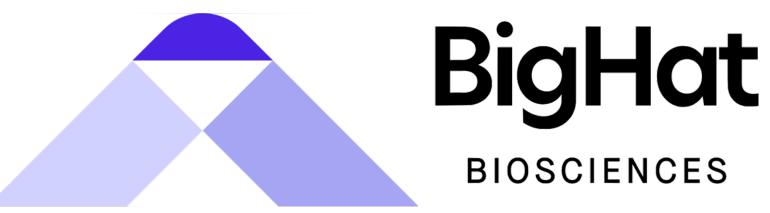
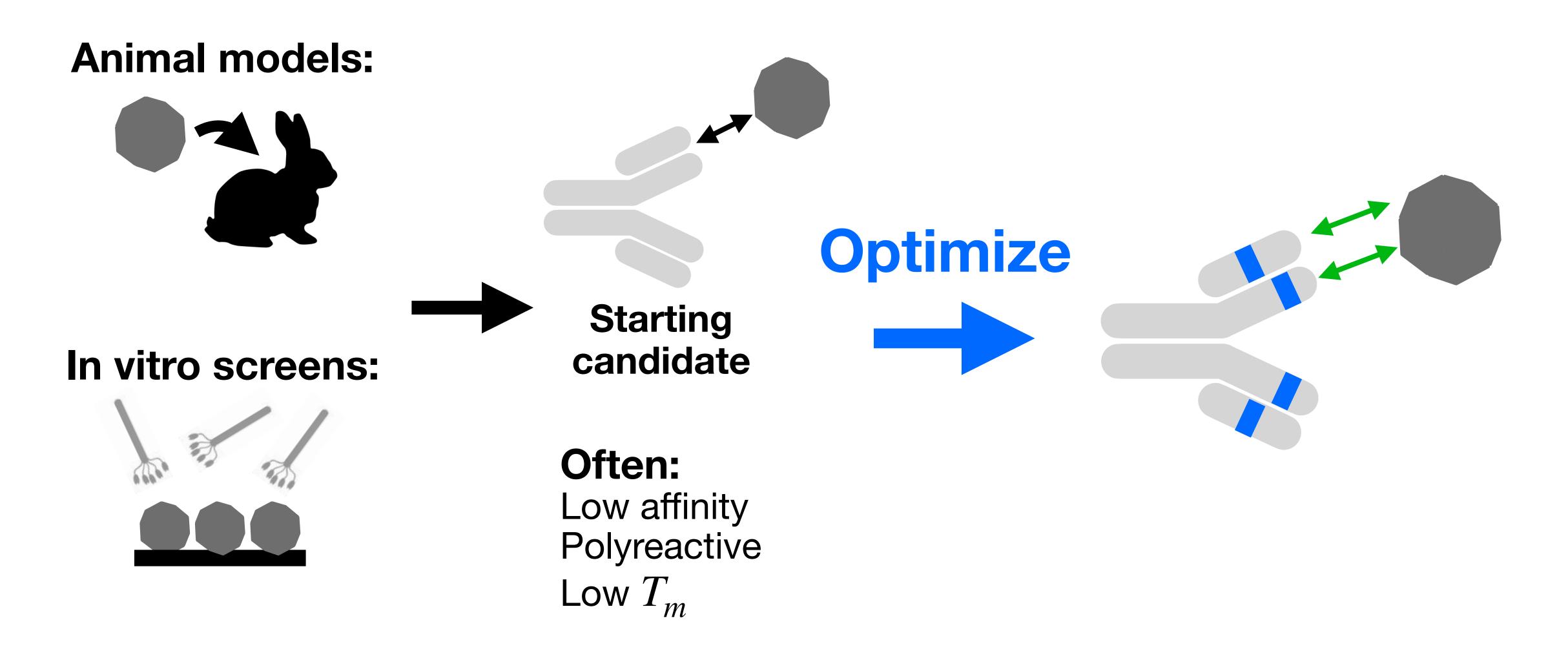
# Bayesian Optimization of Antibodies with a Generative Model of Evolving Sequences

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### To build antibody drugs, we need to optimize "hits" to be strong binders that are stable in the human body



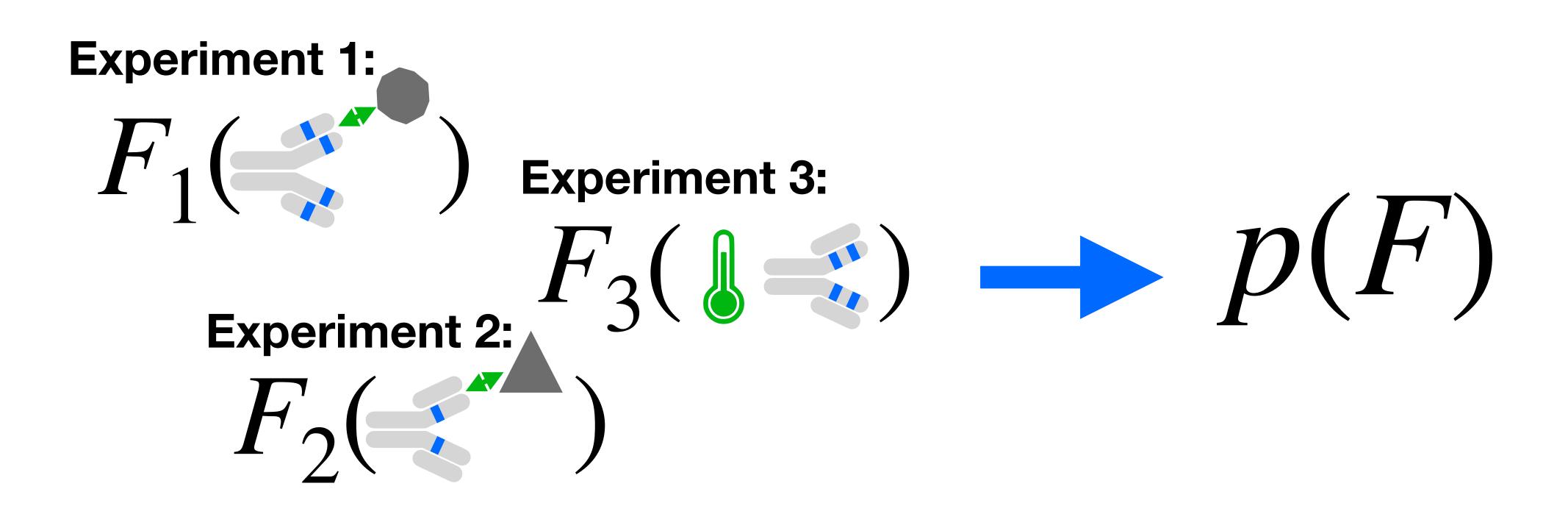
### Optimization by iterative design is hard because most of the many mutations we can test do not help

 $X_0$ 

QVQLRESGPGLVKPSQTLSLTCTVSGGSFNSGGYYWNRIRQHPGNGLEWIGYMYYSGSTYYNPFIRSRVIISGDTSVNHFSLKLSSVTAADTAVYFCARGYRQSGYSSSWVVDYWGQGTLVNVSS

- Goal: iteratively suggest and measure  $X_1, X_2, \ldots, X_{100}$  to have no immunogenicity, have high affinity, or have high melting temperature,  $F(X_N)$
- Possible strategies: random mutations, avoid mutations that don't often appear in humans
- Challenge: search space is huge

