$\frac{db/dP_{01}}{db/dP_{10}} = \frac{\pi}{(1-\pi)} \left[\frac{(u(Y)-u(Y-L))}{u'(Y)} - c + \frac{(P(1,1)\frac{(u(Y)-u(Y-L))}{u'(Y)} - P(s=1)c)}{D} \frac{(u'(Y)-u'(Y-L))}{u'(Y)} \right]$$

Note that the corresponding equation for the risk-neutral decision-maker puts the ratio of sensitivities to:

$$\frac{db/dP_{01}}{db/dP_{10}} = \frac{\pi}{(1-\pi)} [L - c]$$

Hence the question of comparison of two ratios is equivalent to the question of the sign of the following inequality:

$$\frac{(u(Y)-u(Y-L))}{u'(Y)} + \frac{(P(1,1)\frac{(u(Y)-u(Y-L))}{u'(Y)} + P(s=1)c)}{D} \frac{(u'(Y-L)-u'(Y))}{u'(Y)} >< L$$

However note that the first component in the left-hand sum is already greater $\frac{(u(Y)-u(Y-L))}{u'(Y)} > L$ for any strictly risk-averse decision-maker by a mean value theorem. Risk aversion also makes the second component positive as $u'(Y-L)-u'(Y) < 0$ and $P(1,1)\frac{(u(Y)-u(Y-L))}{u'(Y)} + P(s=1)c > P(1,1)L - P(s=1)c > 0$ is also positive as it equal the expected savings from using a signal. Hence the LHS is greater than the RHS L leading to the ratio of sensitivities to be greater than for a risk-neutral decision-maker. The same argument applied in reverse will show that for a

strict risk-loving decision-maker the ratio of sensitivities will be lower.

3   Experimental Design

Subjects received a USD 5 show-up fee and a USD 25 endowment that they might lose in the experiment. They must make a series of decisions in four sets of tasks: (i) Blind Protection; (ii) Informed Protection; (iii) Belief Elicitation; and (iv) Willingness to Pay Elicitation. Subjects took a quiz before each task and for every wrong response, the correct answer and explanation are given. Additionally, subjects had to answer extra questions if their responses to the Informed Protection questions were incorrect. Informed Protection is the first challenging task in the sequence and whose understanding is essential for the rest of the tasks. Each task has 6 rounds, for a total of 24 rounds. One round is randomly selected as the payment round. A copy of the instruction is included in Appendix XX.

Blind Protection (BP).   Subjects must decide whether to insure (or "protect") against an adverse event (a random draw of a black ball). They are informed of the prior probability of a black ball. The cost to protect is USD 5. An unprotected subject who draws a black ball will lose USD 20. Subjects played six rounds with a probability (of a black ball) $p \in \{0.05, 0.10, ..., 0.3\}$. In this task, subjects received no feedback on how each round would have been realized were it selected as the payment round.

Informed Protection (IP).   Similar to the BP task, subjects must make a protection decision given a prior probability of a black ball. However, in addition to the prior, subjects also received a signal with varying degrees of inaccuracy. Following **?**, we use a group of hinting gremlins to convey signal accuracy: a gremlin, randomly drawn from a group, gives out the signal. The gremlin is one of three types: (i) honest; (ii) "black-swamp" who always says that the ball is black; and (iii) "white-swamp" who always says that the ball is white. Figure XX illustrates how the different gremlin types were presented to the subjects.

   The composition of the group from which the gremlin is drawn determines signal accuracy: a higher share of black(white)-swamp gremlins will produce a signal with higher false-positive(negative) rate. Subjects know the group composition, but do not know which gremlin provides the hint. We vary the proportion of black balls in the box (prior probability of a black ball) and the composition of gremlins (signal quality) between rounds.

Belief Elicitation (BE).   As in the IP task, subjects were told the prior probability of a black ball and the hinting gremlin's group composition. However, instead of making a protection decision, subjects are asked to estimate the probability that: (i) the ball is black ball when the gremlin says that it is white; (ii) the ball is black when the gremlin says that it is black.

   To elicit incentive-compatible responses, we follow the stochastic version of the Becker-DeGroot-Marshak mechanism developed by **?** and **?**: the subject submits their belief of the

probability of the event $\mu \in [0, 1]$. If this belief is above some uniform random number $r \in [0, 1]$, they receive the payoff x only if the stated event happens. Otherwise their payoff is determined by an independent lottery which pays x with probability r and 0 otherwise.[3] We also provide our subjects with the heuristics that under this mechanism, truthful reporting of beliefs is the dominant strategy.

Willingness to Pay Elicitation (WTPE). The WTPE task measures subjects' willingness to pay (WTP) for signals. Subjects know the prior probability of a black ball and the group composition of the gremlins that will determine signal quality. We then ask subjects for their WTP for a hint. Subjects can choose a value from USD 0 to 5 with USD 50-cent increments. Their decisions are incentive compatible: if a WTPE round is selected as the payment round, a random price of a hint will be drawn. If that price exceeded the subjects' WTP, they will play a BP round. Otherwise, the subject would pay their WTP and play an IP round.

After completing the WTPE task, subjects were asked a few demographic questions. The session concluded with the random selection and realization of the payment round, after which subjects were paid and dismissed. Table 1 shows the values of the different priors in our treatments, as well as the gremlin groupings (along with the associated false positive and false positive rates) that we used for the different tasks.

Table 1: List of Treatments

| | Gremlins composition | | | | |
Prop. of black balls (p)	Honest	Black-eyed	White-eyed	FP rate	FN rate
0.1, 0.2, 0.3, 0.5	2	0	0	0	0
0.1, 0.2, 0.3, 0.5	3	1	0	0.33	0
0.1, 0.2, 0.3, 0.5	3	0	1	0	0.33
0.1, 0.2, 0.3, 0.5	3	1	1	0.33	0.33
0.1, 0.2, 0.3, 0.5	5	1	0	0.2	0
0.1, 0.2, 0.3, 0.5	5	0	1	0	0.2
0.1, 0.2, 0.3, 0.5	5	1	1	0.2	0.2

We conducted this experiment in the Behavioral Business Research Lab (BBRL) at the University of Arkansas between October and November 2021. The experiment was implemented using Qualtrics. There were a total of 105 subjects. 84 percent of the subjects were university students and 41 percent were male. About 60 percent of the subjects had taken at least one statistics course. On average, including the show-up fee, subjects received around USD 26 for a session lasting around 45 minutes.

