

Algorithms and Data Structures 2 CS 1501

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Announcements

- Upcoming deadlines:
 - Lab 4 due on 2/18
 - Homework 5 due on 2/21

Previous lecture ...

- Prefix Searching Problem
- Multiple solutions:
 - DST
 - RST
 - multi-way RST

CourseMIRROR Reflections (Interesting)

- I found the idea of using an optimal number of bits for digital search trees to be interesting
- prefix symbol tables were interesting
- I found the prefix searching interesting and how it works with RSTs
- All the different tree types! Very interesting
- The applications of a radix sort trie and a digital search tree were most interesting today.
- I enjoyed learning about Radix Search Tries and how different they are.
- Different types of ADTs for searching problems such as DST, RST and large branching tries. Cool to see different ways to populate trees
- adding into DSTs and RSTs
- How a digital search tree uses only the bits not the values to place nodes

CourseMIRROR Reflections (Confusing)

- I'm not sure how the code can store the bits in the path/between the nodes.
- Also, is there no key comparison when searching a RST because you just need to check if the correct bit path exists?
- why we want to determine that it is prefix problem?
 We can ignore prefix and keep using RST, DST
- Runtime comparisons of the different tree types
- the thing that was confusing was radials search tree runtimes
- I would like to go over more on the run time of Digital Search Tree operations

Prefix Searching (contd.)

Input:

- a (large) dynamic set of data items in the form of
 - n (key, value) pairs; key is a string from an alphabet of size R
 - Each key has b bits or w characters (the chars are from the alphabet)
 - What is the relationship between b and w?
- a target string

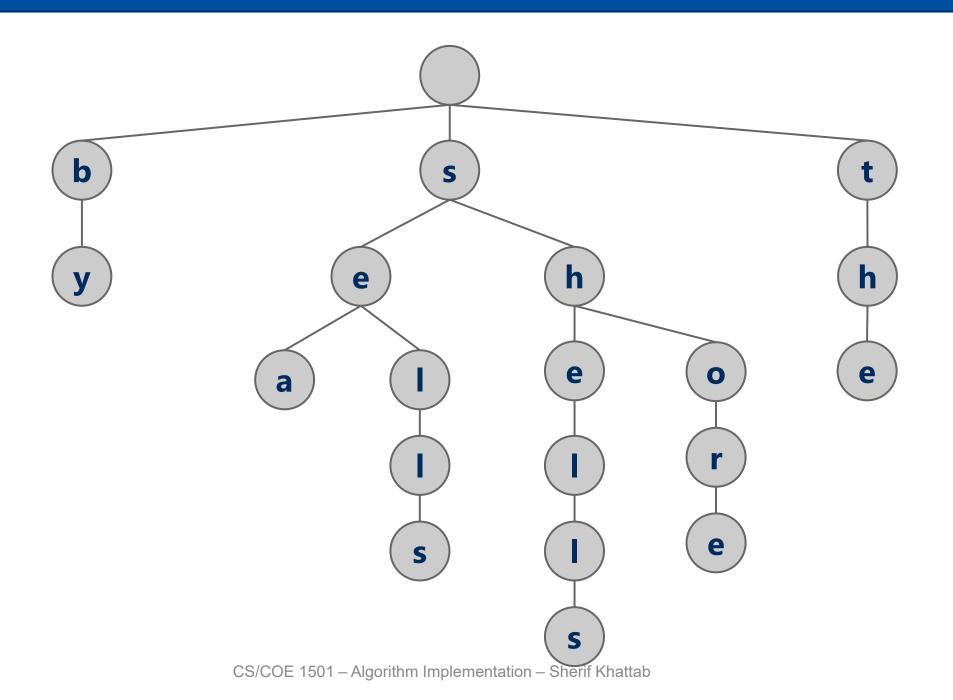
Output:

- 0: string is not a prefix of nor equal to any of the keys
- 1: string is a prefix of at least one key but not equal to any
- 2: string is not a prefix of any key but is equal to a key
- 3: string is both a prefix of at least one key and equal to one of the keys

Larger branching factor tries

- In our binary-based Radix search trie, we considered one bit at a time
- What if we applied the same method to characters in a string?
 - O What would this new structure look like?
- Let's try inserting the following strings into an trie:
 - O she, sells, sea, shells, by, the, sea, shore

