

# Data Assimilation Research Testbed Tutorial

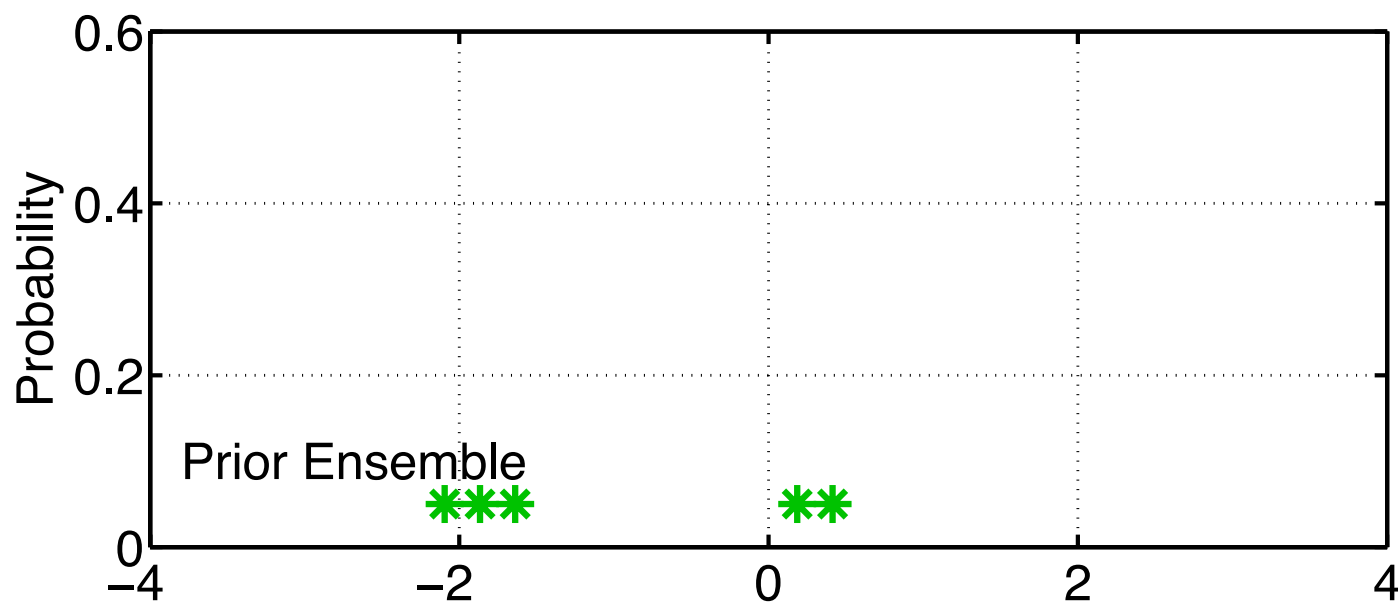


## Section 4: Other Updates for an Observed Variable.

# The Ensemble Kalman Filter (Perturbed Observations)

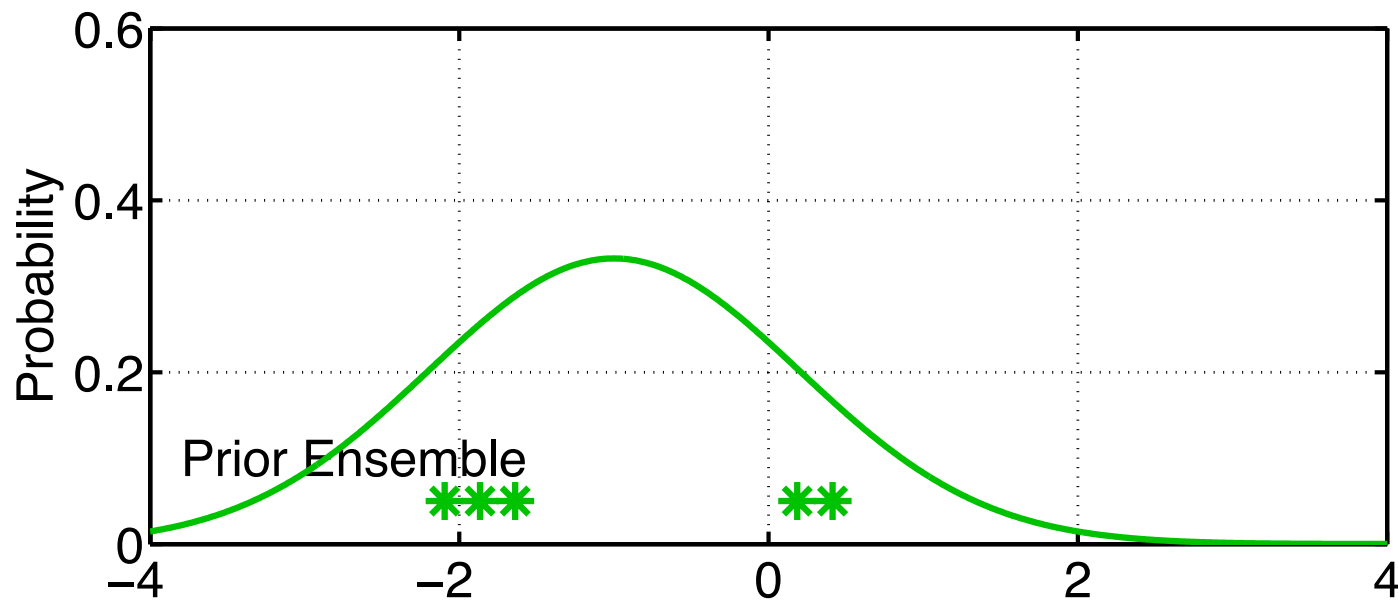
‘Classical’ Monte Carlo algorithm by Evensen.

Note: earliest references have error, use caution.



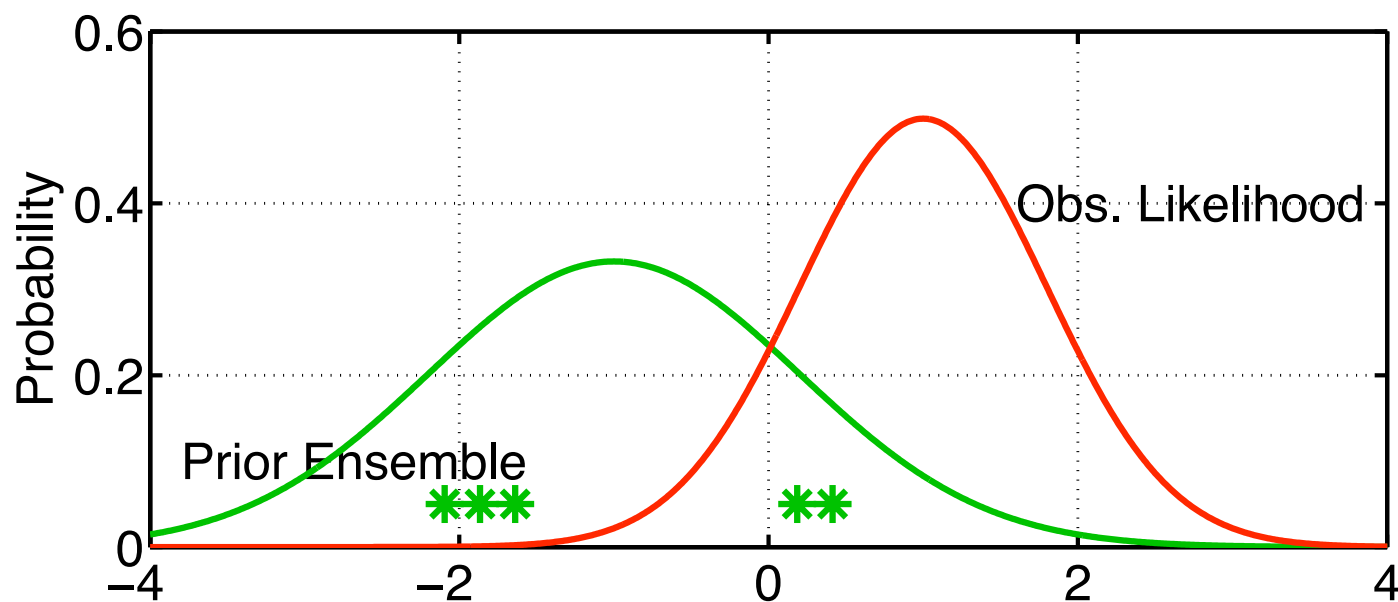
# The Ensemble Kalman Filter (Perturbed Observations)