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[3]The benefit of this mechanism versus other probability elicitation mechanism (for example, quadratic scoring) is that reporting truthfully is a dominant strategy regardless of risk preferences (**?**). The only requirements a subject needs to satisfy are probabilistic sophistication and dominance: they rank lotteries based on their probabilities only and prefer higher probabilities of higher payoffs.

4 Subject Decisions By Task

We use the BP, IP, and BE tasks to construct measures of the components of WTP suggested by our model. The BP task reveals subjects' responses to the prior and their risk preference. The IP task provides insights into how signal characteristics affect their protection decisions. Finally, the BE task shows how subjects would update for a given signal quality. Some of these tasks can be quite challenging. However, we show below that on average, subjects appear to exhibit a reasonable understanding of these tasks.

4.1 Blind Protection

Figure 1 plots the probability of protection decision against posterior probability of a black ball for the BP task, where the posterior is equivalent to the prior, and the IP task. On aggregate, subjects protect more with a higher probability of a negative outcome: only 13% subjects protect when the probability of a black ball is 10% in contrast to 70% protecting when the probability is 30%.

At the individual level, BP responses indicate significant heterogeneity in risk preferences. For approximately 70% of subjects (XXX X/Y XXX), protection action increases monotonically in probability. The remaining 30% make at least one switch from protecting to not protecting and back, which is inconsistent with EU maximization. Among these switchers, however, 83% (24/39) skip only a single increment of the presented probability scale, suggesting an inattention error.[4]

Risk-neutral agents who maximize their expected utility should start protecting when the prior exceeds 0.25 (the ratio of the protection cost to the potential loss = \$5/\$20). Many of our subjects started protecting at lower priors, indicating strict risk aversion.[5] A smaller group of subjects makes choices consistent with risk loving by protecting at a probability of 0.3 or never protecting.

4.2 Informed Protection

In the IP task, subjects receive a signal (on top of a prior) to help them form a posterior probability of a black ball. Figure 1 shows that protection actions are increasing in the posteriors. Roughly 28% of subjects break monotonicity in their protection responses with respect to posterior probabilities — approximately the percentage of non-monotonic responses in the BP task.[6] At the individual level, we also find that the total number of times subjects protect in

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[4]For comparison, Holt and Laury (2002) for a similar instrument find that 28 of 212 subjects (13%) switched back to a low-risk option with an increasing likelihood of high payoffs in a risky option at least once.

[5]As a reference, switching at the probability 0.1 corresponds to a CRRA risk aversion $\theta = 2$, while switching at 0.2 corresponds to $\theta = 0.57$.

[6]They do not protect for some treatments with posterior probability P while protecting for a posterior probability $P' < P$.

the BP task significantly correlates with their likelihood to protect in the IP task conditional on posteriors, but this explains only a very small part ($<1\%$) of variation in the IP decisions.[7]

Figure 1: Average Protection Response
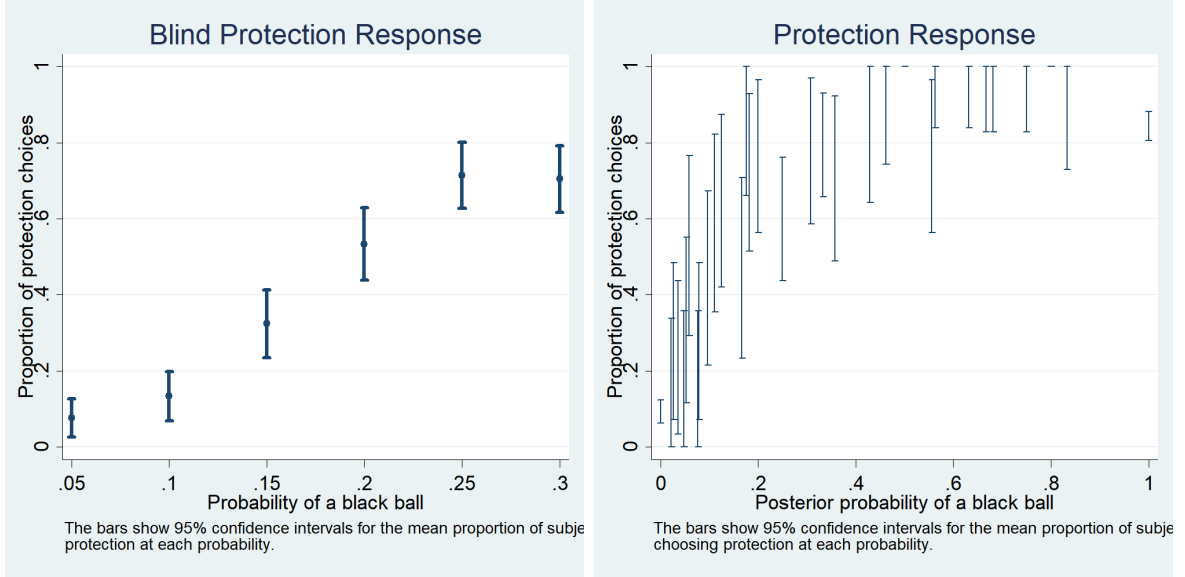
(a) Note BP. Put note in latex instead of in figure title.

(b) Note IP. Put note in latex instead of in figure title.

Table 2 presents the average protection decisions by signal characteristics. The first three columns summarize the signal characteristics information that is available to the subject. Column 4 shows the posterior probability of a black ball averaged across all the treatments within a group. Column 5 shows the subjects' share of empirical protection responses, next to the theoretical optimum for risk-neutral subjects in Column 6. Column 7 presents the p-value for a test of equality between empirical and theoretical protection responses.

We have three main findings. First, we find that regardless of FP and FN rates, a black signal substantially increases the share of protection decisions. Second, subjects' protection decisions in most treatments significantly deviate from what is optimal for risk-neutral subjects, evidenced by column 7. Subjects tend to overprotect when facing white signals (rows 1–4) and underprotect when facing black signals (rows 5–8). The exceptions are treatments with a black signal and positive FP rates where the statistical equality of columns 5 and 6 cannot be rejected (rows 7–8).

