

# Étude MCMC - MixtureOfUniforms

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1<sup>er</sup> avril 2025

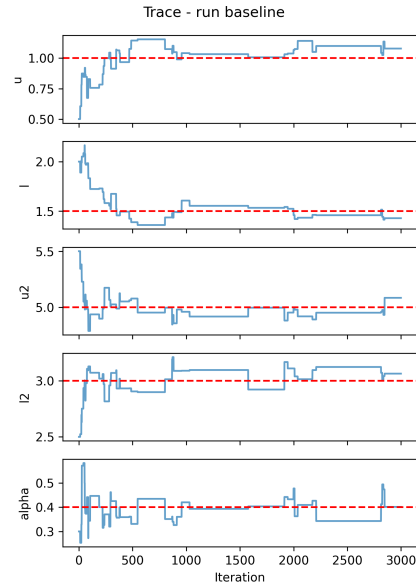
## 1 Explication de l'Expérience

Nous considérons un mélange de deux lois Uniform. Les paramètres  $(u, l)$  définissent la première loi  $\text{Uniform}(u, u + l)$ , tandis que  $(u2, l2)$  définissent la seconde loi  $\text{Uniform}(u2, u2 + l2)$ . Une observation est tirée de la première loi avec probabilité  $\alpha$ , et de la seconde loi sinon. Nous cherchons à estimer  $(u, l, u2, l2, \alpha)$  par MCMC et à mesurer l'erreur de convergence.

## 2 Baseline

Si un run est étiqueté **baseline**, nous le présentons ci-dessous, puis comparons les autres runs qui ne diffèrent de **baseline** que par un seul paramètre.

Run baseline	
$N$	200
bandwidth	0.05
n_sim	2000
proposal_scale	0.1
n_iter	3000
pm_u	1.06
pm_l	1.49
pm_u2	4.96
pm_l2	3.06
pm_alpha	0.38
err_u	0.065
err_l	0.011
err_u2	0.041
err_l2	0.063
err_alpha	0.016
err_global	0.101



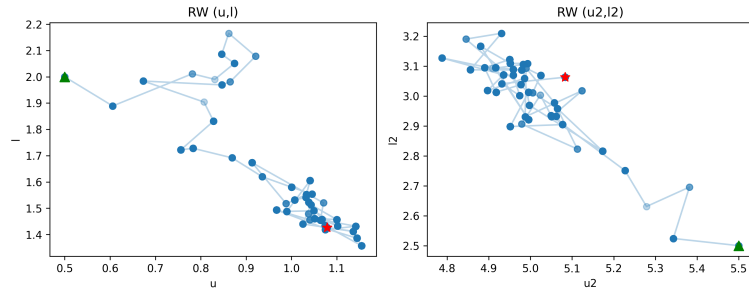


FIGURE 1 – Random-walk pour run baseline

## Variation de $n_{\text{sim}}$

Run nsim_low	
$N$	200
bandwidth	0.05
$n_{\text{sim}}$	500
proposal_scale	0.1
$n_{\text{iter}}$	3000
$\text{pm}_u$	0.79
$\text{pm}_l$	1.76
$\text{pm}_{u2}$	5.02
$\text{pm}_{l2}$	3.02
$\text{pm}_{\alpha}$	0.51
$\text{err}_u$	0.205
$\text{err}_l$	0.259
$\text{err}_{u2}$	0.017
$\text{err}_{l2}$	0.015
$\text{err}_{\alpha}$	0.115
$\text{err}_{\text{global}}$	0.351

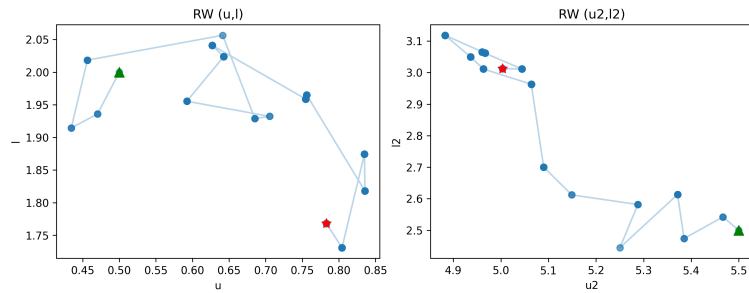
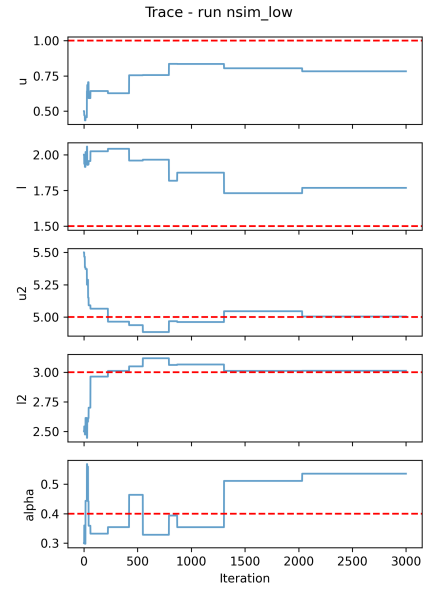