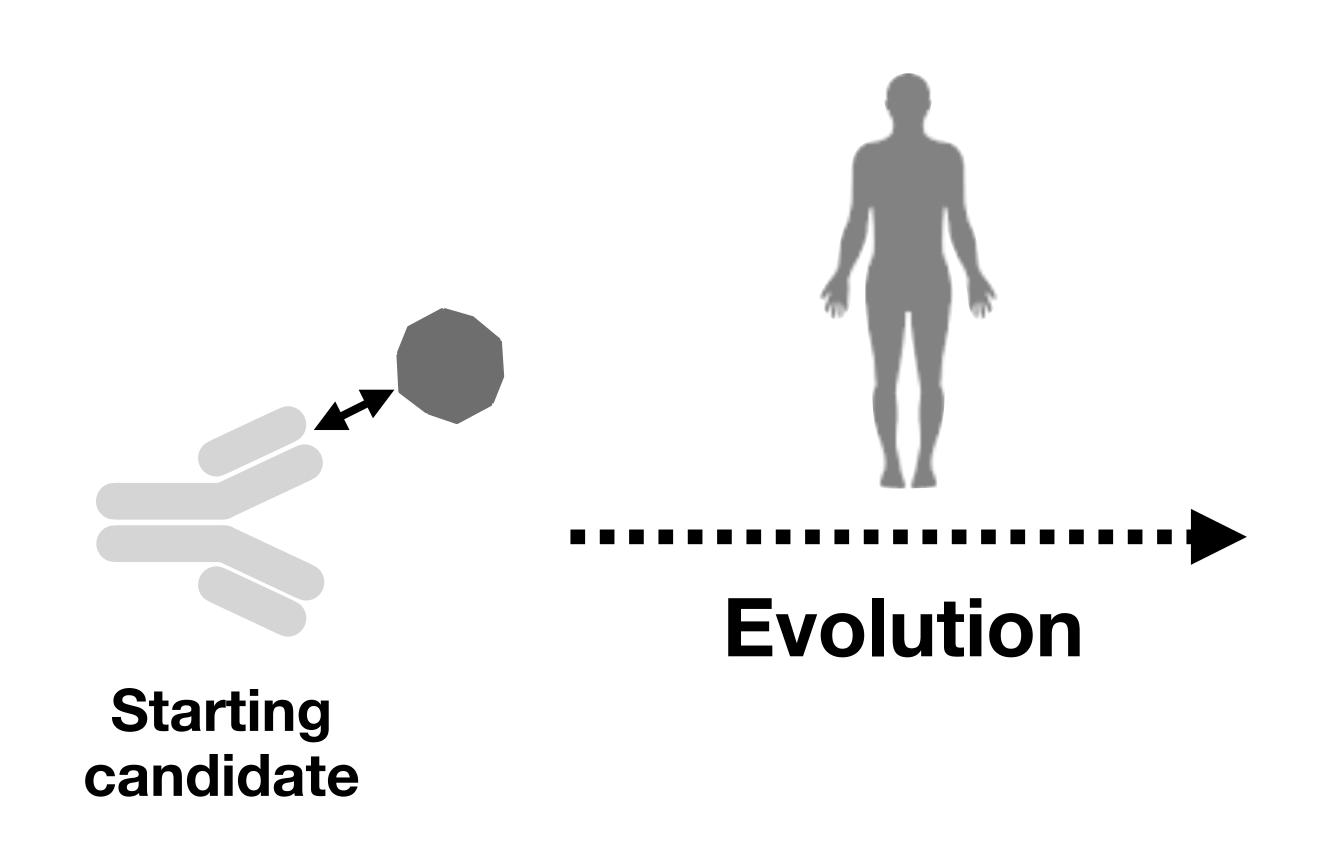
## Ideally we could build a prior on the objectives F(X) of binding strength and stability

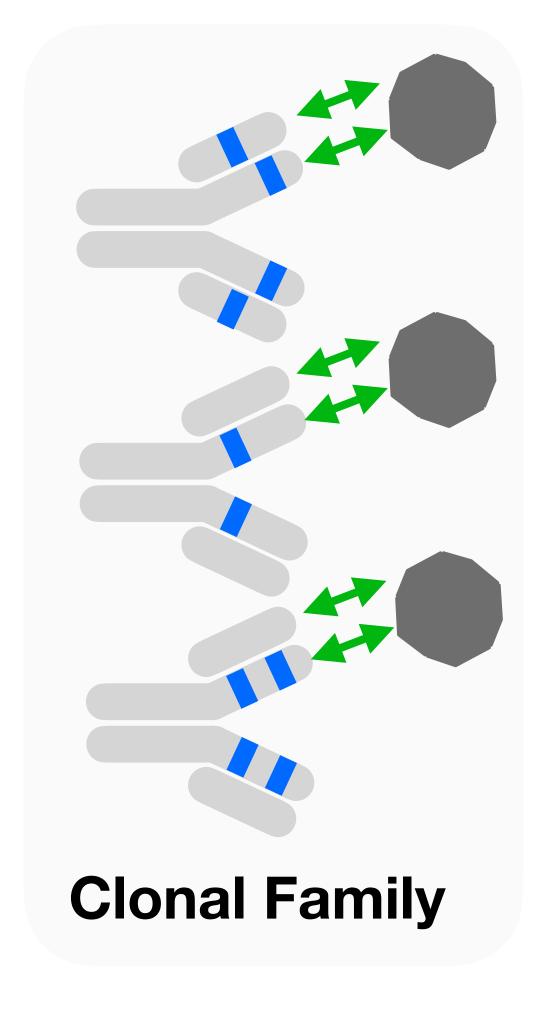


Optimal design strategy: suggest  $X_{N+1}$  based on  $p(F | X_1, ..., X_N)$ 

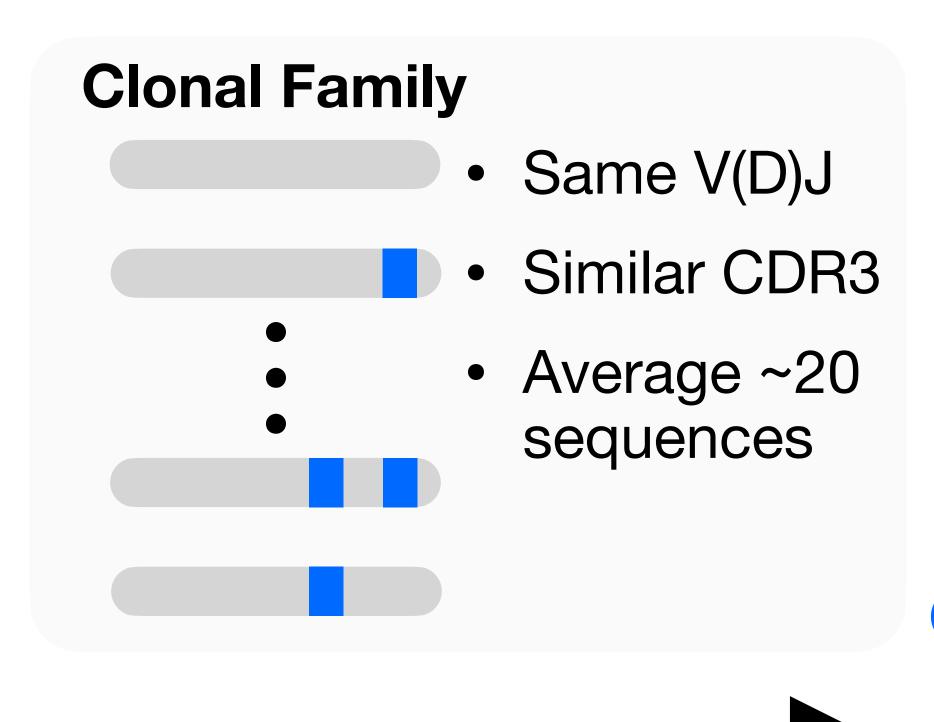
But we don't have this data!

