

ECE 485/585 – Computer Organization and Design

HOMEWORK #3

Due date: Friday, September 30th 2022 11:59PM

Solve the following exercises from the textbook (Chapter 3)

1. What is 6FD4-273B when these values represent signed 16-bit hexadecimal numbers stored in sign-magnitude format? The result should be written in hexadecimal. You MUST show your work.
2. Assume 174 and 85 are signed 8-bit decimal integers stored in sign-magnitude format. Calculate 174+85. Is there overflow, underflow or neither? You MUST show your work.
3. Using a table similar to the below Table 1, calculate 60 divided by 22 by using the hardware described in Figure 1. You should show the contents of each register on each step. Assume both inputs are unsigned 6-bit integers, *NOT 32-bit integers*, and modify the division hardware shown in Figure 1. (Refer to Lecture Note #5 Page 12-14.)

| Iteration | Step | Quotient | Divisor | Remainder |
|-----------|---|----------|-----------|-----------|
| 0 | Initial values | 0000 | 0010 0000 | 0000 0111 |
| 1 | 1: Rem = Rem – Div | 0000 | 0010 0000 | ⓪110 0111 |
| | 2b: Rem < 0 \Rightarrow +Div, sll Q, Q0 = 0 | 0000 | 0010 0000 | 0000 0111 |
| | 3: Shift Div right | 0000 | 0001 0000 | 0000 0111 |
| 2 | 1: Rem = Rem – Div | 0000 | 0001 0000 | ⓪111 0111 |
| | 2b: Rem < 0 \Rightarrow +Div, sll Q, Q0 = 0 | 0000 | 0001 0000 | 0000 0111 |
| | 3: Shift Div right | 0000 | 0000 1000 | 0000 0111 |
| 3 | 1: Rem = Rem – Div | 0000 | 0000 1000 | ⓪111 1111 |
| | 2b: Rem < 0 \Rightarrow +Div, sll Q, Q0 = 0 | 0000 | 0000 1000 | 0000 0111 |
| | 3: Shift Div right | 0000 | 0000 0100 | 0000 0111 |
| 4 | 1: Rem = Rem – Div | 0000 | 0000 0100 | ⓪000 0011 |
| | 2a: Rem \geq 0 \Rightarrow sll Q, Q0 = 1 | 0001 | 0000 0100 | 0000 0011 |
| | 3: Shift Div right | 0001 | 0000 0010 | 0000 0011 |
| 5 | 1: Rem = Rem – Div | 0001 | 0000 0010 | ⓪000 0001 |
| | 2a: Rem \geq 0 \Rightarrow sll Q, Q0 = 1 | 0011 | 0000 0010 | 0000 0001 |
| | 3: Shift Div right | 0011 | 0000 0001 | 0000 0001 |

Table 1. Division example (Figure 3.10 of textbook)

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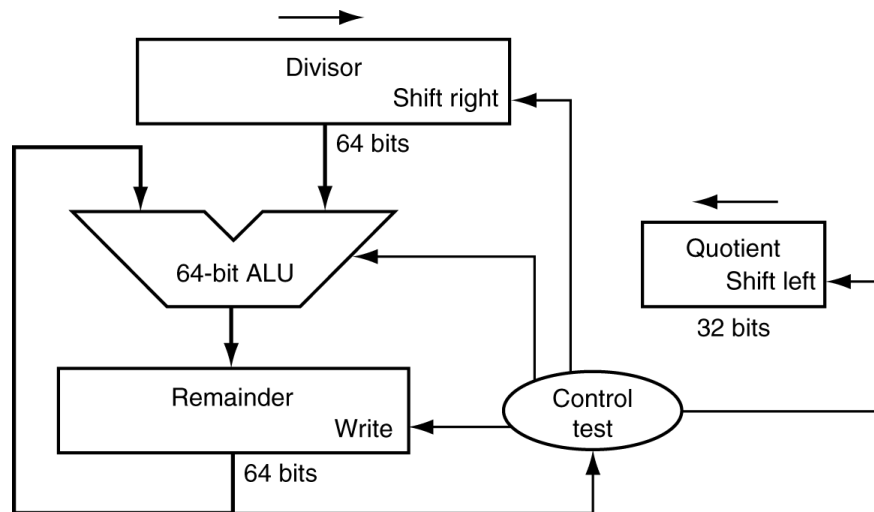


Figure 1. Division Hardware

4. Write down the binary representation of the decimal number 56.93 assuming the IEEE 754 double precision format.
5. IEEE 754-2008 standard contains a half precision that is only 16 bits wide. Leftmost bit, which is the most significant bit (MSB), is still the sign bit, the exponent is 5 bits wide and has a bias of 15, and the fraction is 10 bits long. A hidden 1 is assumed. Write down the bit pattern to represent -1.585×10^{-1} assuming a version of this format, which uses an excess-16 format (exponent bias = 15) to store the exponent. Comment on how the range and accuracy of this 16-bit floating point format compares to the single precision IEEE 754 standard.