



University of
Pittsburgh

Algorithms and Data Structures 2

CS 1501

Fall 2021

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Announcements

- Upcoming Deadlines
 - Homework 1: this Friday at 11:59 pm
- Recitations start(ed) this week
 - Lab 1 available on Canvas
- Assignment 1 and Homework 2 to be posted this Friday
- TAs student support hours available on the syllabus page

Previous lecture

- ADT Tree

Muddiest Points

Tree Implementation: Code Walkthrough

- Available online at:
 - <https://cs1501-2231.github.io/slides-handouts/CodeHandouts/TreeADT/Slides>
 - The slides are under the CodeHandouts/TreeADT/slides folder in the handout repository
 - <https://github.com/cs1501-2231/slides-handouts>

buildTree method

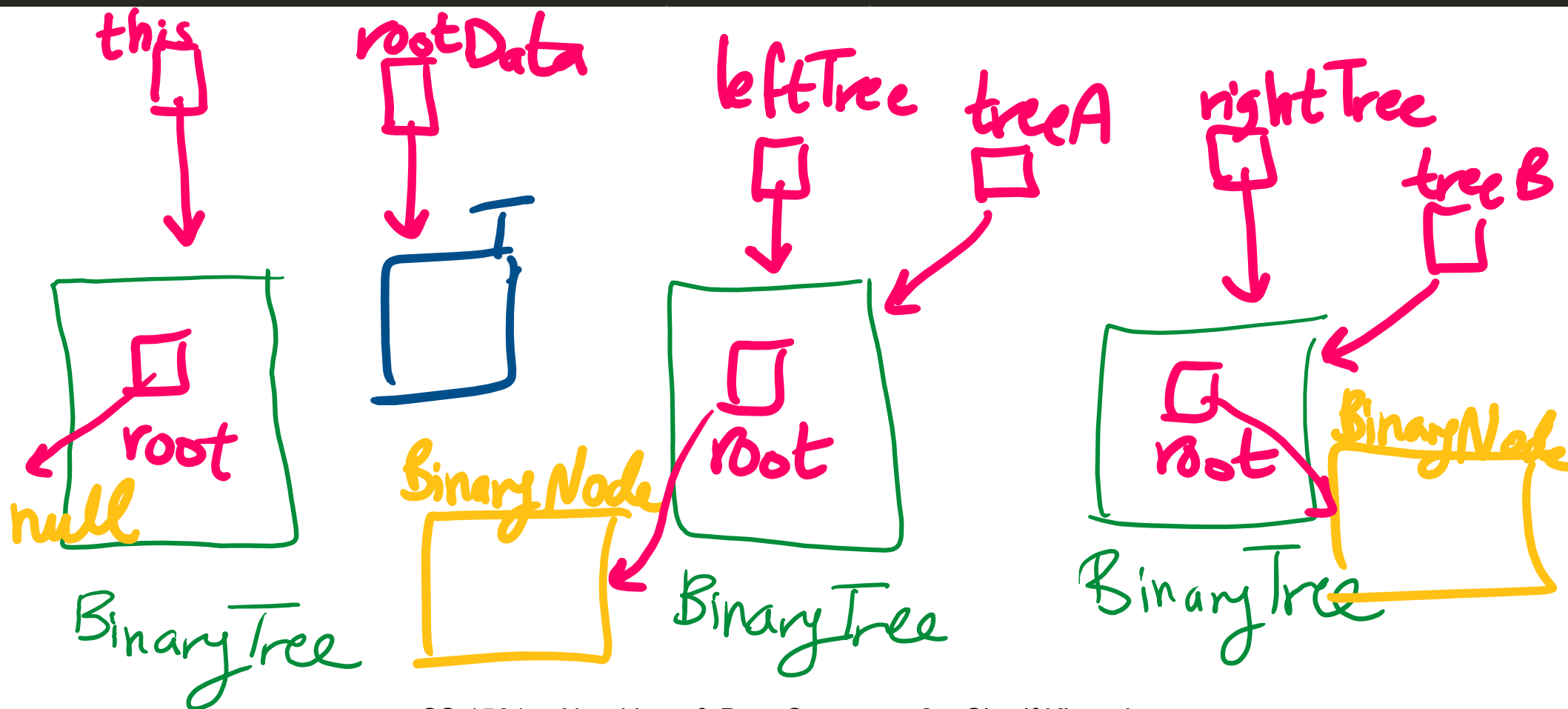
```
private void privateBuildTree(T rootData, BinaryTree<T> leftTree,  
                               BinaryTree<T> rightTree){
```