## In principle, we can learn from how our body builds strong and stable binders





### In principle, we can learn from massive data about human clonal families in the OAS database



Observed Antibody Space (OAS):

 $2 \times 10^9$  heavy chains

 $4 \times 10^8$  light chains

FastBCR (Wang K et al 2023)

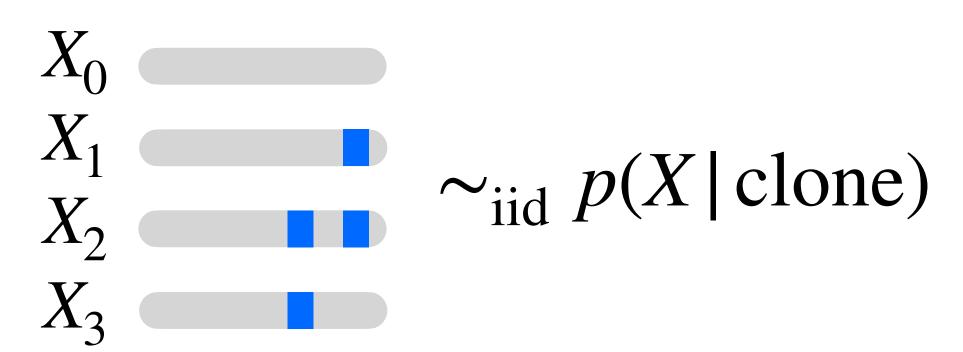
**Observed Clonal Space:** 

 $9 \times 10^5$  heavy clonal families

 $3 \times 10^4$  light clonal families

## In theory, we can build a prior over ${\cal F}$ by looking at the abundance of sequences in each clone

### Distribution of sequences in a clonal family:



Stronger, more stable binders are more abundant:

$$p(X | \text{clone}) = \text{Fitness}(X) =: F(X)$$
 (Like protein families!)

$$F_{2}$$

$$F_{3}$$

$$F_{1}$$

$$F_{3}$$

$$F_{4}$$

$$F_{5}$$

$$F_{6}$$

$$F_{7}$$

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$$F_{9$$

#### CloneLM learns the distribution of clonal families

#### CloneLM (400 M transformer) trained on:

seq1<separator>seq2<separator>seq3<separator>...

Clo	nal
fan	nily

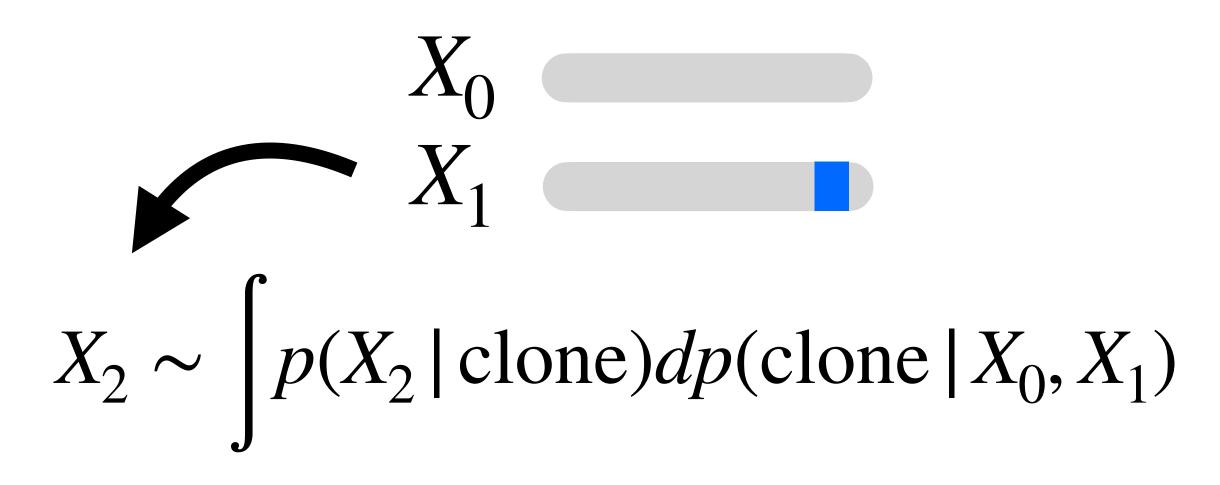
QVQLRESGPGLVKPSQTLSLTCTVSGGSFNSGGYYWNRIRQHPGNGLEWIGYMYYSGSTYYNPFIRSRVIISGDTSVNHFSLKLSSVTAADTAVYFCARGYRQSGYSSSWVVDYWGQGTLVNVSS

QVQLRESGPGLVKPSQTLSLTCTVSGGSINSGGYYWNWIRQHPGKGLEWIGYMYYSGSTYYNPFLRSRVIISADTSENHFSRKLSYVTAADTAVYFCARGYRQSGNSSSWVFDYWGQGTLVNVSS QVQLRESGPGLVKPSQTLSLTCTVSGGSINSGGYYWNWIRQHPGKGLEWIGYMYYSGSTYYNPFLRSRVIILADTSENHFSRKLSSVTAADTAVYFCARGYRQSGYSRSWVFDYWGQGTLVNVSS QVQLRESGPGLVKPSQTLSLTCTVSGGSINSGGYYWNWIRQHPGKGLEWIGYMYYSGSTYYNPFLSSRLIISADTPENHFSRRLSSVTAADTAVYFCATGYPQSGYSSSWVFNYWGQGTLVNVSS

- Sample 1
- QVQLQESGPRLVKPSQTLSLTCTVSGGSLNSGGYYWSWFRQPPGKRLEWIGYMYHTGNTYYNPSLKCRVTISGDTSKSHFPLRLTAVTAADTAAYYCARGYRQGGYSSSWLADYGGQGTLGADSS QVQLQESGPRLVKPSQTLSLTCTVSGGSLNSGGYYWGWIRQPPGKGLEWIGYMYHTGNTYYNPSLKSRVTISGDTSKNHFSLRLTSVTAADTAVYYCARGYRQGSYSSSWLADYWGQGTLVTVSS QVQLRESGPGLVKPSQTLSLTCTVSGGSFNSGGYYWNWIRQHPGKGLEWIGYMYYSGSTYYNPSLRSRVTISGGTSVNPFSLKLSSVTAADTAVYFCARGYRHSGYSSSLLVDYWAEETVVNVSS
- Sample 2
- QVQLRESGPGLVKPSQTLSLTCTVSGGSFNSGGYYWNWIRQHPGKGLEWIGYMYYSGSTYYNPYLRSRVIISGDTSENQFSLKLSSVTAADTAVYLCPRGYRQSCYSSSWVFDYWGQGTLVTVSS QVQLRESGPGLVKPSQTLSLTCTVSGGSFNSGGYYWNWIRQHPGKGLEWIGYMYYSGSTYYNPSLRSRVIISGDTSENHFSLKLSSVTAADTAVYFCARGYRQSGYSSSWVLDYWGQGTLVTVSS QVQLRESGPGLVKPSQTLSLTCTVSGGSFNSGGYYWNWIRQHPGKGLEWIGYMYYSGSTYYNPSLRSRVIISGDTSENHFSLKLSSVTAADTAVYFCARGYRQSGYSASWVFDYWGQGTLVTVSS
- Sample 3
- QVQLRESGPGLVKPSQTLSLTCTVSGGSFNSGGYYWNWIRQHPGNGLEWIGYMYYSGSTYYNPFLKSRVIISGDTSVTHFSLKLSSVTAADTAVYFCARGYRQSGSSSSWVIDYWGQGTLVTVSS QVQLRESGPGLVKPSQTLSLTCTVSGGSFNSGGYYWNWIRQHPGNGLEWIGYMYYSGSTYYNPFLMSRVIIRGETSVKHFSLKLSSVTAADTAVYFCARGYSQSSSSWVIDYWGQGTLVTVSS QVQLRESGPGLVKPSQTLSLTCTVSGGSFNSGGYYWNWIRQHQGDGLEWIGYLYYSGSTYYNPFVKRRVIISGDKSVNHFSLKLSSVTAADTDVYFCARGYGQSGYSSAWVIDYWGQGTLVTVSS