FIGURE 2 – Random-walk pour run nsim\_low

Run nsim_high	
$N$	200
bandwidth	0.05
n_sim	5000
proposal_scale	0.1
n_iter	3000
pm_u	0.99
pm_l	1.56
pm_u2	4.95
pm_l2	2.99
pm_alpha	0.34
err_u	0.013
err_l	0.056
err_u2	0.050
err_l2	0.015
err_alpha	0.056
err_global	0.096

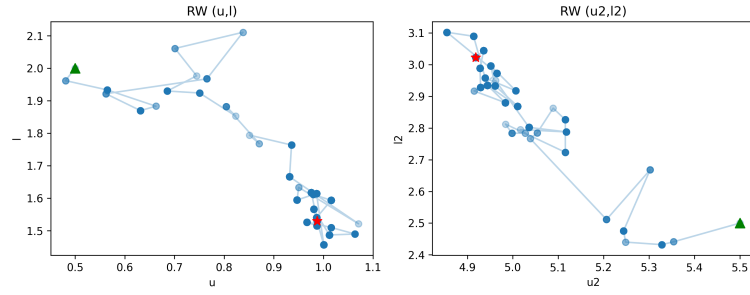
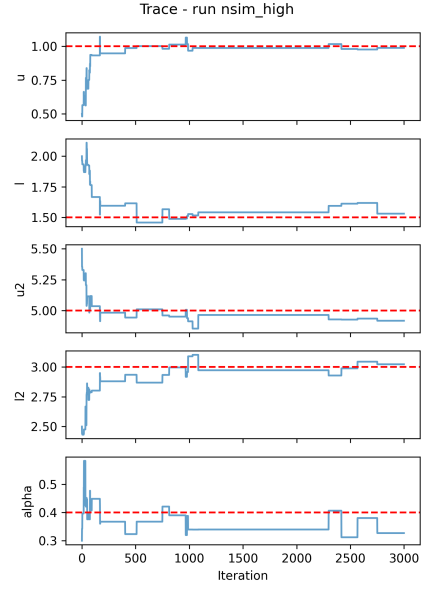


FIGURE 3 – Random-walk pour run nsim\_high

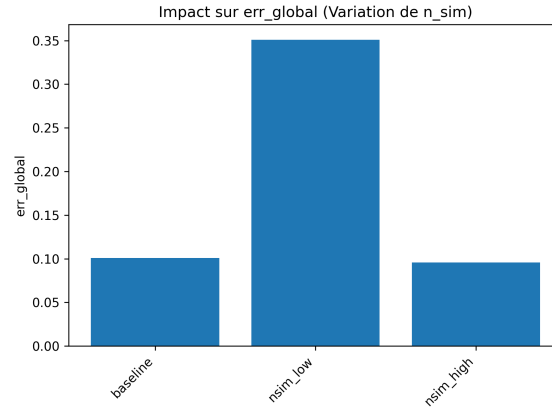
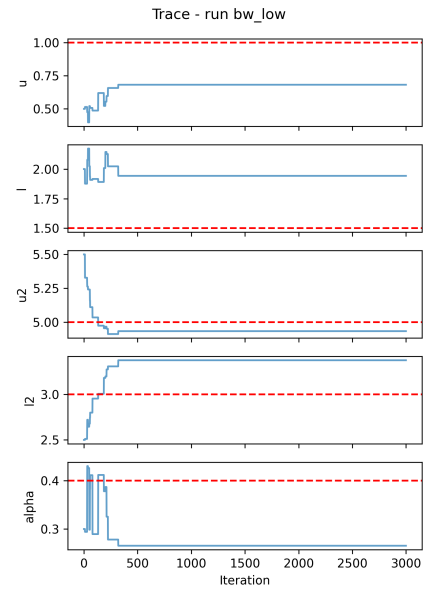


