

LES of Turbulent Flows: Project #1

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Fall 2016



① Overview of Project #1



- The ultimate test of an LES SFS model is to examine its performance in actual turbulent flow simulations
- Many different types of flows have been used for this purpose. Homogeneous turbulent flows are popular candidates, including
 - homogeneous shear flow
 - rotating turbulence
 - forced isotropic turbulence
 - decaying isotropic turbulence
- These flows are chosen for many reasons including lack of difficulties associated with filtering and modeling at boundary conditions and the relative ease (compared to more complex flows) in analyzing the resulting turbulent flow fields



- In addition to these traditional flows used to study the performance of LES SFS models, researchers have also used simplified mathematical models
- One example is the stochastic Burgers equation (or Burgulence) to test models (e.g., Basu, 2009).
- This offers the advantage of simple model implementation and overall low computational costs (even for DNS).



Project Description

- The class project will be to conduct your own *a posteriori* study of SFS models
- You will do this using the provided Burgers turbulence code (Matlab). The minimum requirement will be to examine three SFS models
- You will submit the assignment in the form of a short report (maximum of 4-5 pages, including references and figures)
- In this project, you will need to implement the models in the provided stochastic 1D Burgers equation code



Project Description

- Don't just implement the two easiest models that you can find (the code already includes constant coefficient Smagorinsky model)
- Choose models based on their properties that make them ideal for your problem of interest
- Don't feel confined to the limited description given here and contact me if you want to do something closer to your research topic but are unsure of how to proceed
- The project report is due by Tuesday November 22nd



Report Components

- The report should contain the following components (or equivalent)
- You don't need to think of this list as defining the sections of your paper, rather it offers key elements that I will be looking for



- A brief introduction explaining the general idea of LES and the goal of your study. You don't have to show all the LES equations, but you must include at least a description of the LES methodology. This includes a description of scale separation using a low-pass filter and the closure problem (*i.e.*, what SFS stress term must be modeled). You should also briefly describe the rationale of using the 1D filtered Burgers equation as a model for the full LES equations.



- A description of the three models you have chosen to evaluate, including at least their general basis, any key assumptions they make, and any interesting model coefficients etc. that they use.



Report Components

- A short description of the numerical implementation (e.g., pseudospectral methods, etc.). The Matlab code that you will be using is based on Basu (2009) and will be discussed during the next lecture. You should make sure to mention:
 - numerical methods used to solve the equation
 - initial conditions
 - simulation parameters that govern the evolution and initial velocity field
 - grid resolution and time step that you used for each case and the total execution time – also specify the type of computer used and version of Matlab



- You should cite references when possible, although citing a reference does not completely get you off the hook from describing the code you are using. The requirement is that an informed reader (in numerical methods and turbulence) doesn't have to check the references just to get a basic idea of your numerical treatment. I expect your description to be as brief as possible.



Report Components

- Key results (statistical) from your study.
- A summary of the major findings from your study. It is fine if these are similar results to what has been found previously or are not completely conclusive. Still, your summary should demonstrate knowledge of the models you tested and their strengths, limitations, and any differences.
- Any references you used in your report

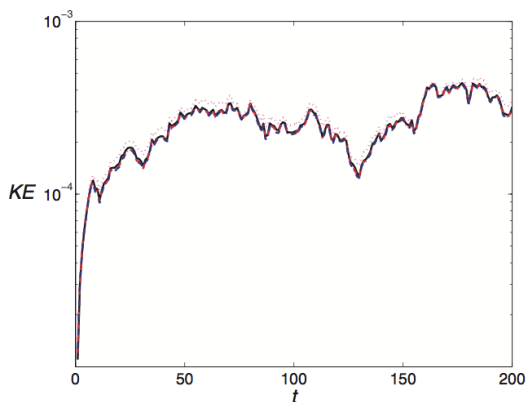


- Your report should give as a minimum the following statistics.
- Note, you are encouraged to calculate other relevant turbulence and SFS statistics depending on your application/interests and the models that you choose to study.
- All statistics should be compared to statistics calculated from the provided DNS data or your own DNS run.