### In theory, CloneLM performs approximate Bayesian inference over evolutionary landscapes

Predictions should integrate over F:



Predictions should converge to F:

$$X_{0}$$

$$X_{1}$$

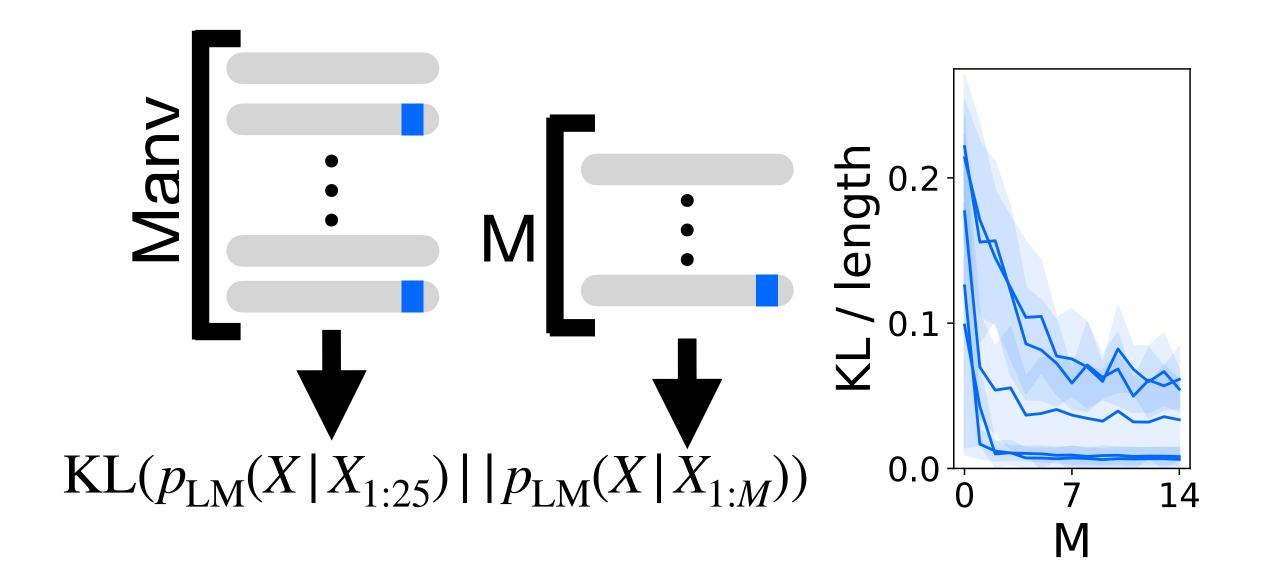
$$\vdots$$

$$X_{N+1} \sim \int p(X_{N+1} | \text{clone}) dp(\text{clone} | X_{1:N})$$

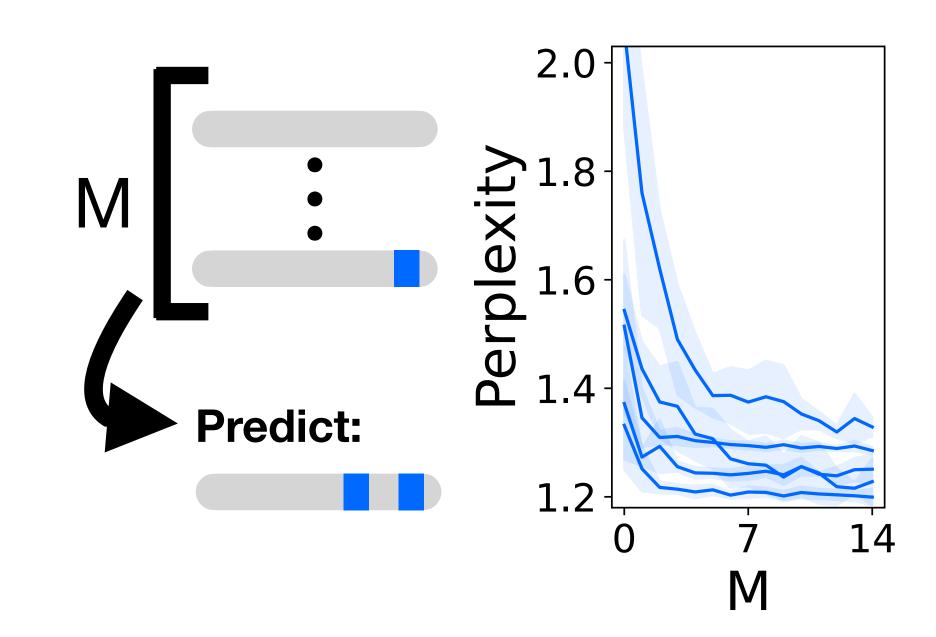
$$\approx p(X_{N+1} | \text{clone})$$

## Given more sequences from a clonal family, CloneLM predictions converge to p(X | clone)

#### Predictions converge:

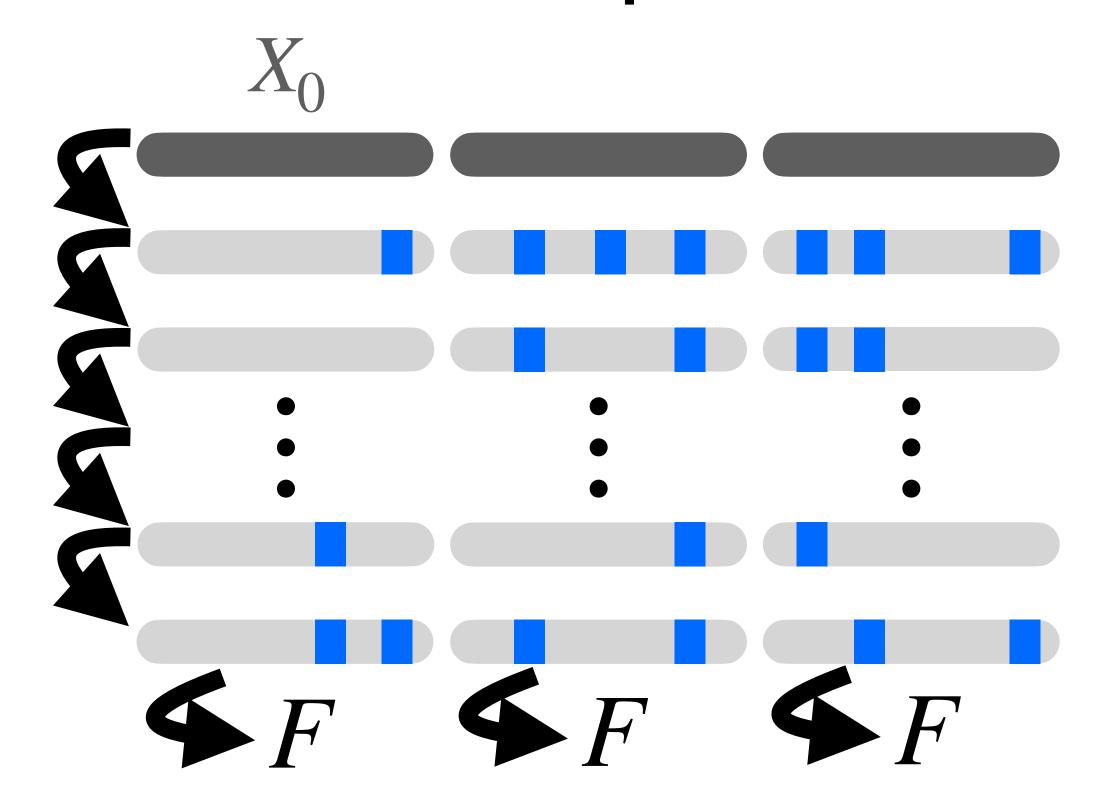


### Predictions approach p(X | clone):

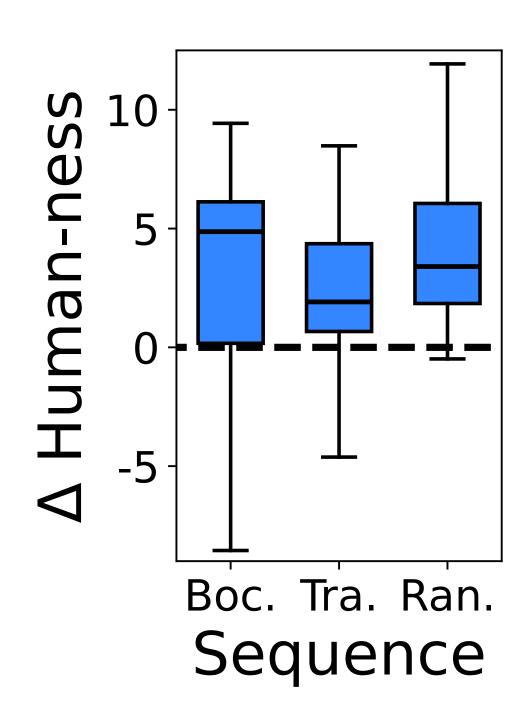