First fit a gaussian to ensemble sample.



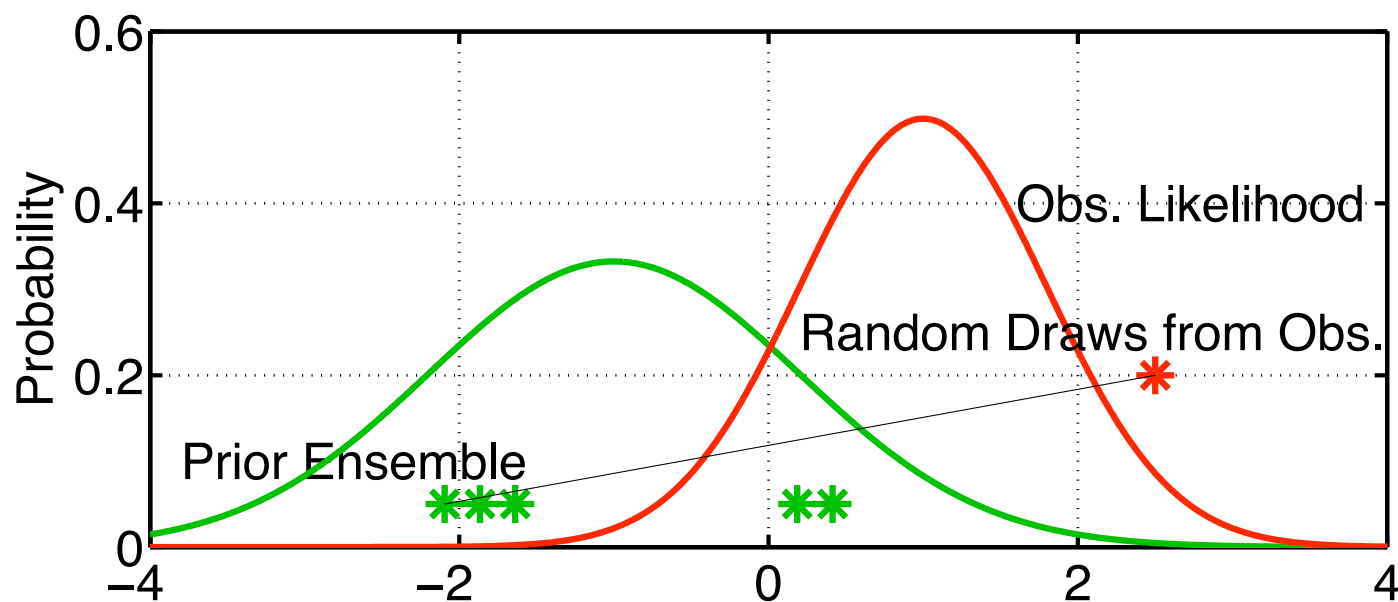
# The Ensemble Kalman Filter (Perturbed Observations)

Obtain observation and observational error distribution.



## The Ensemble Kalman Filter (Perturbed Observations)

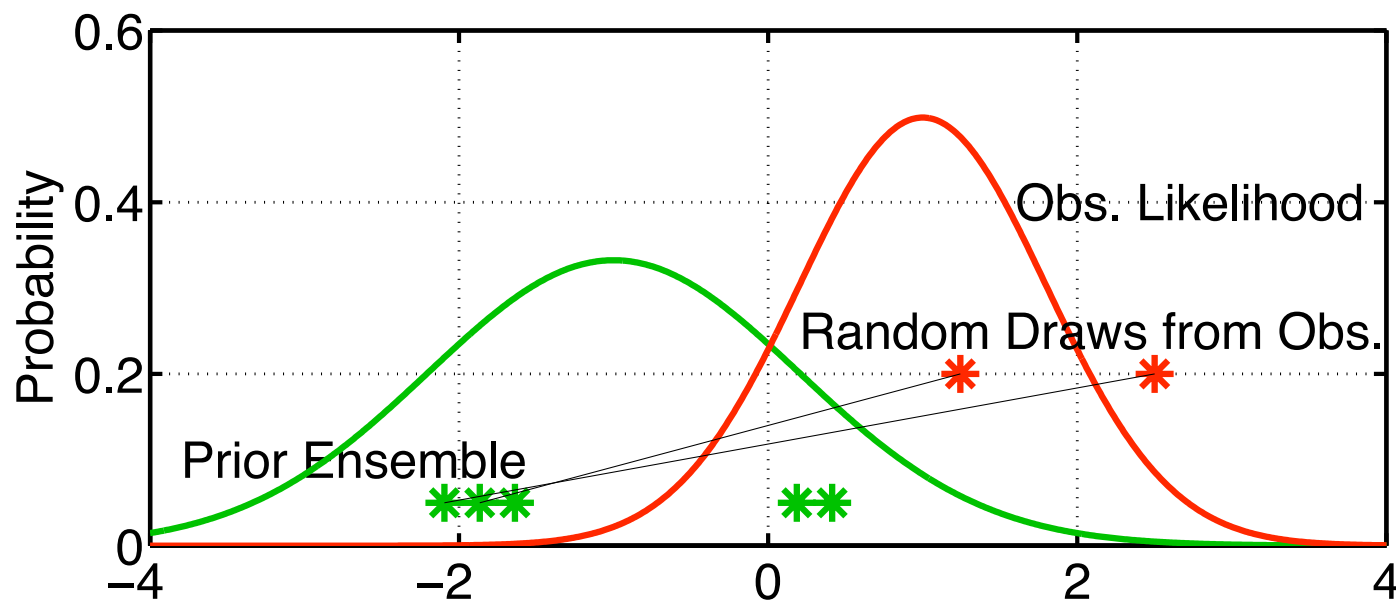
Generate a random draw from the observation likelihood.  
Associate it with the first sample of the prior ensemble.



# The Ensemble Kalman Filter (Perturbed Observations)

Associate a random draw from observation likelihood with each prior ensemble member.