Finally, we find that some deviations cannot be explained by the expected utility maximization for any degree of risk aversion. For example, consider rows 1 and 3: even though an increase in the signal's FP rate does not change the posterior (because the signal is white), the protection rate increases by 6 percentage points (pp.). Similarly, row 4 shows that when both FP and FN are positive, the protection rate increases to 56 percent — even though the average (maximum) posterior probability for the signal characteristics is just 13 percent. As

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[7]We use LPM to estimate this relationship, and while the coefficient on the total number of protection choices is significant at 99%, R^2 increases from 0.295 to 0.3.

a benchmark, with no signal in the BP task, only 13 (32) percent of subjects chose to protect when the probability is 10 (15) percent.

Table 2: Average Protection by Signal Type

|	Signal Characteristics			Posterior	Share Protect	Share Optimal	P-val (H_0: (5) = (6))
Row	Signal	False Positive	False Negative				
	(1)	(2)	(3)	(4)	(5)	(6)	(7)
(1)	White	No	No	0.000	0.067	0.000	0.000
(2)	White	No	Yes	0.100	0.333	0.000	0.000
(3)	White	Yes	No	0.000	0.130	0.000	0.000
(4)	White	Yes	Yes	0.131	0.564	0.121	0.000
(5)	Black	No	No	1.000	0.846	1.000	0.000
(6)	Black	No	Yes	1.000	0.841	1.000	0.000
(7)	Black	Yes	No	0.550	0.833	0.870	0.355
(8)	Black	Yes	Yes	0.483	0.886	0.871	0.685

Notes:

4.3 Belief Elicitation

Subject decisions in the IP task capture how signals are used to make protection decisions, but conflate risk preferences with potential errors in updating posteriors. The BP task can be used to construct a measure of the former. Here, we use the BE task to measure the latter.

Figure 2: Errors in Bayesian Updating

(a) Error Distribution
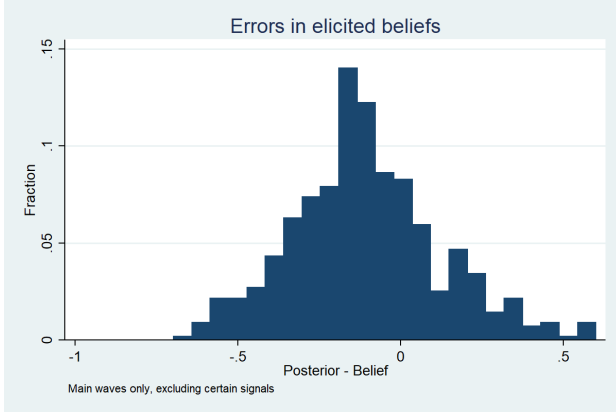
(b) Error v. Posterior
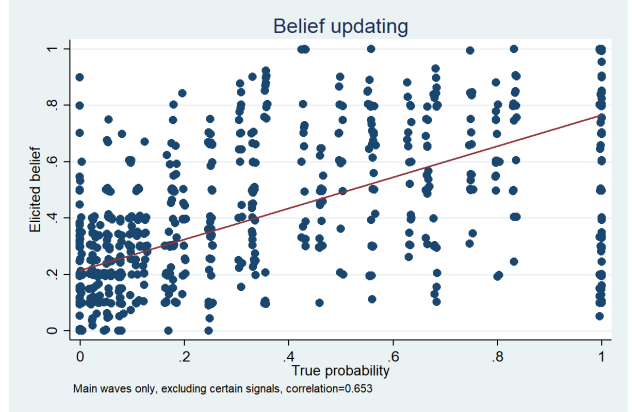
(c) Error Distribution, Certain Posterior
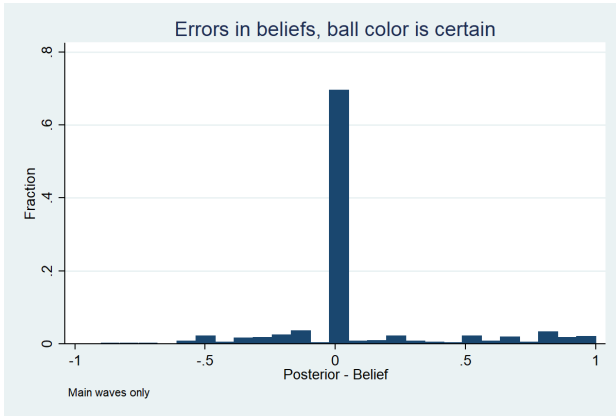
(d) Error v. Posterior, Certain Posterior
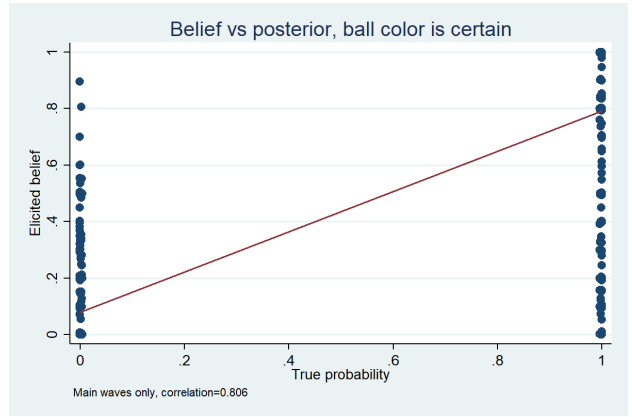
(e) Error Distribution, Uncertain Posterior
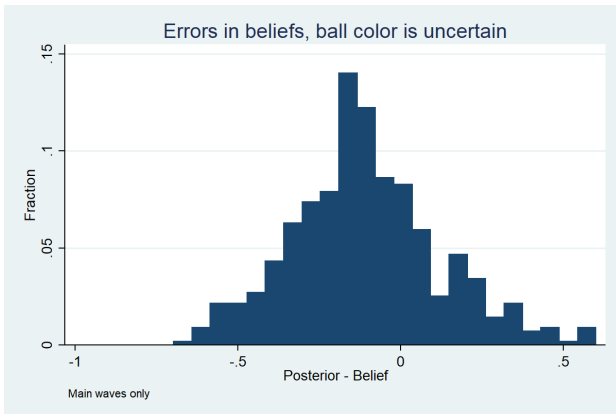
(f) Error v. Posterior, Uncertain Posterior
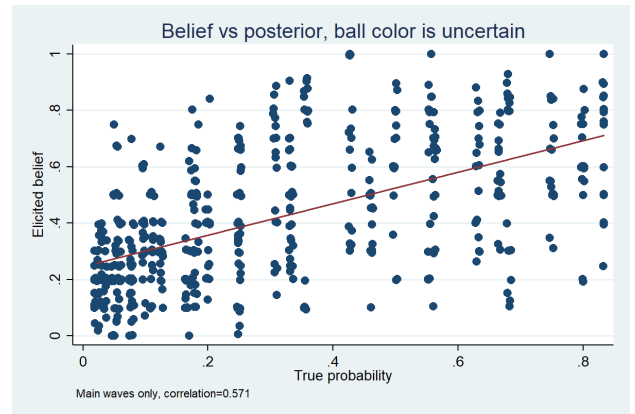
We define updating errors as the difference between the posterior and subjects' elicited belief on the posterior probability of a black ball for a given signal. The left-hand column of Figure 2 shows the distribution of the updating errors, while its right-hand column presents a scatter plot of the elicited beliefs against the true posterior with a fitted line. Panel A uses all observations and suggests that, while errors occur, beliefs are still sensible. The distribution