Another trie example



Analysis

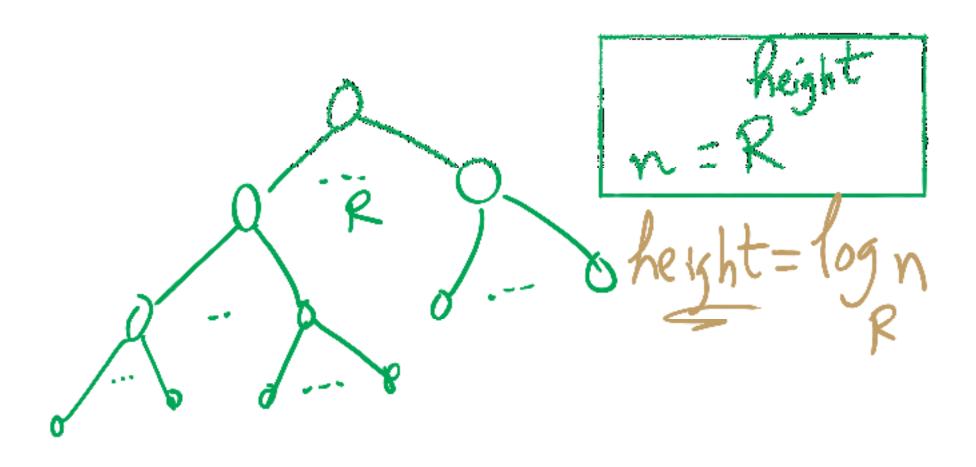
• Runtime?

Further analysis

- Miss times
 - \bigcirc Require an average of $\log_R(n)$ nodes to be examined
 - Where R is the size of the alphabet being considered
 - Proof in Proposition H of Section 5.2 of the text

- \bigcirc Average # of checks with 2^{20} keys in an RST?
- O With 2²⁰ keys in a large branching factor trie, assuming 8-bits at a time?

Search Miss



Implementation Concerns

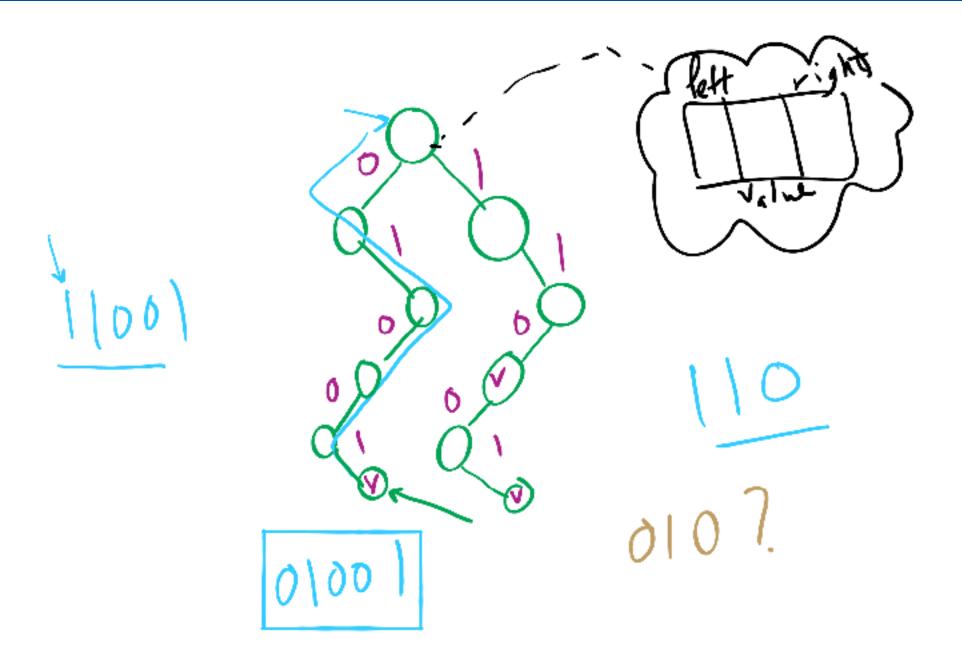
- See TrieSt.javaO Implements an R-way trie
- Basic node object:

