Scalar Spherical Harmonics and Slepian Functions

1 Plot a single spherical harmonic function

We will demonstrate plotting a spherical-harmonic on a sphere, in a standard Matlab plot, on a Mollweide projection, and on random points of a sphere.

First, designate a spherical-harmonic to be plotted:

For example,

```
1 = 3; m = -2;
```

0 1 fixes the degree and m fixes the order.

1.1 Plot on sphere

1. Create a grid on the sphere

```
lon = 0:0.5:360; lat = -90:0.5:90;
```

This creates a coordinate point every half-degree.

2. Calculate the values of the function for coordinate points on the sphere

```
Y = ylm(1, m, pi/180*(90-lat), pi/180*lon);
```

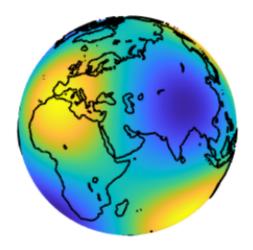
The function $slepian_alpha/ylm.m$ evaluates the spherical harmonic function of degree 1 and order m at every point pi/180*(90-lat), pi/180*lon on the grid. We name the vector of the spherical-harmonic values Y.

Note that 90-lat is needed to convert latitude to colatitude and pi/180 is needed to convert degrees to radians.

3. Plot

```
figure; plotplm(Y, pi/180*lon, pi/180*lat,2)
```

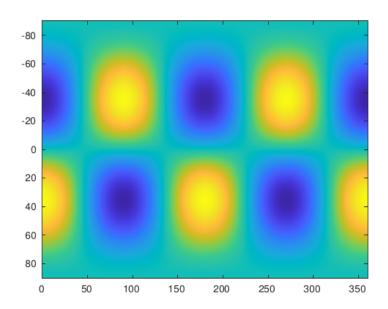
The function slepian_alpha/plotplm.m is here used to plot the vector Y using the grid specified by lon and lat in step 1. The input 2 dictates that the graph be on a sphere.



1.2 Plot in standard Matlab plot

Do steps 1 and 2, and then run

imagesc(lon, lat, Y)

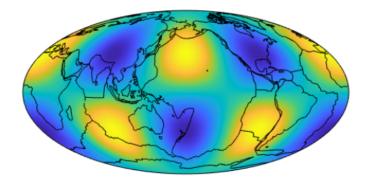


1.3 Plot on Mollweide projection

Do steps 1 and 2, and then run

figure; plotplm(Y, pi/180*lon, pi/180*lat,1)

The input 1 dictates that the graph be on the Mollweide projection.



1.4 Plot for random points on a sphere

1. Generate a subset of the sphere consisting of random points

In particular, we will create N randomly-generated coordinate points within a spherical cap of opening angle TH and centered at longitude lon0 and colatitude cola0

For example,

```
TH = 120; lon0 = 30; cola0 = 40; N=1000;
[lon, lat] = randpatch(N,TH,lon0,cola0);
```

The function slepian_alpha/randpatch.m creates the set of random points within the spherical cap of the specified values. We name those coordinate points [lon,lat].

2. Calculate the values of the spherical harmonic at those points

```
Y = ylm(1, m, pi/180*(90-lat), pi/180*lon,[],[],[],1);
```

ylm.m takes the arguments 1, m, pi/180*(90-lat), pi/180*lon as before. Run help ylm for information on all eight arguments.

3. Plot

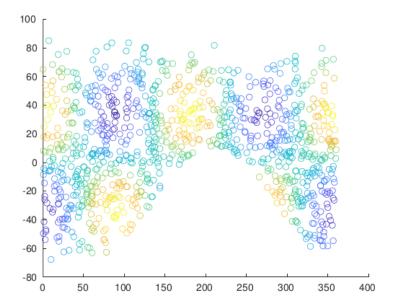
If necessary, use the Matlab command

clf;

To clear existing figures, and then run the Matlab command

scatter(lon, lat, [], Y)

To create a scatter plot of circles having locations [lon, lat]. Here, [] indicates the default value for circle size and the vector of spherical-harmonic values Y is used to determine circle color.



Please see ${\tt Ch_01}$ in the .edu folder for more detailed information.