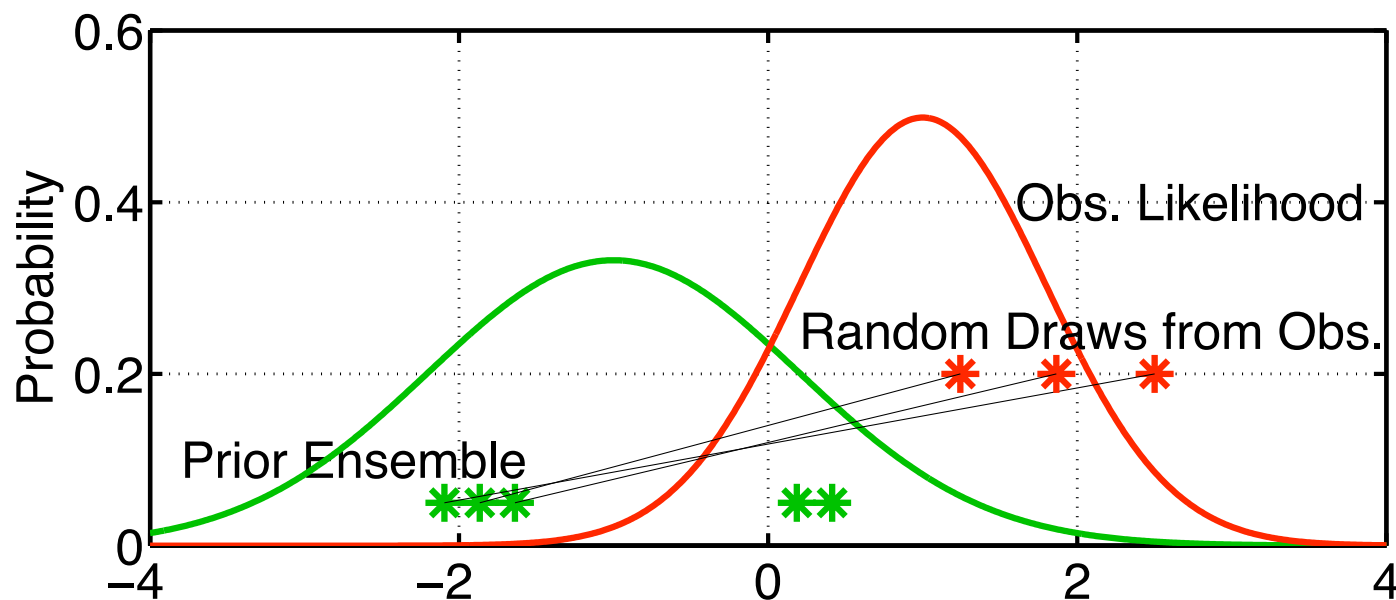
This is called generating perturbed observations.



# The Ensemble Kalman Filter (Perturbed Observations)

Associate a random draw from observation likelihood with each prior ensemble member.

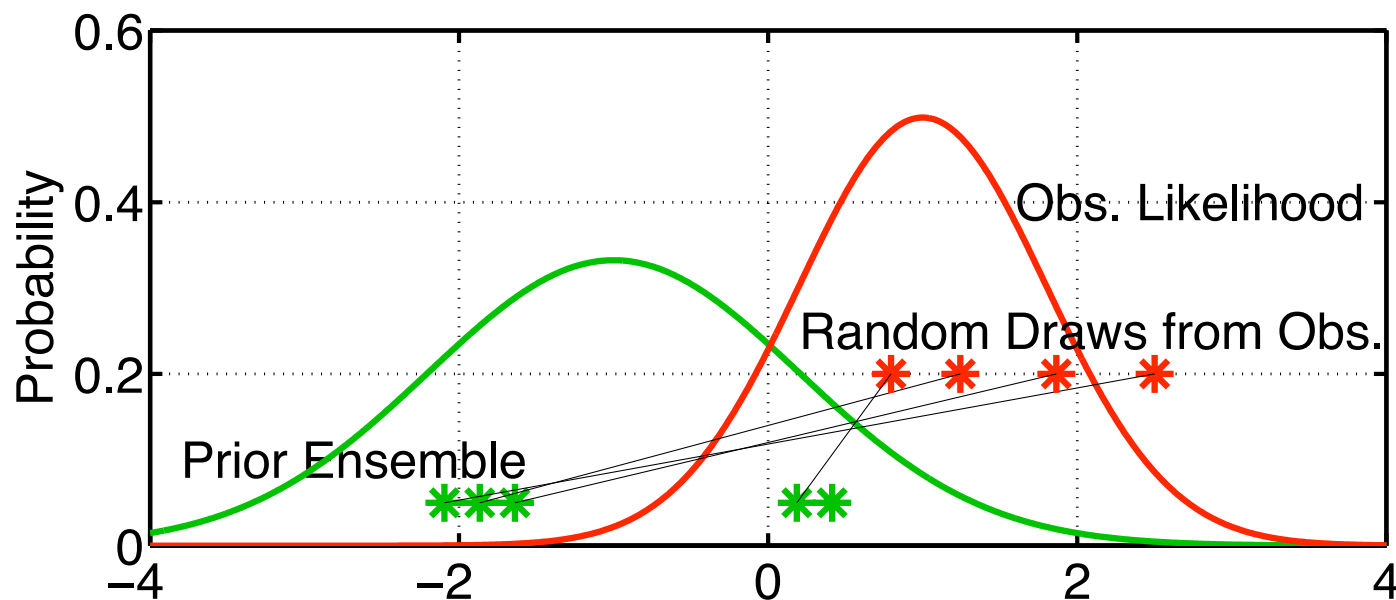
This is called generating perturbed observations.



# The Ensemble Kalman Filter (Perturbed Observations)

Associate a random draw from observation likelihood with each prior ensemble member.

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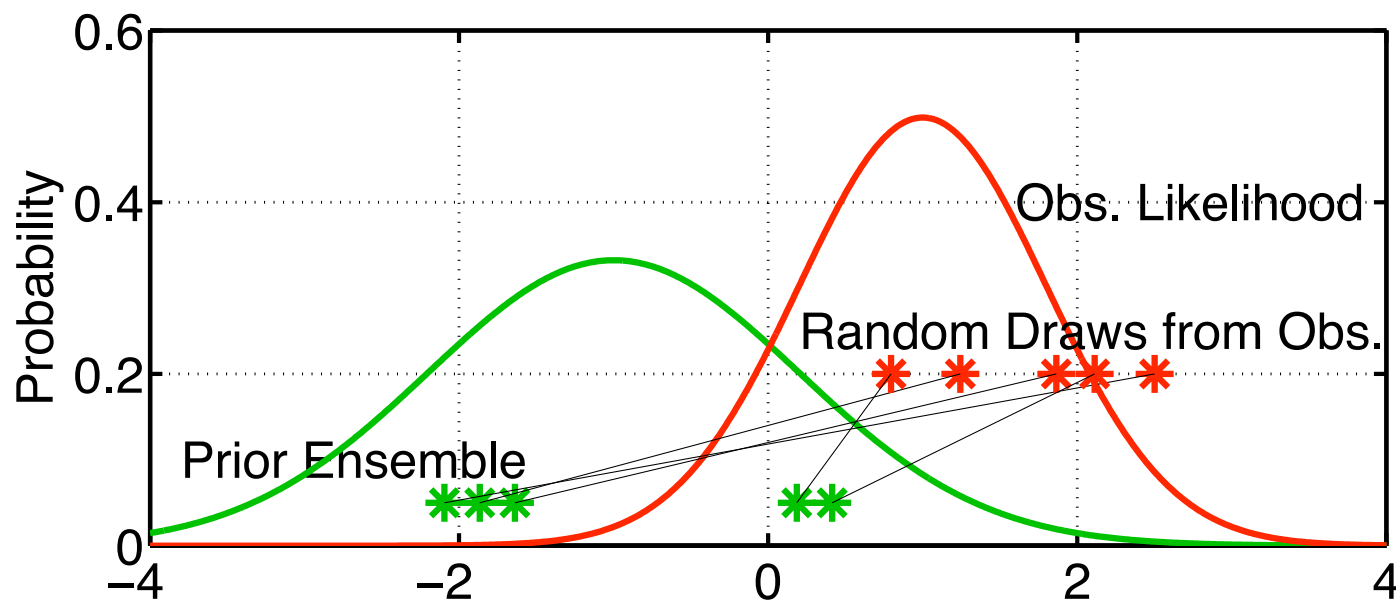