FIGURE 4 – Comparaison de  $\text{err\_global}$  (baseline vs variations de  $n\_sim$ )

## Variation de bandwidth

Run bw_low	
$N$	200
bandwidth	0.01
$n\_sim$	2000
proposal_scale	0.1
$n\_iter$	3000
$pm\_u$	0.68
$pm\_l$	1.94
$pm\_u2$	4.93
$pm\_l2$	3.38
$pm\_alpha$	0.27
$err\_u$	0.318
$err\_l$	0.443
$err\_u2$	0.067
$err\_l2$	0.375
$err\_alpha$	0.135
$err\_global$	0.678



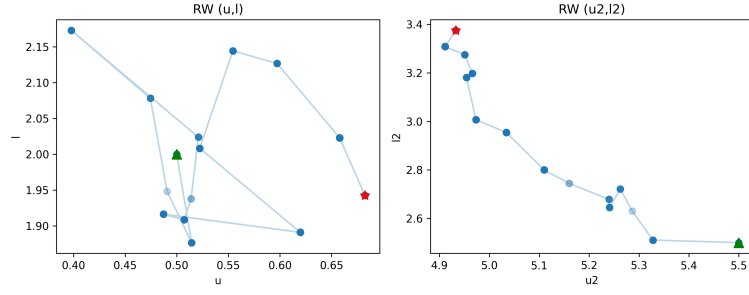


FIGURE 5 – Random-walk pour run **bw\_low**

Run <b>bw_high</b>	
$N$	200
bandwidth	0.1
n_sim	2000
proposal_scale	0.1
n_iter	3000
pm_u	1.06
pm_l	1.43
pm_u2	5.09
pm_l2	2.85
pm_alpha	0.38
err_u	0.057
err_l	0.069
err_u2	0.092
err_l2	0.155
err_alpha	0.024
err_global	0.203

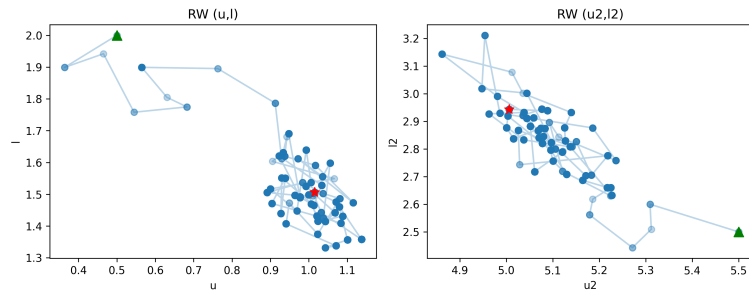
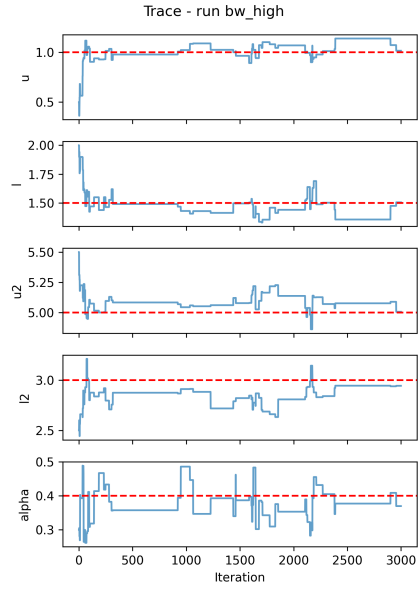


FIGURE 6 – Random-walk pour run **bw\_high**

Run bw_higher	
$N$	200
bandwidth	0.5
n_sim	2000
proposal_scale	0.1
n_iter	3000
pm_u	1.39
pm_l	1.27
pm_u2	4.95
pm_l2	2.38
pm_alpha	0.46
err_u	0.389
err_l	0.229
err_u2	0.047
err_l2	0.618
err_alpha	0.058
err_global	0.769