Let's draw a picture of the before state

- Given the call

```
privateBuildTree(data, treeA, treeB);
```

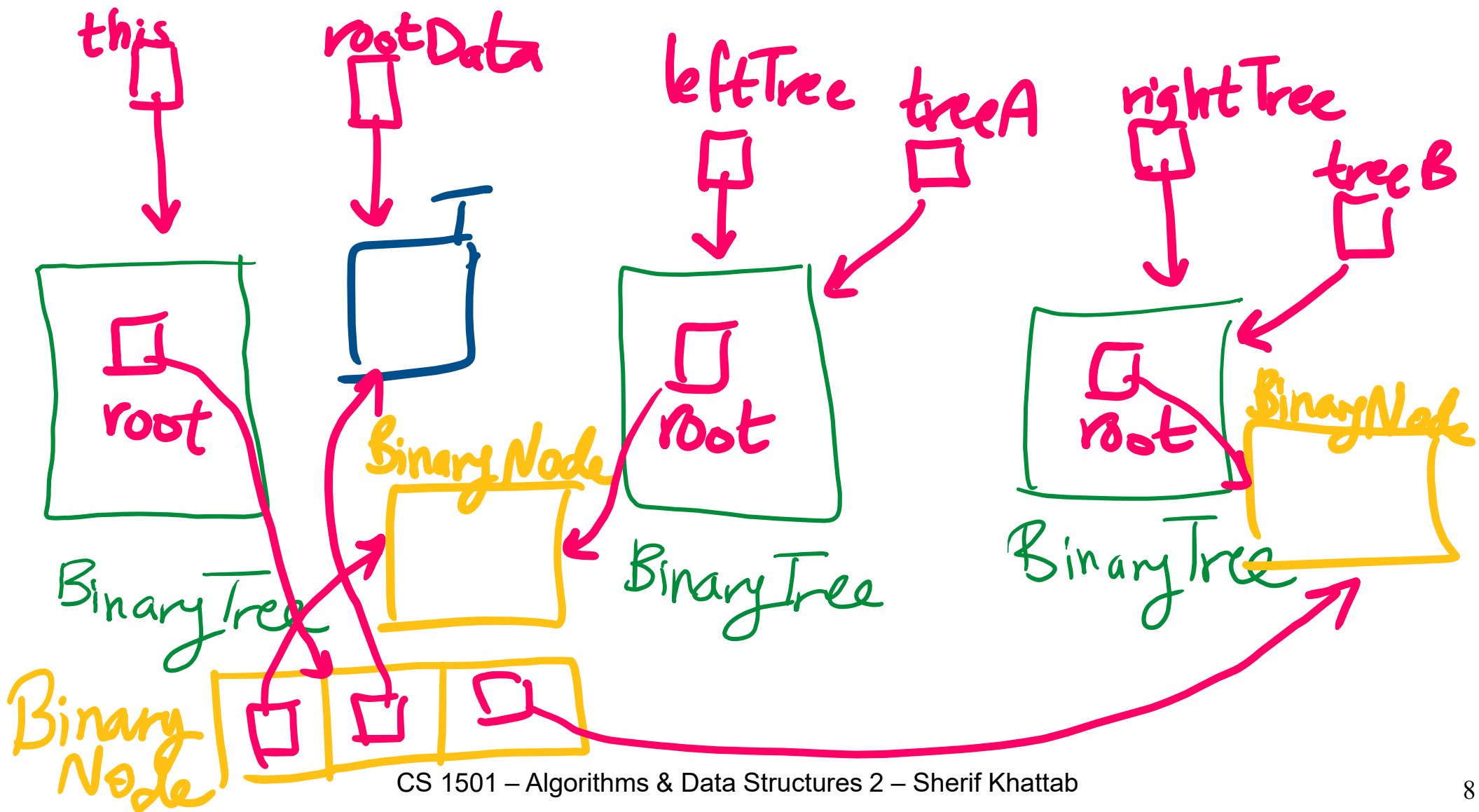
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private void privateBuildTree(T rootData, BinaryTree<T> leftTree,  
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Let's draw a picture of the after state

```
privateBuildTree(data, treeA, treeB);
```

