

Optimization-Based Coordination of Large-Scale Multi-Agent AI Systems: A Technical Survey and Research Roadmap

Executive Summary

This report provides a comprehensive technical survey and research gap analysis for the optimization-based coordination of the ATLAS/TURING multi-agent AI research system. The coordination of 40+ specialized agents presents a multi-faceted optimization challenge, spanning static assignment, dynamic scheduling, resource allocation, architecture discovery, and system robustness.

The analysis indicates that the field is at a critical inflection point, moving from manually-designed, static coordination workflows (e.g., simple agent chains) to *dynamically optimized, self-evolving, and robust agentic architectures*. The state-of-the-art (SOTA) in 2024-2025 is defined by (1) the application of classical Operations Research (OR) techniques (e.g., Quadratic Assignment, Bandits-with-Knapsacks) in novel, *contextual*, and *learned* settings; (2) the emergence of powerful evolutionary frameworks (EvoFlow, EvoAgentX) and Neural Architecture Search (NAS) analogues (MASS) that *auto-discover* workflow topologies; and (3) a new, urgent focus on robustness, addressed via adversarial testing (DeepTeam, AgentSafety) and min-max optimization (RobustFlow).

The primary recommendation is to architect the ATLAS/TURING system as a *hybrid* of these approaches:

1. **For Task Assignment:** Utilize **Market-Based Mechanisms (Combinatorial Auctions)** for decentralized, scalable assignment, falling back on **ML-hybridized QAP metaheuristics** (e.g., learned cost functions) for centralized, synergy-critical subproblems.
2. **For Workflow Routing:** Employ a **stateful, cyclical graph framework** (i.e., LangGraph) to manage the core "dialectical chains" (Designer \rightarrow Critic \rightarrow Refactorer). This loop should be formally modeled as a **Stochastic Shortest Path problem**, with Reinforcement Learning (RL)

used to learn the optimal "stop/continue" policy.

3. **For Resource Allocation:** Implement **Hierarchical Contextual Bandits with Knapsacks (HBwK)**, using Thompson Sampling to manage exploration/exploitation at both the *agent-group* and *individual-agent* levels.
4. **For Performance Evolution:** Use a **Population-Based Training (PBT)** scheduler (from Ray Tune) to continuously optimize agent hyperparameters (prompts, model configs), using an **Elo rating system** (fed by Validator scores) as the fitness function.
5. **For Architecture Optimization:** Build a custom auto-discovery layer based on SOTA frameworks like **EvoFlow** and **MASS** to *evolve* the coordination graphs themselves, using *constrained evolutionary operators* to ensure system safety and validity.
6. **For Robustness:** Establish a "Red Team" subsystem using frameworks like **DeepTeam** to continuously generate adversarial tests. These tests will serve as the *inner loop* of a **bi-level min-max optimization** process to proactively design failure-resistant workflows.

This report is structured in three parts. Part 1 is a technical survey of the methods. Part 2 analyzes the tools and frameworks for implementation. Part 3 details seven novel, high-impact research contributions, providing a concrete publication roadmap.

Part 1: A Technical Survey of Multi-Agent Coordination and Optimization

Section 1: Agent-Task Assignment Optimization

The problem of assigning N agents to M tasks is a foundational challenge in combinatorial optimization (CO). In its most sophisticated form, the Quadratic Assignment Problem (QAP), the objective is to minimize a cost function that accounts for both the linear cost of assigning an agent to a task and the quadratic, interdependent costs that arise from synergies or conflicts between pairs of agents assigned to pairs of tasks.

1.1 Classical QAP: Exact, Metaheuristic, and Learned Approaches

The QAP was formally introduced in 1957 by Koopmans and Beckmann in the context of

facility location.¹ It is NP-hard and widely regarded as one of the most difficult CO problems to solve in practice.² Given n facilities (agents) and n locations (tasks), along with two $n \times n$ matrices F (flow, e.g., required information transfer between agents) and D (distance, e.g., communication cost or dissimilarity between tasks), the objective is to find a permutation ϕ of $\{1, \dots, n\}$ that minimizes the total cost²:

$$\min_{\phi \in \Phi_n} \sum_{i=1}^n \sum_{j=1}^n F_{i,j} D_{\phi(i), \phi(j)}$$

Exact Methods:

Exact algorithms, such as branch-and-bound and cutting-plane methods, aim to find the provably optimal solution. However, their computational complexity makes them unusable for large-scale problems. The largest, non-trivial instances from the benchmark QAPLIB (a standard collection of QAP instances⁴) that have been solved to optimality are only around $n=36$.² For a system of $N=40+$ agents, these methods are computationally infeasible for real-time (or even offline) assignment.