# The Ensemble Kalman Filter (Perturbed Observations)

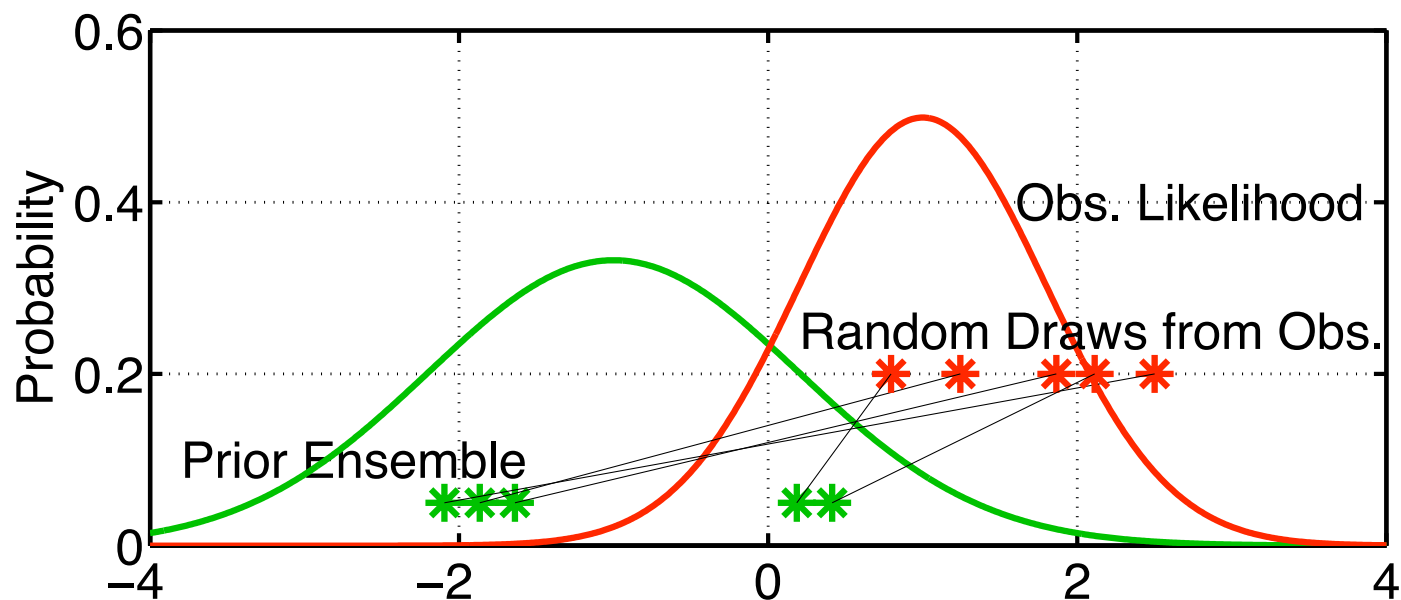
Associate a random draw from observation likelihood with each prior ensemble member.

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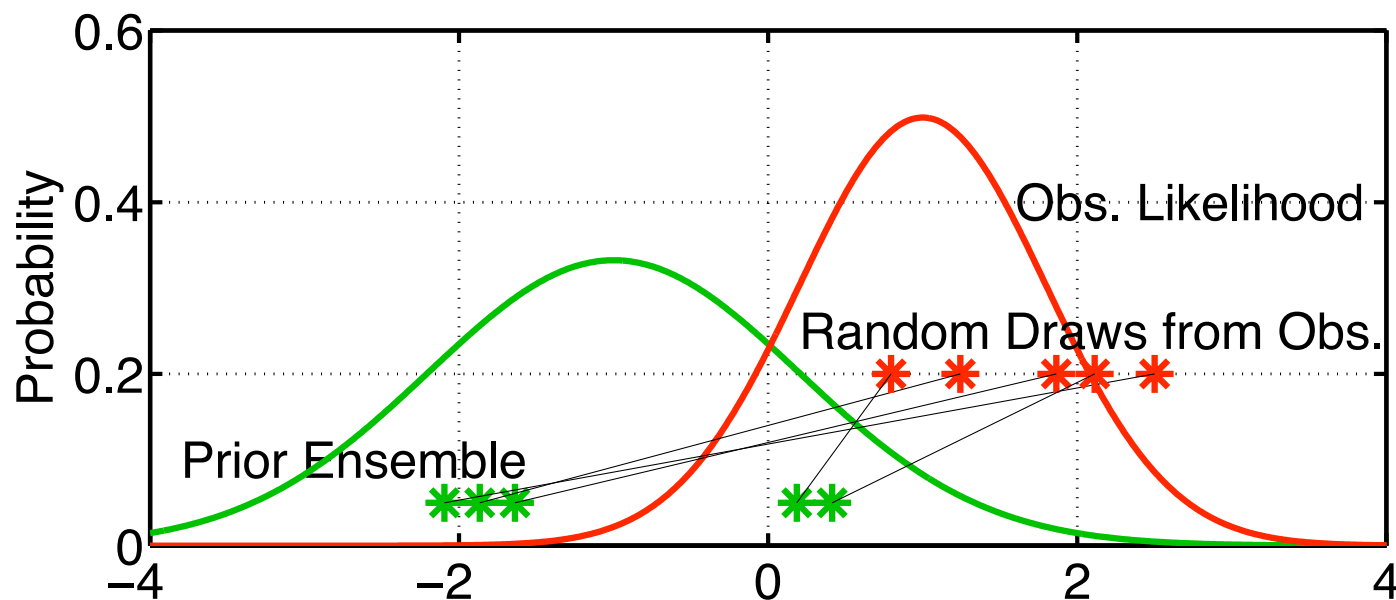
# The Ensemble Kalman Filter (Perturbed Observations)

Have sample of joint distribution of prior and mean and observation.