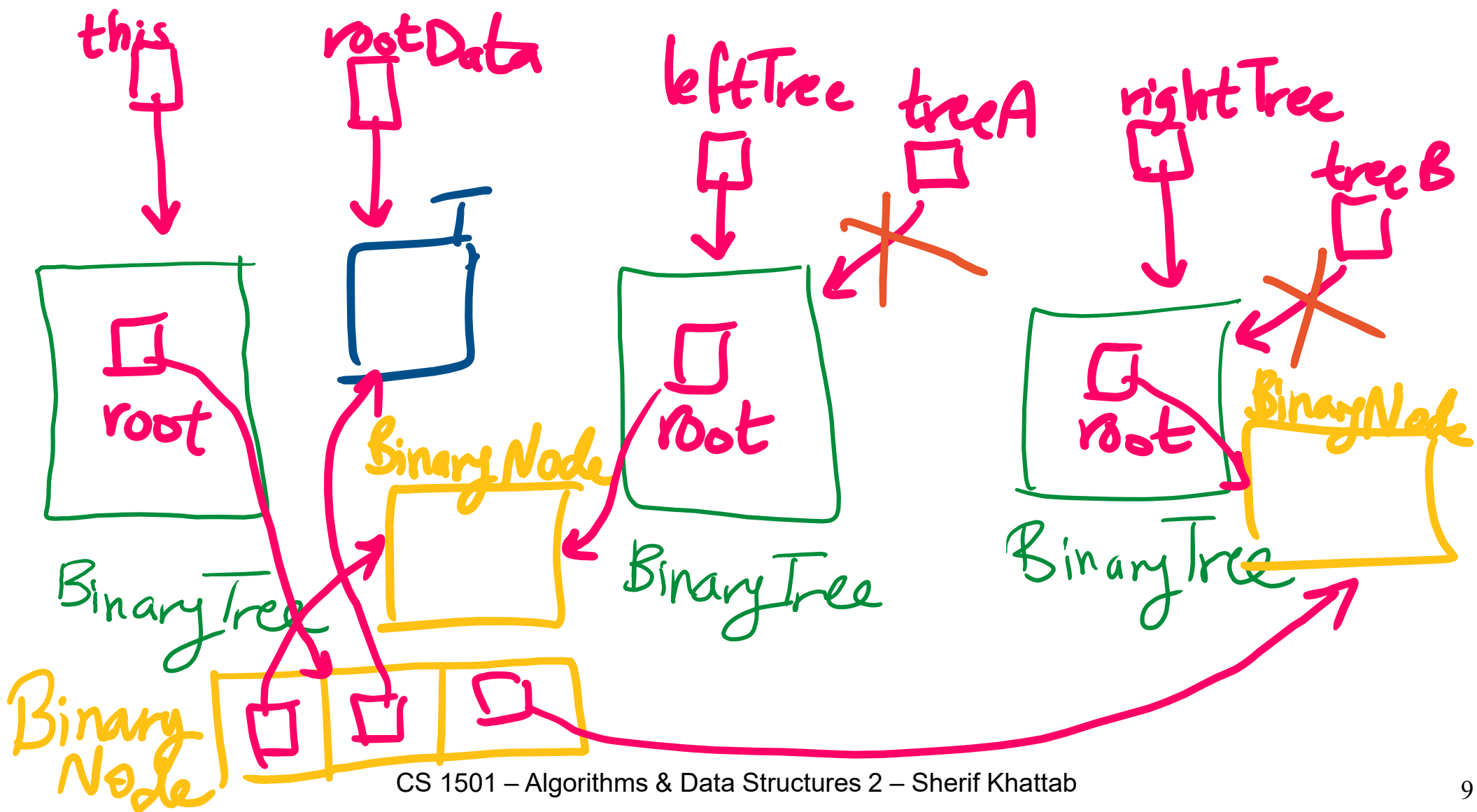
```
private void privateBuildTree(T rootData, BinaryTree<T> leftTree,  
    BinaryTree<T> rightTree){
```



Let's draw a picture of the after state

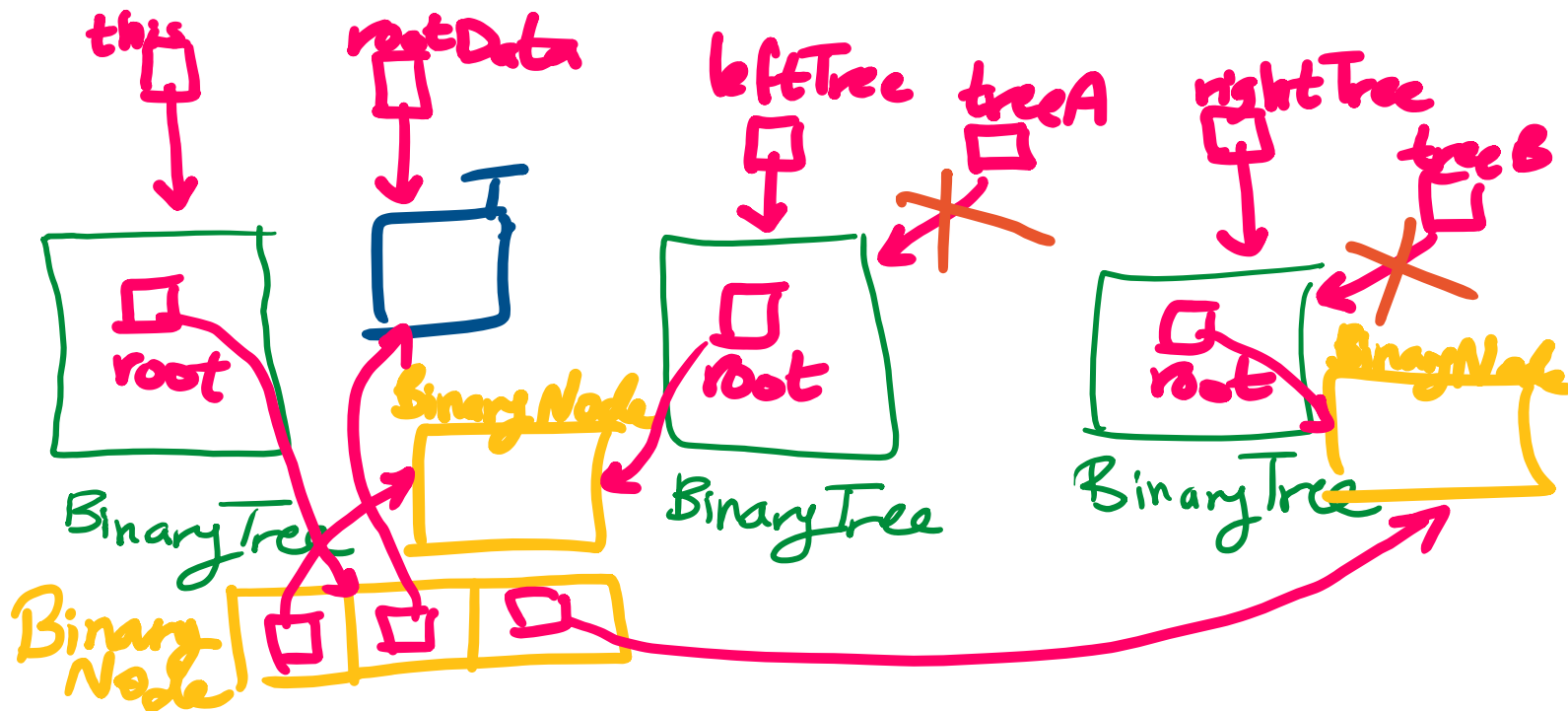
Need to also Prevent client direct access to this

treeA shouldn't have access this.root.left (same for treeB)