Metaheuristics:

For practical purposes, heuristic and metaheuristic algorithms are the standard approach for large-scale QAPs. They sacrifice provable optimality for the ability to find high-quality solutions in a feasible amount of time.³

- **Algorithms:** The most widely applied metaheuristics for QAP include Tabu Search (TS), Simulated Annealing (SA), and Genetic Algorithms (GA).³ Comparative studies often find that TS, in particular, demonstrates very good performance across a range of QAP instances.⁶
- **Implementations:** The QAPSolver C++ library provides accessible implementations of these heuristics, allowing for rapid prototyping (e.g., `model.TS(initial, 50, 7, 10)`).⁴
- **Performance:** The performance bottleneck for large instances remains significant. 2021 research highlights the necessity of using massively parallel implementations (e.g., on GPUs) to reduce execution time.⁵ This performance drive continues, with 2025 research exploring novel local search heuristics specifically designed for in-memory computing (IMC) hardware, which can compute full neighborhoods simultaneously to accelerate the search.¹

State-of-the-Art Solvers (2024):

A search for "QAP solvers" reveals a critical distinction. The most active and well-benchmarked Python ecosystem is `qpsolvers`⁷ and its associated benchmark suite, `qpbenchmark`.⁸ This ecosystem provides a unified Python wrapper for a wide array of high-performance QP solvers, including Clarabel, OSQP, PIQP, ProxQP, Gurobi, and MOSEK.⁸ However, these are solvers for *general* Quadratic Programming (QP), which includes a broad class of problems. QAP is a specific, highly-structured *integer* QP with permutation constraints. General-purpose QP solvers are not typically optimized for this specific structure and are often intended for continuous or less-constrained convex problems.

The true SOTA for large-scale QAP falls into two categories:

1. **Commercial Solvers:** Commercial Mixed-Integer Programming (MIP) solvers like Gurobi and CPLEX have exceptionally powerful branch-and-cut algorithms that can be applied to the QAP (typically by linearizing the quadratic objective).¹⁰
2. **Specialized Metaheuristics:** As discussed, highly-tuned parallel implementations of TS, SA, or GAs.⁵
3. **Machine Learning for CO (ML4CO):** A new SOTA direction involves using deep learning, particularly Graph Neural Networks (GNNs), to *learn* heuristics that solve CO problems. The awesome-ml4co repository lists several key papers (ICML 2023, AAAI 2024) where models learn to solve routing and assignment problems.¹¹ This hybrid approach is a highly promising avenue for the ATLAS system.

1.2 Extensions for Dynamic and Contextual AI Contexts

The primary limitation of classical QAP is its static nature. The F and D matrices are assumed to be fixed and known in advance.² In the ATLAS system, this assumption is invalid. The "flow" (synergy) between a Designer and a Critic and the "cost" (e.g., predicted time) of assigning the Critic to a task are *dynamic*. They depend on:

- **System State:** Current load, queue length, agent availability.
- **Agent Confidence:** The Designer's confidence in its last artifact.
- **Historical Performance:** The track record of this specific agent pairing.

This defines a **Contextual QAP**, a significant research gap. While the 2024 literature is replete with "context-aware" multi-agent systems¹² and dynamic agent orchestration¹⁵, the formal optimization problem of "Online Contextual QAP" is not well-established.

The SOTA literature (2024-2025) suggests that for highly dynamic LLM-based agent systems, the assignment problem is not being solved as a single, large-scale, global QAP. Instead, it is being *reframed* as a sequential, dynamic routing or task decomposition problem.

- The **TDAG framework** (2024) focuses on *dynamic* task decomposition and sub-agent generation, emphasizing "adaptability and context awareness".¹⁶ This implies the set of tasks M is itself not static.
- Recent agent architectures (2024) feature components like a "Delegator" that "is responsible for assigning tasks to the appropriate agents or tools" based on the current context and graph state.¹⁸
- This approach transforms the single, intractable global QAP into a series of smaller, local, and context-dependent assignment decisions, which are more tractable and adaptive.

1.3 Auction and Market Mechanisms

As a scalable, decentralized alternative to a centralized QAP solver, Auction-Based Task Allocation (ATA) is a highly effective mechanism.¹⁹ In this model, the 40+ agents act as self-interested actors that *bid* for tasks.

- **Combinatorial Auctions:** This is the most relevant formulation for the ATLAS system. It allows agents to place bids on *bundles* of tasks.²¹ For example, an agent might bid: "I will do Literature_Review (Task 1) and Hypothesis_Generation (Task 2) for a combined cost of \$\$, which is less than the sum of their individual costs." This bidding language directly captures the *synergies* that the QAP models via its quadratic term.
- **State-of-the-Art (2024):** This is a very active field.
 - A 2023 paper proposes an architecture that *unifies* market-inspired combinatorial auctions with Behavior Trees for task execution, specifically designed to handle multi-stage, dynamic tasks.²¹
 - A 2024 survey paper from IJCAI²² explores "Intelligent Agents for Auction-based Federated Learning (IA-AFL)." This serves as a strong analogue, where "data owners" (agents) bid to participate in "FL tasks" (research tasks). This work highlights the role of intelligent agents in supporting the stakeholders (bidders, sellers, auctioneer) in their decision-making.²²
 - ATA is also heavily used in multi-robot and UAV swarm coordination (2024), where distributed, auction-based algorithms are essential for dynamic environments with limited communication.¹⁹

For a system with 40+ agents, a centralized QAP optimizer represents a single point of failure and a severe scalability bottleneck. An auction mechanism is far more robust and scalable. Furthermore, it addresses the *incentive problem*. By designing an incentive-compatible mechanism (e.g., a Vickrey-Clarke-Groves auction), the system can encourage agents to report their *true* costs and capabilities, which is a major challenge for a central QAP solver that must *estimate* all costs.