of updating errors is centered at 0, with roughly one-half (51%) concentrated within +/- 0.1 interval around zero. Overall, the correlation between the elicited beliefs and the true posteriors was 0.653.

Some combinations of priors and signals led to completely certain posteriors where updating should be trivial. Panel B plots such cases, which account for 56% of the sample and includes: (i) treatments with all-honest gremlins; and (ii) treatments with obviously irrelevant dishonest gremlins (e.g., a gremlin from a group with honest and white-swamp gremlins announcing that the ball is black — or vice versa). Reassuringly, 69% of reported beliefs are correct. About half of the errors involve reporting a probability of one when it should have been zero.

Meanwhile, Panel C plots observations without such these observations. The median error is now -0.12, with with 90% of errors between -0.48 and 0.3, suggesting that subjects tend to overestimate the likelihood of adverse events for uncertain posteriors. The correlation between beliefs and posteriors in this sub-sample falls to 0.571.

The overall pattern of belief updating is consistent with the existing literature which shows that despite updating in the correct direction, people tend to underreact both to priors and the signals. The effect of underweighting priors — first noted in the psychology literature (**???**) — is known as *representativeness bias* or *base-rate neglect*. Using the regression approach of **?**, we find both base-rate neglect and signal underweighting. Our estimates of these parameters are significantly below one with $\hat{\alpha} = 0.43$ $\hat{\beta} = 0.25$ (see Column 1 in **??**). These values are within the range found by the meta-analysis of **?** which calculates the average $\hat{\alpha}$ estimate to be around 0.22 (0.4 for incentivized studies only) and the average $\hat{\beta}$ to be 0.6 (0.43 for incentivized) for studies (like ours) that presented their signals simultaneously.[8]

Table 3: Average Updating Error by Signal Type

Row	Signal Characteristics			Posterior	Updating Error*	P-val (H_0 : $Error = 0$)
	False Positive	False Negative	Signal			
	(1)	(2)	(3)	(4)	(5)	
(1)	No	No	White	0.000	0.050	0.000
(2)	No	Yes	White	0.100	0.122	0.000
(3)	Yes	No	White	0.000	0.122	0.000
(4)	Yes	Yes	White	0.131	0.218	0.000
(5)	No	No	Black	1.000	-0.163	0.000
(6)	No	Yes	Black	1.000	-0.279	0.000
(7)	Yes	No	Black	0.550	0.039	0.130
(8)	Yes	Yes	Black	0.483	0.048	0.021

Notes: *Updating error = $Posterior - Belief$.

Table 3 summarizes how the updating errors vary with signal characteristics. We find that subjects overestimate the probability of a black ball when they received a white signal.

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[8]The common name for this kinds of experiments is *bookbag-and-poker-chip experiments*

Introducing FP rates to the signal exacerbated their upward bias. To illustrate, consider the change between rows 1 and 3, where introducing a FP rate would not change the posterior because the signal is white. Yet, subjects update their posterior upward, magnifying their updating error. The FN rates also have a similar effect of exacerbating this upward bias for a white signal.

The updating bias for black signals, however, varies by the information structure. Subjects slightly underestimate the probability even when the signal is honest, but introducing FN rates leads subjects to underestimate it further. To illustrate, the introduction of a FN rate given a black signal does not change the posterior (rows 5 and 6), but subjects decrease their beliefs. When there is a risk of a false-positive (i.e., FP>0), subjects again overestimate the probability of a black ball with little difference in errors between treatments with FP events only and with both FP and FN events. It seems that because the false-positive rate negatively affects the posterior, subjects fail to adjust their beliefs enough in response to FP rates.

5   WTP and Signal Characteristics

5.1   Are Subjects Risk Neutral, Expected Utility Maximizers?

Hypothesis 1. *Subjects' WTPs for signals are equal to their value for risk-neutral agents.*

Hypothesis 2. *Subjects' preferences demonstrate equal sensitivity to costs generated by false-positive and false-negative events.*

Result 1. *XXXXXXXXXXXXXXXXXXXXX*

Result 2. *On average for our signal and sample structure, we cannot reject the hypothesis of equal sensitivity. However, we observe significant heterogeneity with respect to priors: subjects tend to overvalue false-negative costs for low probability events and overvalue false-positive costs for high probability events.*

