

1.

a. Define half adder.

Ans: A form of combinational logic circuit known as the Half Adder adds two 1-bit binary digits.

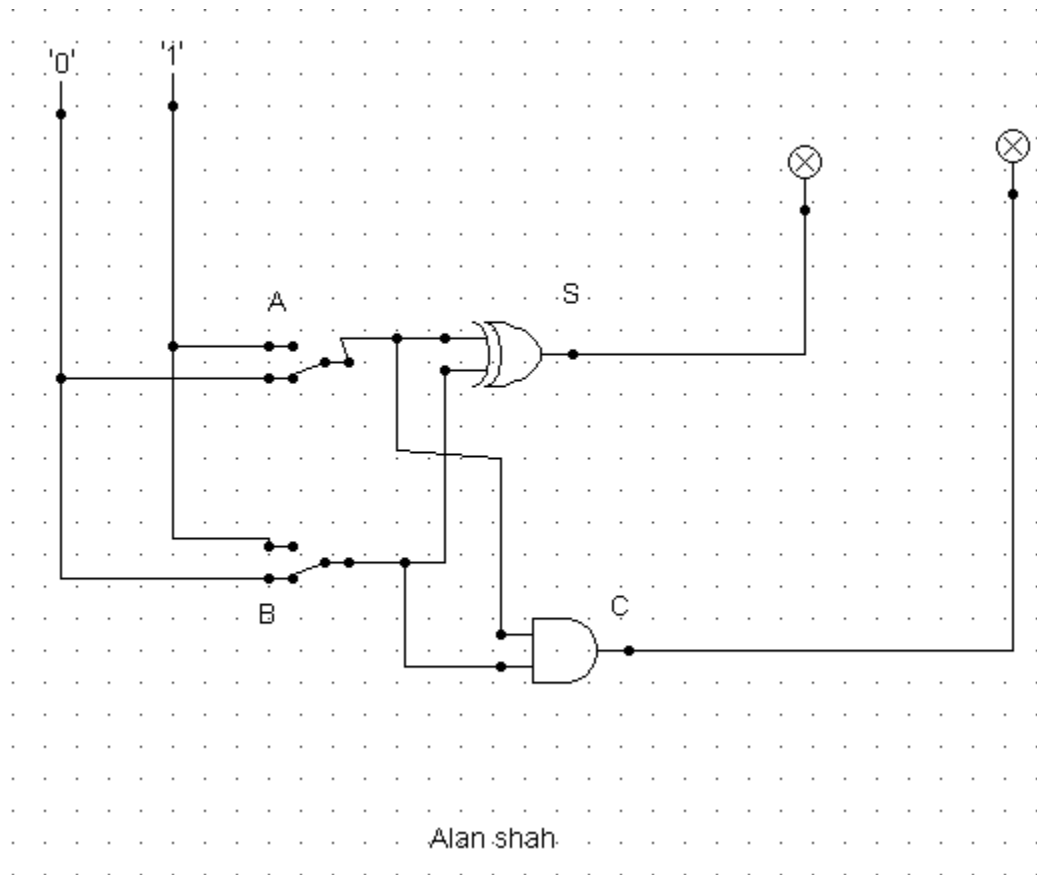
b. Draw a truth table for the sum and carry of half adder.

A	B	C	S
0	0	0	0
0	1	0	1
1	0	0	1
1	1	1	0

c. Write the sop expression from the truth table.

Ans: $S = x'y + xy'$, $C = xy$

d. Draw the circuit using logsim.



2.