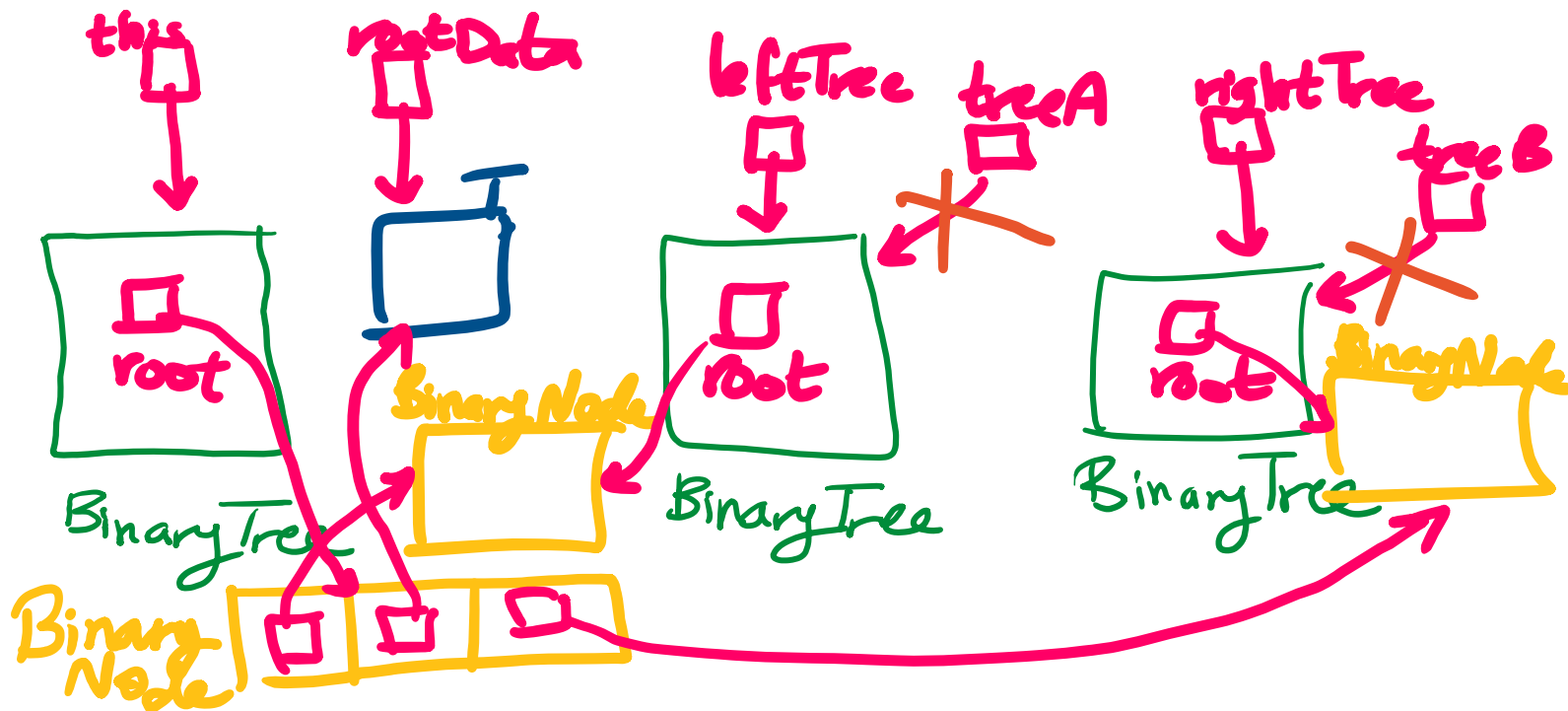
Main logic

- `root = new BinaryNode<>(rootData);`
- `root.left = leftTree.root;`
- `root.right = rightTree.root;`
- How to prevent client access?