The theoretical value of a signal for a utility maximizing risk-neutral subject (hereafter, risk-neutral signal value) in equation 2 provides a useful benchmark of our subjects' WTP. Figure 3 plots the distribution of the differences between subjects' WTP and the signal value. The WTP is centered around the risk-neutral signal value, which is suggestive that subjects approximates a risk-neutral utility maximizing agent. However, there is substantial variation: only 25% of actual WTP are within $0.50 of the risk-neutral signal value, and subjects overvalue by at least $1.5 in 22% of cases and undervalue it by at least $1.5 in 19% of cases.
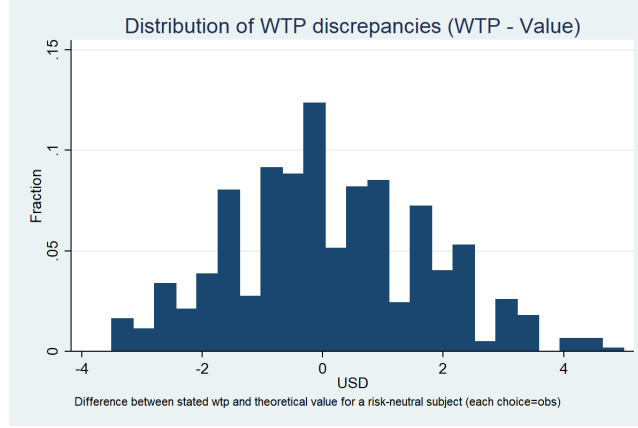
Figure 3: Discrepancy (Observed WTP - Signal value)

Our non-parametric analysis in Table 4 also finds no differences between the (empirical) WTP and the risk-neutral signal value for 3 out of 4 broad categories of signal characteristics: honest signals; signals with only false-positive events; and signals with only false-negative events. When there are both false positives and false negatives, however, subjects significantly overvalue signals relative to the theoretical benchmark. These signals also tend to cause over-protection in the IP task.

Table 4: Average WTP discrepancy (WTP-Value) by Signal Type

False positive	False negative	Mean WTP discrepancy	$\mathbf{P}(= 0)$
No	No	-0.106	0.433
No	Yes	0.143	0.250
Yes	No	0.081	0.502
Yes	Yes	0.492	0.000

We estimate these relationships more formally with the following regression:

$$\Delta b_{is} = \beta_0 + \beta_1 FP + \beta_2 FN + \varepsilon_{is}$$

where $\Delta b_{is} = (b_{is} - b_s^*)$ is the difference between the WTP of individual i for signal s and b_s^* is the signal value; FP (FN) is the false positive (false negative) cost. All specifications include subject fixed effects, with standard errors clustered at the subject level. If subjects are risk-neutral expected-utility-maximizing subjects, we expect $\beta_1 = 0$ and $\beta_2 = 0$. The result, reported in column 1 of Table 5, shows positive and statistically significant coefficients for both FP and FN costs. In other words, subjects deviate from the benchmark model and overpay for inaccurate signals.

- PETE's OLD COMMENT: Can we plot the distributions of deviations for these 4 cases?.

- XXX Is a false positive event = having a black gremlin in the group? Should we write false positive rate or is there a distinction you want to highlight? XXX

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Table 5: Deviations from Signal Value (WTP - Value) and Signal Characteristics

| | All | | | Prior | |
| | | | | {.1, .2} | {.3, .5} |
	(1)	(2)	(3)	(4)	(5)
FP costs	0.231	0.204	0.720	0.604	0.004
	(0.126)*	(0.339)	(0.303)**	(0.276)**	(0.571)
FN costs	0.319	0.232	0.192	-0.516	0.275
	(0.070)***	(0.286)	(0.264)	(0.486)	(0.257)
Risk-averse × FP costs		-0.020	-0.427	-0.054	-0.398
		(0.378)	(0.365)	(0.355)	(0.653)
Risk-averse × FN costs		0.061	0.233	0.432	0.147
		(0.299)	(0.319)	(0.585)	(0.319)
Risk-loving × FP costs		0.165	-0.474	0.027	-0.238
		(0.438)	(0.426)	(0.412)	(0.751)
Risk-loving × FN costs		0.177	0.357	0.970	0.040
		(0.309)	(0.295)	(0.558)*	(0.271)
Constant	-0.182	-0.184	-0.024	-0.068	0.114
	(0.083)**	(0.084)**	(0.104)	(0.111)	(0.130)
R^2	0.480	0.482	0.504	0.738	0.750
Obs	624	624	624	312	312
Risk-Averse Subjects:					
False Positive		0.184	0.293	0.551	-0.394
se		(0.168)	(0.204)	(0.223)	(0.316)
p-value		[0.274]	[0.154]	[0.015]	[0.216]
False Negative		0.293	0.425	-0.083	0.422
se		(0.089)	(0.178)	(0.326)	(0.189)
p-value		[0.001]	[0.019]	[0.799]	[0.028]
Risk-Loving Subjects:					
False Positive		0.369	0.246	0.631	-0.234
se		(0.277)	(0.299)	(0.305)	(0.488)
p-value		[0.186]	[0.414]	[0.041]	[0.633]
False Negative		0.409	0.549	0.454	0.315
se		(0.117)	(0.132)	(0.275)	(0.086)
p-value		[0.001]	[0.000]	[0.102]	[0.000]
Subject FE	Yes	Yes	Yes	Yes	Yes
Inaccurate Belief Interactions	No	No	Yes	Yes	Yes
Prior Probability FE	No	No	No	Yes	Yes

Notes: */**/*** denotes 10/5/1 percent significance levels.

The model of a risk-neutral agent suggests that subjects' preferences value the marginal costs from false-negative and false-positive information symmetrically. We find that the coefficients on FN costs is slightly larger indicating higher sensitivity to FP costs, but we cannot reject the hypothesis that the two coefficients are equal. It means that on average and given our priors (!), the risk-neutral model still provides good guidance with choosing optimal trade-off between false-positive and false-negative costs. However later we note that this equivalency breaks down when considering specific priors.

5.2 Risk Preference and Belief Accuracy

Our baseline estimation in column 1 indicates significant deviations from the model's predictions. Since the benchmark signal value is based on the optimal choice of a risk-neutral Bayesian updater, deviations can arise from at least two sources. First, Proposition 2 suggests that risk preferences can influence the sensitivity of WTP to these signal characteristics. Second, systematic biases during the updating process can also lead to deviations.

We find that risk preferences have limited explanatory power for sensitivity to signal characteristics. We use data from the BP game to categorize subjects by their risk preference. We classify all the subjects with internally consistent BP choices into three risk-preference categories: risk averse, risk neutral, and risk loving.[9] Column 2 explores the heterogeneity of subject responses to FP and FN costs by their risk preference, with risk-neutral as the default category. The point estimates for risk-neutral subjects are about 1/3 smaller than those of the overall subjects (column 1) and statistically insignificant. This indeed indicates convergence towards prediction of a risk-neutral model, but with still sizable remaining discrepancies. Given the magnitudes of coefficients on the interaction of risk preferences with FP and FN costs, only risk-loving subjects have plausibly different sensitivities though the interaction terms are not statistically significant.