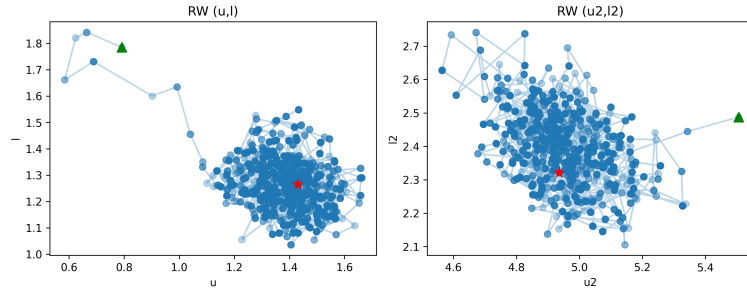
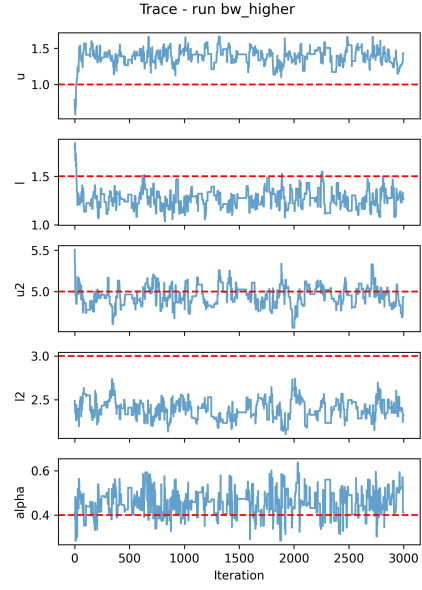


FIGURE 7 – Random-walk pour run bw\_higher

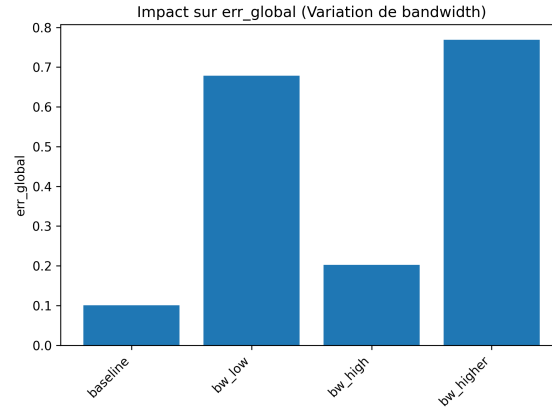
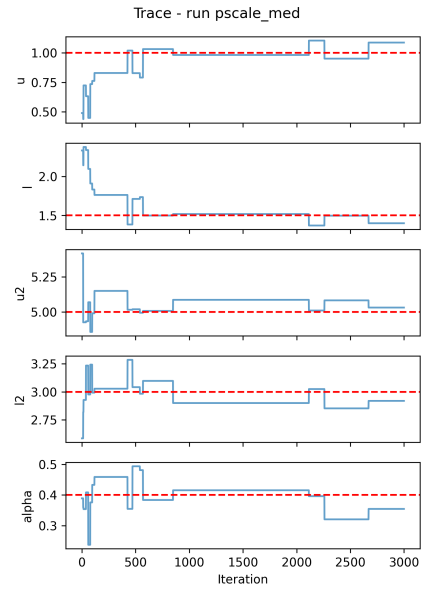


FIGURE 8 – Comparaison de err\_global (baseline vs variations de bandwidth)

## Variation de proposal\_scale

Run pscale_med	
$N$	200
bandwidth	0.05
n_sim	2000
proposal_scale	0.3
n_iter	3000
pm_u	1.00
pm_l	1.48
pm_u2	5.07
pm_l2	2.90
pm_alpha	0.38
err_u	0.004
err_l	0.021
err_u2	0.070
err_l2	0.097
err_alpha	0.019
err_global	0.123



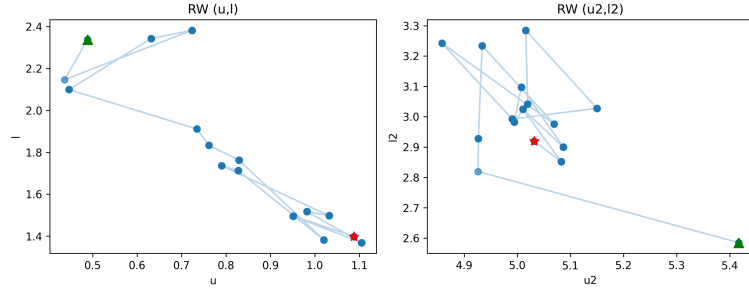


FIGURE 9 – Random-walk pour run pscale\_med

Run pscale_high	
$N$	200
bandwidth	0.05
n_sim	2000
proposal_scale	0.5
n_iter	3000
pm_u	1.07
pm_l	1.40
pm_u2	4.91
pm_l2	2.90
pm_alpha	0.45
err_u	0.072
err_l	0.101
err_u2	0.094
err_l2	0.095
err_alpha	0.049
err_global	0.189

