

Building an ALU (Part 2):

PICK UP HANDOUT.

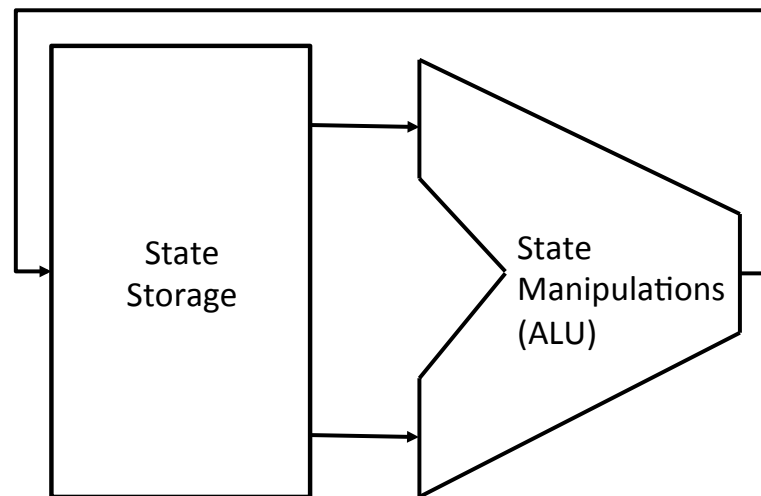
SIGN UP FOR CBT & EXAM 1

State – the central concept of computing

Computer can do 2 things

1) Store state

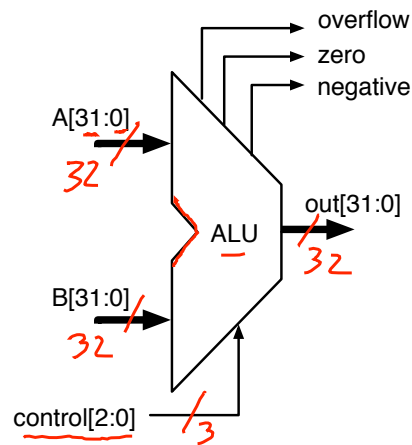
2) Manipulate state (Combine arithmetic and logical operations into one unit)



Today's lecture

- We'll finish the 32-bit ALU today!
 - 32-bit ALU specification
- Complete 1-bit ALU
- Assembling them to make 32-bit ALU
- Handling flags:
 - zero, negative, overflow

A specification for a 32-bit ALU



010
011
100
101
110
111

control	out=
0	<u>undefined</u>
1	<u>undefined</u>
2	A + B
3	A - B
4	A AND B
5	A OR B
6	A NOR B
7	A XOR B

```

module alu32(out, overflow, zero, negative, A, B, control);
    output[31:0] out;
    output      overflow, zero, negative;
    input [31:0] A, B;
    input  [2:0] control;
    
```

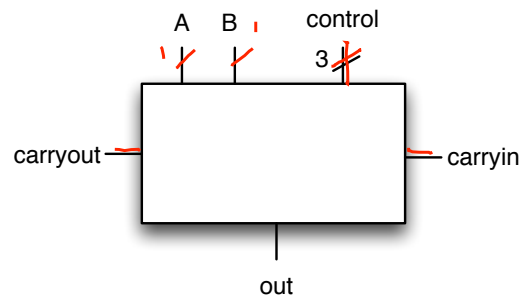
Did overflow occur?

Is the output equal to zero?

Is the output negative?

Use a modular 1-bit ALU to build 32-bit ALU

- Previously we showed 1-bit adder/subtractor, 1-bit logic unit
 - Time to put them together.



control	out _i =
0	undefined
1	undefined
2	$A_i + B_i$
3	$A_i - B_i$
4	$A_i \text{ AND } B_i$
5	$A_i \text{ OR } B_i$
6	$A_i \text{ NOR } B_i$
7	$A_i \text{ XOR } B_i$