### The CloneLM prior over fitness functions optimizes antibodies to become more human-like

Sample possible fitness landscapes F:



Optimize over three mutations with respect to F:



### To update our belief in F, we assume measurements in the lab are proportional to fitness

#### **Experiment:**

## 

#### Posterior:

$$p(F|X_0, (X_n, Y_n)_n) \propto p(F|X_0) \prod_n p(Y_n|F(X_n))$$

#### Likelihood:

$$p(Y|F(X)) \sim \mathcal{N}(\beta F(X) + C, \sigma^2)$$

Uniform prior on  $\beta$ , C

### How do we sample from the posterior?

#### Importance sample (naive):

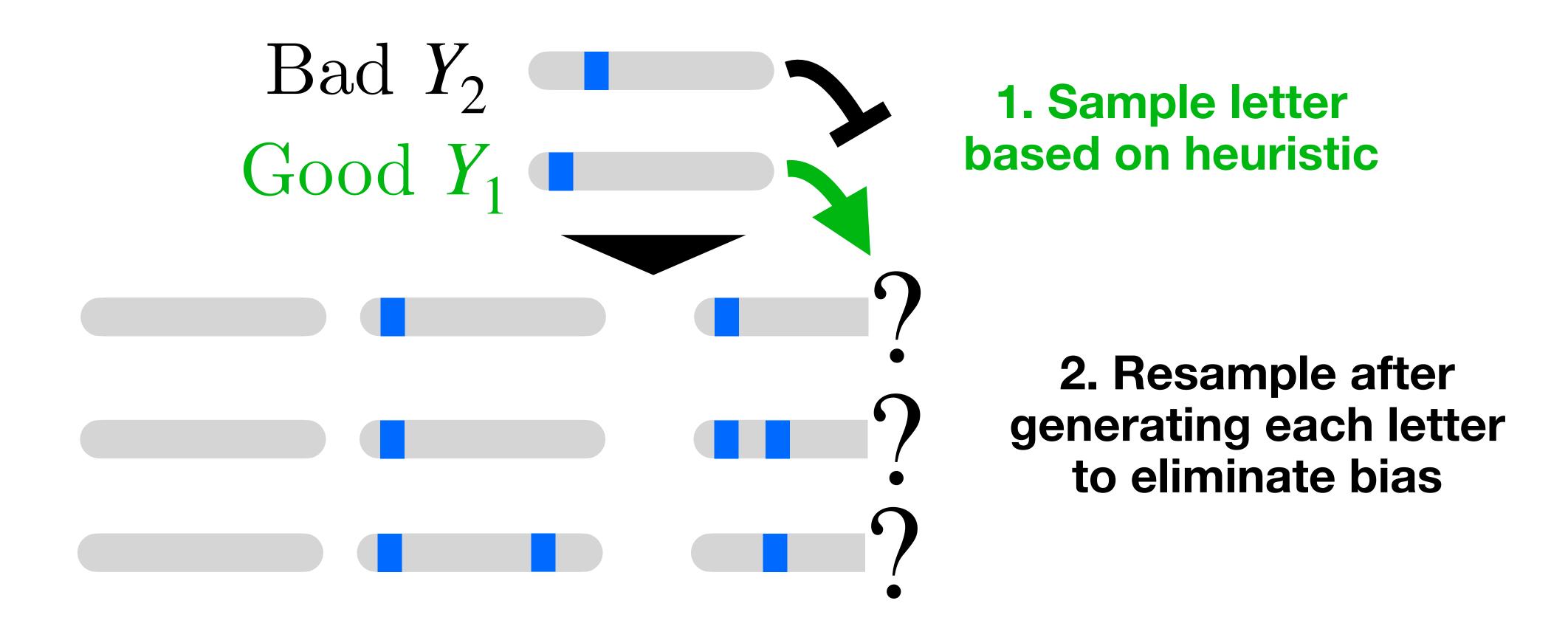
1. Sample many F from prior  $F \sim p(F | X_0)$ 