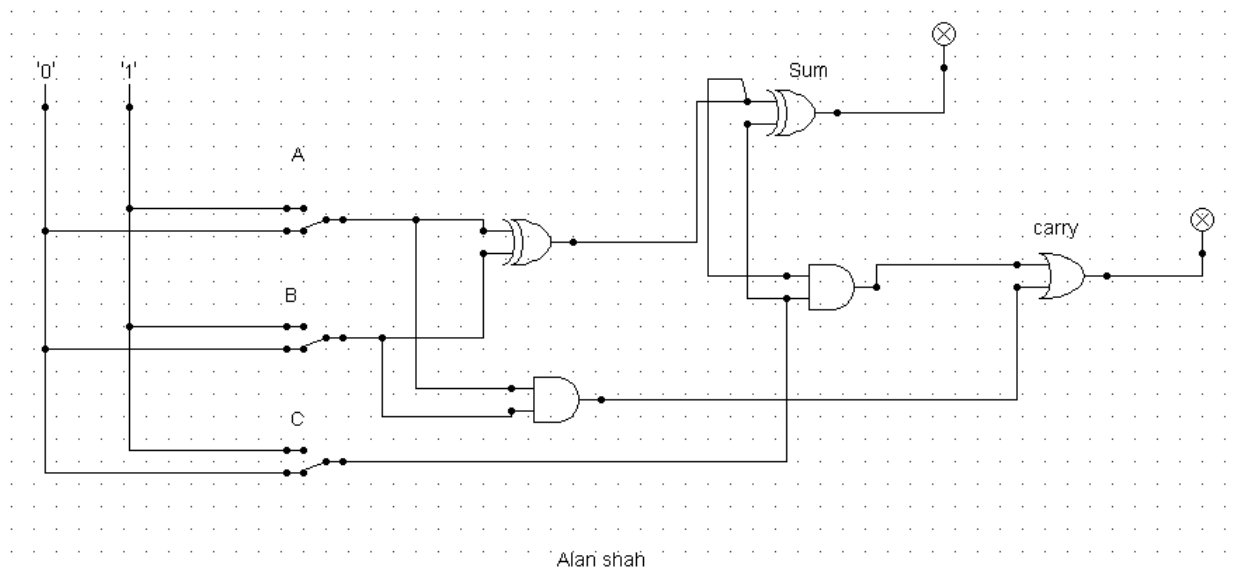
a. Draw the truth table for the outputs of the full adder.

A	B	C-IN	S	C-OUT
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

b. Write the corresponding sop expression for sum and carry of full adder and simplify the expression

Ans: SUM = (A XOR B) XOR Cin = $(A \oplus B) \oplus C_{in}$ CARRY-OUT = A AND B OR Cin(A XOR B) = $A.B + C_{in}(A \oplus B)$

c. Draw a full adder using two half adders and an OR gate.



3. Using the three stages of design, construct the circuits for the following input /output values. Here A, B, and C are the inputs whereas D, E, F, G, H

and I are the outputs. *Note: Draw a circuit diagram using logsim corresponding to the simplified expression of outputs D, E, F, G, H, and I.*

A	B	C	D	E	F	G	H	I
0	0	0	1	0	1	0	1	1
0	0	1	1	0	1	1	0	1
0	1	0	1	0	1	1	1	1
1	0	0	1	0	0	1	0	1
1	1	1	1	1	1	1	1	1
1	1	0	1	1	0	1	0	1
1	0	1	1	1	1	1	1	0
0	1	1	0	0	0	1	1	1

