# A4 - $\beta$ (Modality) via Conative Markers and Directional Alignment (clarification)

Scope. This note clarifies the operationalization of the  $\beta$  (modality) component without changing hypotheses H1 – H4, decision thresholds, or the fixed weights  $\alpha \dots \varepsilon$  specified in the preregistration. It is a predata clarification.

#### **Definitions**

- For a document d and a telos T.
- Directional alignment  $a(d,T) \in [0,1]$  derived from  $\theta$  (e.g.,  $a = (\cos \theta + 1)/2$ ), or any preregistered projection re-mapped to [0,1].
- Conative markers:
- push *p*(*d*) ∈ [0,1] : modal/actional cues (e.g., devoir / must, falloir / need, accelerate, demand, it is time to...).
- inhibit h(d) ∈ [0,1]: blocking/negation cues (e.g., block, prevent, oppose, refuse to, do not + VERB).
   Marker intensities come from a fixed lexicon (lemma/phrase weights [0,1]), negation rules, then p90 normalization and clipping to [0,1].
- Cross-term coefficient  $\lambda$  is fixed a priori to 0.5 (theoretical compromise between instrumental vs. substantive readings).

## Construction of $F_c$ , $F_i$

$$F_c(d,T) = p(d) \cdot a(d,T) + \lambda \cdot h(d) \cdot (1 - a(d,T)),$$
  

$$F_i(d,T) = h(d) \cdot a(d,T) + \lambda \cdot p(d) \cdot (1 - a(d,T)),$$

with  $\lambda = 0.5$ . By construction,  $F_c, F_i \in [0,1]$ . Invariants

- 1. Bounds:  $F_c, F_i \in [0,1]$ .
- 2. Neutrality: if p = h = 0, then  $F_c = F_i = 0$ .
- 3. Monotonicity: for fixed p, h,  $F_c$  increases with a;  $F_i$  decreases with a.
- 4. Anti-telos behavior: if  $a \approx 0$  and p > 0, push contributes to  $F_i$  (pushing against T); if  $a \approx 1$  and h > 0, inhibition contributes to  $F_i$  (blocking within the telos direction).

## Modality scalar for $N_{\text{tel}}$

The  $\beta$  component used in the weighted norm  $N_{\text{tel}}$  is a scalar derived from  $F_c$ ,  $F_i$ :

$$M(d,T) = F_c(d,T) - F_i(d,T) \in [-1,1], \beta(d,T) = \frac{M(d,T) + 1}{2} \in [0,1]$$

Other channels and weights  $(\alpha, \gamma, \delta, \varepsilon)$  remain unchanged and fixed a priori as preregistered.

#### Compliance note

This clarification does not modify any confirmatory tests (H1 – H4), thresholds ( $\Delta AUC, \Delta R^2$ , FDR, etc.), or the fixed weights  $\alpha \dots \varepsilon$ . It only specifies how  $\beta$  is computed from already defined quantities (conation + alignment), with  $\lambda = 0.5$  fixed a priori.

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Links: OSF preregistration (reference) • Git tag prereg-clarif-v1.1