Accounting both for belief accuracy and for risk preferences also does little to explain the pattern of underreacting to FP and FN rates. To study the role of subjects' ability to Bayesian update, we use data from the BE task to categorize the WTP responses by belief accuracy.[10] Column 3 presents the most flexible specification that controls for belief accuracy and risk preference by including triple interactions of belief accuracy, risk preference, and signal characteristics. The baseline group is the group of risk-neutral subjects with relatively accurate beliefs. We find that baseline subjects' sensitivity to FN costs declined (and remained insignificant), but their sensitivity to FP costs increased.

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[9]Subjects who switched from no protection to protection at exactly the cost-loss ratio $\pi = 0.2$ are considered risk-neutral, while switching at lower (higher) levels indicates risk aversion (risk-loving). In addition, we created a dummy variable for subjects whose BP choices are inconsistent.

[10]We calculate a belief error as the absolute value of the difference between the subject's belief and the true posterior probability and then average these errors across all the decisions with identical priors, false positive and false negative rates. A subject's posterior belief for a decision is defined as accurate if its error is less than the median error across all the subjects making the same decision.

5.3 Heterogeneity by Prior

We motivate our experiment with real world problems of designing signals for low-probability disasters. With a low prior, the default action of risk-neutral subject would be not to protect, and vice versa with a high prior. The signal would help risk-neutral subjects decide whether to keep the default action or to switch. We split the prior by below/above 0.25 (= protection cost/potential loss). For estimation, we incorporated prior-probability fixed effects to the aforementioned flexible specification.

- Is this how we will interpret the results? As some kind of stickiness to the default action? We prime readers to expect that his would happen. Are we ruling other explanations? Should discuss!

Column 4 presents the results for low-prior WTPE tasks. With a low prior, subjects overvalue false positive signals relative to the risk-neutral baseline. This overvaluation is similar for different risk preference profiles. In other words, with low priors, subjects overvalue signals that would induce them to overprotect. Both risk-neutral and risk-averse subjects do not (over-)value false-negative signals, while risk-loving subjects value such signals more positively — with a difference that is statistically significant at 0.1 — than risk-neutral subjects. The total coefficient of false-negative cost for risk-loving subjects is large, but is barely significant at 0.1 level.

Column 5 presents the results for high-prior WTPE tasks. With a high prior, risk-neutral subjects report a WTP that aligns with the signal value. False positive signals are not overvalued, but both risk-averse and risk-loving subjects overvalue false negative signals. Our sample size cannot detect statistically significant differences in the extent of the overvaluation of false negative signals between both types and the risk-neutral subjects. These results imply a slight tendency (particularly for non-risk-neutral subjects) to overvalue signals that would induce them to underprotect.

To sum up, subjects overreact to false-negative rates and underreact to false-positive costs with low priors, but this pattern reverses for high priors. In practice, it implies that users would tend to overpay for alert signals with high false-positive costs, while excessively discounting systems with significant false-negative rates. For example, they would prefer a smoke alarm which never misses fires even if it involves higher expected costs of false alarms. Risk preferences have weak explanatory power: controlling for risk preferences reduces only the extra sensitivity of false-positive costs with priors but does not explain away the interaction between false-negative costs and priors.

5.4 Other Heterogeneity Analysis

We find little evidence for heterogeneous effects by demographic characteristics or statistical education. We show in (Appendix (?????) Table ??) that gender or previous statistical education do not have significant effects on sensitivities for false-positive and false-negative rates.

We find weak evidence that older (23+) subjects have a lower WTP for signals though the age variation is pretty limited.

5.5 Discussion: What Accounts for the Heterogeneity by Prior?

- Motivate why we dig deeper into het by prior.

- At the end, we shot down the anchoring explanation. Do we want to make this sort of two hypotheses we are examining? Also, I feel that there can be a better way to describe our preferred explanation.

We show in (Section XX? Equation XXX?) that risk-averse individuals should have even higher sensitivity to false-negative rates, hence risk aversion on its own cannot explain this pattern. Similarly, risk-loving subjects should always put a higher relative weight on false-positive costs compared to a risk-neutral decision-maker, but this should hold for all priors as long as WTP b and protection costs c are low enough relative to the potential loss L. Hence neither risk aversion nor risk-loving are consistent with the pattern.

- ALEX: Not sure about heterogeneity of risk preferences if this heterogeneity does not much BP

In Table **??** we estimate directly the regression of reported willingness-to-pay on false-positive and false-negative costs given to subjects directly. We find that the sensitivities to both false-positive and false-negative rates: (i) change relatively smoothly with priors and; (ii) are surprisingly close to each other. For none of the priors can we reject the hypothesis that two sensitivities are equal to each other. This drastically contrasts with the risk-neutral model, predicting that the sensitivity to FP rates should be much higher than the sensitivity to FN rates for low priors, but lower for high priors. This happens because for a given FN rate, false-negative events are much less likely with low priors and hence impose less costs on the agent. Increasing priors in theory makes FN rates more salient while the saliency of FP rates should go down.

The closeness of coefficient estimates for FP and FN rates for Table **??** suggests one possible explanation for the observed pattern of sensitivities. If subjects' neglect the difference between false-positive and false-negative risks when choosing their WTP, it would explain both coefficients' similarity and flatness of sensitivities with respect to priors. If subjects treat FP and FN rates the same and treat only about the total proportion of false signals, they would assign equal weights to each of them. And because the sensitivity of theoretical value to FP and FN rates changes in opposite ways with priors, the best fit line for the sum of FP and FN rates should be much flatter with respect to priors.