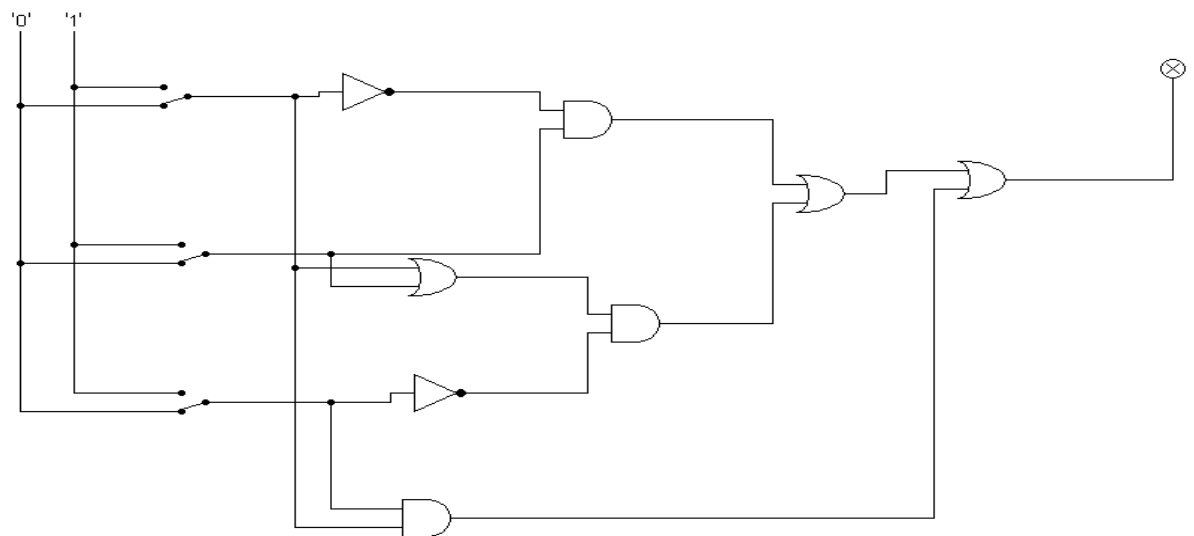
Ans:

$$D = A'B'C' + A'B'C + A'BC' + AB'C' + ABC + ABC' + AB'C$$

$$= A'B'(C' + C) + B(A'C' + AC') + AC(B + B') + AB'C'$$

$$= A'B' + BC'(A' + A) + AC + AB'C'$$

$$= A'B + C'(B + A) + AC$$



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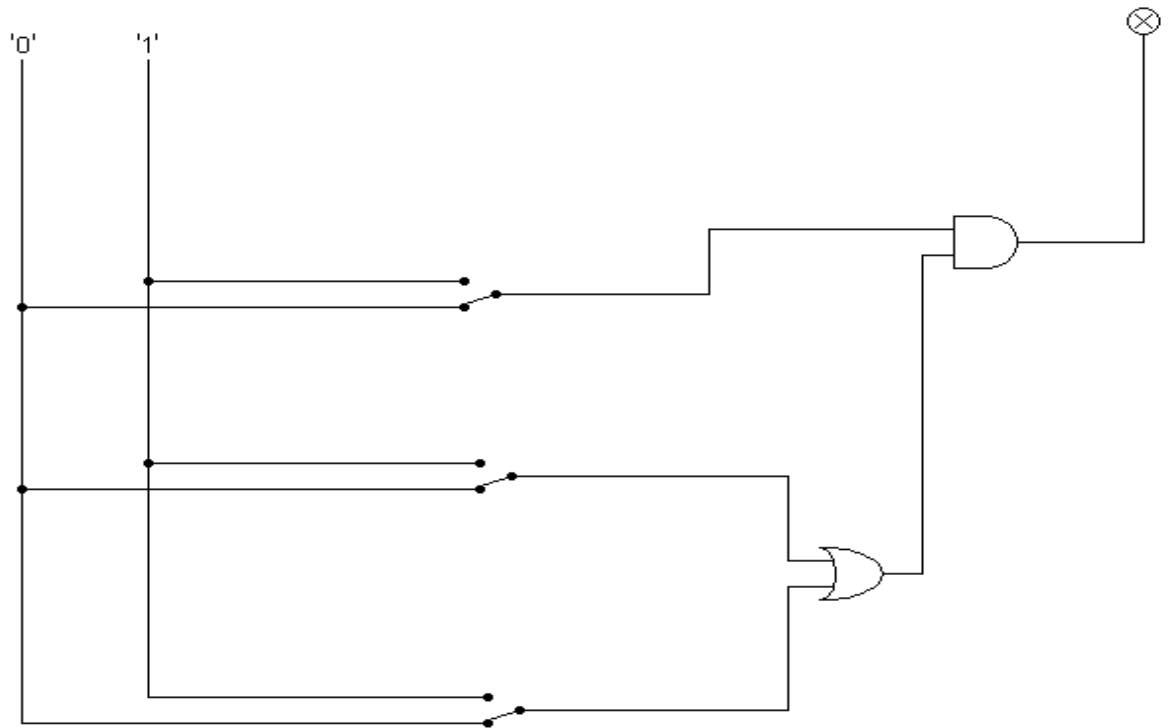
$$E = ABC + ABC' + AB'C$$