Where R is the branching factor

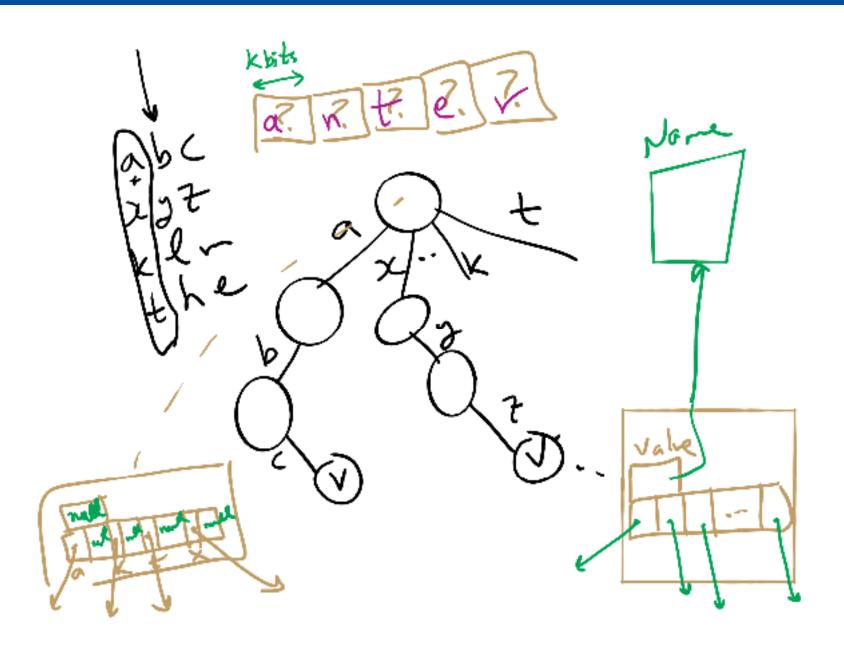
```
private static class Node {
    private Object val;
    private Node[] next = new Node[R];
}
```

- Non-null val means we have traversed to a valid key
- Again, note that keys are not directly stored in the trie at all

Binary RST



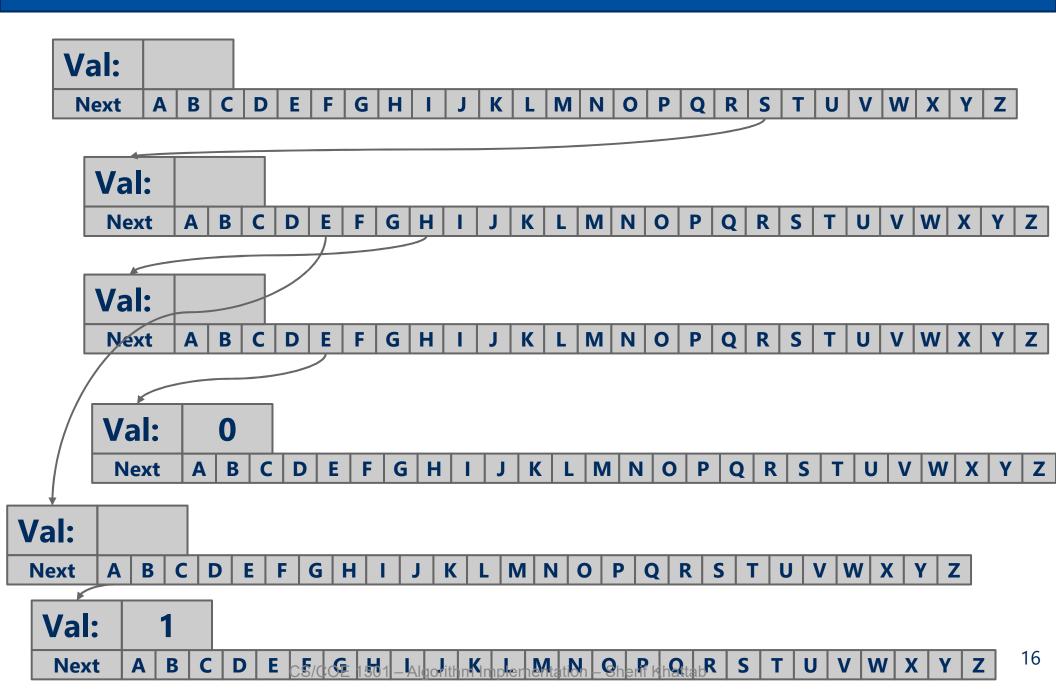
Multi-way RST



Summary of running time

	insert	Search hit	Search
binog BT	0(1)	$\theta(b)$	A (log n) average
multi-Way RST	(w)	(w)	Search muss O(log n) overage O(log n)