1.4 Multi-Objective Assignment

The ATLAS system must optimize for multiple, conflicting objectives: maximizing research quality, minimizing completion time, and minimizing resource cost (e.g., GPU usage, API credits).²³

- **Pareto Optimality:** The goal is not a single "best" solution, but the set of all *Pareto-optimal* solutions—the **Pareto frontier**. A solution is Pareto-optimal if no single

objective can be improved without degrading at least one other objective.²³

- **Methods:**
 1. **Multi-Objective Reinforcement Learning (MORL):** This is the SOTA *learning* approach. MORL algorithms are designed to learn a set of optimal policies (a "Pareto set") simultaneously, rather than a single one.²⁵ This allows the system to dynamically adapt to different user preferences (e.g., "fastest" vs. "highest quality") without retraining.²⁵ However, MORL can suffer from low efficiency in finding *dense* Pareto solutions.²⁶
 2. **Multi-Objective Evolutionary Algorithms (MOEAs):** Evolutionary methods like NSGA-II are highly effective at discovering Pareto fronts in complex, multi-modal search spaces.²⁷ This approach is central to frameworks like EvoFlow (see Section 4.1).
 3. **Weighted Sum:** The simplest method, where objectives are scalarized with weights (e.g., $\text{TotalCost} = w_1 * \text{speed} + w_2 * (1 - \text{quality}) + w_3 * \text{compute}$). This is a common technique used in reinforcement learning reward functions.²³
- **Constraint Handling:** Hard constraints (e.g., "The Validator agent *must* be included in the workflow") are handled differently. In classical OR solvers (CPLEX, Gurobi, OR-Tools)¹⁰, these are added as linear constraints to the model. In MOEAs or MORL, they are handled via constrained optimization techniques, such as penalty functions or "safe" operators that ensure solutions remain in the feasible space.

Table 1.1: Comparison of Agent-Task Assignment Approaches

Method	Scalability (Max N)	Optimality	Dynamics	Architecture	SOTA Implementation (2024/2025)	Key Limitation
Exact QAP Solver	Low ($N \approx 36$) ²	Exact	Static	Centralized	Gurobi, CPLEX ¹⁰	Intractable for 40+ agents.
QAP Metaheuristic	Medium-High	Approximate	Static	Centralized	QAPSolver (C++) ⁴ , OR-Tools ²⁸	Assumes static, known cost

						matrices.
ML-Lear ned Heuristic	High	Approxim ate	Static	Centraliz ed	ML4CO ¹¹	Learns to solve a <i>static</i> problem; doesn't handle dynamic contexts.
Context ual MAB	Very High	Approxim ate	Dynamic	Decentral ized	LinUCB ²⁹	Ignores quadratic <i>synergy</i> costs; only linear assignme nt.
Combina torial Auction	Very High	Approxim ate	Dynamic	Decentral ized	IA-AFL frameworks ²²	Winner determin ation is NP-hard, but good heuristics exist.

Section 2: Workflow Routing and DAG Scheduling

This problem moves from *who* does *what* (assignment) to *when* they do it (sequencing). The core challenge in the ATLAS system is that its workflows are not static. The "dialectical chain" (Designer \rightarrow Critic \rightarrow Refactorer \rightarrow Validator) is a dynamic, quality-dependent, and potentially *cyclical* graph, not a simple Directed Acyclic Graph (DAG).

2.1 DAG Scheduling Fundamentals

Workflows are conventionally modeled as DAGs, where nodes are tasks (agents) and edges represent precedence constraints.³⁰

- **Classical Methods:** These serve as essential baselines for any static sub-problems.
 - **Critical Path Method (CPM)/PERT:** Identifies the longest path (the "critical path") through the DAG, which defines the minimum possible project completion time (makespan).
 - **List Scheduling:** A family of effective heuristics. A "ready list" of tasks whose dependencies are met is maintained. An algorithm then repeatedly selects a task from this list based on a priority rule (e.g., shortest processing time, critical path priority) and assigns it to an available resource.
- **Relevance:** These methods are necessary for any *known, static* portions of a research plan (e.g., "Run Literature Scout, *then* in parallel run 3 Hypothesis Generators, *then* aggregate"). They are, however, insufficient for adaptive logic.