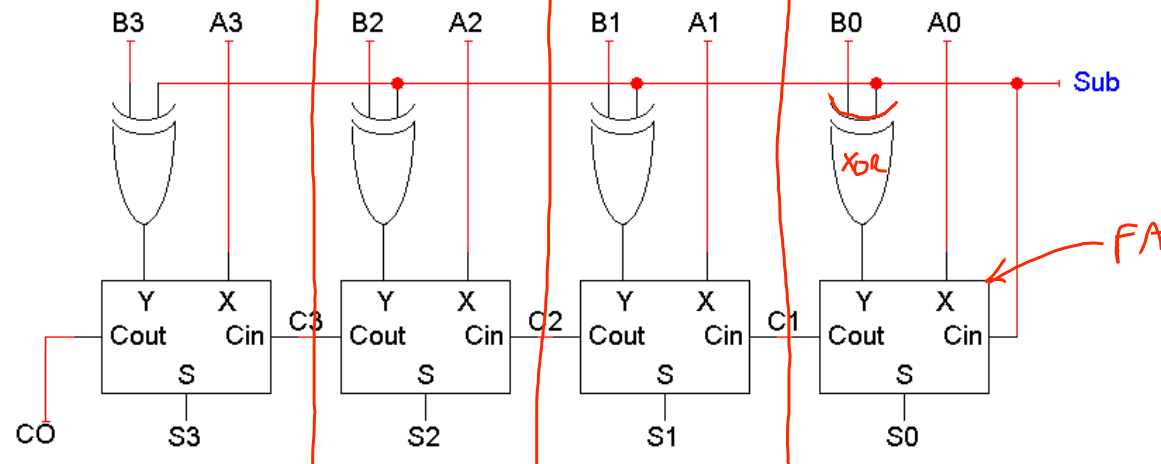
```

module alu1(out, carryout, A, B, carryin, control);
    output      out, carryout;
    input       A, B, carryin;
    input [2:0] control;

```

Addition + Subtraction in one circuit (1-bit Arithmetic Unit)

- When $\text{Sub} = 0$, $Y = B$ and $\text{Cin} = 0$. Result = $A + B + 0 = A + B$.
- When $\text{Sub} = 1$, $Y = \sim B$ and $\text{Cin} = 1$. Result = $A + \sim B + 1 = A - B$.

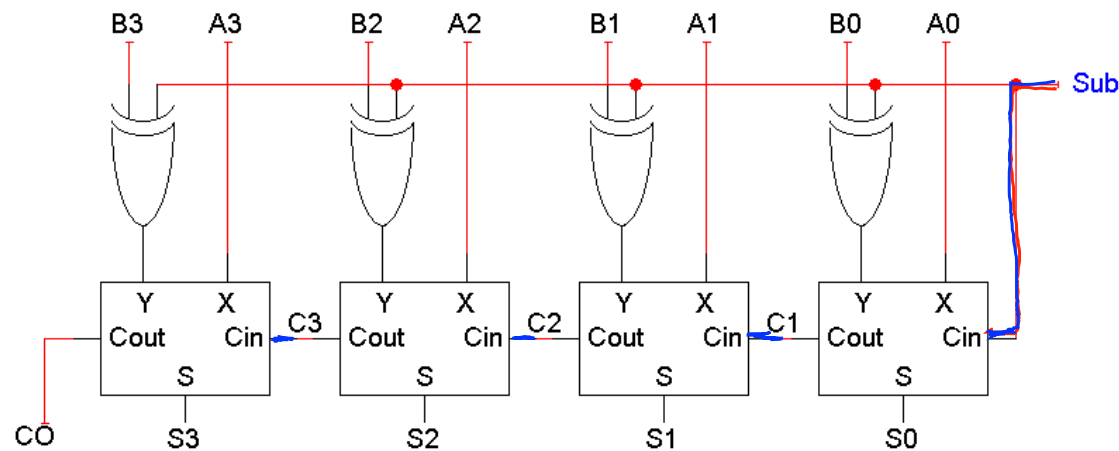


- Which parts belong in inside the 1-bit ALU?

A) the Full Adder, B) the XOR gate, C) Both, D) Neither

Addition + Subtraction in one circuit (1-bit Arithmetic Unit)

