Scoping Note

Synthetic Data Augmentation for Trading Strategy Calibration and Risk Forecasting

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1. Background

The increasing reliance on machine learning models in financial forecasting tasks is often limited by the amount and diversity of available data. Synthetic data generation offers a promising solution, particularly in the context of financial time series where regime shifts and structural breaks may impair model generalization. This project explores whether realistic, regime-aware synthetic return series can improve both trading strategy calibration and tail-risk forecasting performance.

2. Objectives

The main objectives of the project are to:

- Design a regime-aware synthetic data generation process using Variational Autoencoders (VAEs).
- Evaluate the impact of synthetic data on the calibration and out-of-sample performance of a cross-sectional momentum strategy.
- Assess the influence of synthetic data on the calibration and statistical consistency of Value-at-Risk (VaR) forecasts.

3. Scope of Work

- 1. Data Cleaning: Handle missing data, validate time consistency, and normalize returns.
- 2. **Regime Detection:** (Handled separately by co-author; excluded from this document)
- 3. **Synthetic Data Generation:** Use a regime-specific VAE to generate realistic log-returns per market regime.
- 4. **Trading Strategy Calibration:** Optimize a long-short cross-sectional momentum strategy via grid search on real vs augmented data.
- 5. **Backtesting:** Compare in-sample and out-of-sample performance using cumulative return, Sharpe ratio, and max drawdown.
- 6. **VaR Forecasting:** Model 1-month VaR using Student-t historical simulation, and assess exceedance frequency using the Kupiec test.
- 7. Comparative Analysis: Contrast the performance and risk profiles of models trained on real versus augmented datasets.

4. Deliverables

- Cleaned and interpolated dataset of asset returns.
- Regime-tagged synthetic return panel.
- Grid-search calibration results for real and real+synthetic data.
- Full backtesting plots and metrics (cumulative return, drawdown, Sharpe ratio).
- VaR forecast plots and Kupiec test outputs.
- A structured LaTeX report including all code, results, and visualizations.

5. Constraints and Assumptions

- Synthetic data is assumed to be statistically similar to real data in each regime.
- Strategy hyperparameters are optimized only on the training set to preserve out-of-sample integrity.
- The same test set is used across all model evaluations for comparability.