2.2 Adaptive and Confidence-Aware Routing

The "dialectical chain" presents a far more complex problem. The decision to route an artifact *back* to the Refactorer (creating a cycle) or *forward* to the Validator is not pre-defined; it is a *dynamic, probabilistic* decision based on an intermediate quality/confidence score.

This is a central topic in 2024/2025 agentic AI research, which is moving beyond static chains to dynamic routing.

- **STRMAC (State-Aware Routing Framework) (Nov 2025):** This SOTA framework proposes a lightweight router that adaptively selects the *single most suitable agent* at each step.³³ It explicitly encodes the "interaction history" (the current state) and "agent knowledge" (expertise) as separate embeddings.³³ The router, trained via contrastive learning, then matches the current state embedding to the best agent embedding (e.g., via cosine similarity) to make the routing decision.³⁶ This provides a formal mechanism for dynamic agent selection.
- **SelfOrg (Oct 2025):** This framework takes an even more dynamic approach, *constructing the DAG on the fly*.³² Agents independently generate responses to a query. A graph is then dynamically constructed based on each agent's "Shapley value" (a game-theoretic measure of contribution), ensuring that information flows from high-contributing agents to others.³² This is ideal for "swarming" on a complex problem.
- **GATES (May 2025):** This method³¹ uses **Graph Attention Networks (GATs)** combined with an **Evolution Strategy** for *cost-aware dynamic workflow scheduling*. This is a full-blown ML-based scheduler that *learns* the optimal scheduling policy for dynamic,

DAG-based tasks.³¹

- **RL for Routing (Mar 2025):** This work³⁸ proposes a more direct RL approach. It uses an RL agent to *dynamically tune the weighting factors* of an adaptive routing algorithm (based on Dijkstra's). The weights are a function of context like task complexity, priority, and agent load.³⁸

Stochastic Scheduling: The underlying theoretical field is stochastic scheduling, which deals with uncertainty in task durations or outcomes. For example, Stochastic Job Shop Scheduling (SJSSP) models processing times as random variables.⁴⁰ The ATLAS system's "confidence-aware" routing is a form of stochastic scheduling where the *graph structure itself* is stochastic.

2.3 AI Pipeline Orchestration Tools

A critical implementation decision is selecting the right tool to execute these workflows. The main contenders are traditional task orchestrators and newer agent-specific frameworks.

- **Traditional Orchestrators:**
 - **Airflow:** The enterprise incumbent. It is fundamentally *static*.⁴¹ While DAGs are defined in Python, they are not dynamically modified at runtime. It is operationally complex, requiring multiple services.⁴² It is *not* suitable for implementing dynamic, confidence-based loops.⁴¹
 - **Prefect / Dagster:** Modern, Python-native alternatives.⁴³ Their key advantage is support for *dynamic dataflows*.⁴¹ Prefect, for example, allows simple Python functions to be "flows" and excels at dynamic event management and reacting to changing data states.⁴¹
- Architectural Synthesis (Orchestrator vs. Agent Framework):

A common architectural mistake is to misuse these tools. An orchestrator like Airflow or Prefect is designed to schedule tasks, which are typically long-running, reliable, and have static dependencies. An agent framework like LangGraph is designed to schedule LLM-based actors, whose interactions are fast, cyclical, stateful, and dynamic.⁴⁵ The optimal architecture for ATLAS/TURING is therefore *hierarchical*:

 1. **Level 1 (Task Orchestrator):** Use **Prefect** (or Dagster)⁴³ to manage the high-level, mostly linear research plan (e.g., Task A: Run Project_Alpha, Task B: Run Project_Beta).
 2. **Level 2 (Agent Framework):** Task A internally invokes a workflow built with **LangGraph**.⁴⁵ This LangGraph workflow manages the complex, cyclical, confidence-based logic of the Designer \rightarrow Critic \rightarrow Refactorer loop.

This design uses the right tool for the right job, leveraging Prefect's dynamic task management ⁴³ and LangGraph's explicit support for stateful, cyclical graphs.⁴⁵

2.4 Research Gap: Optimizing the Dialectical Chain

While SOTA (2025) frameworks like STRMAC ³³ and SelfOrg ³² provide powerful mechanisms for *dynamic agent routing* (i.e., "who goes next?"), a critical gap remains. There is no formal work on optimizing the *convergence* of a "dialectical chain" (Designer \rightarrow Critic \rightarrow Refactorer).

The problem is not just "who is next?" but "when do we stop?". The rise of "multi-agent validation" ⁴⁶, "critic" agents ⁴⁸, and "dialectical reasoning" frameworks ⁴⁹ confirms this is a nascent, ad-hoc field. Agentic coding systems like ChatDev ⁵² implement this loop, but the decision to stop or continue is based on simple heuristics (e.g., "run for k cycles" or "stop when Critic score > 0.9"). This can lead to infinite refinement loops ⁴⁶ or, conversely, premature stopping that yields a suboptimal result. This is a prime research opportunity, which will be detailed in Section 7.2.