2. Resample based on likelihood

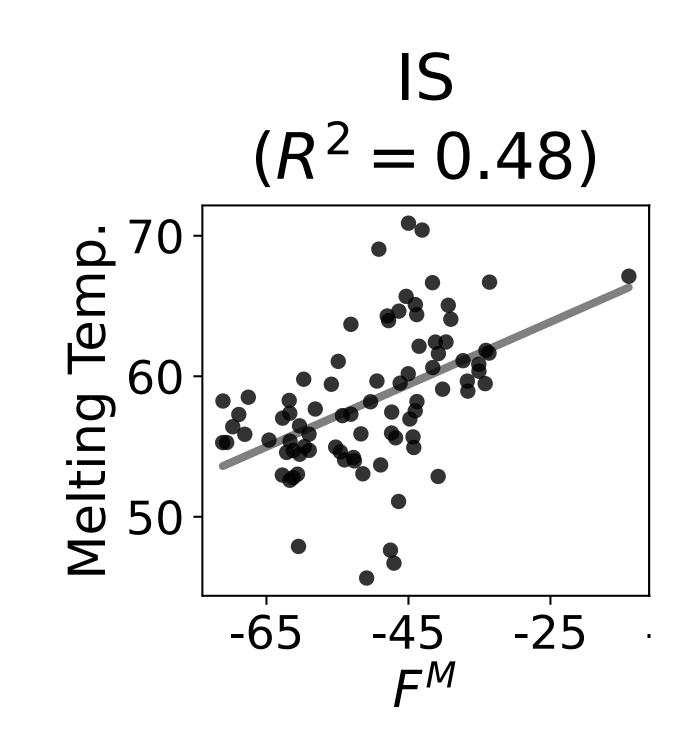
$$\prod_{n} p(Y_n | F(X_n))$$

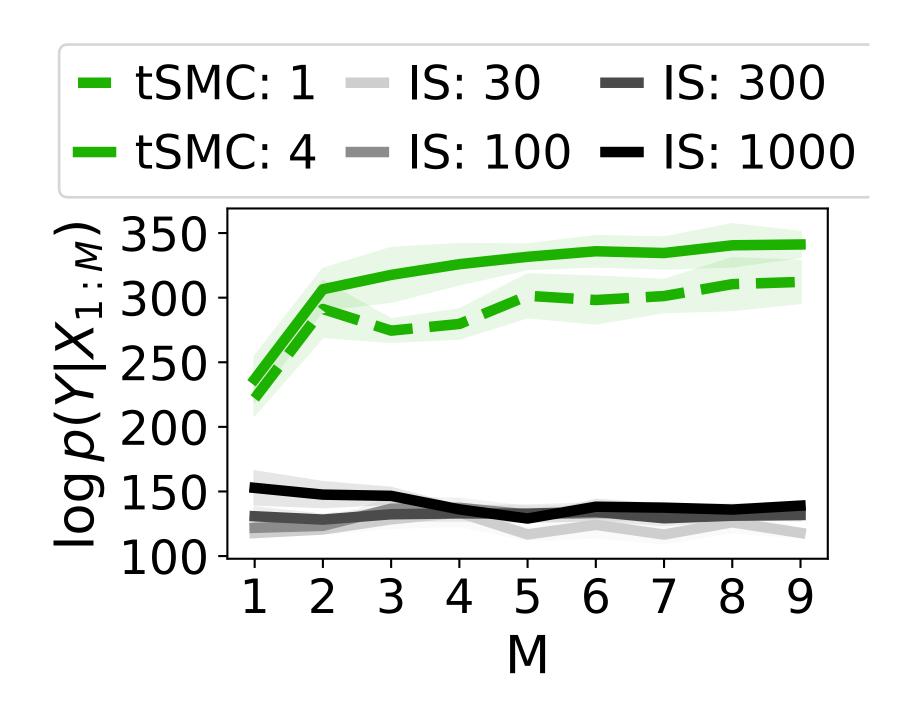
### We inform our sampling with twisted stochastic Monte Carlo



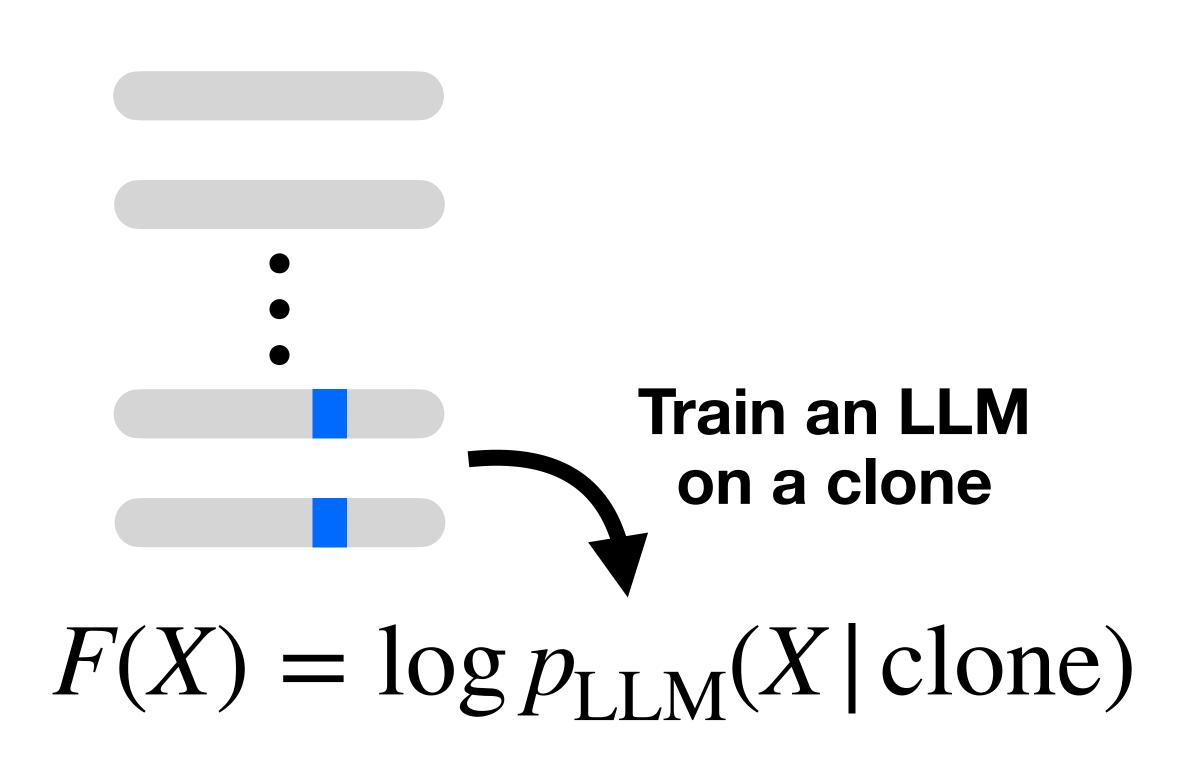
### tSMC efficiently samples from the posterior

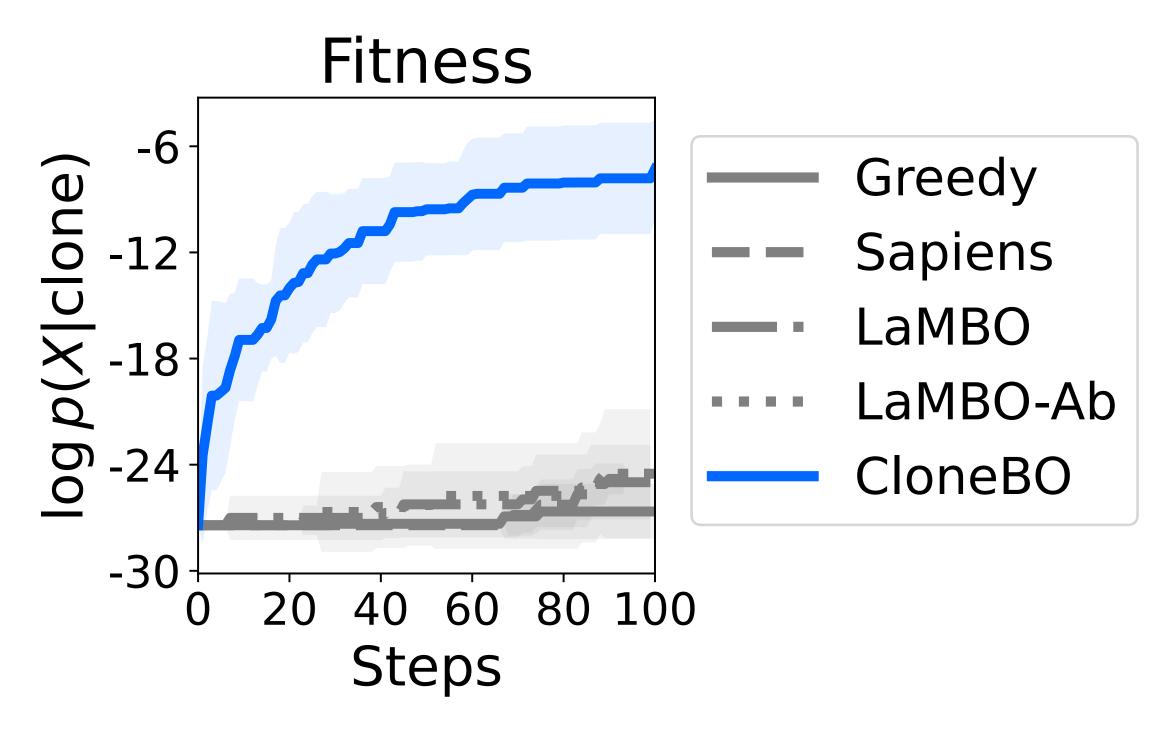
#### Condition on real $T_m$ measurements





