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In [13]: #Alan Uthuppan

import math
from math import comb
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In [14]: print("Problem 1\n")

n = 4000
p = 0.001

avg = p*(n-1)
print("Graph would have an average degree = " + str(avg) + "\n")

print("Graph would have a variance = " + str(avg*(1-p)) + "\n")

atLeastTwiceLarger = []
for i in range(math.ceil(2*avg), 100):
    atLeastTwiceLarger.append(comb(n-1, i)*(p**i)*(1-p)**(n-1-i))
print("# of nodes with degree greater than or equal to average times 2 = " + str
```

Problem 1

Graph would have an average degree = 3.999

Graph would have a variance = 3.99500100000000002

of nodes with degree greater than or equal to average times 2 = 203.93917397722828

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In [15]: print("Problem 2\n")

print("Part a:\nProbability of creating an edge = (# of edges)/(Maximum # of edges)

print("Partb:\nWe need three nodes all sharing edges for a triangle. There are
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Problem 2

Part a:

Probability of creating an edge = (# of edges)/(Maximum # of edges). Therefore, $p = (c*n/2)/(n(n-1)/2) = c/(n-1)$

Partb:

We need three nodes all sharing edges for a triangle. There are n choose 3 possible triangles which equals $n!/(3!(n-3)!)$. Every edge has a $c/(n-1)$ probability of existing (as shown in part a). Therefore, in order for a particular triangle to exist there is a $(c/(n-1))^3$ chance.

Therefore, total number of triangles equals the probability of a triangle existing times the # of potential triangles, which equals $n!/(3!(n-3)!)*(c/(n-1))^3$, which simplifies to $(c^3)/6$ as n approaches infinity.