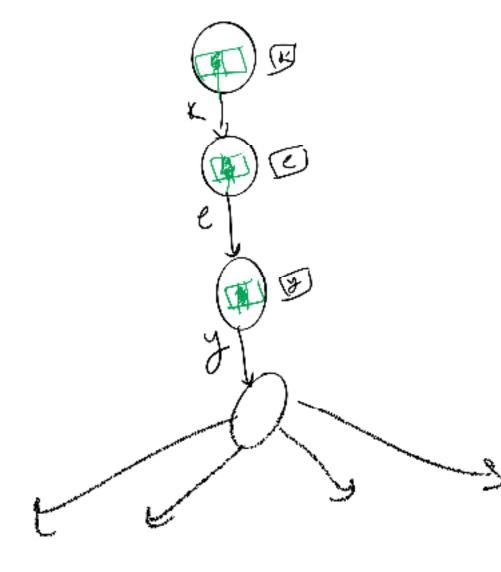
R-way trie example



So what's the catch?

Space!

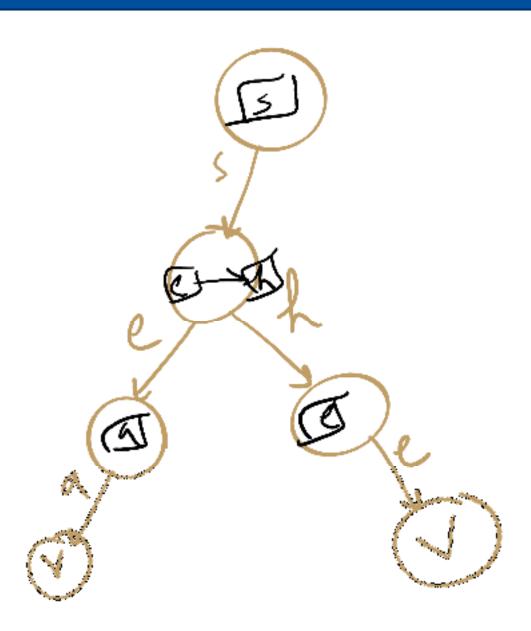
- Considering 8-bit ASCII, each node contains 28 references!
- O This is especially problematic as in many cases, alot of this space is wasted
 - Common paths or prefixes for example, e.g., if all keys begin with "key", thats 255*3 wasted references!
 - At the lower levels of the trie, most keys have probably been separated out and reference lists will be sparse



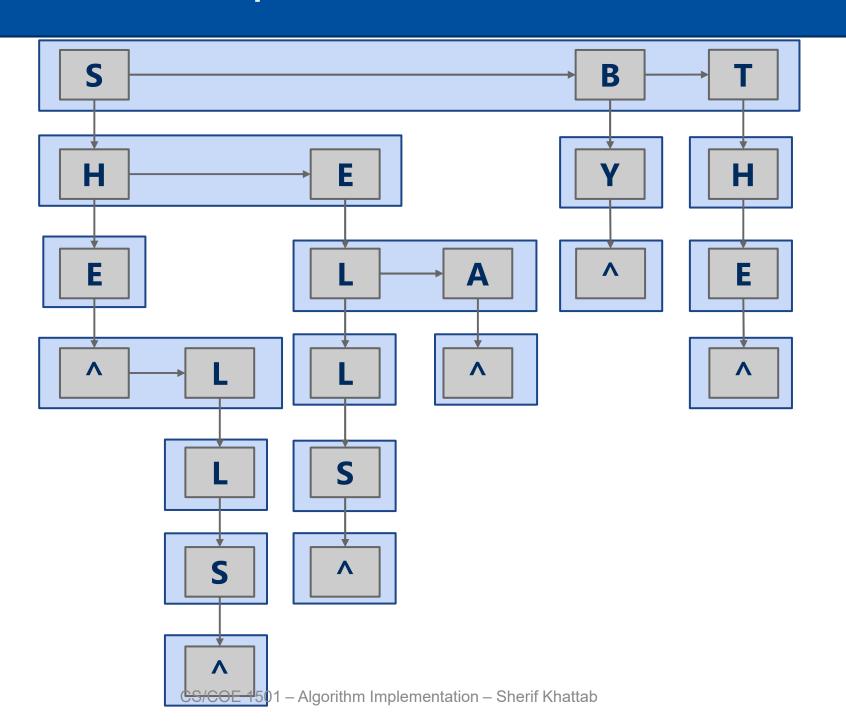
De La Briandais tries (DLBs)

