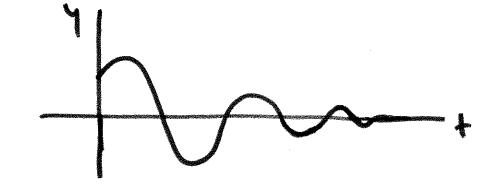
$$48 \quad y'' + 6y' + 13y = 0$$

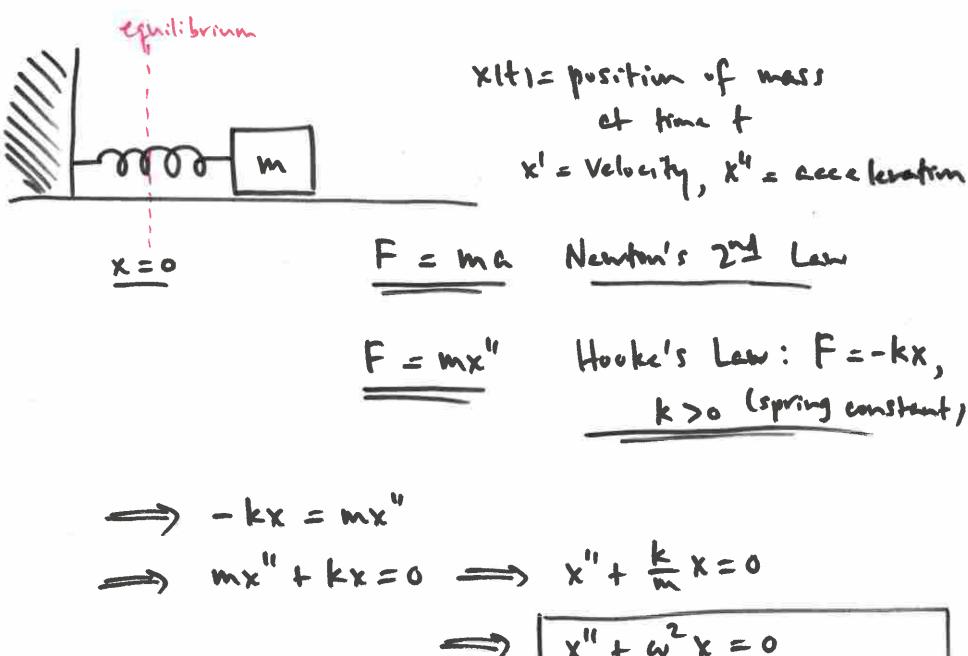
$$y = e^{rt} \implies r^2 + 6r + 13 = 0 \implies r = \frac{-6 \pm \sqrt{36 - 52}}{2}$$

Typical solution:



#13
$$y'' - 2y' + 5y = 0$$
, $y(\frac{\pi}{2}) = 0$, $y'(\frac{\pi}{2}) = 2$
 $r^2 - 2r + 5 = 0 \implies r = \frac{2 \pm \sqrt{y} - 20}{2} = 1 \pm 2i$
 $\Rightarrow \text{ general}: \quad y(t) = c_1 c^{\frac{1}{2}} \cos(2t) + c_2 c^{\frac{1}{2}} \sin(2t)$
 $y(\frac{\pi}{2}) = 0 \implies 0 = c_1 e^{\frac{\pi}{2}} \cos(\pi) + c_2 e^{\frac{\pi}{2}} \sin(\pi) = -c_1 e^{\frac{\pi}{2}}$
 $\Rightarrow c_1 = 0$
 $\Rightarrow y(t) = c e^{\frac{\pi}{2}} \sin(2t)$
 $\Rightarrow y'(t) = c e^{\frac{\pi}{2}} (\sin(\pi) + 2\cos(\pi)) = -2ce^{\frac{\pi}{2}} = 2$
 $\Rightarrow c = -e^{\frac{\pi}{2}}$

Solution of $\text{IVP}: \quad y(t) = -e^{\frac{\pi}{2}} e^{t} \sin(2t)$



$$\Rightarrow x'' + k = 0$$

$$\lambda'' + \omega^2 x = 0$$

$$\omega^2 - k (\omega - \sqrt{k})$$

$$x'' + \omega^2 x = 0$$
, $x = x(t)$
 $\Rightarrow r^2 + \omega^2 = 0 \Rightarrow r = \pm i\omega$
 $\Rightarrow x(t) = c_1 e \omega s(\omega t) + c_2 sin(\omega t)$

Harmonic motion/harmonic oscillator

Friction:

 $F = mx''$, $F = -kx + Yx'$

Hooke friction $Y < 0$
 $\Rightarrow -kx + Yx' = mx''$
 $\Rightarrow -kx + Yx' = mx''$
 $\Rightarrow -kx + Yx' = mx''$
 $\Rightarrow -kx + Yx' = kx = 0$
 $\Rightarrow -kx + Yx' + kx = 0$

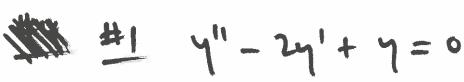
capacitor: like a bettern; changes &

discharges; I = CV'

inductor: wil of wire;

Ve LI'

Kirchhoff: Ve+Ve=0



=> | y2 = tet |

$$e^{rt} \Rightarrow r^2 - 2r + 1 = 0 \Rightarrow r = 1$$

$$\frac{(r - 1)^2 = 0}{}$$

$$\Rightarrow | y_1(t) = e^t$$

$$| y(t) = c_1e^t + c_2e^t$$

$$| y(t) = c_1e^t + c_2e^t$$

$$y_2 = ue^t \implies y_2 = u^1e^t + ue^t$$

$$y_1'' = u^1e^t + u^1e^t + u^1e^t + ue^t$$

$$= u^1e^t + 2u^1e^t + ue^t - 2u^1e^t - 2ue^t + ue^t = 0$$

$$\implies u^1e^t = 0 \implies u^1 = 0 \implies u^1 = at + X$$