$$= AB(C + C') + AB'C$$

$$= AB + AB'C$$

$$= A(B + B'C)$$

$$= A(B + C)$$



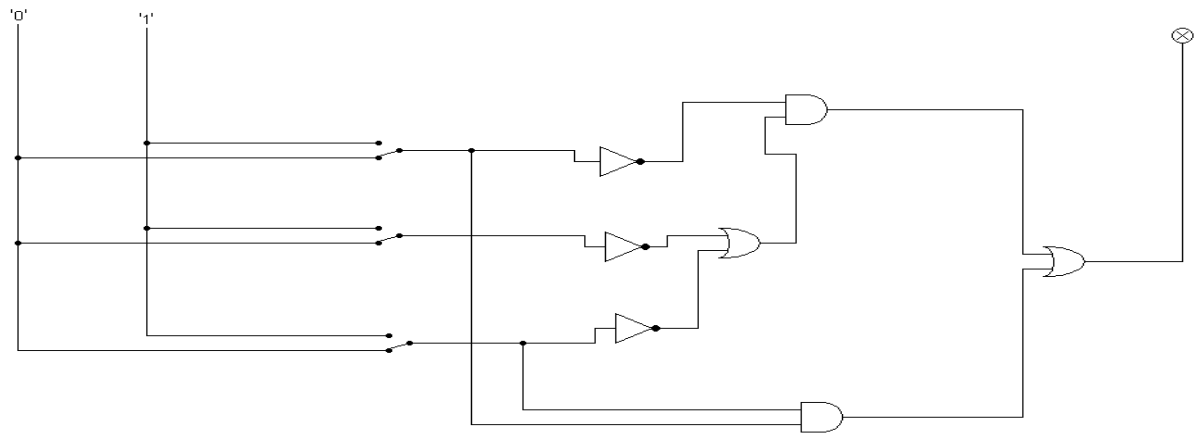
$$F = A'B'C' + A'B'C + A'BC' + ABC + AB'C$$

$$= A'B'(C' + C) + AC(B' + B) + A'BC'$$

$$= A'B' + AC + A'BC'$$

$$= A'(B' + BC') + AC$$

$$= A'(B' + C') + AC$$



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$$G = A'B'C + A'BC' + AB'C' + ABC + ABC' + AB'C + A'BC$$

