Macros and Streams

Discussion 10: November 7, 2018

1 Macros

So far we've been able to define our own procedures in Scheme using the define special form. When we call these procedures, we have to follow the rules for evaluating call expressions, which involve evaluating all the operands.

We know that special form expressions do not follow the evaluation rules of call expressions. Instead, each special form has its own rules of evaluation, which may include not evaluating all the operands. Wouldn't it be cool if we could define our own special forms where we decide which operands are evaluated? Consider the following example where we attempt to write a function that evaluates a given expression twice:

```
scm> (define (twice f) (begin f f))
twice
scm> (twice (print 'woof))
woof
```

Since twice is a regular procedure, a call to twice will follow the same rules of evaluation as regular call expressions; first we evaluate the operator and then we evaluate the operands. That means that woof was printed when we evaluated the operand (print 'woof). Inside the body of twice, the name f is bound to the value undefined, so the expression (begin f f) does nothing at all!

The problem here is clear: we need to prevent the given expression from evaluating until we're inside the body of the procedure. This is where the define-macro special form, which has identical syntax to the regular define form, comes in:

```
scm> (define-macro (twice f) (list 'begin f f))
twice
```

define-macro allows us to define what's known as a macro, which is simply a way for us to combine unevaluated input expressions together into another expression. When we call macros, the operands are not evaluated, but rather are treated as Scheme data. This means that any operands that are call expressions or special form expression are treated like lists.

If we call (twice (print 'woof)), f will actually be bound to the list (print 'woof) instead of the value undefined. Inside the body of define-macro, we can insert these expressions into a larger Scheme expression. In our case, we would want a begin expression that looks like the following:

```
(begin (print 'woof) (print 'woof))
```

As Scheme data, this expression is really just a list containing three elements: begin and (print 'woof) twice, which is exactly what (list 'begin f f) returns. Now,

when we call twice, this list is evaluated as an expression and (print 'woof) is evaluated twice.

```
scm> (twice (print 'woof))
woof
woof
```

To recap, macros are called similarly to regular procedures, but the rules for evaluating them are different. We evaluated lambda procedures in the following way:

- 1. Evaluate operator
- 2. Evaluate operands
- 3. Apply operator to operands, evaluating the body of the procedure

However, the rules for evaluating calls to macro procedures are:

- 1. Evaluate operator
- 2. Apply operator to unevaluated operands
- 3. Evaluate the expression returned by the macro in the frame it was called in.

Quasiquoting

Recall that the quote special form prevents the Scheme interpreter from executing a following expression. We saw that this helps us create complex lists more easily than repeatedly calling cons or trying to get the structure right with list. It seems like this form would come in handy if we are trying to construct complex Scheme expressions with many nested lists.

```
scm> (define a 1)
a
scm> '(cons a nil)
(cons a nil)
```

Consider that we rewrite the twice macro as follows:

```
(define-macro (twice f)
  '(begin f f))
```

This seems like it would have the same effect, but since the quote form prevents any evaluation, the resulting expression we create would actually be (begin f f), which is not what we want.

The **quasiquote** allows us to construct literal lists in a similar way as quote, but also lets us specify if any sub-expression within the list should be evaluated.

At first glance, the quasiquote (which can be invoked with the backtick ` or the quasiquote special form) behaves exactly the same as ' or quote. However, using quasiquotes gives you the ability to **unquote** (which can be invoked with the comma , or the **unquote** special form). This removes an expression from the quoted context, evaluates it, and places it back in.

scm> `(cons a nil)
(cons a nil)
scm> `(cons ,a nil)
(cons 1 nil)

By combining quasiquotes and unquoting, we can often save ourselves a lot of trouble when building macro expressions.