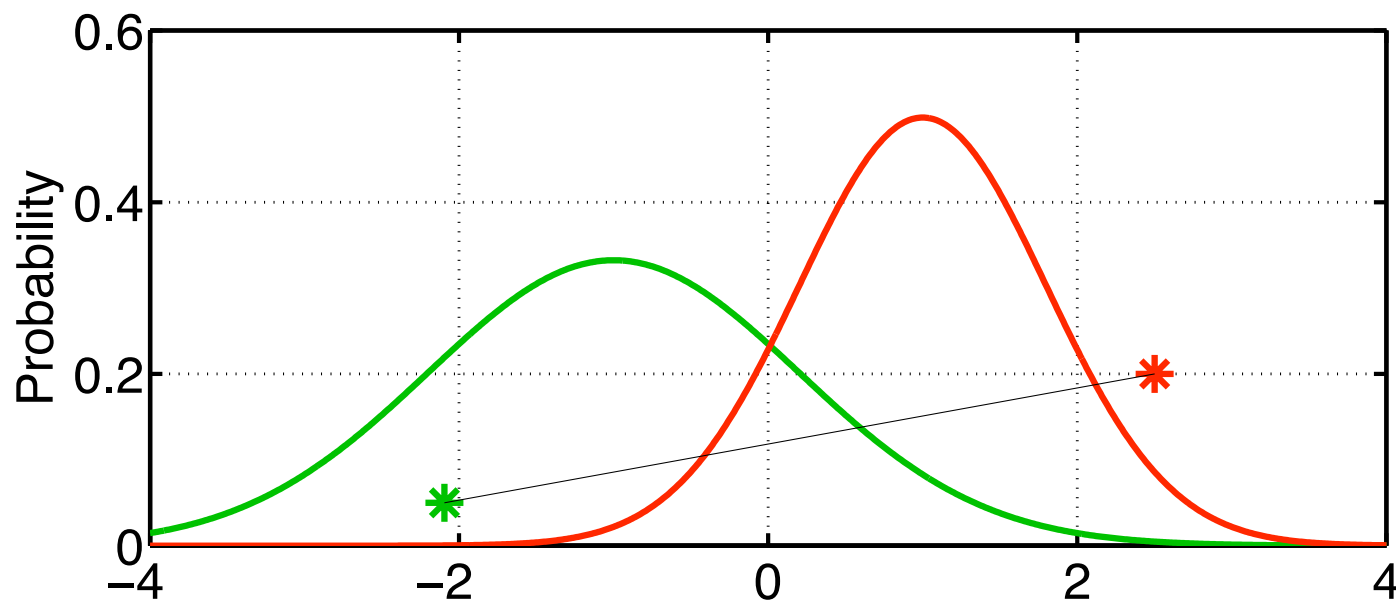
# The Ensemble Kalman Filter (Perturbed Observations)

Adjusting the mean of the observation sample helps.  
Adjusting the variance to be exact may also help (or not).  
Outliers are a potential problem but could be removed.



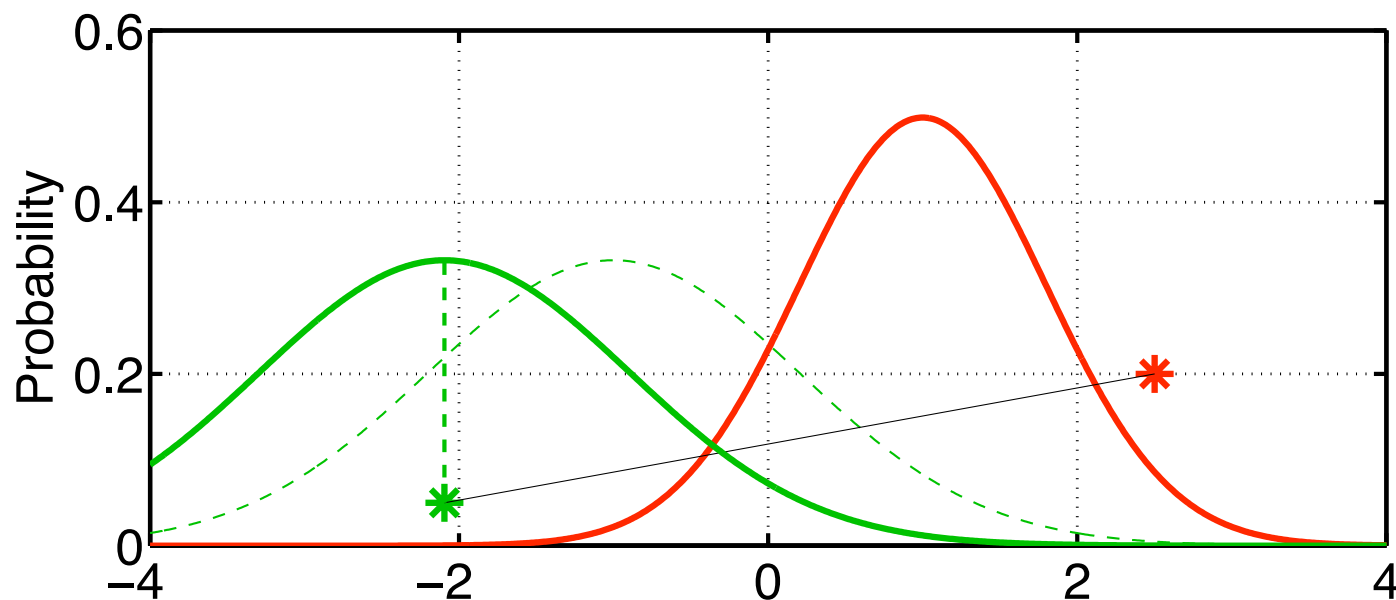
# The Ensemble Kalman Filter (Perturbed Observations)

For each prior/observation pair, find mean of posterior distribution.



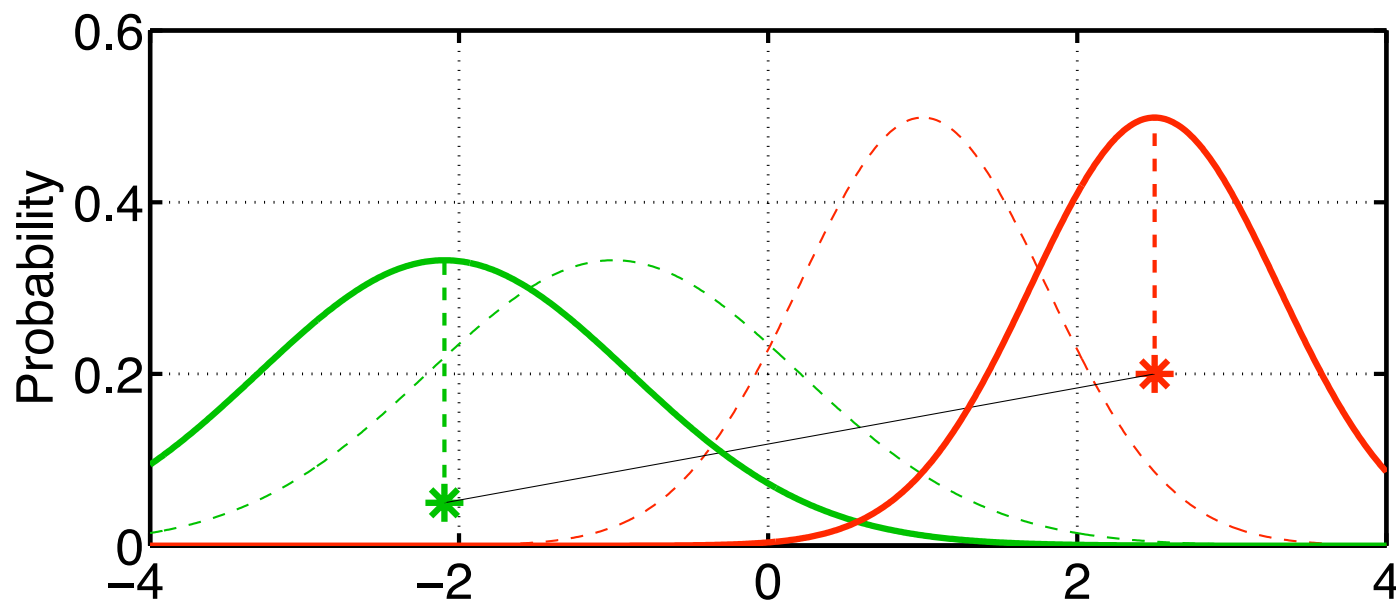
# The Ensemble Kalman Filter (Perturbed Observations)