Subjects' verbal explanations of choices made in Informed Protection provide additional credence for the hypothesis that subjects bundle FP and FN rates together. For example, the

Table 6: WTP for Information, by prior (tobit)

	(1) 0.1	(2) 0.2	(3) 0.3	(4) 0.5
model				
FP rate	-2.91***	-2.08**	-4.46***	-3.25**
	(1.1)	(1.0)	(1.0)	(1.3)
FN rate	-2.48**	-2.73***	-3.7***	-3.65***
	(1.1)	(1.0)	(1.0)	(1.3)
Constant	1.79***	2.33***	2.71***	3.32***
	(0.2)	(0.2)	(0.2)	(0.3)
sigma				
Constant	1.83***	1.7***	1.72***	2.16***
	(0.1)	(0.1)	(0.1)	(0.2)
P(FP rate=FN rate)	.792	.669	.617	.832
Adjusted R^2	.	.	.	.
Observations	159	153	159	153

Standard errors in parentheses

* $p < 0.10$, ** $p < 0.05$, *** $p < 0.01$

explanation from one of the subjects states *"I took into consideration how many honest there were and looked at the chances of picking a ball."*, while another also states *"If there were only honest gremlins then I never protected but even if there was one white-swamp gremlin or one black-swamp gremlin then I payed for protection."*. In total, we find that 39 subjects out of 105 subjects in the main waves refer to the percentage of dishonest gremlins as their rationale for choosing protection. Many other could rely on this heuristic without giving a complete accurate explanation.

In order to test this hypothesis, we use choices from other tasks also using imperfect signals: Belief Elicitation and Informed Protection. If subjects systematically neglect the difference between false-positive and false-negative rates, we expect to find the pattern of abnormal reaction to FP and FN rates in cases when they do not affect the posterior. Namely, subjects would show sensitivity to FP rates when the signal is white and sensitivity to FN rates with black (positive) signals. This happens because some subjects react to FP (FN) rates as if they are FN (FP) rates.

First, we test this pattern for the BE choices by estimating the relationship between belief errors and FP and FN rates by signal type. Table **??** reports our results. We estimate a linear regression of updating error (actual posterior - reported belief) on FP and FN rates by signal color. We used fixed effects to control for individual updating biases. Consistent with our hypothesis, we observe that the FP rate has significant positive effect on the error when the signal is white (negative), and that FN rate has a significant negative effect when the signal is black (positive). False-positive rates should not affect beliefs with white signals because a white signal (negative) can never be a false positive. The significance of FN rate for black signals is similarly an anomaly inconsistent with rational updating.

Table 7: Updating Errors in BE Task

	All	Signal Received	
		White	Black
	(1)	(2)	(3)
FP rate	.6***	.292***	.908***
	(0.1)	(0.1)	(0.1)
FN rate	.0108	.273***	-.251***
	(0.1)	(0.1)	(0.1)
Constant	-.0784***	.314***	-.47***
	(0.0)	(0.0)	(0.0)
Subject FE	Yes	Yes	Yes
Observations	1248	624	624
Adjusted R^2	0.15	0.41	0.52
Subject FE	Yes	Yes	Yes

Notes: Standard errors in parentheses. * $p < 0.10$, ** $p < 0.05$, *** $p < 0.01$.

In Table **??**, we regress informed protection decisions on FP and FN rates and flexible controls of both posteriors and reported beliefs:[11]

$$Prob(s_{ij} = 1) = \alpha_i + \beta_1 FP + \beta_2 FN + Z(p_{ij}) + Z(\mu_{ij}) + \epsilon_{ij}$$

where s_{ij} is the protection decision of subject i in treatment j, α_i - subject FE, P_{10}, P_{01} are FP and FN false positive and false negative rates and $Z(p_{ij}), Z(\mu_{ij})$ are the splines of corresponding variables P_{ij}, μ_{ij} to control for these variables in the flexible way. Each spline is a function $Z(x)$ which is just linear $x + C$ within one interval, and constant everywhere else. The splines are constructed so that their linear intervals cover the whole domain of probabilities and beliefs $[0, 1]$. [12] of posteriors and reported beliefs μ_{ij} for corresponding treatments. Columns 1 and 2 include only the flexible controls of the true posteriors. Columns 3 and 4 add further flexible controls to account for subjects' (often incorrect) estimates of the posterior, inferred from their BE responses.

Columns 1 and 2 show that even conditional on posterior and subject FE to control for risk preferences, IP responses are still affected by FP and FN rates. For a white signal, FP and FN rates increase the tendency to overprotect; while for a black signal, FP rate had an opposite effect with comparable magnitude but without statistical significance. Hence the first prediction of FP/FN rate confusion hypothesis holds: FP rates increase protection when the signal is white conditional on the posterior. The effect holds if allowing for heterogeneity of sensitivities to

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[11]Given that the true functional form is unknown, we use a linear probability model to get unbiased coefficient estimates.

[12]We use Stata mkspline command to create 5 splines $z_1(x), z_2(x), ..z_5(x)$ of initial variable x over the range $[0, 1]$ such that $z_k(x) = \min[0, x - x_{k-1}, x_k - x_{k-1}]$ with x_k being equally spaced knot values. Splines account for potential nonlinear effects of posteriors and beliefs on protection decision with limited effect on degrees of freedom.

FP/FN rates with respect to priors (Column 2). The coefficient on FN rate for black signals however is small in magnitude and statistically insignificant at 10%. Adding flexible controls for subjects' beliefs reduces the coefficient magnitude on FP rate for white signals (Columns 3 and 4), but the coefficients still remains significant. This indicates that while belief partially contribute to these protection anomalies, they cannot explain them completely (possibly due to subjects re-evaluating their beliefs between tasks).

Table 8: Informed Protection Response

	(1)	(2)	(3)	(4)
FP rate x (S=White)	.461***	.494**	.282**	.286
	(3.3)	(2.4)	(2.0)	(1.4)
FN rate x (S=White)	.544***	.474**	.195	.125
	(2.9)	(2.1)	(1.0)	(0.5)
S=Black	.42***	.429***	.316**	.336**
	(2.7)	(2.7)	(2.0)	(2.1)
FP rate x (S=Black)	-.256	-.225	-.379	-.389
	(-0.5)	(-0.4)	(-0.8)	(-0.7)
FN rate x (S=Black)	.0494	-.027	-.00394	-.0879
	(0.5)	(-0.2)	(-0.0)	(-0.6)
p=0.2	.113***	.101***	.09***	.0723**
	(4.2)	(2.8)	(3.6)	(2.1)
FP rate x (p=0.2)		-.0363		.00218
		(-0.2)		(0.0)
FN rate x (p=0.2)		.122		.127
		(0.9)		(0.9)
N	1224	1224	1224	1224
Pseudo R-squared	.551	.552	.578	.578
Log-likelihood	-379	-378	-356	-356
Subject FE	Yes	Yes	Yes	Yes
Flexible controls for:				
Posterior	Yes	Yes	Yes	Yes
Beliefs	No	No	Yes	Yes

Notes: Coefficients are average marginal effects. t-statistics in parentheses. Standard errors are clustered at the subject level. * $p < 0.10$, ** $p < 0.05$, *** $p < 0.01$.