Here is how we could use quasiquoting to rewrite our previous example:

```
(define-macro (twice f)
  `(begin ,f ,f))
```

Questions

1.1 Write a macro that takes an expression and returns a parameter-less lamba procedure with the expression as its body

```
(define-macro (make-lambda expr)
```

```
scm> (make-lambda (print 'hi))
(lambda () (print (quote hi)))
scm> (make-lambda (/ 1 0))
(lambda () (/ 1 0))
scm> (define print-3 (make-lambda (print 3)))
print-3
scm> (print-3)
3
```

1.2 Write a macro that takes in two expressions and or's them together (applying short-circuiting rules). However, do this without using the or special form. You may also assume the name v1 doesn't appear anywhere outside of our macro. Fill in the implementation below.

```
(define-macro (or-macro expr1 expr2)
```

```
`(let ((v1 ______))

(if ______))

scm> (or-macro (print 'bork) (/ 1 0))

bork

scm> (or-macro (= 1 0) (+ 1 2))

3
```

2 Streams

In Python, we can use iterators to represent infinite sequences (for example, the generator for all natural numbers). However, Scheme does not support iterators. Let's see what happens when we try to use a Scheme list to represent an infinite sequence of natural numbers:

Because cons is a regular procedure and both its operands must be evaluted before the pair is constructed, we cannot create an infinite sequence of integers using a Scheme list.

Instead, our Scheme interpreter supports *streams*, which are *lazy* Scheme lists. The first element is represented explicitly, but the rest of the stream's elements are computed only when needed. Computing a value only when it's needed is also known as *lazy evaluation*.

We use the special form cons-stream to create a stream:

```
(cons-stream <operand1> <operand2>)
```

cons-stream is a special form because the second operand is not evaluated when evaluating the expression. To evaluate this expression, Scheme does the following:

- 1. Evaluate the first operand.
- 2. Construct a promise containing the second operand.
- 3. Return a pair containing the value of the first operand and the promise.

To actually get the rest of the stream, we must call cdr-stream on it to force the promise to be evaluated. Note that this argument is only evaluated once and is then stored in the promise; subsequent calls to cdr-stream returns the value without recomputing it. This allows us to efficiently work with infinite streams like the naturals example above. We can see this in action by using a non-pure function to compute the rest of the stream:

```
scm> (define (compute-rest n)
...> (print 'evaluating!)
...> (cons-stream n nil))
compute-rest
scm> (define s (cons-stream 0 (compute-rest 1)))
s
scm> (car (cdr-stream s))
evaluating!
1
scm> (car (cdr-stream s))
```

Here, the expression compute-rest 1 is only evaluated the first time cons-stream is called, so the symbol evaluating! is only printed the first time.

Streams are very similar to Scheme lists in that they are also recursive structures. Just like the cdr of a Scheme list is either another Scheme list or nil, the cdr-stream of a stream is either a stream or nil. The difference is that whereas both arguments to cons are evaluated upon calling cons, the second argument to cons-stream isn't evaluated until the first time that cdr-stream is called.

Here's a summary of what we just went over:

- nil is the empty stream
- cons-stream constructs a stream containing the value of the first operand and a promise to evaluate the second operand
- car returns the first element of the stream
- \bullet $cdr\mbox{-stream}$ computes and returns the rest of stream

Questions

```
2.1 What would Scheme display?
    scm> (define (has-even? s)
           (cond ((null? s) #f)
                 ((even? (car s)) #t)
                 (else (has-even? (cdr-stream s)))))
    has-even?
    scm> (define (f x) (* 3 x))
    scm> (define nums (cons-stream 1 (cons-stream (f 3) (cons-stream (f 5) nil))))
    nums
    scm> nums
    scm> (cdr nums)
    scm> (cdr-stream nums)
    scm> nums
    scm > (define (f x) (* 2 x))
    scm> (cdr-stream nums)
    scm> (cdr-stream (cdr-stream nums))
    scm> (has-even? nums)
   Write a function range-stream which takes a start and end, and returns a stream
    that represents the integers between start and end - 1 (inclusive).
    (define (range-stream start end)
        nil
        (cons-stream _____
    scm> (define s (range-stream 1 5))
    scm> (car (cdr-stream s))
```

