## Questions to Exam on the course «Mathematical methods in forecast» Prof. Yaroslavna Pankratova

- 1) Give the definition of a time series. What is a strictly stationary time series?
- 2) Give the definition of a time series. What is a weakly stationary time series?
- 3) What is autocorrelation function and private autocorrelation functions? Name their applications.
- 4) What is "white noise"?
- 5) Describe an autoregressive process of order p. Under which condition is the process the AR(1)-process stationary?
- 6) What are the relations between the coefficients of the equation for the AR(1)-process and the values of its autocorrelation function?
- 7) What are the relations between the coefficients of the equation of the AR(2)-process and the values of its autocorrelation function?
- 8) Describe the moving average process of order q. Under which condition is the process SS(1) stationary?
- 9) Let the process  $y_t \phi_1 y_{t-1} = \delta + \varepsilon_t \theta_1 \varepsilon_{t-1}$  be given. Determine the type of this process. Under which conditions is the process stationary?
- 10) Describe the process of a random walk and give its properties.
- 11) Describe the problem of nonstationary time series and its consequences. Give methods for detecting nonstationarity and correcting the series.
- 12) What is an integrable time series of order d?
- 13) What is the evaluation of the quality of ARIMA models? Provide some well-known criteria of the quality for ARIMA models.
- 14) Write the following process using the lag operator

$$y_t = \mu + \phi_1 y_{t-1} + \phi_2 y_{t-2} + \dots + \phi_p y_{t-p} + \varepsilon_t.$$

- 15) List the possible composition of the non-random components of a time series and some methods for determining their presence in the series.
- 16) Describe the moving average method. What is it used for?
- 17) Describe the weighted moving average method. What is it used for?
- 18) What is the difference between the simple exponential smoothing and the linear exponential smoothing?
- 19) What is the essence of Brown's method? What is the multiple exponential smoothing?
- 20) Write down the Gauss-Markov conditions for a multiple linear regression.
- 21) Give the definition of the coefficient of determination, its interpretation and applications.
- 22) Give definitions of a point forecast and an interval forecast. How to calculate the interval forecast if the point forecast and the standard error of the forecast are given?
- 23) What is the meaning of the "standard error of a regression coefficient"?
- 24) Which test is used to check significance of a linear regression equation?
- 25) Based on which indicators can you judge the quality of coefficients of the regression model?
- 26) What are the standardized coefficients of a multiple regression? What is their meaning?
- 27) Define and interpret the partial elasticity coefficients. For what purpose are they used?
- 28) What properties should the errors of the linear regression equation satisfy?
- 29) What is the method of least squares?
- 30) The regression  $y = \beta_0 + \beta_0 x + \varepsilon$  is estimated based on two observations. What is the coefficient of determination?
- 31) Describe the concept of multicollinearity. Consequences multicollinearity, methods of its detection and ways to get rid of multicollinearity.
- 32) Give the definition of the coefficient of determination and the adjusted coefficient of determination. What is their difference? Application area?