

- Algorithm: bfs_dfs

Input: Undirected graph $graph$, start node $start$ in the $graph$, end node end in the $graph$, restricted access container class rac_class

Output: $parent_{node}$, for each $node$ in $graph$: the parent of $node$ in the exploration of the $graph$ starting from $start$

1. Initialize rac to be an instance of rac_class ;
2. Initialize $dist$ to be an empty mapping;
3. Initialize $parent$ to be an empty mapping;
4. **foreach** $node$ in $graph$ **do**
 - a. $dist_{node} \leftarrow \infty$;
 - b. $parent_{node} \leftarrow null$;
5. $dist_{start} \leftarrow 0$;
6. push $start$ onto rac ;
7. **while** rac is not empty **do**
 - a. pop $node$ off from rac ;
 - b. **if** $node = end$, **then**
 - i. **return** $parent$
 - c. **foreach** neighbor nbr of $node$ **do**
 - i. **if** $dist_{nbr} = \infty$, **then**
 - a. $dist_{nbr} \leftarrow dist_{node} + 1$;
 - b. $parent_{nbr} \leftarrow node$;
 - c. push nbr onto rac ;
8. **return** $parent$

- Recipe for recursive_dfs

Base Case:

If start node equals end node, then return true as we found the end node in the graph.

If start node has no neighbors that have not been explored yet, then the function should return.

Recursive Case:

If start node has neighbors that have not yet been explored, then we will do the following for each of such neighbors nbr of start node:

1. Update parent mapping so that the parent of nbr will be the start node
2. Perform DFS with same graph, nbr as new start node, same end node, updated parent mapping

Algorithm: DFS (recursive version)

Input: Undirected graph *graph*, start node *start* in the *graph*, end node *end* in the *graph*, *parent_{node}*, for each *node* in *graph*: the parent of *node* in the exploration of the *graph* starting from *start*

Output: If *end* is found in *graph*, return *true*; otherwise, return *false*

1. **if** *start* = *end* **then**
 - a. **return** *true*
2. **foreach** *nbr* of *start* **do**
 - a. **if** *nbr* is not in the mapping *parent* **then**
 - i. $parent_{nbr} \leftarrow start$;
 - ii. DFS (*graph*, *nbr*, *end*, *parent*), where *nbr* is as start node in calling DFS
3. **return** *false*

- Algorithm: A*

Input: Undirected graph *graph*, start node *start* in the *graph*, end node *end* in the *graph*; function *edge_distance* (*node1*, *node2*, *graph*) which returns the actual distance required to travel from *node1* to *node2* in *graph*, where *node1* and *node2* are neighbors; function *straight_line_distance* (*node3*, *node4*, *graph*) which returns heuristic distance from *node3* to *node4* in *graph*, where *node3* and *node4* are not necessarily neighbors.

Output: *parent_{node}*, for each *node* in *graph*: the parent of *node* in the exploration of the *graph* starting from *start*

1. Initialize *f_cost* to be an empty mapping;
2. Initialize *g_cost* to be an empty mapping;
3. Initialize *h_cost* to be an empty mapping;
4. Initialize *parent* to be an empty mapping;
5. Initialize *openset* to be an empty set;
6. Initialize *closedset* to be an empty set;
7. **foreach** *node* in *graph* **do**
 - a. $parent_{node} \leftarrow null$
8. $g_cost_{start} \leftarrow 0$;
9. $h_cost_{start} \leftarrow straight_line_distance(start, end, graph)$;
10. $f_cost_{start} \leftarrow h_cost_{start} + g_cost_{start}$;
11. **add** *start* to *openset*;
12. **while** *openset* is not empty **do**
 - a. $current \leftarrow null$;
 - b. $f_lowest \leftarrow \infty$;
 - c. **foreach** *node* in *openset* **do**
 - i. **if** $f_cost_{node} < f_lowest$ **then**
 1. $f_lowest \leftarrow f_cost_{node}$;
 2. $current \leftarrow node$;
 - d. **if** *current* = *end* **then**
 - i. **return** *parent*;
 - e. **remove** *current* from *openset*;

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f. add current in closedset;
g. foreach nbr, neighbor of current do
    i. if nbr is not in openset nor closedset then
        1.  $parent_{nbr} \leftarrow current$ ;
        2.  $g\_cost_{nbr} \leftarrow g\_cost_{current} +$ 
            $edge\_distance(current, nbr, graph)$ ;
        3.  $h\_cost_{nbr} \leftarrow straight\_line\_distance(nbr, end, graph)$ ;
        4.  $f\_cost_{nbr} \leftarrow h\_cost_{nbr} + g\_cost_{nbr}$ ;
        5. add nbr in openset;
    ii. if nbr is in openset only then
        1. if  $g\_cost_{nbr} > g\_cost_{current} +$ 
            $edge\_distance(current, nbr, graph)$ 
           then
            a.  $g\_cost_{nbr} \leftarrow g\_cost_{current} +$ 
                $edge\_distance(current, nbr, graph)$ ;
            b.  $f\_cost_{nbr} \leftarrow h\_cost_{nbr} + g\_cost_{nbr}$ ;
            c.  $parent_{nbr} \leftarrow current$ ;
13. return parent

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- Discussion

problem 1: They are the same in concepts. Both will traverse along a deep path firstly. Yet, the recursive version calls itself (utilize python) to keep track of the state while bfs_dfs version uses stack to keep track of the state. bfs_dfs version looks at every neighbor of each node it explores in order to utilize stack while recursive version does not look at the next neighbor. bfs_dfs version is better because once we arrive at one node away from the destination, we are done while recursive version is done only when we actually reach the destination.

problem 2: A* gives the best routes. Only A* takes the weight of edge (distance) into account among all.

problem 3: DFS gives the worst routes. Because DFS does not try to find the shortest path while traversing the graph, it circles around the destination and takes much effort to finally reach the target. And between two version of DFSs, recursive version is worse because we have to reach the destination as said in **problem1**.

problem 4: Although A* algorithm may give the shortest path in terms of distance and Google does not generate shorter path, A* does not give the shortest path in terms of time. However, Google considers other factors such as traffic, road work, etc., to generate the path that takes least time (among other options such as least road turns, etc.).