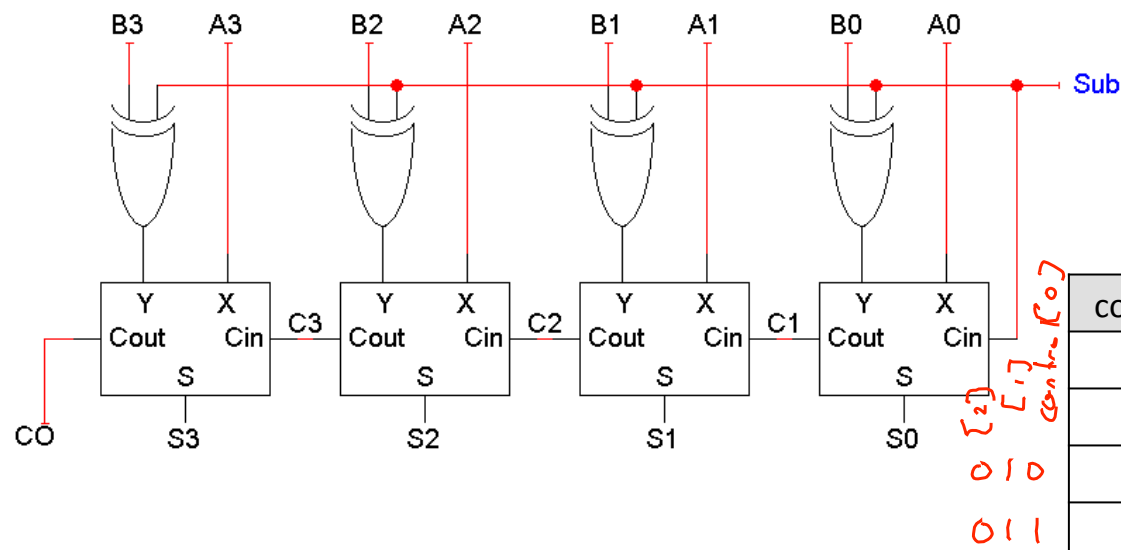
- When Sub = 0, Y = B and Cin = 0. Result = $A + B + 0 = A + B$.
- When Sub = 1, Y = $\sim B$ and Cin = 1. Result = $A + \sim B + 1 = A - B$.



- What should we do with the full adder's Cin input?
A) Connect to Sub, B) Connect to 1-bit ALU's carryin

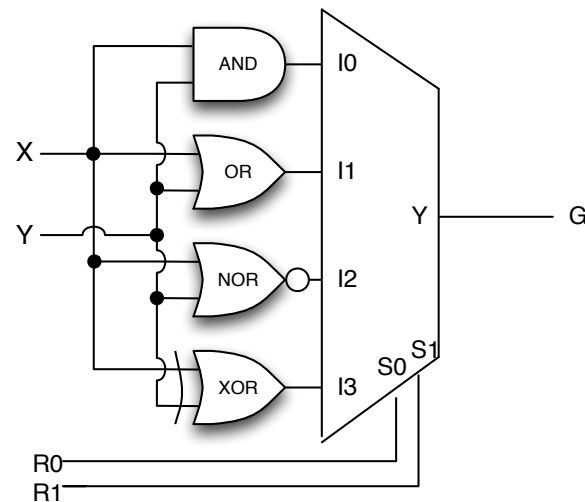
Addition + Subtraction in one circuit (1-bit Arithmetic Unit)

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- Where will the “Sub” signal come from?

Complete 1-bit Logic Unit



R_1	R_0	Output
0	0	$G_i = X_i Y_i$
0	1	$G_i = X_i + Y_i$
1	0	$G_i = (X_i + Y_i)'$
1	1	$G_i = X_i Y_i$