Prior sample standard deviation measures uncertainty of prior mean estimate.



# The Ensemble Kalman Filter (Perturbed Observations)

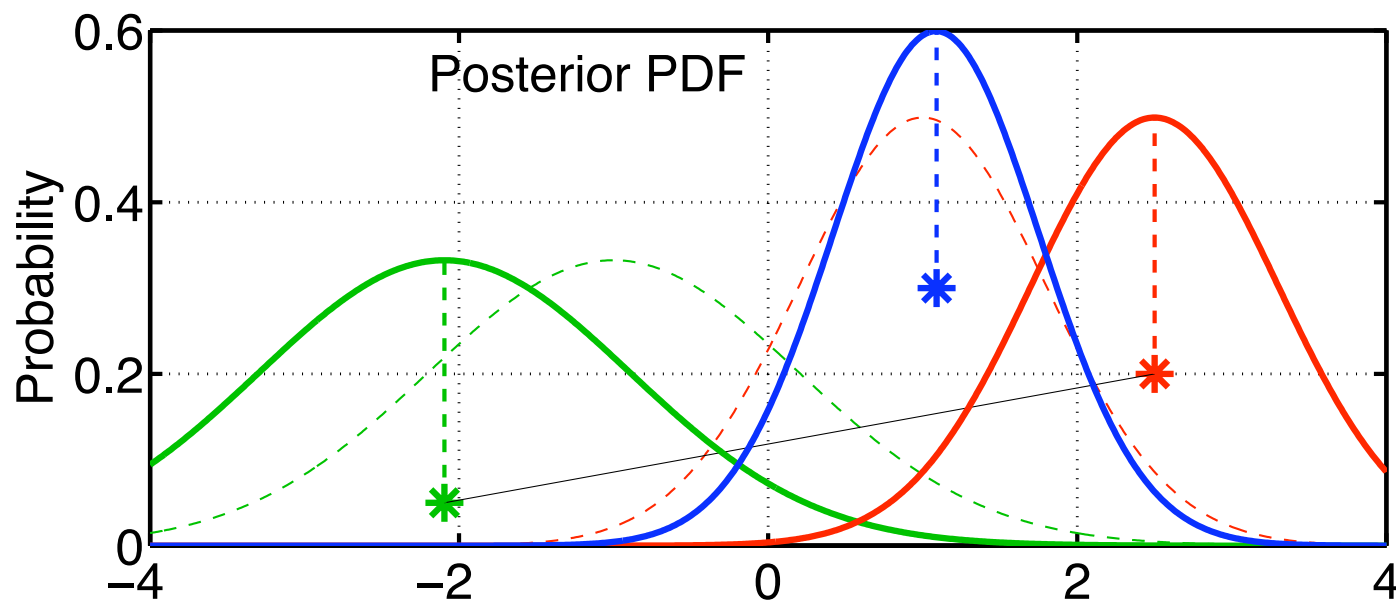
Observation likelihood standard deviation measures uncertainty of observation estimate.



# The Ensemble Kalman Filter (Perturbed Observations)

Take product of the prior and observation distributions for the first sample

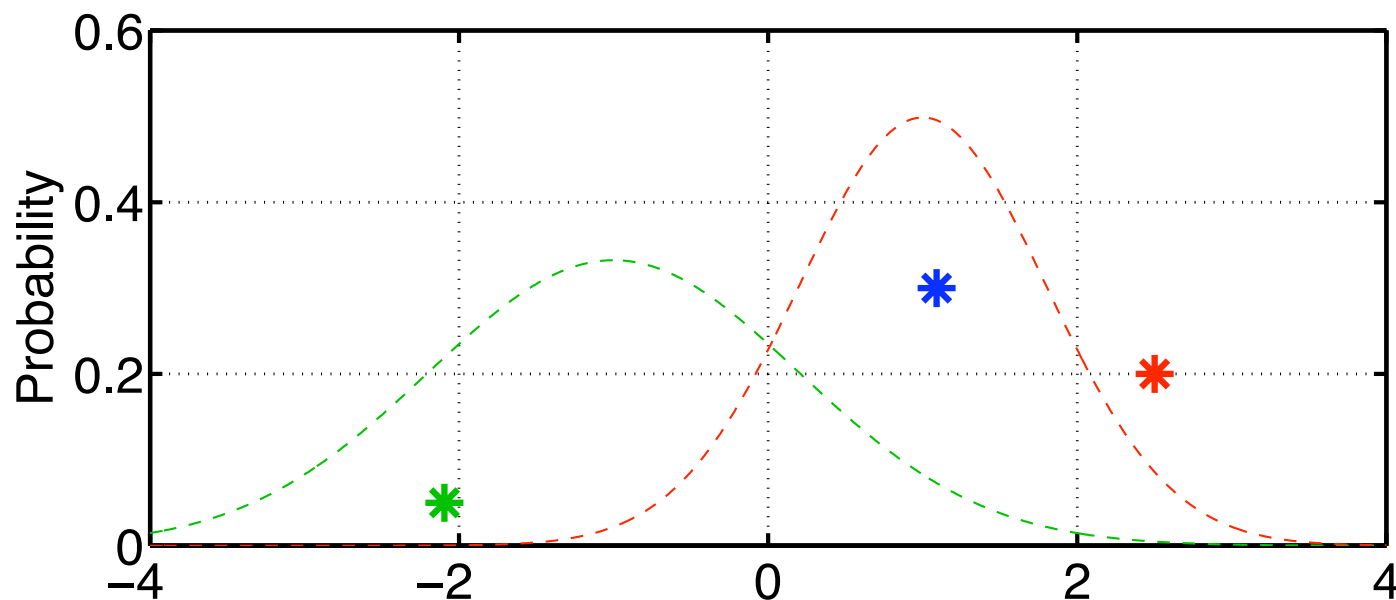
This is a standard product of gaussians.



# The Ensemble Kalman Filter (Perturbed Observations)

Mean of product is random sample of posterior.