Replace the .next array of the R-way trie with a linked-list

DLB Example

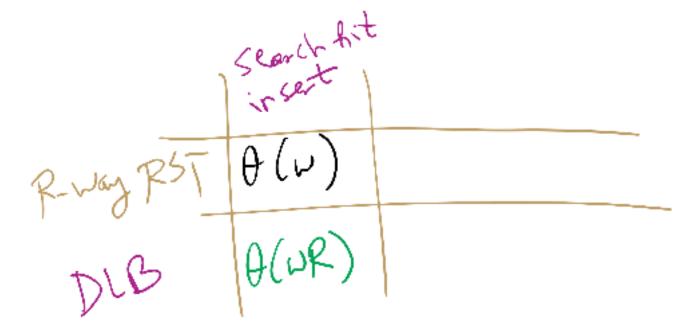


DLB Example 2: nodes vs. nodelets

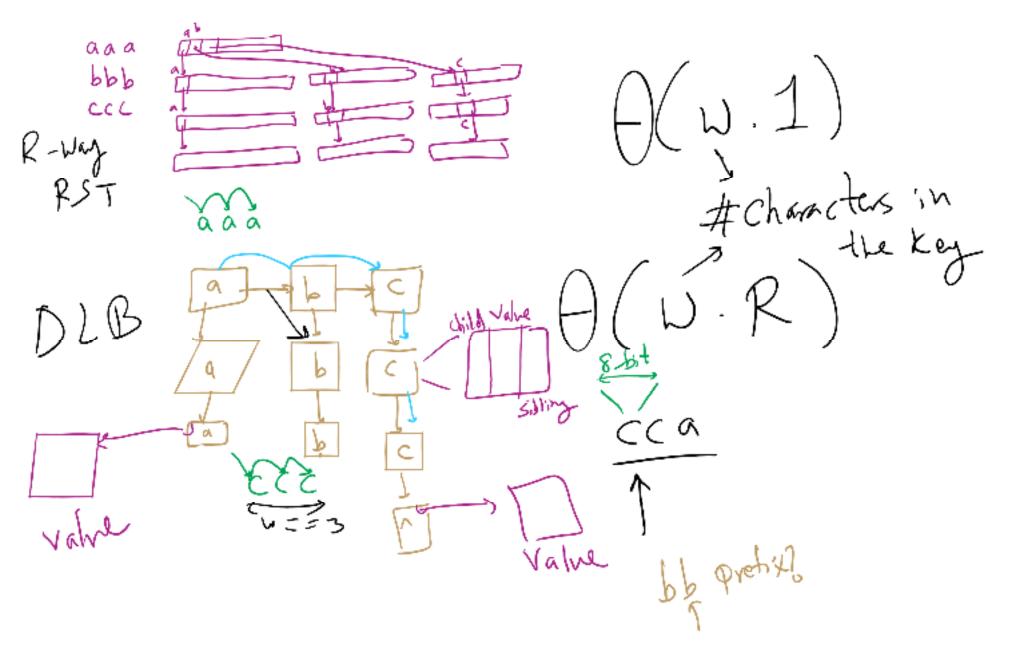


DLB analysis

- How does DLB performance differ from R-way tries?
- Which should you use?



R-way RST vs. DLB



Let's go back to our Prefix Symbol Table an ADT!

- The Prefix Symbol Table ADT
 - A set of (key, value) pairs
- Operations of the PST ADT
 - insert
 - delete
 - prefixSearch
 - search
- How can we implement prefixSearch?