Table 2.1: Orchestration Tools vs. Adaptive DAG Scheduling Requirements

Tool	Primary Use Case	Graph Type	State Management	Confidence-Based Routing	Recommended ATLAS Use
Airflow	Batch Task Orchestration	Static DAG ⁴¹	Via Task Instances	No (Must be custom-built)	Not Recommended (Too rigid).
Prefect	Dynamic Task Orchestration	Dynamic Python Flows ⁴¹	First-class object ⁴¹	Yes (via Python logic)	Level 1 (Task Orchestrator): Triggering

					high-level research plans.
LangGraph	Agent Orchestration	Stateful, Cyclical Graph ⁴⁵	Explicit State Object ⁴⁵	Native Support (via conditional edges)	Level 2 (Agent Framework): Implementing the dialectical D-C-R loops.
AutoGen	Agent Orchestration	Conversational (Emergent) ⁵⁴	Message History ⁵⁴	Yes (via agent logic)	Alternative to LangGraph, but less structured and harder to optimize.
STRMAC	Agent Routing	Dynamic (Single-step) ³³	Encoded State Vector ³⁶	Yes (This is its purpose)	Research Baseline: A SOTA method to compare against for routing.

Section 3: Resource Allocation and Meta-Learning

This section addresses the problem of distributing finite computational resources (e.g., CPU, GPU, API credits) among the 40+ competing agents. This is an exploration-exploitation problem: should resources go to a "proven" high-performing Designer agent (exploitation), or to a new, experimental Refactorer agent to see if it's better (exploration)?

3.1 Multi-Armed Bandit (MAB) Algorithms

The canonical model for the exploration-exploitation dilemma is the Multi-Armed Bandit (MAB).⁵⁶ Each of the K agents is an "arm." Pulling an arm (assigning a task) yields a stochastic "reward" (e.g., a quality score from the Validator). The goal is to maximize the cumulative reward over a time horizon T .

- **Algorithms:**
 - **Upper Confidence Bound (UCB):** An "optimism in the face of uncertainty" algorithm. It computes a high-confidence upper bound for each arm's true mean reward and pulls the arm with the highest UCB.²⁹
 - **Thompson Sampling (TS):** A Bayesian approach. It maintains a *probability distribution* (a "belief") over each arm's reward (e.g., a Beta distribution for binary rewards, Gaussian for continuous). At each step, it samples one value from each arm's distribution and pulls the arm with the highest sample.⁵⁶ Empirically, TS often demonstrates lower regret (better performance) than UCB.⁵⁶
- **Contextual and Non-Stationary Bandits:** The simple MAB model is insufficient for the ATLAS system.
 1. **Non-Stationary MABs (NSMAB):** Agent performance is not static; it will change (e.g., after a prompt update). This is a non-stationary environment.⁵⁷ NSMAB algorithms (like Sliding-Window UCB or Discounted Thompson Sampling) are required, as they give more weight to recent data.
 2. **Contextual Bandits:** The reward of an agent (arm) depends on the *context* (e.g., task type, difficulty, associated artifacts). At each step t , a context vector x_t is observed.²⁹ Algorithms like LinUCB and Contextual Thompson Sampling²⁹ learn a function that maps contexts to rewards, allowing for generalized, intelligent decisions.

Recent SOTA (2023-2025) applications of MABs align perfectly with this, including dynamic RAG (where each retrieval method is an arm)⁵⁸, LLM-informed MABs for non-stationary environments⁵⁹, and secure VM allocation.⁶⁰

3.2 Constrained Resource Allocation: Bandits with Knapsacks (BwK)

This is the precise formulation required for the ATLAS system. In the **Bandits with Knapsacks (BwK)** problem, pulling an arm (running an agent) yields not only a reward (quality) but also incurs a cost (e.g., API credits, GPU-seconds). The agent must maximize cumulative reward *without exceeding a total budget* (the knapsack).⁶¹

This is a highly active research area in 2024–2025:

- **SOTA Algorithm:** A key 2025 paper⁶¹ proposes **LinCBwK9TS**, a new **Thompson Sampling** algorithm for **Linear Contextual Bandits with Knapsacks (CBwK)**. This work is motivated by the superior empirical performance of TS over UCB-based methods and provides a strong theoretical regret bound.⁶¹ This algorithm is a perfect SOTA baseline for the ATLAS resource allocator.
- **Delayed Feedback:** The DORAL algorithm (2024)⁶³ specifically addresses the BwK problem where the reward feedback is *delayed*—which is highly relevant for research tasks that may take hours or days to validate.
- **Dynamic Constraints:** A 2025 paper⁶⁴ introduces "Budgeted UCB," an algorithm for environments where the *constraints themselves are dynamic* (e.g., a "decaying violation budget").