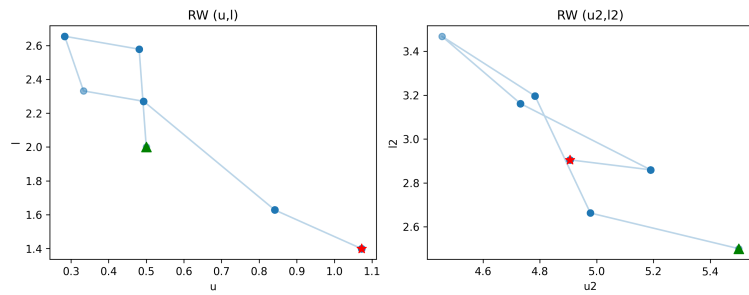
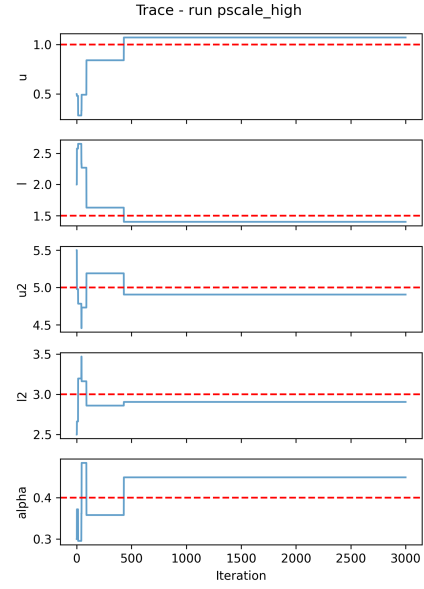


FIGURE 10 – Random-walk pour run pscale\_high



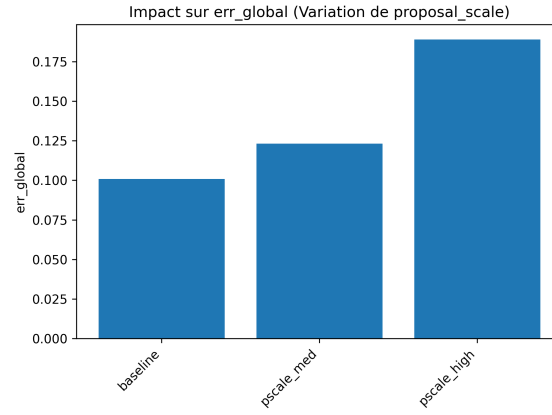
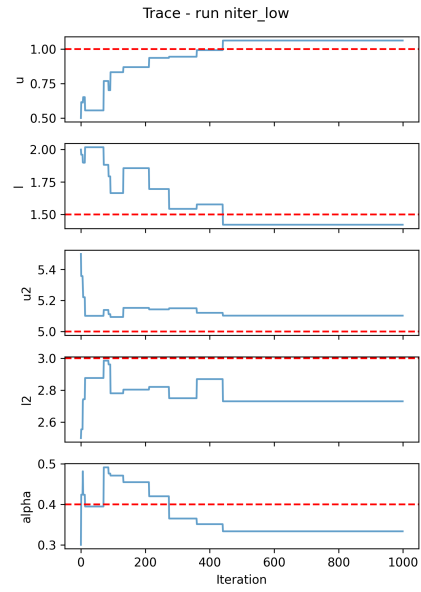


FIGURE 11 – Comparaison de `err_global` (baseline vs variations de `proposal_scale`)

## Variation de `n_iter`

Run niter_low	
$N$	200
bandwidth	0.05
n_sim	2000
proposal_scale	0.1
n_iter	1000
pm_u	1.06
pm_l	1.43
pm_u2	5.10
pm_l2	2.74
pm_alpha	0.33
err_u	0.056
err_l	0.068
err_u2	0.103
err_l2	0.260
err_alpha	0.065
err_global	0.300