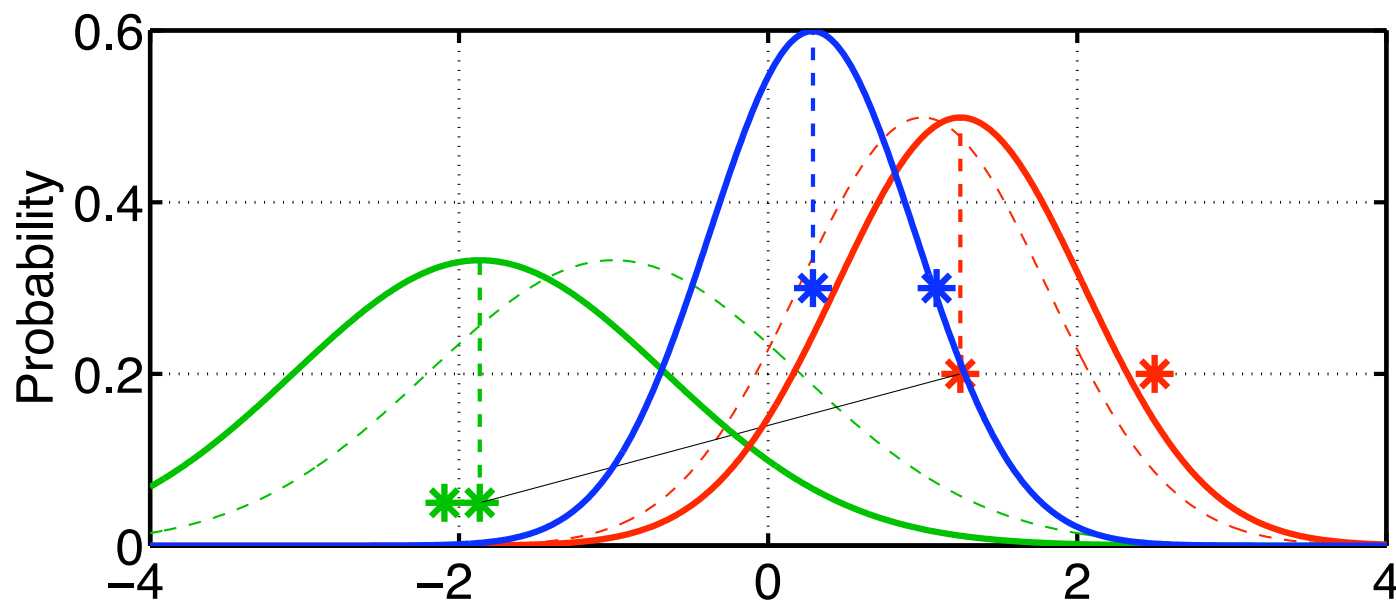
Product of random samples is random sample of product.





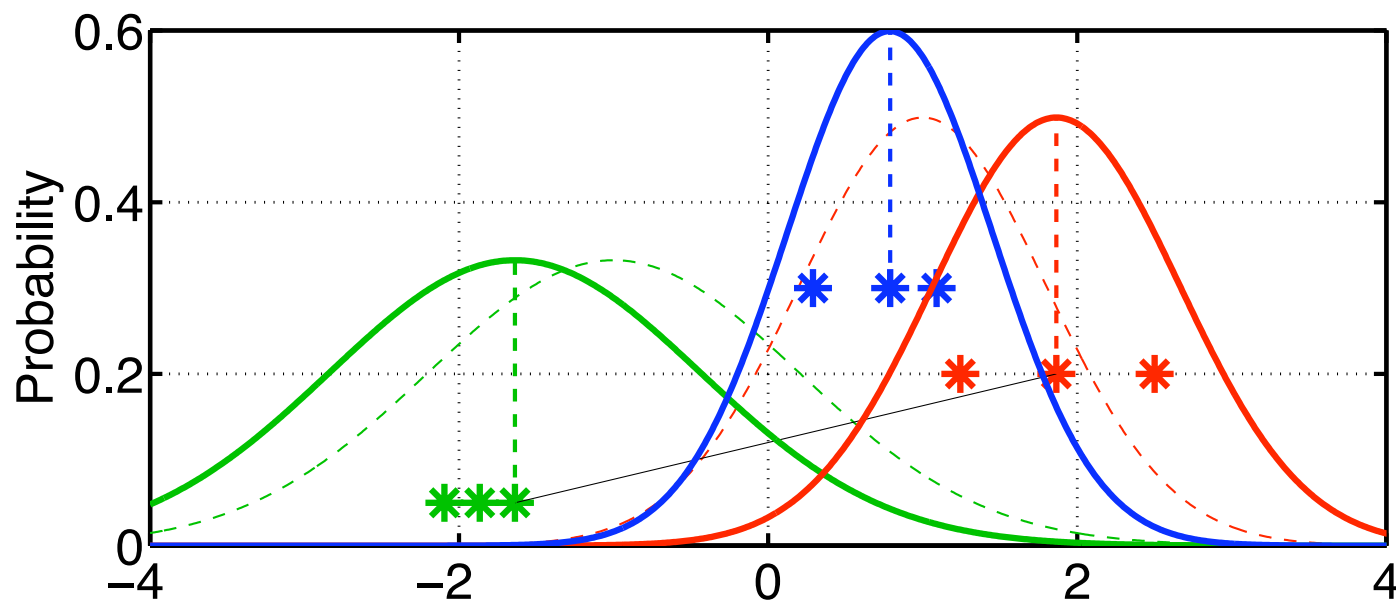
# The Ensemble Kalman Filter (Perturbed Observations)

Repeat this operation for every pair of prior and observation.