The current research frontier (2025) in this area is moving toward handling complex real-world scenarios like delayed feedback⁶³ and *bi-level* allocation (e.g., allocating budgets to *groups* of agents, then individuals)⁶⁶, which leads directly to the novel contribution in Section 7.3.

3.3 Meta-Learning for Algorithm Selection

The ATLAS system will not just *use* optimization; it *is* an optimizer. At different times, it may need to solve a QAP, a scheduling problem, or a resource allocation problem. **Meta-Learning**, or "learning to learn"⁶⁷, is a framework for selecting the *best* optimization algorithm for the *specific problem instance* at hand.

A 2024 survey⁶⁸ formally defines this field as **Meta-Black-Box-Optimization (MetaBBO)**. MetaBBO uses a meta-level learner (which can be an RL agent, a supervised model, or even an LLM) to automate algorithm design tasks, including:

1. **Algorithm Selection:** Choosing from a portfolio of solvers (e.g., "This QAP is small, use Gurobi; this one is large, use Tabu Search").⁶⁸
2. **Algorithm Configuration:** Setting the hyperparameters of a chosen solver (e.g., "For this problem, set the TS tabu list size to 20").⁶⁸
3. **Algorithm Generation:** The most advanced form, where the meta-learner *generates* a new, bespoke heuristic algorithm.⁶⁸

SOTA (2024) work uses RL agents to *dynamically* control the parameters of evolutionary algorithms during their run.⁷² The introduction of the MetaBox benchmark⁷³ in 2024 for MetaBBO-RL indicates this field is rapidly maturing. For ATLAS, a MetaBBO layer could learn a high-level policy for selecting its own coordination strategies.

3.4 Agent Tournaments and Performance Tracking

To optimize the 40+ agents over time, the system needs a mechanism to (1) evolve their configurations (prompts, models) and (2) measure their performance.

- **Population-Based Training (PBT):** This is a SOTA hyperparameter optimization (HPO) technique that is far more efficient than grid search.⁷⁴ PBT trains an entire *population* of agents (e.g., 20 versions of Designer) in parallel.⁷⁵ Periodically, it "exploits" by copying the weights and hyperparameters from the top-performing agents to the bottom-performing ones, and then "explores" by perturbing (mutating) those new hyperparameters.⁷⁶ The Ray Tune library has a mature, scalable PBT implementation.⁷⁶ Generalized PBT (GPBT) (2024)⁷⁸ is a recent extension.
- **Elo Rating System:** PBT requires a *fitness function* to identify the "top performers." For complex research outputs, a simple accuracy metric is insufficient. The SOTA solution for ranking models on open-ended tasks is the **Elo rating system**.⁷⁹ This system, famously used by Chatbot Arena⁸¹, turns pairwise comparisons ("Is output A better than output B?") into a cardinal numeric score.⁸³

Architectural Synthesis (PBT + Elo = Continual Improvement):

These two concepts can be combined to create a fully autonomous, continual improvement engine for the ATLAS agent population.

1. **Population:** The 40+ agents are managed as a population within Ray Tune's PBT scheduler.⁷⁶
2. **"Battles":** As agents produce artifacts, the Validator and Critic agents are tasked with performing pairwise comparisons (e.g., Designer_v1.2's output vs. Designer_v1.3's output for the same task).
3. **Leaderboard:** These pairwise "votes" are continuously fed into an internal **Elo rating system**⁸⁰, maintaining a real-time leaderboard of all agent versions.
4. **Evolution:** At each PBT "exploit" step, the scheduler queries this Elo leaderboard to identify the "top performers," thus closing the loop.

This creates a robust, asynchronous, and continuous process for evolving and optimizing all agents in the system based on their demonstrated performance.

Section 4: Evolutionary Architecture Search and Auto-Discovery

This section addresses the most advanced coordination problem: moving from

hand-designing the 40-agent workflow to enabling the system to *automatically discover* superior coordination patterns. This treats the workflow architecture itself as a "genome" that can be optimized.

4.1 Evolutionary Workflow Optimization

This is the bleeding-edge SOTA (2025) in agent coordination. Instead of optimizing a *fixed* graph, these frameworks evolve the *graph structure itself*.