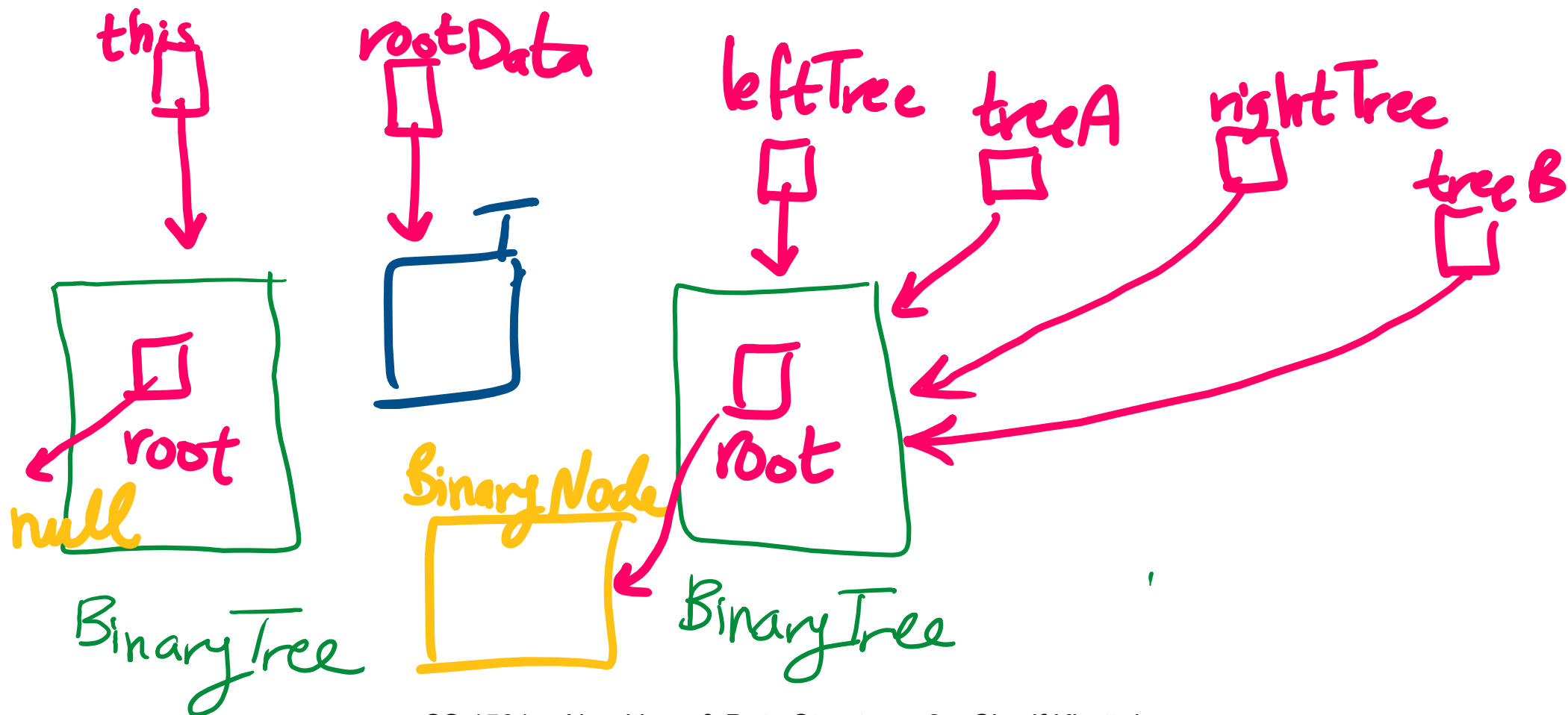
How to prevent client access?

- `treeA = treeB = null; //is that possible?`
- `leftTree = rightTree = null; //would that work?`
- `leftTree.root = null; rightTree.root = null;`