AND

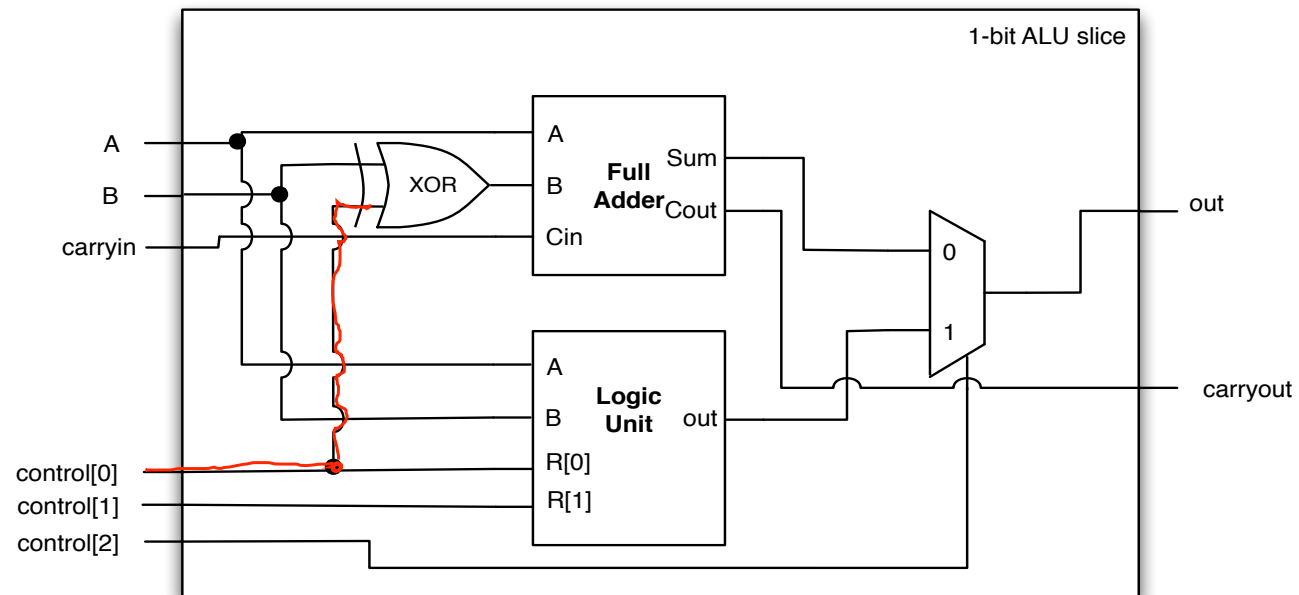
OR

NOR

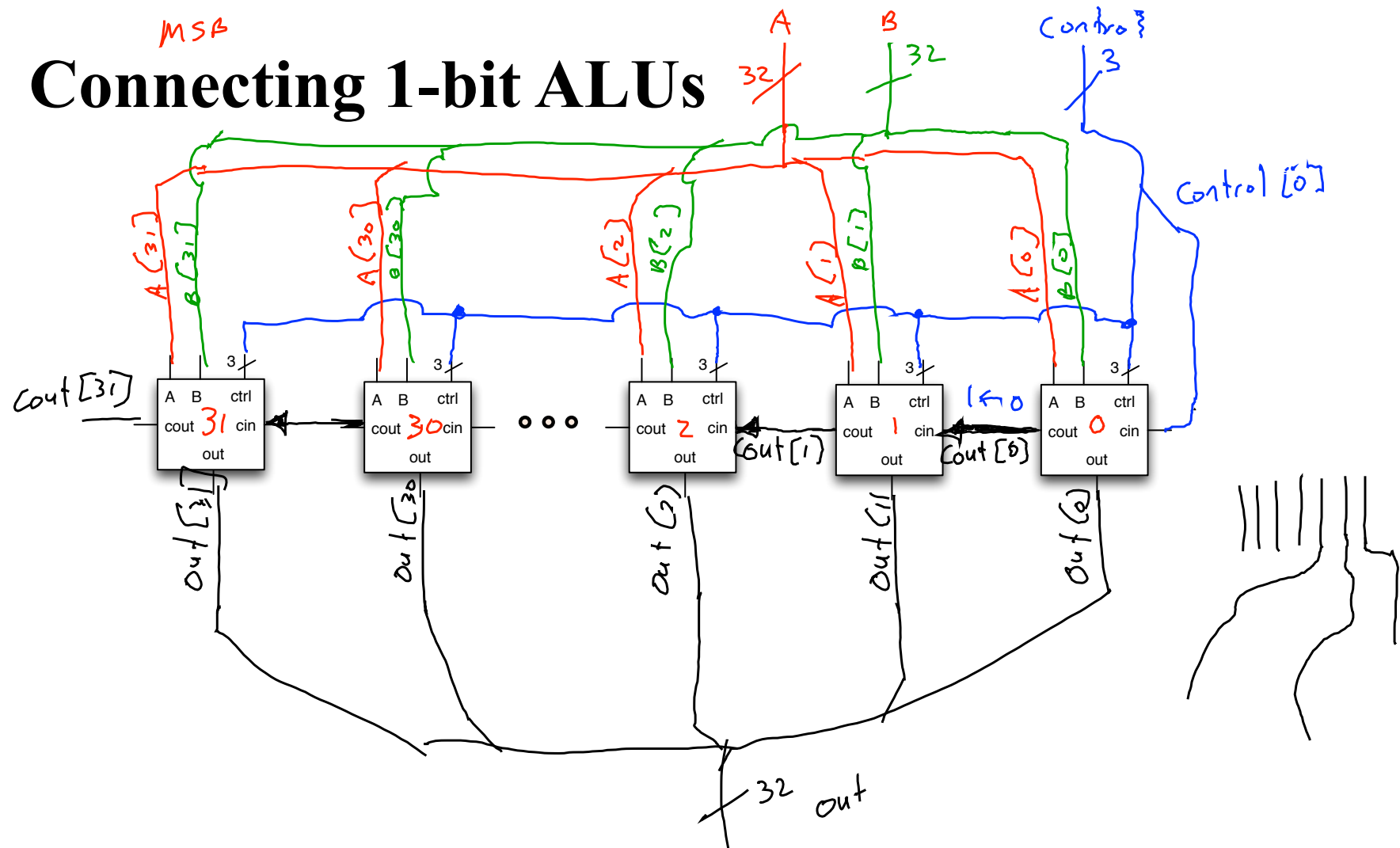
XOR

- What should the control inputs (R_0 , R_1) connect to?
- How do we select between the adder and the logic unit?
- How do we control the selection?

Complete 1-bit ALU



Connecting 1-bit ALUs



Flags (overflow, zero, **negative**)

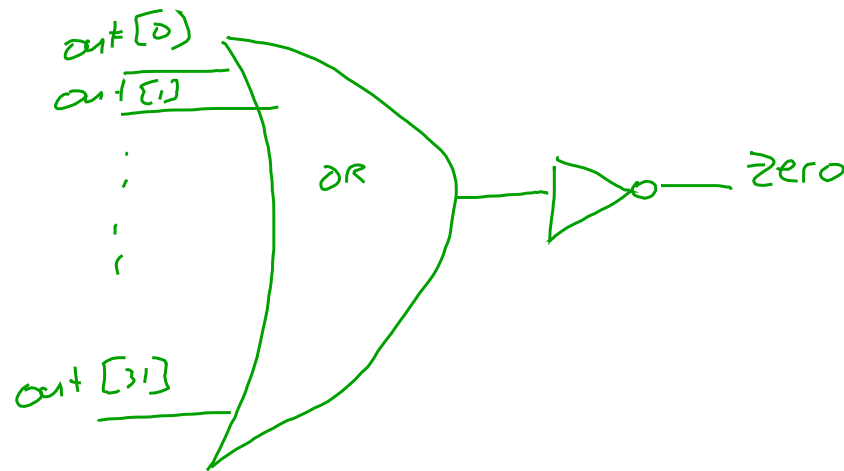
- Let's do negative first; negative evaluates to:
 - 1 when the output is negative, and
 - 0 when the output is positive or zero
- Negative =
 - a) `control[0]`
 - b) `carryout[32]`
 - c) `output[32]`
 - d) `carryout[31]`
 - e) `output[31]`

Flags (overflow, **zero**, negative)

- zero evaluates to:
 - 1 when the output is equal to zero, else 0

$\text{Nor}(\text{output}, \text{input1}, \text{input2}, \text{input3}, \text{input4}, \dots)$

- Zero =



Flags (**overflow**, zero, negative)

