

ECE 485/585 – Computer Organization and Design

HOMEWORK #1 SOLUTION

Solve the following exercises from the textbook (Chapter 1)

1. Exercise 1.2
 - a. Performance via Pipelining
 - b. Dependability via Redundancy
 - c. Performance via Prediction
 - d. Make the Common Case Fast
 - e. Hierarchy of Memories
 - f. Performance via Parallelism
 - g. Design for Moore's Law
 - h. Use Abstraction to Simplify Design

2. Exercise 1.6

Class A: 10^5 instr. Class B: $2 \cdot 10^5$ instr. Class C: $5 \cdot 10^5$ instr. Class D: $2 \cdot 10^5$ instr.

$$Global\ CPI = \frac{Total\ Time * Clock\ Rate}{No.\ Inst.}$$

$$Total\ Time = \sum_i \frac{Inst.\ Count_i * CPI_i}{Clock\ Rate}$$

$$Clock\ Cycles = \sum_{i=1}^n (CPI_i * C_i)$$

a. Total Time P1 = $(10^5 \cdot 1 + 2 \cdot 10^5 \cdot 2 + 5 \cdot 10^5 \cdot 3 + 2 \cdot 10^5 \cdot 3) / (2.5 \cdot 10^9) = 10.4 \cdot 10^{-4} \text{ s}$

Total Time P2 = $(10^5 \cdot 2 + 2 \cdot 10^5 \cdot 2 + 5 \cdot 10^5 \cdot 2 + 2 \cdot 10^5 \cdot 2) / (3 \cdot 10^9) = 6.66 \cdot 10^{-4} \text{ s}$

CPI P1 = $(10.4 \cdot 10^{-4} * 2.5 \cdot 10^9) / (10^6) = 2.6$

CPI P2 = $(6.66 \cdot 10^{-4} * 3 \cdot 10^9) / (10^6) = 2.0$

b. Clock Cycles P1 = $10^5 \cdot 1 + 2 \cdot 10^5 \cdot 2 + 5 \cdot 10^5 \cdot 3 + 2 \cdot 10^5 \cdot 3 = 26 \cdot 10^5$

Clock Cycles P2 = $10^5 \cdot 2 + 2 \cdot 10^5 \cdot 2 + 5 \cdot 10^5 \cdot 2 + 2 \cdot 10^5 \cdot 2 = 20 \cdot 10^5$

3. Exercise 1.9

a.

p	Arith	L/S	B	Cycles	Exec Time	Speedup
1	2.56E+09	1.28E+09	2.56E+08	1.92E+10	9.60 s	1.00
2	1.83E+09	9.14E+08	2.56E+08	1.41E+10	7.04 s	1.36
4	9.14E+08	4.57E+08	2.56E+08	7.68E+09	3.84 s	2.50
8	4.57E+08	2.29E+08	2.56E+08	4.48E+09	2.24 s	4.29

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b.

p	Arith	L/S	B	Cycles	Exec Time
1	2.56E+09	1.28E+09	2.56E+08	2.18E+10	10.9
2	1.83E+09	9.14E+08	2.56E+08	1.59E+10	7.95
4	9.14E+08	4.57E+08	2.56E+08	8.59E+09	4.30
8	4.57E+08	2.29E+08	2.56E+08	4.94E+09	2.47

c.

$$\frac{(\# Inst_{Ar} * CPI_A) + (\# Inst_L * CPI_L) + (\# Instr_B * CPI_B)}{0.7 * 4} = \frac{(\# Inst_{Ar} * CPI_A) + (\# Inst_L * CPI_{L,new}) + (\# Instr_B * CPI_B)}{Clock\ Rate}$$

$$\frac{(\# Inst_{Ar} * CPI_A) + (\# Inst_L * CPI_L)}{0.7 * 4} = (\# Inst_{Ar} * CPI_A) + (\# Inst_L * CPI_{L,new})$$

$$(2.56E9 * 1 + 1.28E9 * 12) / 2.8 = 2.56E9 * 1 + 1.28E9 * CPI_{L/S, New}$$

$$CPI_{L/S, New} = 3$$

4. Exercise 1.13

$$T_{total} = 250s, T_{fp} = 70s, T_{L/S} = 85s, T_B = 40s, T_{INT} = 55s$$

a. $T_{fp,new} = 70 * 0.8 = 56\ s$

$$T_{new} = T_{fp,new} + T_{L/S} + T_B + T_{INT} = 56 + 85 + 40 + 55 = 236s$$

$$Reduction = 1 - T_{new}/T_{old} = 1 - 0.944 = \mathbf{5.6\%}$$

b. $T_{new} = 250 * 0.8 = 200\ s$

$$T_{fp} + T_{L/S} + T_B = 70 + 85 + 40 = 195\ s$$

$$T_{int} = 200 - 195 = 5\ s$$

$$Reduction = 1 - 5/55 = \mathbf{90.9\% reduction}$$

c. $T_{new} = 200s$

$$T_{fp} + T_{INT} + T_{L/S} = 70 + 55 + 85 = 210\ s \rightarrow \mathbf{no\ room\ for\ reduction\ so\ NO}$$

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5. Exercise 1.14

$$\text{Clock Cycles} = \sum_{i=1}^n (CPI_i * C_i)$$

$$\text{Initial Clock Cycles} = 1*(50E6) + 1*(110E6) + 4*(80E6) + 2*(16E6) = 512E6$$

a. $CPI_{TP,New} * 50E6 + 1*(110E6) + 4*(80E6) + 2*(16E6) = 256E6$

$$CPI_{TP,New} * 50E6 + 462E6 = 256E6$$

CPI cannot be negative so not possible

b. $1*(50E6) + 1*(110E6) + CPI_{L/S,New}*(80E6) + 2*(16E6) = 256E6$

$$192E6 + CPI_{L/S,New}*(80E6) = 256E6$$

$$CPI_{L/S,New} = 0.8$$

c. $\text{Cycles} = 0.6*(50E6) + 0.6*(110E6) + 0.7*4*(80E6) + 0.7*2*(16E6) = 342.4E6$

$$Time = \frac{Cycles}{Clock Rate}$$

$$Time_{initial} = (512E6)/(2E9) = 0.256 \text{ s}$$

$$Time_{new} = (342.4E6)/(2E9) = 0.1712 \text{ s}$$