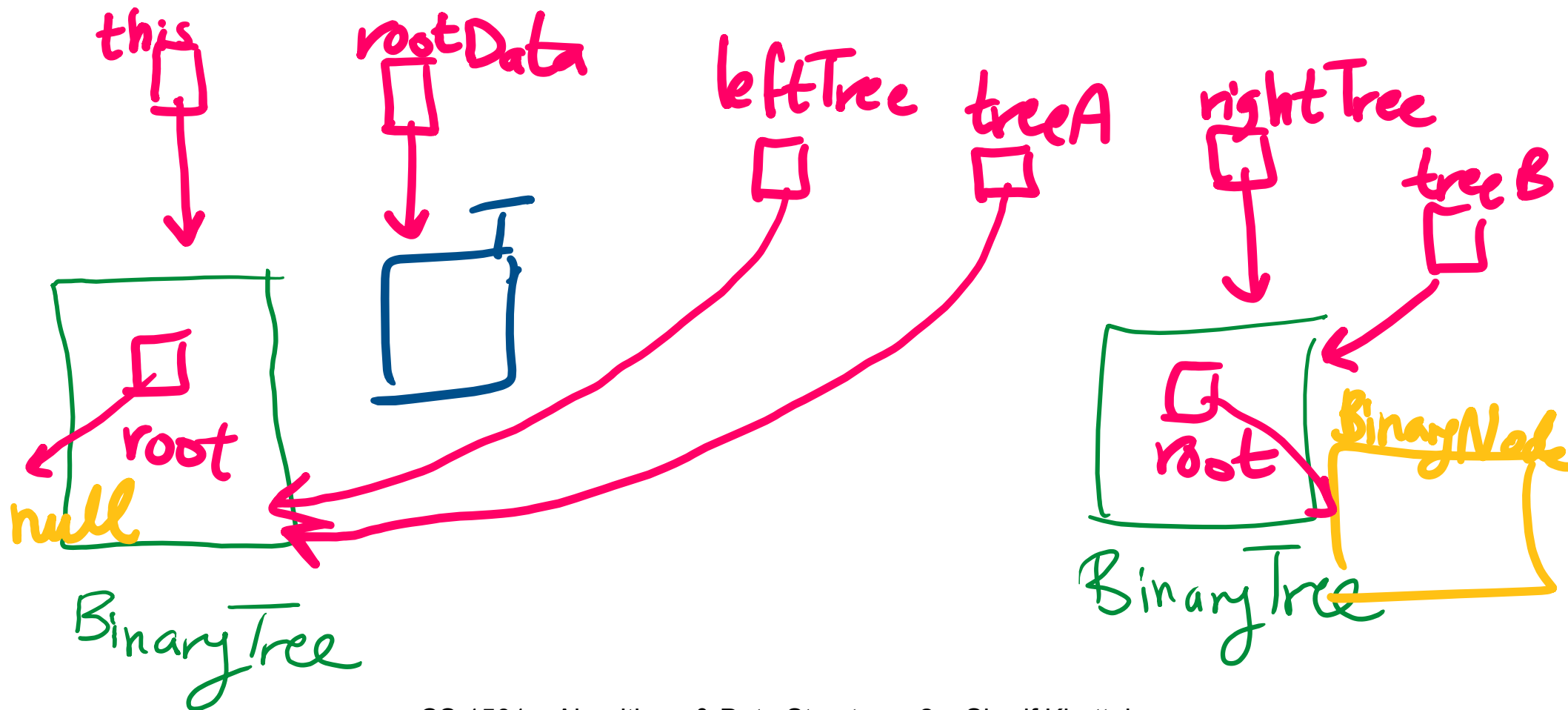
Special case: `treeA == treeB`

Need to make a copy of `leftTree.root`



Special case: treeA == this or treeB == this

Need to be careful before leftTree.root = null and rightTree.root = null



Tree Traversal Methods

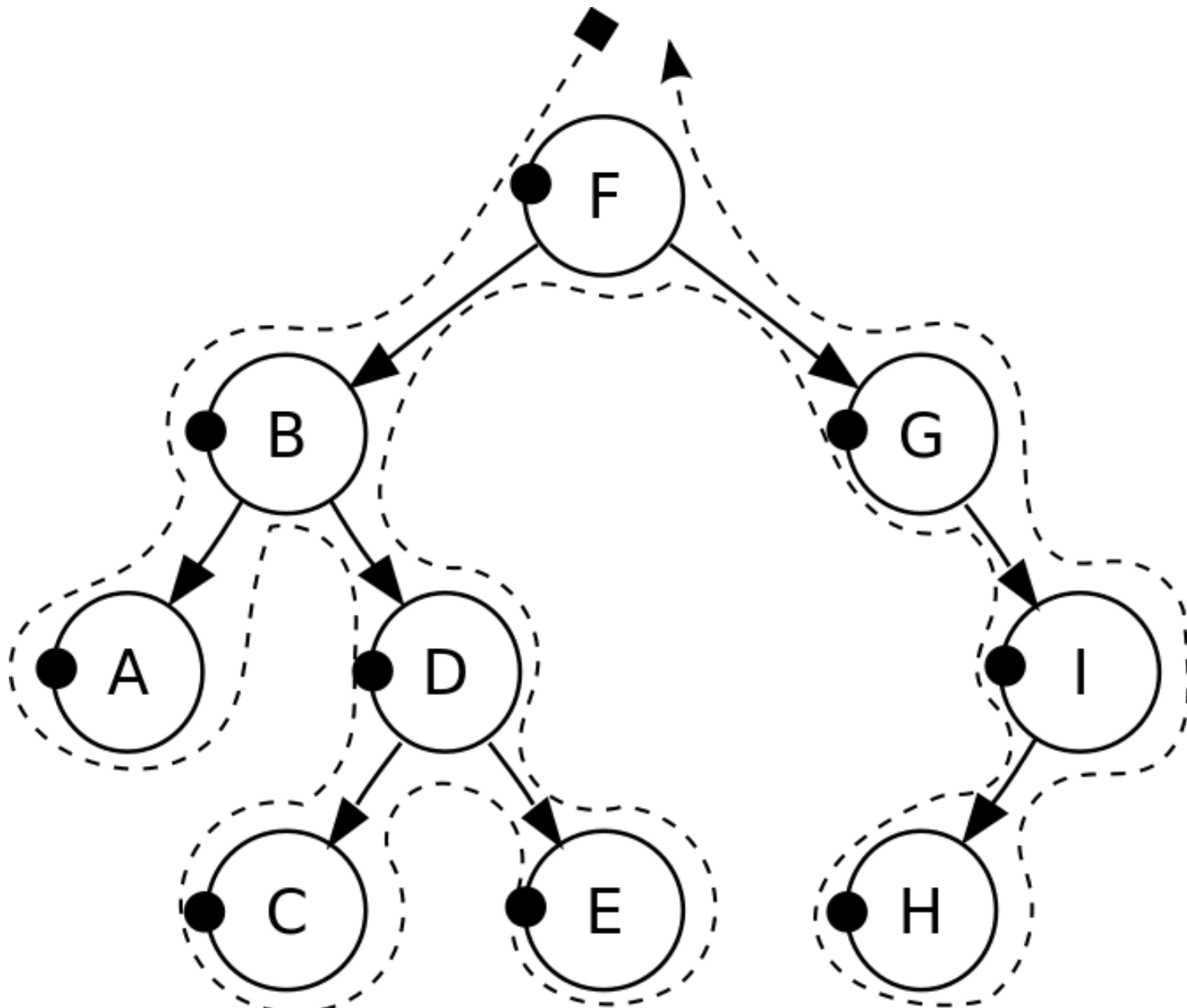
- How to traverse a Binary Tree
 - General Binary Tree
 - Pre-order, in-order, post-order, level-order