- **EvoFlow (Feb 2025):**
 - **Concept:** This framework⁸⁴ uses a niching-based evolutionary algorithm to optimize a *population* of diverse, heterogeneous agentic workflows *on the fly*.⁸⁴
 - **Multi-Objective:** It frames the search as a multi-objective problem: *cost* vs. *performance*.⁸⁴ The output is not one "best" workflow, but a *Pareto-optimal set* (e.g., a cheap, fast workflow for simple tasks and an expensive, complex workflow for hard tasks).⁸⁵
 - **Genome and Operators:** The workflow is the genome. Evolutionary operators are applied, including **LLM Mutation** (swap the model), **Prompt Mutation**, and **Operator Mutation** (change the agent/tool).⁸⁴ Selection is "tag-based" (finds relevant parents for crossover) and "niching-based" (maintains population diversity).⁸⁴
 - **Implementation:** github.com/bingreeky/EvoFlow.⁸⁴
- **EvoAgentX (July-Nov 2025):**
 - **Concept:** This is an open-source *platform* and *integrator* that automates multi-agent workflow generation from high-level goals.⁸⁶
 - **Integrated Optimizers:** Its primary contribution is its "evolving layer," which integrates several SOTA optimization algorithms⁸⁶ to iteratively refine prompts, tools, and topologies:
 1. **TextGrad** (2024)⁸⁶: For prompt optimization.
 2. **AFlow** (2024)⁸⁶: For workflow graph optimization.
 3. **MIPRO** (2024)⁸⁶: For prompt optimization.
 - **Performance:** The framework demonstrates significant performance gains on SOTA benchmarks like GAIA, MATH, and HotPotQA.⁸⁸
 - **Implementation:** github.com/EvoAgentX/EvoAgentX.⁸⁷
- **EvoAgent (NAACL 2025):**
 - **Concept:** A related framework⁹⁴ that proposes a generic method using evolutionary algorithms (mutation, crossover, selection) to *automatically extend* a specialized single-agent system into a more capable *multi-agent system*.⁹⁴ This is a powerful

"bootstrapping" mechanism.

4.2 Neural Architecture Search (NAS) for Agent Topologies

This approach adapts principles from Neural Architecture Search (NAS)—the field of auto-discovering optimal neural network architectures—to the problem of discovering optimal *agent network topologies*.

- **MASS (Multi-Agent System Search) (Feb 2025):**
 - **Concept:** A NAS-inspired optimization framework designed to automate MAS design by optimizing both *prompts and topologies* simultaneously.⁹⁵
 - **Method:** It employs a 3-stage interleaved optimization process⁹⁶:
 1. **Stage 1:** Block-level (local) prompt optimization.
 2. **Stage 2:** Workflow topology optimization (searching over the graph structure).
 3. **Stage 3:** Workflow-level (global) prompt optimization (refining prompts for the chosen topology).
 - **Key Finding:** The MASS paper⁹⁹ reveals that optimizing individual agent prompts *first* (Stage 1) is critical for success before attempting to optimize the large-scale topology (Stage 2).
- **NADER (CVPR 2025):**
 - **Concept:** This framework¹⁰⁰ presents a fascinating reversal: it uses a *multi-agent collaboration* of LLM agents (e.g., Proposer, Reflector) to *perform Neural Architecture Design*.¹⁰⁰
 - **Representation:** Both MASS⁹⁹ and NADER¹⁰⁰ emphasize the critical importance of the *search space representation*. NADER advocates for a *graph-based representation* of the architecture, rather than raw code. This allows the optimizing agents to focus on high-level structural decisions without being "distracted by coding".¹⁰⁰
- **Differentiable Workflow Evolution:**

Making the (discrete) workflow graph evolution differentiable, to enable gradient-based optimization (a la DARTS 100), is a major challenge. The TextGrad framework⁸⁶, integrated into EvoAgentX, is a key step in this direction, as it proposes a method to "backpropagate" text-based feedback to optimize prompts. A fully gradient-based search over discrete agent topologies remains a significant open research problem.

4.3 Workflow Genome Representation and Constrained Evolution

- **Representation:** To evolve a workflow, it must be encoded as a "genome." Common representations include:
 - **Graph:** A formal graph with nodes (agents) and edges (connections).¹⁰⁰
 - **Tree:** A prefix tree, as used in classical Genetic Programming (GP).¹⁰⁵
 - **Script:** A coordination script (e.g., Python code) that is itself evolved.¹⁰⁶
- **Operators:** Standard evolutionary operators are adapted: **Mutation** (add/remove agent, change connection, change agent's prompt⁸⁴) and **Crossover** (combine sub-graphs from two parent workflows).⁹⁴
- **Constrained Evolution (Critical Gap):** This is a critical limitation for the ATLAS system's safety. An unconstrained evolutionary algorithm will generate thousands of *invalid* or *unsafe* workflows (e.g., a Refactorer that writes directly to the final Archive without a Validator step).
 - **The Gap:** SOTA frameworks like EvoFlow⁸⁴ and MASS⁹⁵ optimize for performance and cost, but not for *hard safety constraints*.
 - **SOTA:** EvoAgent (NAACL 2025)⁹⁴ mentions assessing an agent's ability to "satisfy individual constraints," but the mechanism is not detailed. This field, which combines agent evolution with "Safe MARL"¹⁰⁸ and "Constrained Policy Optimization"¹⁰⁹, is wide open for novel contributions (see Section 7.4).

