

# **CSCI-UA-102-011-Spring-2025**

Recitation - 11

# Agenda

- Stability in Sorting Algos
- Q12.6
- Q12.7
- Q12.26

## Stability in Sorting Algorithms

2	4	1	3	4'	5
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→ Unsorted Array

1	2	3	4	4'	5
---	---	---	---	----	---

→ Stable Sort

1	2	3	4'	4	5
---	---	---	----	---	---

→ Unstable Sort

A **stable sorting algorithm** maintains the **relative order** of records with **equal keys**. This means, if two elements a and b have the same key and a comes before b in the input!

Making Bubble Sort Algorithm Stable



```
public static void bubbleSort(int[] A) {  
    int n = A.length;  
    for (int i = 0; i < n; i++) {  
        for (int j = 0; j < n - i - 1; j++) {  
            if (A[j] > A[j + 1]) {  
                int temp = A[j];  
                A[j] = A[j + 1];  
                A[j + 1] = temp;  
            }  
        }  
    }  
}
```

→ Only swap if strictly greater

## 12.6

- A **straggling** algorithm is the *opposite of stable* — if two equal-key entries appear as a before b in the input, then a must appear *after* b in the output.
- To make **Merge Sort straggling**, you can **modify the merge step** like this:

```
public static Entry[] mergeStraggling(Entry[] left, Entry[] right) {
    int i = 0, j = 0, k = 0;
    Entry[] result = new Entry[left.length + right.length];

    while (i < left.length && j < right.length) {
        if (left[i].key < right[j].key) {
            result[k++] = left[i++];
        } else if (left[i].key > right[j].key) {
            result[k++] = right[j++];
        } else {
            result[k++] = right[j++];    → Equal keys – bias towards right to make it straggling
        }
    }
    while (i < left.length) result[k++] = left[i++];
    while (j < right.length) result[k++] = right[j++];

    return result;
}
```

## 12.7 Given two sorted lists A and B, find the sorted union $A \cup B$ without duplicates in $O(n)$ time:

```
public static List<Integer> sortedUnion(int[] A, int[] B) {  
    int i = 0, j = 0;  
    List<Integer> result = new ArrayList<>();  
    while (i < A.length && j < B.length) {  
        if (A[i] < B[j]) {  
            result.add(A[i]);  
            i++;  
        } else if (A[i] > B[j]) {  
            result.add(B[j]);  
            j++;  
        } else {  
            result.add(A[i]);    → A[i] == B[j]  
            i++;  
            j++;  
        }  
    }  
    while (i < A.length) {    → Add remaining elements  
        result.add(A[i++]);  
    }  
    while (j < B.length) {  
        result.add(B[j++]);  
    }  
    return result;  
}
```

12.26

```
public class RemoveDuplicates {  
    public static List<Integer> removeDuplicates(int[] A) {  
        Set<Integer> seen = new HashSet<>();  
        List<Integer> result = new ArrayList<>();  
  
        for (int x : A) {  
            if (!seen.contains(x)) {  
                seen.add(x);  
                result.add(x);  
            }  
        }  
  
        return result;  
    }  
    public static void main(String[] args) {  
        int[] A = {4, 2, 4, 5, 2, 3, 1, 5};  
        List<Integer> unique = removeDuplicates(A);  
  
        for (int num : unique) {  
            System.out.print(num + " ");  
        }  
    }  
}
```

Use a **hash set**  
to track seen  
elements and  
output only  
unique ones!