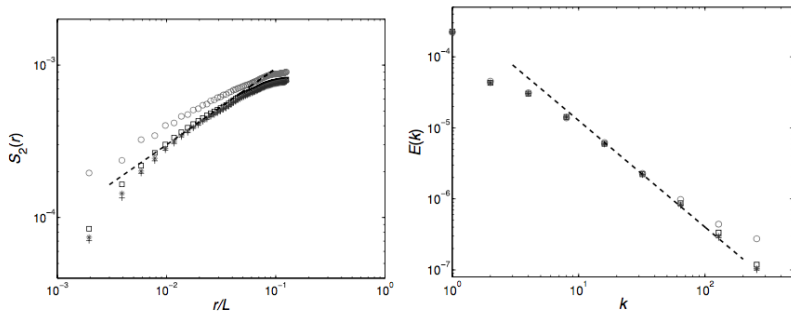
Comparison Statistics

- Evolution of the kinetic energy (KE) for the entire flow field and how it adjusts with time for each model and for at least two filter widths Δ (see Basu figure 6).



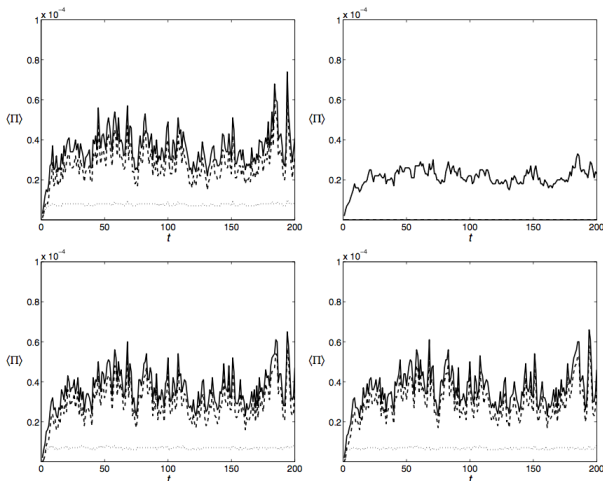
Comparison Statistics

- The second-order structure function and energy spectrum of the velocity both averaged over 100 time increments for each model and for at least two filter widths Δ (see Basu figure 7).



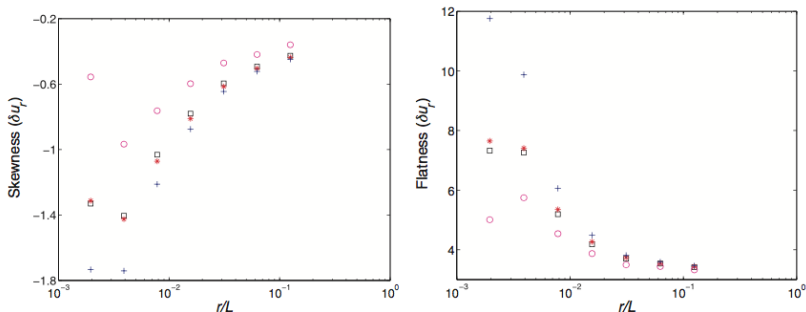
Comparison Statistics

- A plot of the temporal evolution of the mean SFS, molecular, and total energy dissipation for each of your chosen models for at least two filter widths Δ (see Basu figure 8).



Comparison Statistics

- The centralized skewness and flatness factors of the velocity increments as functions of the separation distance for each tested SFS model for at least two filter widths (see Basu figures 3 and 10).



- **Procedurally**, you will calculate your DNS statistics by first separating the velocity field into resolved and SFS components by calculating \tilde{u} and $\widetilde{u^2}$ where the tilde (\sim) is a filter at scale Δ
- Note, calculating $\widetilde{u^2}$ means filtering the product u^2
- Use one of the common filters discussed in class (and that you used in homework #2) that is appropriate for the model you are comparing to.
- Once you have the filtered fields you can calculate the exact SFS stress tensor $\tau^\Delta = \widetilde{u^2} - \tilde{u}\tilde{u}$ and the exact filtered strain rate tensor (simply the filtered velocity derivative in this context)



- You will also need to calculate the other statistics listed above to compare with
- This is an important step when comparing LES to DNS data to make sure that the effect of filter shape is included in the analysis (e.g., for spectra) and that you are comparing the same statistics



Once again, the due date

- The project report is due by Tuesday November 22nd.
- Please don't hesitate to contact me with any questions or problems