Runtime Comparison for Search Trees/Tries

	Search ti:t	Search voiss (avery)	insert
BST	0(n)	(logn)	Ð(n)
RB-BST	Allogn)	Allos.	O(logn)
DST	(b)	Allogn)	D(b)
RST	$\theta(b)$	A(logn)	f()
R-may RST	(ACM)	D((69m)	(W)
DLB	(JCWR)	O(logn. P)	H(W.R)

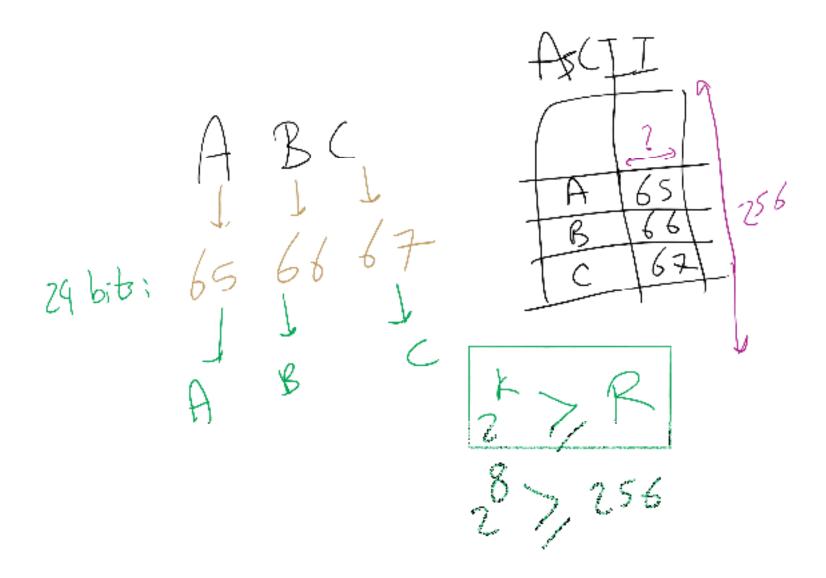
Final notes on Search Tree/Tries

- We did not present an exhaustive look at search trees/tries, just the sampling that we're going to focus on
- Many variations on these techniques exist and perform quite well in different circumstances
 - Ternary search Tries
 - R-way tries without 1-way branching
- See the table at the end of Section 5.2 of the text

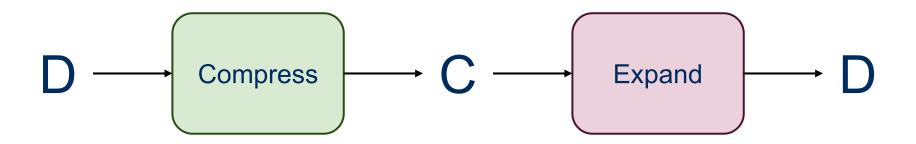
Problem of the Day: Compression

- Input: A sequence of characters
 - *n* characters
 - each encoded as an 8-bit Extended ASCII
- Output: A bit string
 - of length less than 8*n
 - the original sequence can be fully restored from the bitstring

ASCII Encoding

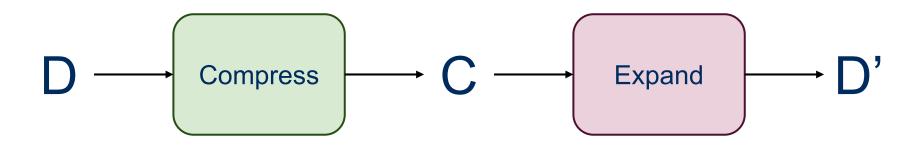


Lossless Compression



- Input can be recovered from compressed data exactly
- Examples:
 - zip files, FLAC

Lossy Compression



- Information is permanently lost in the compression process
- Examples:
 - MP3, H264, JPEG
- With audio/video files this typically isn't a huge problem as human users might not be able to perceive the difference

Lossy examples

MP3

 "Cuts out" portions of audio that are considered beyond what most people are capable of hearing