To sum up, we observe a striking uniformity in sensitivity of WTP to both false-positive and false-negative rates. This pattern is consistent with subjects neglecting the difference between false-positive and false-negative signals. This hypothesis is supported by subjects' explanation and with abnormal sensitivities to false-positive and false-negative rates in other treatments in which they do not affect posterior probabilities. We will leave the discussion of practical implications of this finding for the conclusion.

XXX WHERE SHOULD THIS GO? SHOULD WE ORGANIZE AS ALTERNATIVE EXPLANATIONS AND SHOOT DOWN? OR A FOOTNOTE?We also believe that this pattern of sensitivities does not come from subjects' anchoring on priors or from preferences for non-

instrumental information. Given that each subject goes through two sets of treatments with two different priors and the order of priors is fixed, anchoring remains a theoretical concern. However, we find that most subjects change their decisions when going from one prior to another (92 out of 104). The average belief error in the BE task is actually lower for the second set of priors rather than for the first showing that changing priors does not increase subjects' confusion. And most importantly, there is still uniformity in coefficient ratio even if we limit our attention only to the first priors in each sequence (0.1 or 0.2)[13]. Similarly, while there is multiple evidence on humans valuing information not affecting their decisions (non-instrumental information), the value of this information should increase in false-negative rates for low priors in order to countervail a higher sensitivity predicted in theory. Having the value of non-instrumental information to increase with errors seems a priori implausible.

6   Conclusion

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[13]Depending on session, the first 3 WTP treatments use either the prior of 0.1 or 0.2 and hence there is no anchoring on the previous prior.

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A   Tables

Table 9: Demographic Characteristics of Subjects

	All		$p \in \{0.1, 0.3\}$		$p \in \{0.2, 0.5\}$	
	N	%	N	%	N	%
Male	43	41	22	41	21	41
Age>23yrs old	14	13	6	11	8	16
Students	88	84	46	85	42	82
Had statistics classes	63	60	37	69	26	51
Total	105	100	54	100	51	100

Table 10: Error Decomposition

	(1) OLS	(2) FE	(3) OLS	(4) FE	(5) OLS	(6) FE
Prior	.246***	.202***	.175***	.191**	.14**	.0403
	(5.5)	(4.0)	(3.1)	(2.5)	(2.3)	(0.6)
Signal	.43***	.43***	.327***	.327***	.539***	.539***
	(6.3)	(6.3)	(3.2)	(3.2)	(5.3)	(5.3)
Good quiz × Prior			.143*	.0207		
			(1.7)	(0.2)		
Good quiz × Signal			.193	.193		
			(1.4)	(1.4)		
Stat. class × Prior					.162*	.264***
					(1.9)	(2.8)
Stat. class × Signal					-.166	-.166
					(-1.2)	(-1.2)
Observations	280	280	280	280	280	280
Adjusted R^2	0.31	0.31	0.33	0.32	0.32	0.32

Decomposition works only for imperfect signals

* $p < 0.10$, ** $p < 0.05$, *** $p < 0.01$

Table 11: Informed Protection Response: logit with flexible control for posteriors

	(1)	(2)	(3)	(4)
FP rate	.365***	.472***	.593***	.573***
	(3.3)	(3.4)	(4.0)	(3.7)
FN rate	.168*	.611***	.15	.565**
	(1.8)	(2.8)	(1.5)	(2.5)
p>0.2	.0259	.0664***	.0471*	.0547*
	(1.5)	(2.8)	(1.8)	(2.0)
S=Black	.00422	.426**	-.0229	.473**
	(0.1)	(2.5)	(-0.3)	(2.4)
FP rate x (S=Black)		-.655		-.69
		(-1.4)		(-1.5)
FN rate x (S=Black)		-.561**		-.608**
		(-2.1)		(-2.2)
FP rate x (p>0.2)			-.293**	-.16
			(-2.3)	(-1.2)
FN rate x (p>0.2)			.0843	.264
			(0.5)	(1.6)
Observations	1248	1224	1224	1224
Adjusted R^2				

t statistics in parentheses

Reporting average marginal effects, subject FE, errors are clustered by subject.

With flexible controls of posterior probability

* $p < 0.10$, ** $p < 0.05$, *** $p < 0.01$

Table 12: WTP minus Value of Information: demographic determinants

	(1)	(2)	(3)	(4)	(5)	(6)
FP costs	.283	.352*	.117	.215	.248*	.291**
	(0.2)	(0.2)	(0.2)	(0.2)	(0.1)	(0.1)
FN costs	.322***	.247***	.395***	.303***	.303***	.249***
	(0.1)	(0.1)	(0.1)	(0.1)	(0.1)	(0.1)
Male	-.193	-.157				
	(0.3)	(0.4)				
Male × FP costs	-.153	-.193				
	(0.2)	(0.2)				
Male × FN costs	.0791	.114				
	(0.1)	(0.1)				
Stat. class			-.24	-.142		
			(0.3)	(0.4)		
Stat. class × FP costs			.198	.124		
			(0.3)	(0.3)		
Stat. class × FN costs			-.0834	-.0226		
			(0.1)	(0.1)		
>23 yrs					-.366	-.647*
					(0.4)	(0.4)
>23 yrs × FP costs					-.0679	.0238
					(0.3)	(0.3)
>23 yrs × FN costs					.35	.277
					(0.2)	(0.2)
Constant	-.126	.391	-.0579	.419	-.157	.397*
	(0.2)	(0.3)	(0.3)	(0.4)	(0.2)	(0.2)
Prior dummies	No	Yes	No	Yes	No	Yes
Observations	624	624	624	624	624	624
Adjusted R^2	0.05	0.21	0.05	0.21	0.05	0.21

Standard errors in parentheses

* $p < 0.10$, ** $p < 0.05$, *** $p < 0.01$