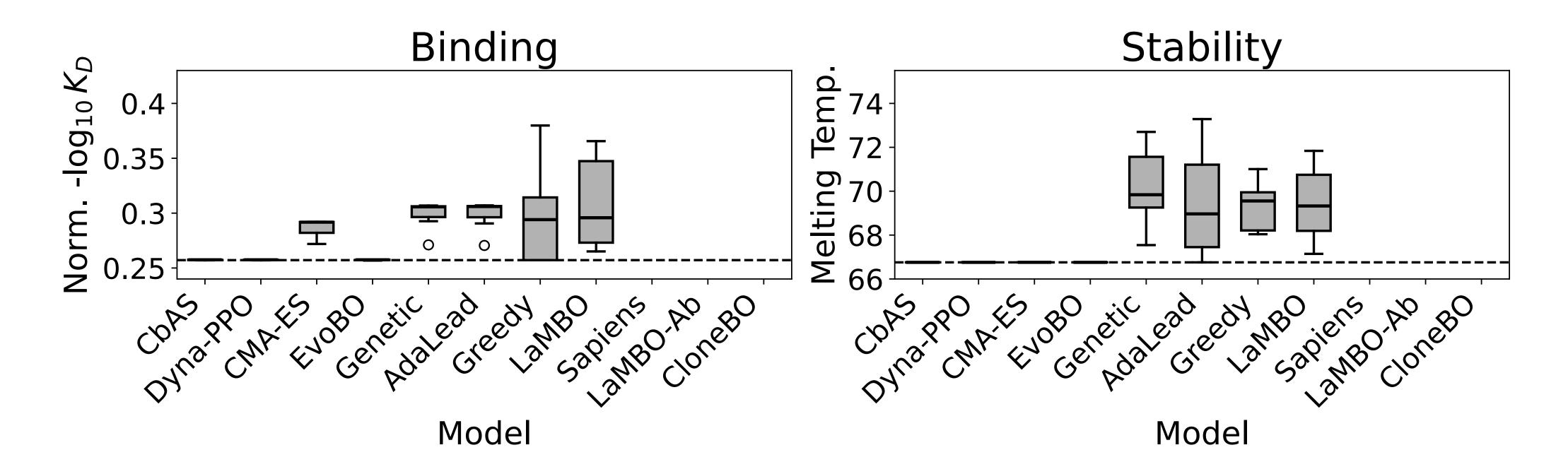
## CloneBO efficiently optimizes a function from its prior



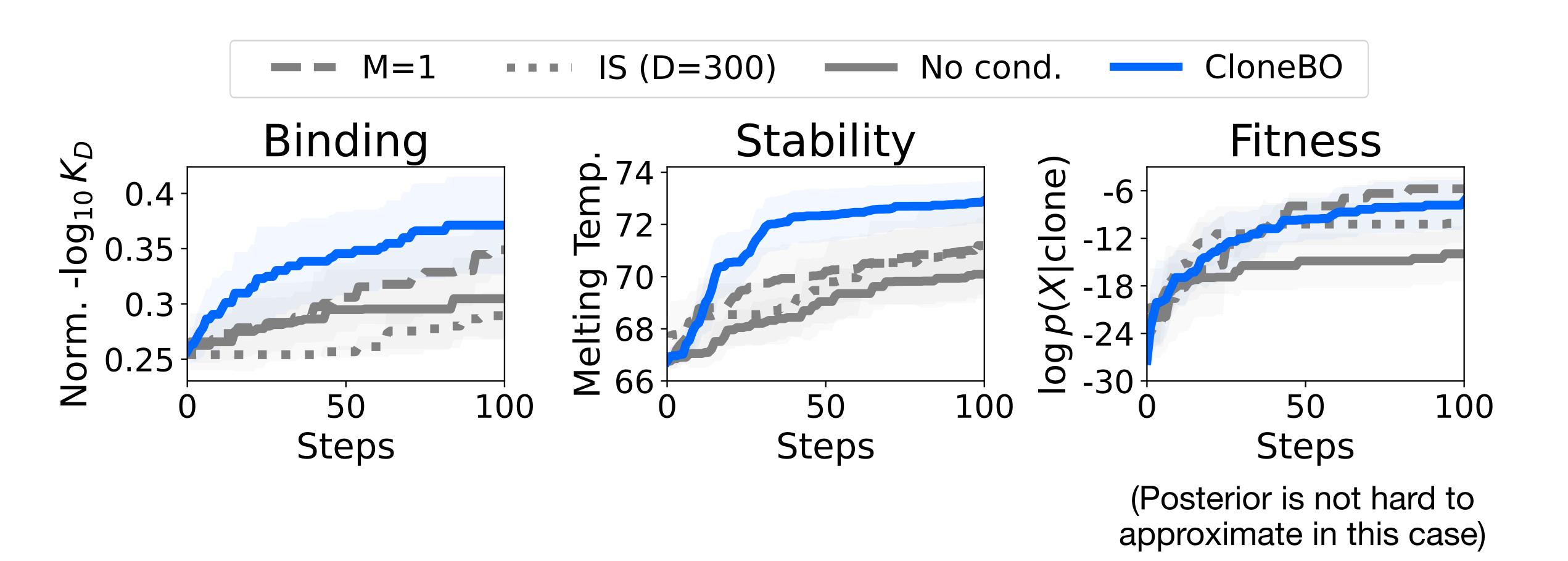


## CloneBO efficiently optimizes for binding and stability in silico

$$F(X) =$$
 neural network trained on thousands of sequences from iterative design experiment



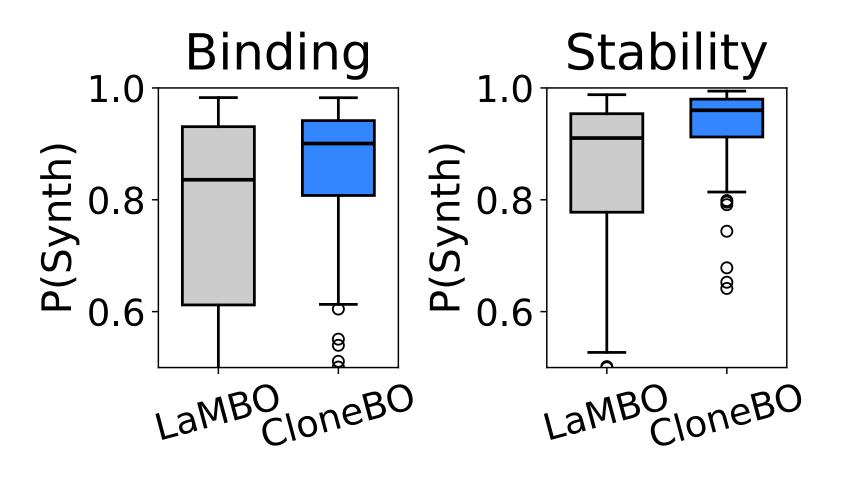
## Ablations demonstrate that CloneBO efficiently optimizes sequences by doing accurate inference