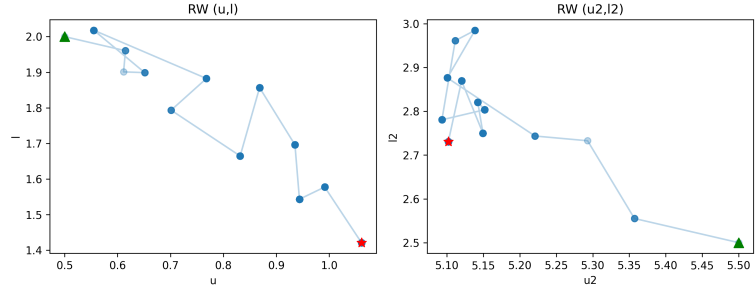


FIGURE 12 – Random-walk pour run niter\_low

Run niter_high	
$N$	200
bandwidth	0.05
n_sim	2000
proposal_scale	0.1
n_iter	5000
pm_u	1.01
pm_l	1.52
pm_u2	5.04
pm_l2	2.95
pm_alpha	0.37
err_u	0.013
err_l	0.021
err_u2	0.037
err_l2	0.054
err_alpha	0.025
err_global	0.074

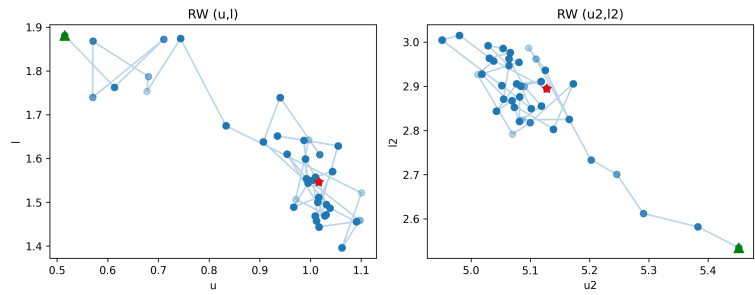
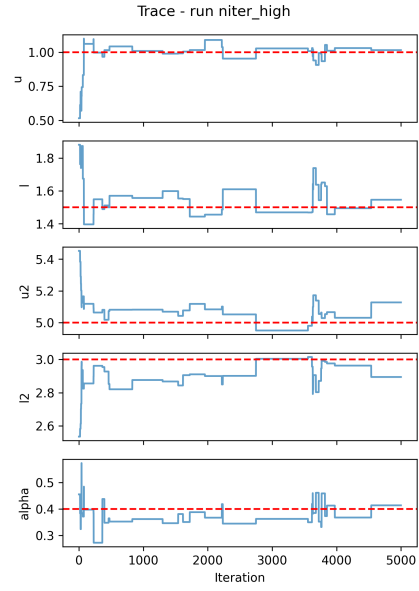


FIGURE 13 – Random-walk pour run niter\_high

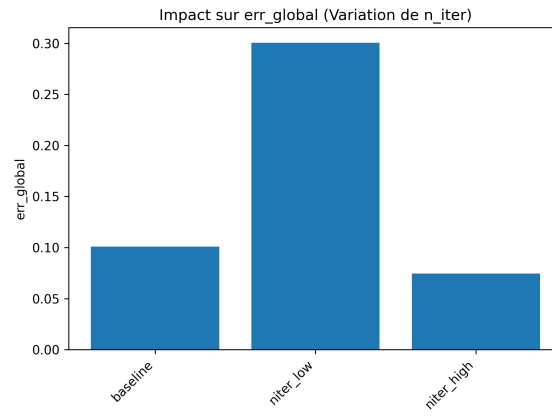
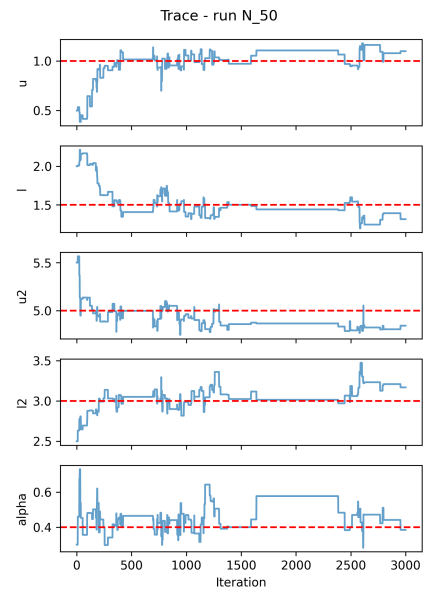