Traversals of a General Binary Tree

- Preorder traversal
 - Visit root **before** we visit root's subtree(s)

Pre-order traversal

F
B
A
D
C
E
G
I
H



Pre-order traversal implementation

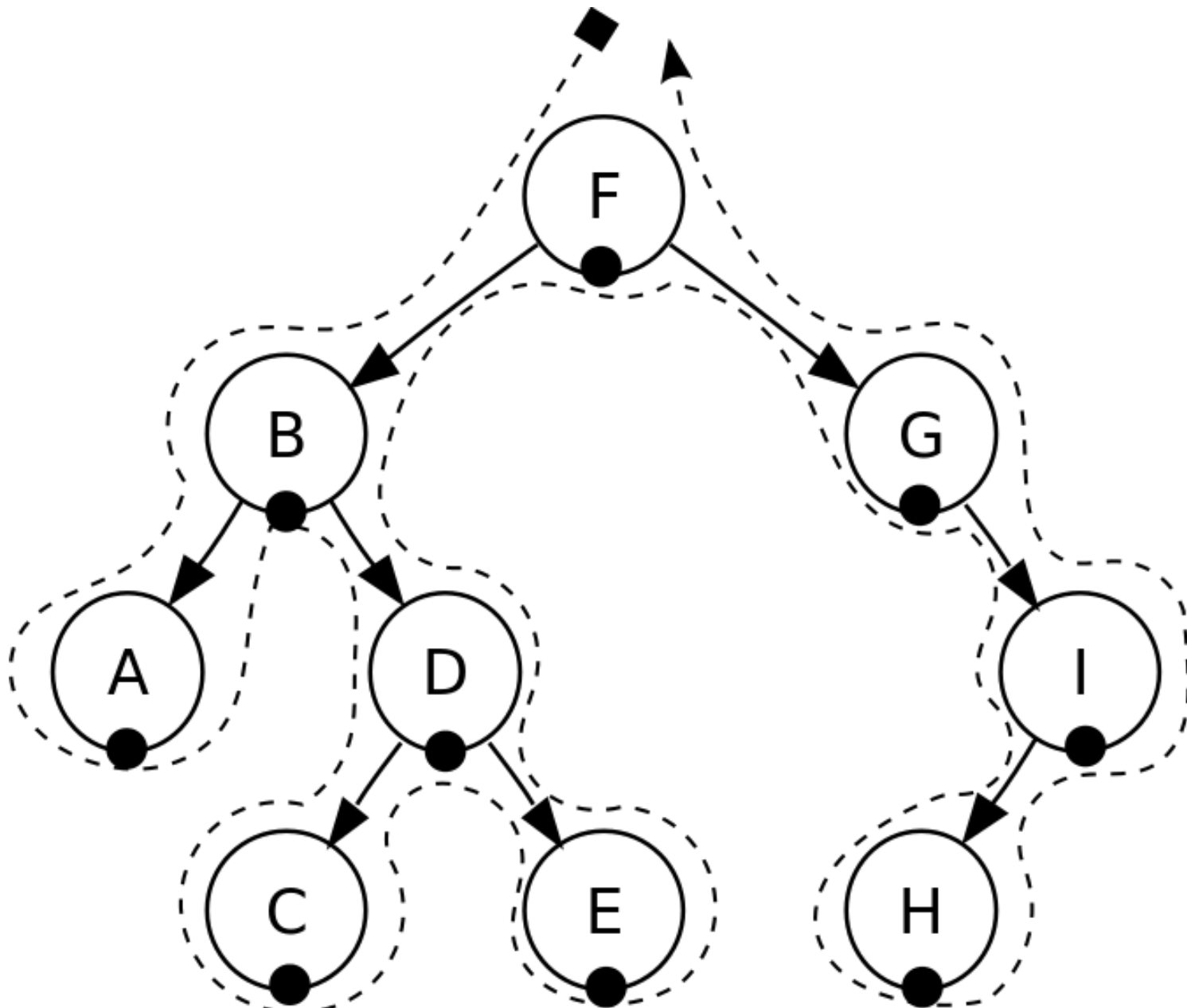
```
void traverse(BinaryNode<T> root) {  
    if (root != null) {  
        System.out.println(root.data);  
        traverse(root.left);  
        traverse(root.right);  
    }  
}
```

Traversals of a Binary Tree

- Preorder traversal
 - Visit root before we visit root's subtrees
- In-order traversal
 - Visit root of a binary tree **between** visiting nodes in root's subtrees.
 - left then root then right

