



# Foundations of Computer Science - Big O Notation

Sparky Training Academy  
Audited by Yuri Malitsky

# Big O Notation Explained

## Introduction to Big O Notation

- **Definition:** Big O Notation ( $O$ ) describes the maximum rate of growth of time complexity as the input size increases, emphasizing the worst-case scenario.
- **Role in CS:** Critical for evaluating how an algorithm's performance scale changes with an increasing dataset or under peak operational load.
- **Practical Example:**
  - Searching for an item in an unsorted list has time complexity  $O(n)$ .
  - In contrast, binary search in a sorted list has time complexity  $O(\log n)$ .
- **Analogy:** Shopping time increases linearly with the number of items if each item is processed individually, compared to multiple registers working concurrently.

# Understanding Big O Notation

## Defining Big O Notation

- Big O: Describes worst-case upper bound complexity.
- Example: Loop runs  $n$  times; complexity is  $O(n)$ .

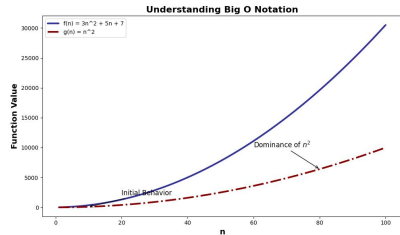
## Importance of the Highest Order Term

- Focus on largest growth term in Big O.
- Lower terms and constants ignored.

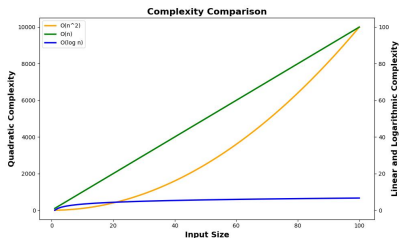
When analyzing complexity, consider function  $f(n) = 3n^2 + 5n + 7$ . In Big O notation, this simplifies to  $O(n^2)$ .

### Explanation:

As  $n$  increases,  $n^2$  term governs the growth, overshadowing  $5n$  and  $7$ , which become negligible.



# Practical Impact of Big O



## Understanding Big O Notation

- **Definition:** Quantifies worst-case scenario efficiency of an algorithm with increasing input size.
- **Algorithm Efficiency:** Essential for performance in large-scale data processing.
- **Practical Example:** Consider sorting algorithms - Selection sort typically exhibits  $O(n^2)$ .

## Real-World Impact of Big O

- **Algorithm Efficiency Comparison:**
  - $O(n)$  vs.  $O(n^2)$  sorting impact.
- **Optimized Algorithms:** Prioritize  $O(n)$  for large datasets.

# Time Complexities Catalog

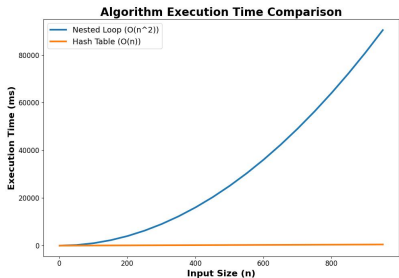
## Time Complexities Catalog

Complexity Type	Characteristics
$O(1)$	Constant: Does not vary with input size
$O(n)$	Linear: Increases directly with input size
$O(n^2)$	Quadratic: Each element interacts with others
$O(2^n)$	Exponential: Doubles with each input increment
$O(\log n)$	Logarithmic: Decreases data input size stepwise

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# Example of Linear Time Complexity  $O(n)$ 
def find_max(data):
    max_val = data[0] # Assume non-empty list
    for num in data:
        if num > max_val:
            max_val = num
    return max_val
```

**Explanation:** The function `find_max` iterates through each element to find the maximum value, reflecting a linear relationship with the size of the data  $n$ .

# Space vs. Time in Algorithms



## Understanding Space and Time Complexity

- **Space Complexity:** Total memory usage, includes constants.
- **Time Complexity:** Worst-case step count as input size grows.

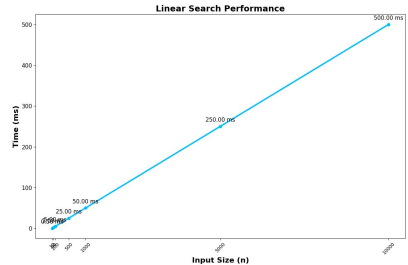
## Trade-offs Between Space and Time Complexity

- **Space vs. Time Complexity:** Nested loop for finding duplicates: Space  $O(1)$ , Time  $O(n^2)$ .
- **Balancing Complexity:** Hash table use: Space  $O(n)$ , Time  $O(n)$ .
- **Practical Application:** Nested loops optimal for small, space-sensitive lists.

# Calculating Big O

## Calculating Big O for Linear Search

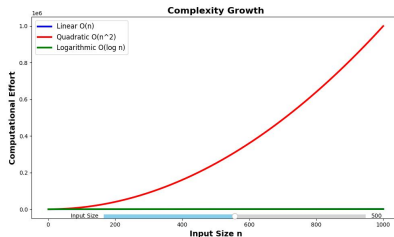
- **Big O Notation:** Measures worst-case efficiency.
- **Linear Search Steps:** Inspect each element till target found.
- **Big O Calculation:**
  - Worst case: target last or absent.
  - Inspect  $n$  elements for  $n$ -sized list.
  - Dominant term:  $n$ , thus  $O(n)$ .
- **Significance:** Predict performance scalability.



# Growth Rates Visualized

## Growth Rates Visualized

- Interactive visual of algorithm complexity.
- Impact of input size on computational effort.
- **Example:** Graph with adjustable slider for 'n' illustrating:
  - $O(n)$ : Linear increase with slider adjustment.
  - $O(n^2)$ : Quadratic spike, inefficiency at large 'n'.
  - $O(\log n)$ : Mild rise, efficient at scale.





# Big O in the Wild

## Big O in Real-World Applications

- **Critical Role in Databases:** Optimizing sorting and searching operations.
- **Sorting Algorithms in Online Searches:** Essential for quick ranking of search results.
- **Database Management:** Enhances data retrieval for rapid querying.
- **Practical Example:** Use of  $O(\log n)$  to optimize sorting by last access date.

## Impact on Industry Scalability and Performance

- **Algorithm Efficiency:** Enhancing operations and scalability.
- **Performance Correlation:** Link between simplicity and performance.

**Practical Example:** Sorting algorithms at  $O(\log n)$  allow smooth handling of more queries, promoting scalability, and cost reduction.

# Recap Big O Essentials

## Recap: Big O Essentials

- **Definition:** Big O Notation quantifies the maximum execution time or space usage of an algorithm relative to input size, emphasizing worst-case scenarios.
- **Upper Bound:** Indicates the asymptotic upper limit, symbolizing the theoretical maximum complexity not exceeded regardless of input size. Ex: For a loop running  $n$  times, the upper bound is  $O(n)$ .
- **Analytical Value:** Helps identify potential inefficiencies, guiding optimization based on worst-case analyses.
- **Practical Relevance:** Important for boosting software performance, enhancing scalability, and efficient resource management, crucial in fields like software engineering and database management.

# Big O Mastery Review

## Big O Mastery Review

- **Identifying Big O Notation:** Recognize complexity classes for algorithm efficiency.
  - $O(n)$ : Scales with data size.
  - $O(\log n)$ : Reduces data subset progressively.
- **Understanding Efficiency:** Evaluate runtime and resource usage.
  - $O(1)$ : Constant time, peak efficiency.
  - $O(n \log n)$ : Good for sorting algorithms.
- **Applying Big O Analysis:** Tailor algorithms to data and needs.
  - Example:  $O(\log n)$  for fast queries in large databases.