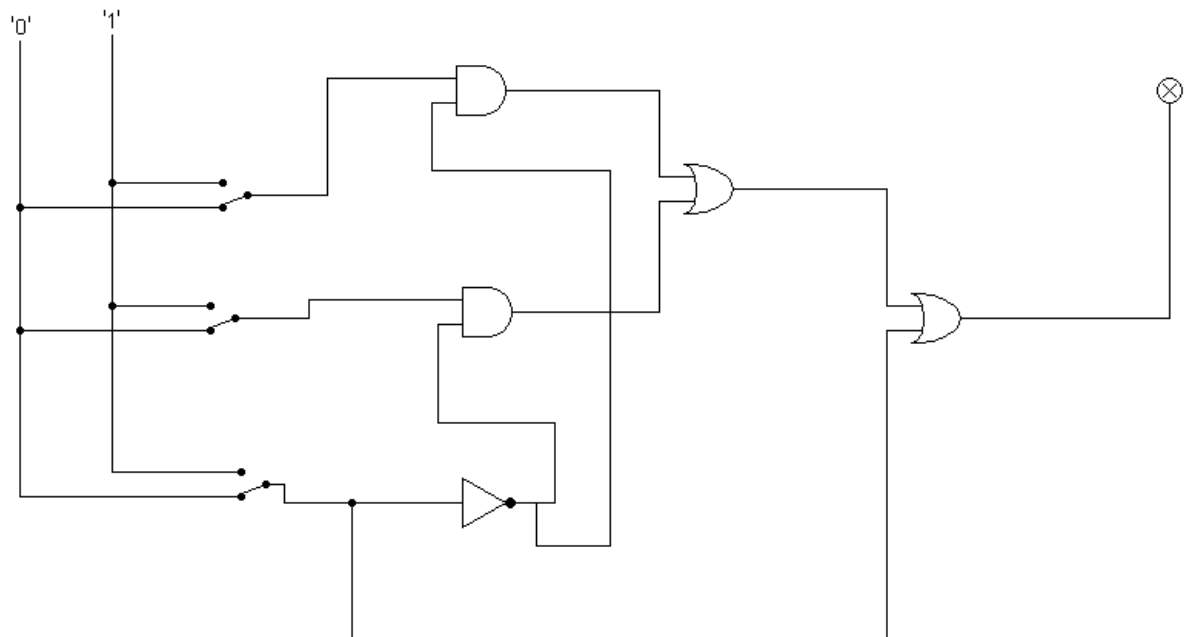
$$= A'C(B' + B) + BC'(A' + A) + AC(B' + B) + AB'C'$$

$$= A'C + BC' + AC + AB'C'$$

$$= C(A' + A) + C'(B + AB')$$

$$= C + C'(B + A)$$

$$= C + C'B + AC'$$



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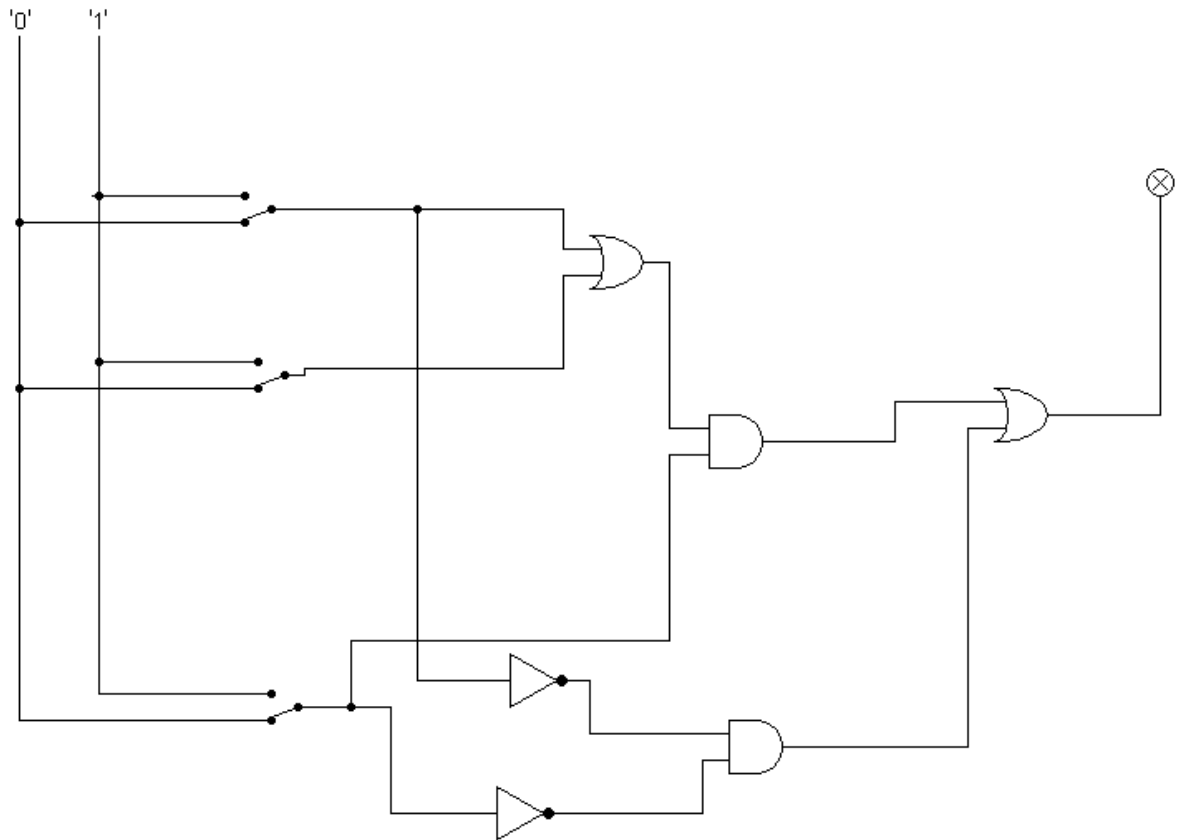
$$H = A'B'C' + A'BC' + ABC + AB'C + A'BC$$