2.3 Write a function slice which takes in a stream s, a start, and an end. It should return a Scheme list that contains the elements of s between index start and end, not including end. If the stream ends before end, you can return nil.

```
(define (slice s start end)
```

```
scm> (define nat (naturals 0)) ; See naturals procedure on page 1
nat
scm> (slice nat 4 12)
(4 5 6 7 8 9 10 11)
```

2.4 Since streams only evaluate the next element when they are needed, we can combine infinite streams together for interesting results! Use it to define a few of our favorite sequences. We've defined the function combine-with for you below, as well as an example of how to use it to define the stream of even numbers.

```
(define (combine-with f xs ys)
  (if (or (null? xs) (null? ys))
   nil
     (cons-stream
        (f (car xs) (car ys))
        (combine-with f (cdr-stream xs) (cdr-stream ys)))))
scm> (define evens (combine-with + (naturals 0) (naturals 0)))
evens
scm> (slice evens 0 10)
(0 2 4 6 8 10 12 14 16 18)
```

For these questions, you may use the naturals stream in addition to combine-with.

i. (define factorials

```
scm> (slice factorials 0 10)
(1 1 2 6 24 120 720 5040 40320 362880)
(Continued on next page)
```

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- ii. (define fibs

```
scm> (slice fibs 0 10)
(0 1 1 2 3 5 8 13 21 34)
```

iii. Write exp, which returns a stream where the nth term represents the degree-n polynomial expantion for e^x , which is $\sum_{i=0}^n x^i/i!$.

You may use factorials in addition to combine-with and naturals in your solution.

(**define** (exp x)

scm> (slice (exp 2) 0 5) (1 3 5 6.333333333 7 7.266666667)

Extra questions

2.1 Write a macro that takes an expression and a number n and repeats the expression n times. For example, (repeat-n expr 2) should behave the same as (twice expr). Note that it's possible to pass in a combination as the second argument (e.g. (+ 1 2)) as long as it evaluates to a number. Be sure that you evaluate this expression in your macro so that you don't treat it as a list.

Complete the implementation below, making use of the replicate function from Discussion 7.

```
(define (replicate x n)
   (if (= n 0) nil
        (cons x (replicate x (- n 1)))))

(define-macro (repeat-n expr n)

scm> (repeat-n (print '(resistance is futile)) 3)
   (resistance is futile)
   (resistance is futile)
   (resistance is futile)
   (resistance is futile)
   scm> (repeat-n (print (+ 3 3)) (+ 1 1)) ; Pass a call expression in as n
6
6
```

2.2 Write a macro that takes in a call expression and strips out every other argument. The first argument is kept, the second is removed, and so on. You may find it helpful to write a helper function.

```
(define-macro (prune-expr expr)
```

```
scm> (prune-expr (+ 10))
10
scm> (prune-expr (+ 10 100))
10
scm> (prune-expr (+ 10 100 1000))
1010
scm> (prune-expr (prune-expr (+ 10 100) 'garbage))
10
```

()

2.3 Earlier in the discussion, we saw how to write a macro that creates a lambda function given an expression. While creating a parameter-less function might not seem that useful at first, it can be helpful in many cases when we don't want to immediately evaluate an expression.

Using the make-lambda macro you defined earlier, define make-stream, a macro which returns a pair of elements, where the second element is not evaluated until cdr-stream is called on it. Also define the procedure cdr-stream, which takes in a stream returned by make-stream and returns the result of evaluating the second element in the stream pair.

Unlike the streams we've seen in lecture and earlier in discussion, if you repeatedly call cdr-stream on a stream returned by make-stream, you may evaluate an expression multiple times.

```
(define-macro (make-stream first second)

(define (cdr-stream stream)

scm> (define a (make-stream (print 1) (make-stream (print 2) nil))))
1
   a
   scm> (define b (cdr-stream a))
2
   b
   scm> (cdr-stream b)
```