## Stat 204 Exam 1 Due 4/16/20

- 1. The book's **Atlanta Commute (distance)** dataset provides the commute distances in miles for 500 randomly chosen people who work in the Atlanta metropolitan area.
- a. Use StatKey to obtain the mean and standard deviation of the commute distances in this sample.
- b. Use *StatKey* to create 5000 bootstrap samples and a bootstrap distribution of bootstrap sample means. What are the mean and standard error of your bootstrap distribution?
- c. What does the formula in Section 6.2 say the standard error should be? How does this theoretical result compare to the standard error of your bootstrap distribution?
- d. Use *StatKey* and your bootstrap distribution to find 90%, 95%, and 99% confidence intervals for the average commute distance of workers in the Atlanta metropolitan area. Determine the margin of error for each of these confidence intervals. What happens to the margin of error as the confidence level increases?
- e. Someone claims that the average commute distance for workers in the Atlanta metropolitan area is 20 miles. State the corresponding null and alternative hypotheses, compute the relevant t-statistic using this sample's average and standard deviation, and use StatKey to compute the p-value. What do you conclude about this person's claim?
- f. In the previous question, you computed a t-score to test a hypothesis. How many degrees of freedom are there for this sample? If you interpret the t-score you just computed as a z-score, what is the p-value? Explain.
- 2. To analyze how well lie detectors perform when subjects are stressed, 48 randomly chosen subjects were connected to a lie detector and asked to read true statements out loud while receiving an electric shock. The lie detector incorrectly reported that 27 of the 48 participants were lying.

**Note**: For this problem, you will have to enter the data into *StatKey*. In particular, do not use the book's *Lie Detector (Missed a lie)* dataset to answer the following questions!

- a. Use *StatKey* to determine the best estimate, based on this data, of the proportion of times the lie detector yields false positives, i.e., inaccurately reports deception.
- b. Use *StatKey* to create 5000 bootstrap samples and a bootstrap distribution of bootstrap sample proportions. What are the center and standard error of your bootstrap distribution?
- c. What does the formula in Section 6.1 say the standard error should be? How does this theoretical result compare to the standard error of your bootstrap distribution?

- d. Use *StatKey* and your bootstrap distribution to find a 95% confidence interval for the overall percentage of false positives reported by the lie detector.
- e. Does this sample provide evidence that lie detectors give innacurate results more than half the time when subjects are stressed? State the relevant null and alternative hypotheses, use *StatKey* to create a randomization distribution based on this sample and the null hypothesis, obtain the *p*-value, and state your conclusion clearly.
- f. You just used a randomization distribution to test whether we have evidence that lie detectors give innacurate results more than half the time when subjects are stressed. Conduct the same hypothesis test by applying the theoretical method from Section 6.1: compute the relevant z-score, obtain the p-value from the normal distribution, and state your conclusion.
- 3. Is sleep or caffeine better for memory? To answer this question, 24 randomly chosen adults were divided equally into two groups and given a list of 24 words to memorize. During a break, members of one group took a 90-minute nap while members of the other group each took a caffeine pill. They were then all tested to see how many of the words they could remember; the results are in the book's **Sleep Caffeine Words** dataset.
- a. State the relevant null and alternative hypotheses.
- b. Use *StatKey* to create a randomization distribution based on this data and the null hypothesis, obtain the *p*-value, and state your conclusion clearly.
- 4. To investigate the influence of smoking on pregnancy, a study collected data on 678 women who had gone off birth control with the intent of becoming pregnant. The data are given in Table A.8 (after problem A.51 in the Review Exercises for Unit A) and Table B.8 (after problem B.32 in the Review Exercises for Unit B) and are available in the book's *Get Pregnant (by Smoker Status)* dataset.
- a. Was this an experiment or an observational study?
- b. Determine the following:
- the overall proportion of women who became pregnant
- the proportion of smokers who became pregnant
- the proportion of non-smokers who became pregnant
- the difference in proportions between smokers and non-smokers
- c. Use StatKey to obtain a 95% confidence interval for the relevant difference in proportions.
- d. Based on this data, is there evidence that the proportion of successful pregnancies is lower among smokers than non-smokers? State the relevant null and alternative hypotheses, use *StatKey* to create a randomization distribution based on this data and the null hypothesis, obtain the *p*-value, and state your conclusion clearly.
- 5. Do problem 6.124 from the Exercises for Section 6.2-HT. Be sure to state the relevant hypotheses, show the steps involved in computing your t-score, and explain your answers with complete sentences.