$$= AC(B' + B) + A'C'(B' + B) + A'BC$$

$$= AC + A'C' + A'BC$$

$$= C(A'B + A) + A'C'$$

$$= C(A + B) + A'C'$$



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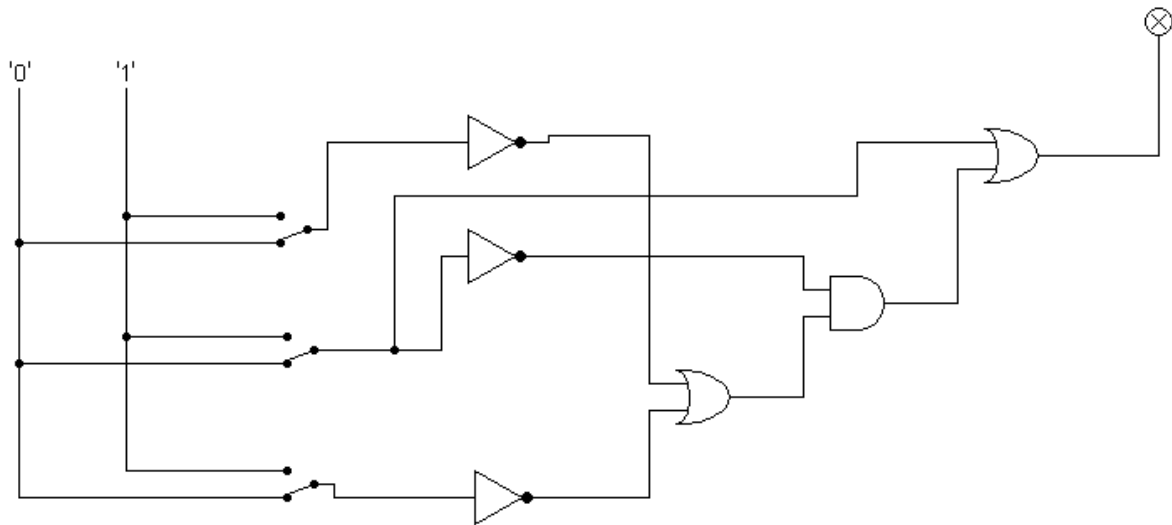
$$I = A'B'C' + A'B'C + A'BC' + AB'C' + ABC + ABC' + A'BC$$

$$= B'C'(A' + A) + AB(C' + C) + A'B(C' + C) + A'B'C$$

$$= B'C' + AB + A'B + A'B'C$$

$$= B(A + A') + B'(A'C + C')$$

$$=B+B'(A'+C')$$



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