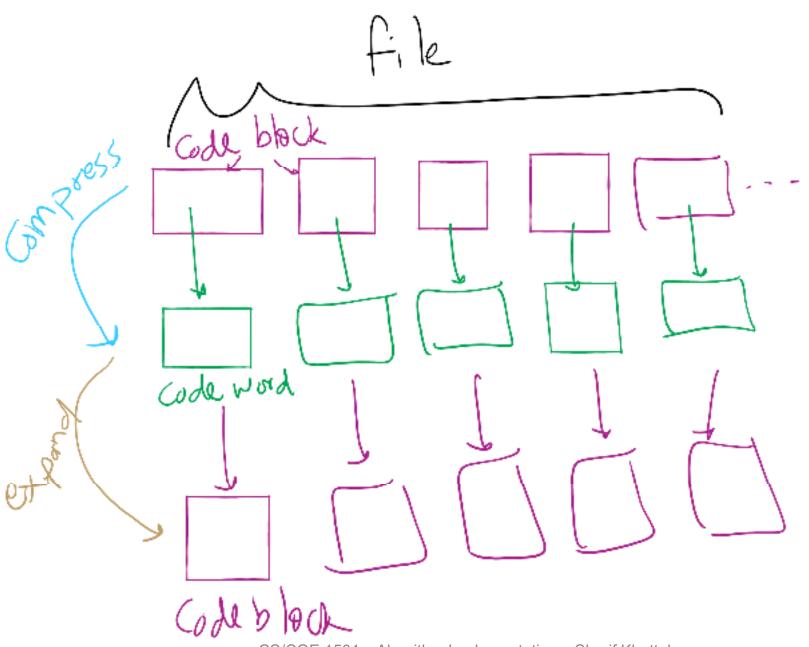
JPEG





40K 28K

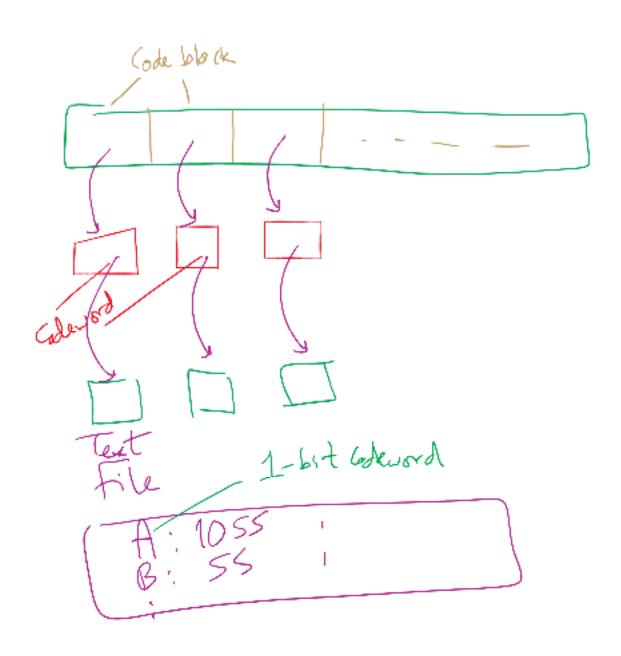
Lossless Compression Framework



Solution 1: Huffman Compression

- What if we used *variable length* codewords instead of the constant 8? Could we store the same info in less space?
 - Different characters are represented using codes of different bit lengths
 - If all characters in the alphabet have the same usage frequency, we can't beat block storage
 - On a character by character basis...
 - What about different usage frequencies between characters?
 - In English, R, S, T, L, N, E are used much more than Q or X

Variable size codewords



But we have to worry about restoring the data!

- Decoding was easy for block codes
 - Grab the next 8 bits in the bitstring
 - How can we decode a bitstring that is made of variable length code words?
 - BAD example of variable length encoding:

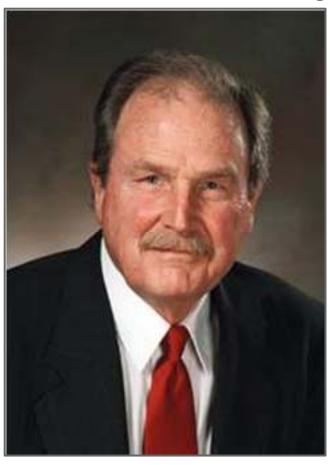
1	Α
00	Т
01	K
001	U
100	R
101	С
10101	Ν

Variable length encoding for lossless compression

- Codes must be prefix free
 - No code can be a prefix of any other in the scheme
 - Using this, we can achieve compression by:
 - Using fewer bits to represent more common characters
 - Using longer codes to represent less common characters

How can we create these prefix-free codes?

Huffman encoding!



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