In-order traversal

A
B
C
D
E
F
G
H
I



In-order traversal implementation

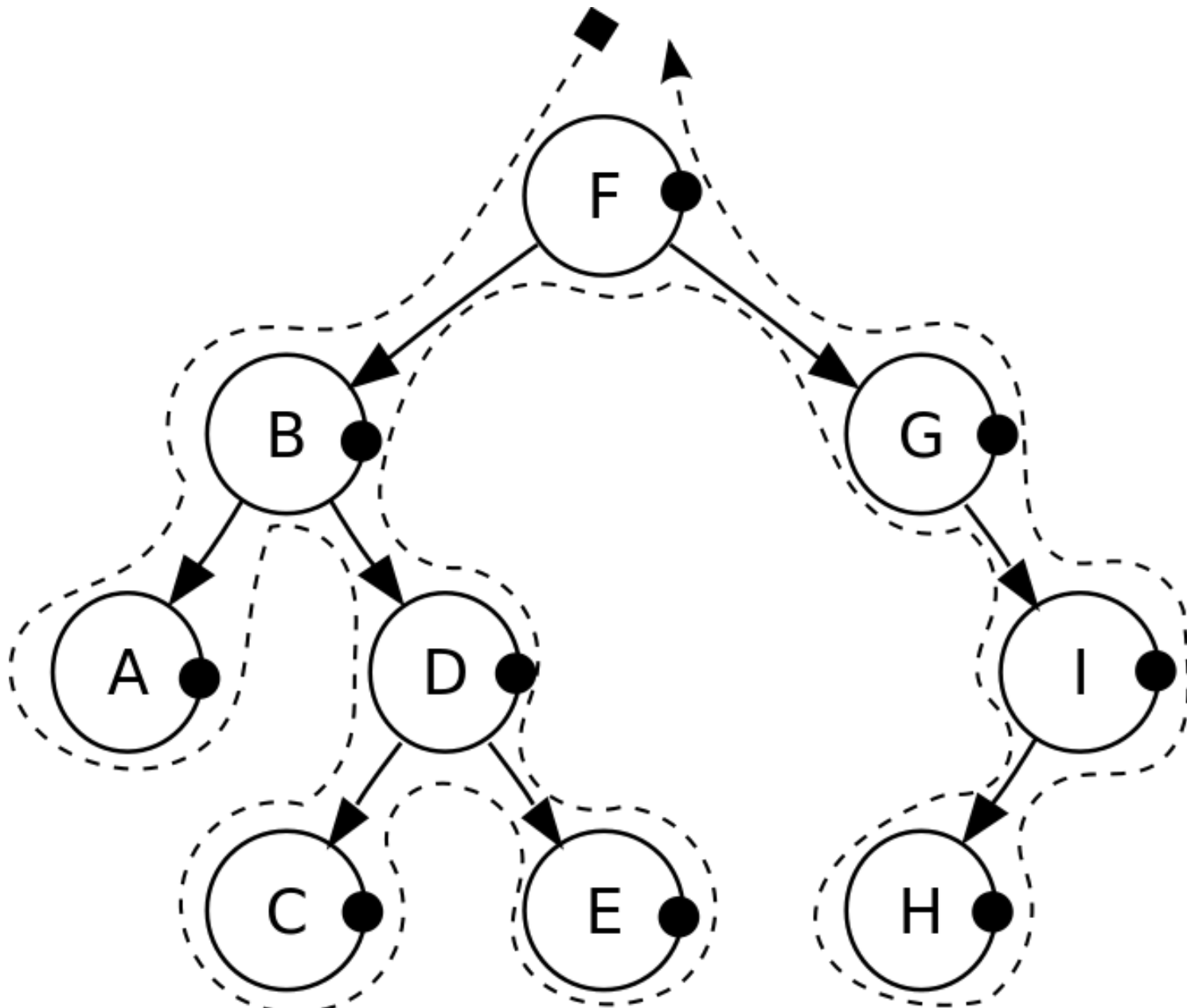
```
void traverse(BinaryNode<T> root) {  
    if (root != null) {  
        traverse(root.left);  
        System.out.println(root.data);  
        traverse(root.right);  
    }  
}
```

Traversals of a Binary Tree

- Preorder traversal
 - Visit root before we visit root's subtrees
- Inorder traversal
 - Visit root of a binary tree between visiting nodes in root's subtrees.
- Postorder traversal
 - Visit root of a binary tree after visiting nodes in root's subtrees

Post-order traversal

A
C
E
D
B
H
I
G
F



Post-order traversal implementation

```
void traverse(BinaryNode<T> root) {  
    if (root != null) {  
        traverse(root.left);  
        traverse(root.right);  
        System.out.println(root.data);  
    }  
}
```

Traversals of a Binary Tree

- Preorder traversal
 - Visit root before we visit root's subtrees
- Inorder traversal
 - Visit root of a binary tree between visiting nodes in root's subtrees.
- Postorder traversal
 - Visit root of a binary tree after visiting nodes in root's subtrees
- Level-order traversal
 - Begin at root and visit nodes one level at a time
 - We will see the implementation when we learn Breadth-First Search of Graphs

Tree Search Take 1

- *Traverse* every node of the tree
 - Is the key inside the node equal to the target *key*?
- How can we traverse the tree?

Tree Search Take 1

What is the runtime?

Can we do better?

Can we traverse the tree more intelligently?

Tree Search Take 2: Binary Search Tree

- Search Tree Property
 - $\text{left.data} < \text{root.data} < \text{right.data}$
 - Holds for each subtree
 - In Java:
 - $\text{root.data.compareTo(left.data)} > 0 \ \&\&$
 - $\text{root.data.compareTo(right.data)} < 0$