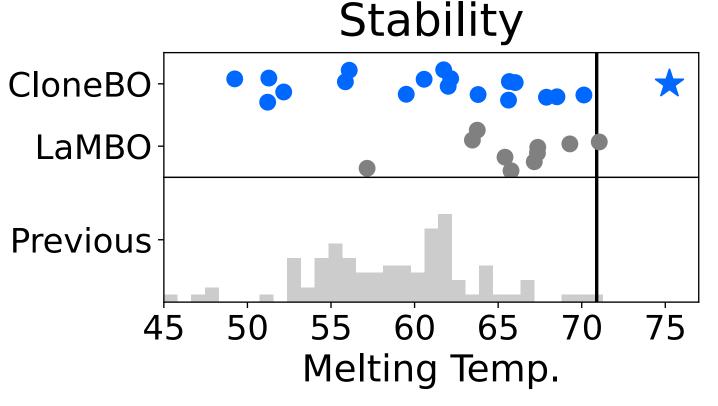
## CloneBO efficiently optimizes for binding and stability in vitro

Given  $X_0, \ldots, X_{1000}$ , measurements for binding and stability, design  $X_{1001}$ 

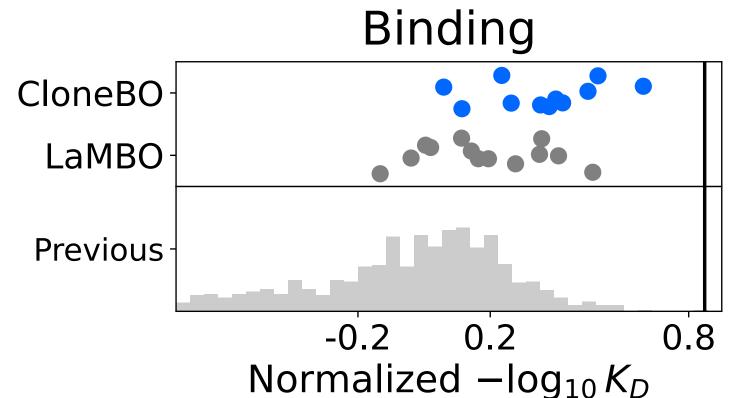
### Designs are predicted to express:



### Designs improve stability:

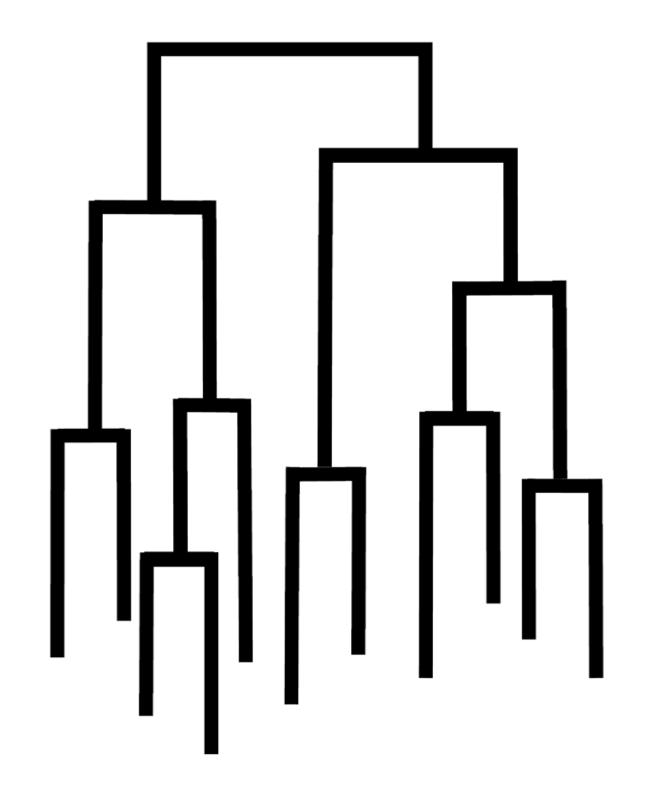


### Designs outperform in binding:

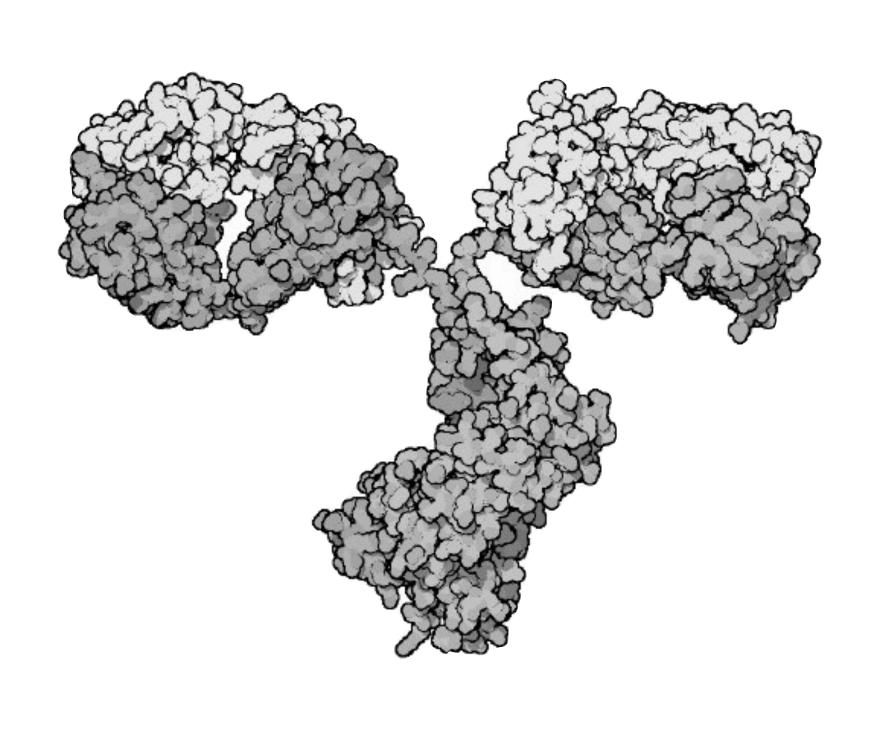


#### **Future directions**

More realistic prior Learn direction of evolution



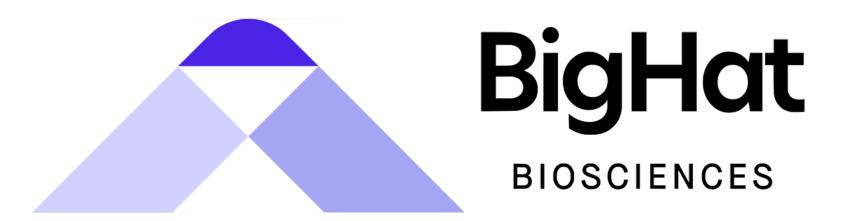
### Build a prior on structure Structure from clonal families



### Acknowledgments



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