FIGURE 14 – Comparaison de err\_global (baseline vs variations de n\_iter)

## Variation de N

Run N_50	
$N$	50
bandwidth	0.05
n_sim	2000
proposal_scale	0.1
n_iter	3000
pm_u	1.07
pm_l	1.42
pm_u2	4.85
pm_l2	3.09
pm_alpha	0.50
err_u	0.071
err_l	0.078
err_u2	0.148
err_l2	0.088
err_alpha	0.097
err_global	0.224



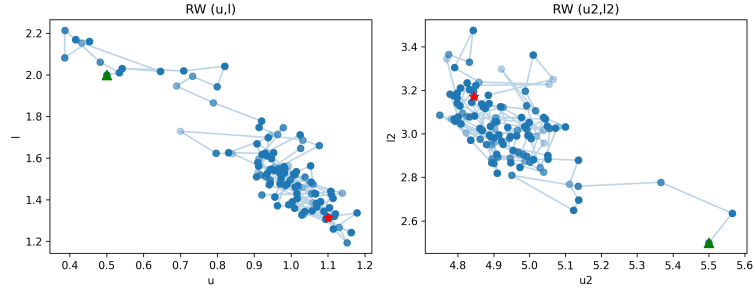


FIGURE 15 – Random-walk pour run N\_50

Run N_300	
$N$	300
bandwidth	0.05
n_sim	2000
proposal_scale	0.1
n_iter	3000
pm_u	1.11
pm_l	1.34
pm_u2	5.01
pm_l2	2.99
pm_alpha	0.41
err_u	0.106
err_l	0.158
err_u2	0.009
err_l2	0.013
err_alpha	0.008
err_global	0.191

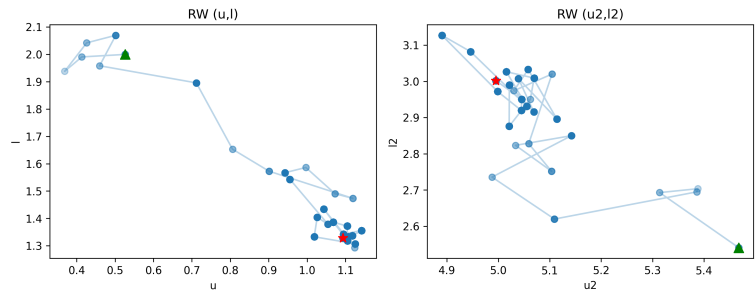
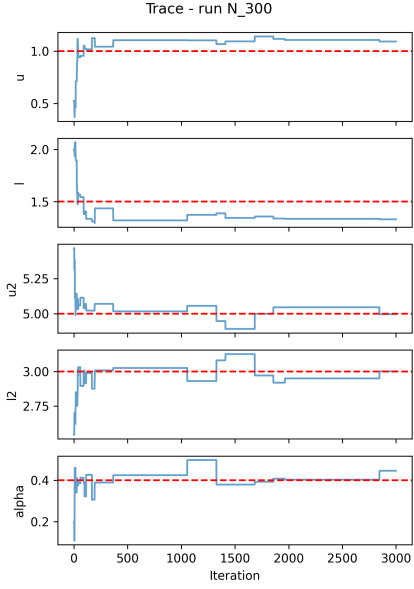


FIGURE 16 – Random-walk pour run N\_300

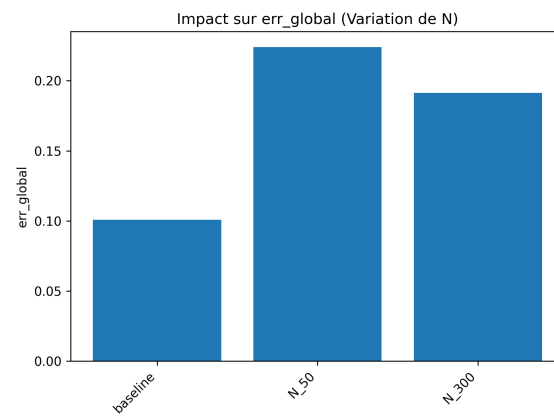


FIGURE 17 – Comparaison de err\_global (baseline vs variations de N)