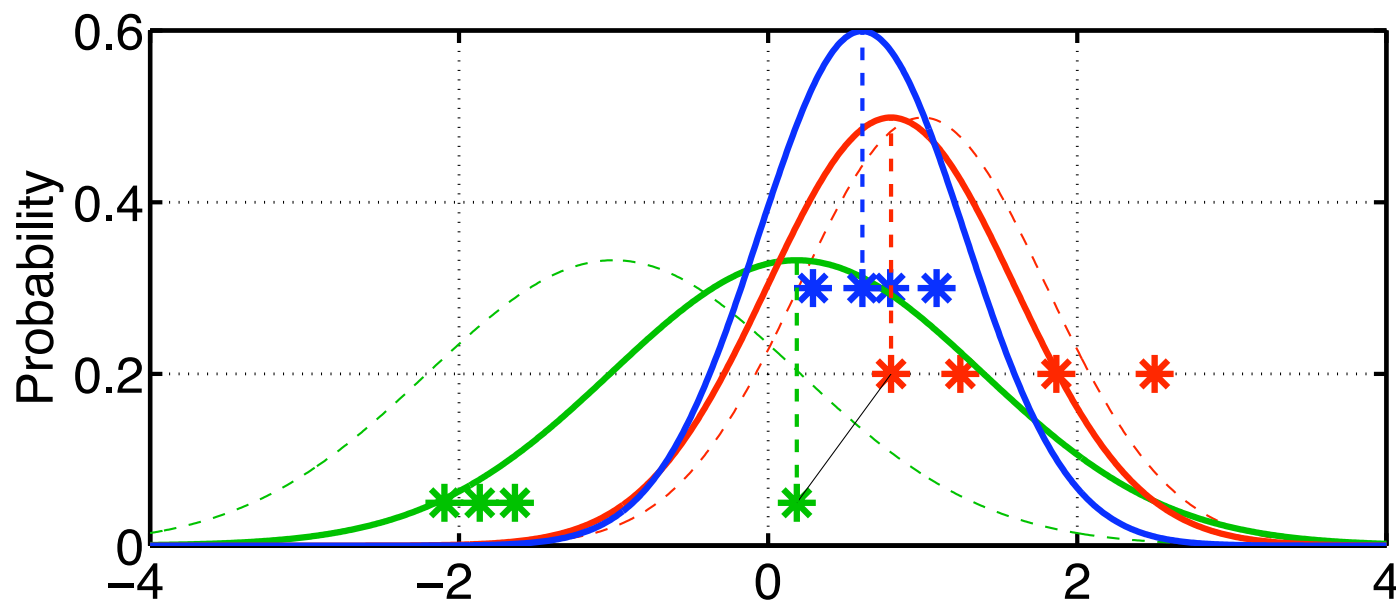
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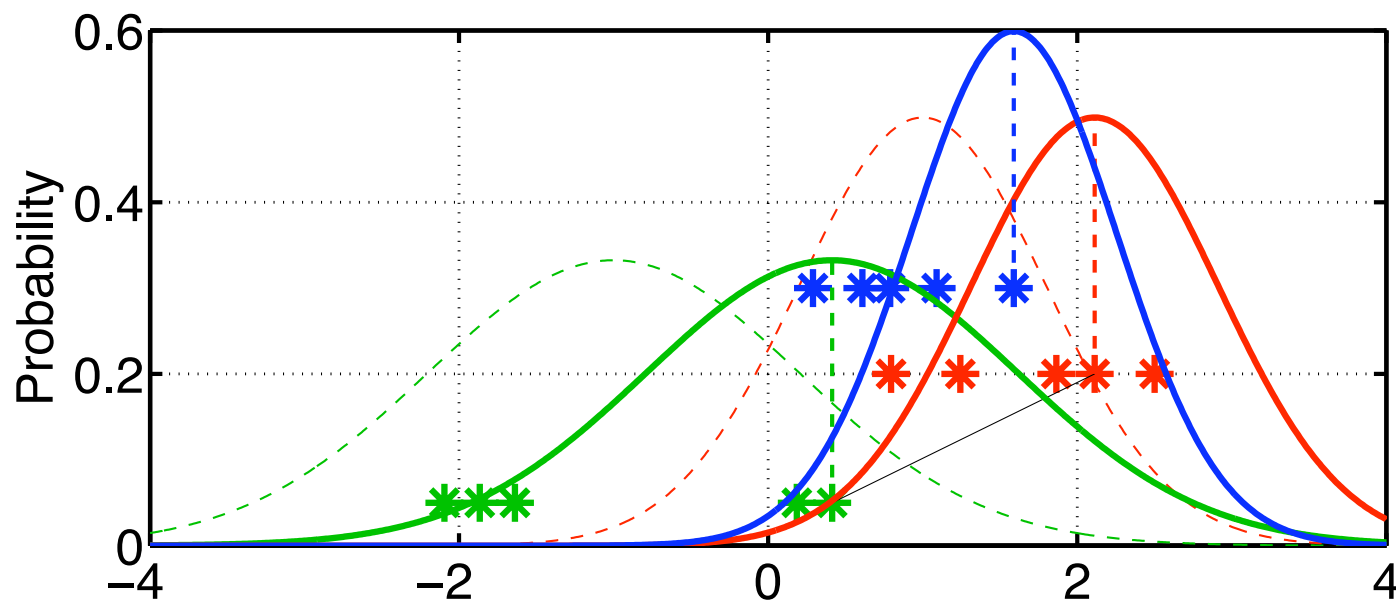
# The Ensemble Kalman Filter (Perturbed Observations)

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# The Ensemble Kalman Filter (Perturbed Observations)

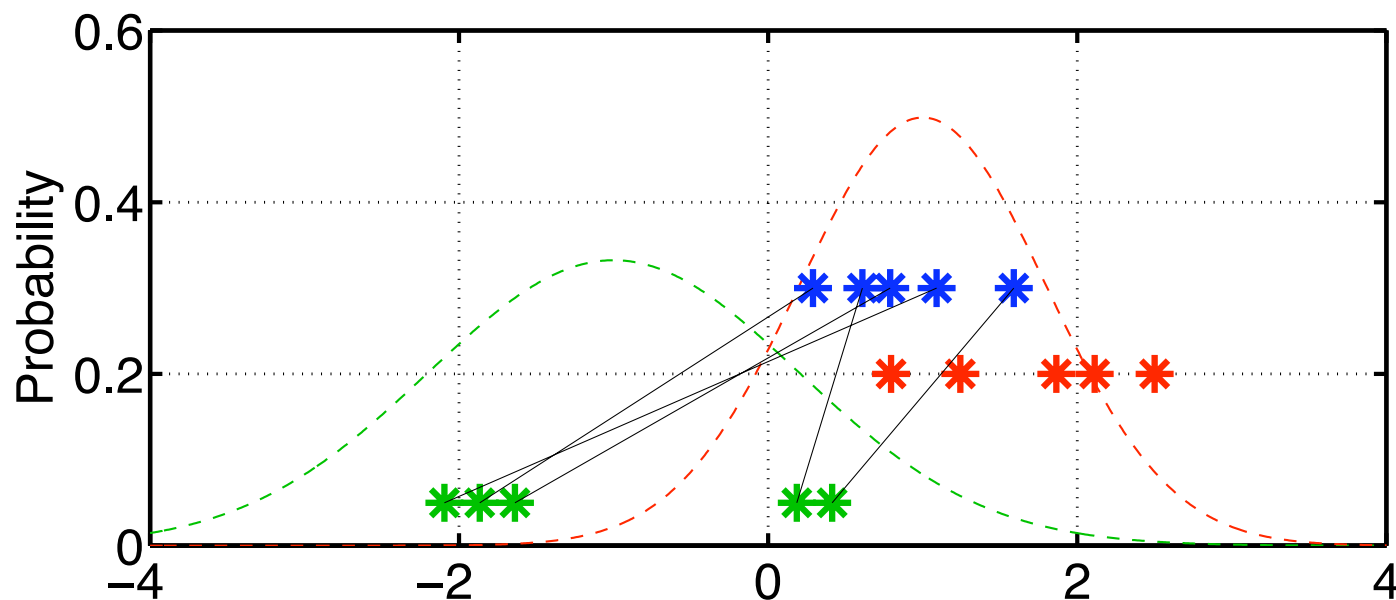
Repeat this operation for every pair of prior and observation.



# The Ensemble Kalman Filter (Perturbed Observations)

Posterior sample retains much of prior samples structure; this is more apparent for larger ensembles.

Posterior sample mean and variance converge as function of ensemble size.



# The Ensemble Kalman Filter (Perturbed Observations)

Matlab exercises `oned_ensemble`, `twod_ensemble`, `oned_model`, `run_lorenz_63` and `run_lorenz_96` all allow selection of EnKF for assimilation.

In `oned_ensemble` and `twod_ensemble`, be sure to try the EnKF repeatedly. It's a stochastic algorithm so produces a different answer each time.