- Overflow (for 2's complement) evaluates to:
 - 1 when the overflow occurred, else 0
 - adding two positive numbers yields a negative number
 - adding two negative numbers yields a positive number
- Consider the adder for the MSB:

X	Y	C _{in}	C _{out}	S
0	0	0	0	0
0	0	1	0	1
0	1	0	0	1
0	1	1	1	0
1	0	0	0	1
1	0	1	1	0
1	1	0	1	0
1	1	1	1	1

- a) cin[31] NOR cout[31]
- b) cin[31] AND cout[31]
- c) cin[31] OR cout[31]
- d) cin[31] XOR cout[31]
- e) cin[31] NAND cout[31]



- Overflow =

Overflow examples

$$\begin{array}{rcccccl} & 1 & 1 & 0 & 1 & (-3) \\ + & 1 & 1 & 0 & 0 & + (-4) \\ \hline \end{array}$$

$$\begin{array}{rcccccl} & 1 & 0 & 1 & 1 & (-5) \\ + & 1 & 1 & 0 & 0 & + (-4) \\ \hline \end{array}$$

$$\begin{array}{rcccccl} & 0 & 1 & 0 & 0 & 4 \\ + & 0 & 1 & 0 & 0 & 4 \\ \hline \end{array}$$

$$\begin{array}{rcccccl} & 0 & 1 & 0 & 0 & 4 \\ + & 1 & 1 & 0 & 0 & + (-4) \\ \hline \end{array}$$