Table 4.1: Frameworks for Evolutionary Workflow Auto-Discovery (2025)

Framework	Optimizati on Goal	Method	Optimized Artifacts	Constraint Support	Key Contributi on
EvoFlow ⁸⁴	Pareto Population (Cost vs. Perf.)	Multi-Objec tive Evolutionar y ⁸⁴	Prompts, LLM Models, Operators	None (Penalty-ba sed)	Evolves a <i>diverse</i> <i>population</i> of workflows, not just one.
EvoAgentX ⁸⁶	Single High-Perfor mance	Integrator (Evolutionar y) ⁸⁶	Prompts, Tools, Topologies ⁸⁸	Unclear (via optimizers)	An <i>integrator</i> <i>platform</i> that

	Workflow				bundles SOTA optimizers (TextGrad, AFlow, MIPRO). ⁸⁶
MASS ⁹⁵	Single High-Performance Workflow	NAS-Inspired Search ⁹⁸	Prompts and Topologies ⁹⁸	None (Unconstrained search)	A 3-stage search that interleaves prompt- and topology-optimization. ⁹⁶
EvoAgent ⁹⁴	Single High-Performance Workflow	Evolutionary ⁹⁴	Agent Settings / Team Structure	Mentioned ⁹⁴	Evolves a <i>single agent</i> into a <i>multi-agent system</i> . ⁹⁴

Section 5: Game Theory, Adversarial Optimization, and Robustness

This section addresses the crucial requirement of ensuring the 40-agent system is robust. This includes robustness to adversarial inputs, unexpected failures, and strategic agent behavior.

5.1 Min-Max and Bi-Level Optimization for Robustness

A robust system is one that performs well even in the *worst-case* scenario. This can be formally modeled as a **min-max optimization** problem: we want to find the workflow W that *minimizes* the *maximum* loss (or "regret") that an *adversary* A can inflict.

This is a formal **bi-level optimization** problem¹¹⁰:

- **Outer Loop:** $\min_{W \in \text{Workflows}} (\text{Loss}(W, \text{Input}^*))$

- **Inner Loop:** $\max_{\text{Input}^* \in \text{AdversarialSet}} (\text{Loss}(W, \text{Input}^*))$

The inner loop finds the worst-case input Input^* for a *given* workflow W , and the outer loop finds the workflow W that is the most robust to its *own* worst-case input.

A SOTA (Sep 2025) framework, **RobustFlow**¹¹⁰, directly addresses this. It is a training framework that *leverages preference optimization (DPO)* to teach the workflow *generator* model to be *invariant to instruction variations* (e.g., paraphrasing).¹¹⁰ It trains the model to learn a single, canonical workflow for a cluster of synonymous queries.¹¹⁰

However, RobustFlow makes the workflow *generation* robust to *input text variations*. It does not make the workflow *execution* robust to *agent failure* or *environmental shifts*. This remains a critical gap (see Section 7.5).

5.2 Adversarial Testing and Red-Teaming Frameworks

This is the practical implementation of the "inner loop" $\max(\text{Loss})$: how to find the "AdversarialSet." A "Red Team" subsystem must continuously attack the ATLAS system to find vulnerabilities.

Several SOTA (2024) open-source frameworks exist for this purpose:

- AgentSafety (Repo)¹¹²: This is a comprehensive GitHub repository from OSU-NLP-Group that curates research and tools for agent safety. It lists numerous attack frameworks, including:
 - AdvWeb: A black-box attack on VLM-based web agents.
 - RedAgent: A multi-agent system designed to *automatically find* jailbreak prompts.¹¹²
 - Environmental Injection Attacks (EIA): Attacks that inject malicious content into the agent's environment.¹¹²
- BrowserART (Oct 2024)¹¹²: The "Browser Agent Red teaming Toolkit".¹¹² This is a concrete *test suite* with 100 diverse harmful behaviors (sourced from HarmBench and AirBench) to test browser-based agents.¹¹²
- DeepTeam (2024)¹¹³: An open-source *LLM red teaming framework* for penetration testing. It is a practical toolkit that simulates 10+ attack methods (e.g., prompt injection, leetspeak, crescendo jailbreaking) and checks for over 40 vulnerabilities (e.g., bias, PII leakage, robustness).¹¹³
- AATMF (2024)¹¹⁴: The "Adversarial AI Threat Modeling Framework." This provides an OWASP-style *methodology* and taxonomy for testing AI systems, with 14 tactics like "Persona Override" (AT-001) and "Reasoning Exploitation" (T3).¹¹⁴

A powerful, novel architecture would unite these components: the *testing* frameworks (DeepTeam, RedAgent) ¹¹² are used to *generate* the training data for the *adversary* in the *inner loop* of the *bi-level optimization* ¹¹¹ that *designs* the robust workflow. This creates a self-improving, adversarially-trained system.

5.3 Game-Theoretic Coordination

When agents have different (potentially conflicting) objectives, their coordination can be modeled as a "game."

- **Robust MARL (2023-2024):** A significant body of research ¹¹⁵ focuses on "Robust MARL." A 2024 SOTA paper ¹¹⁸ explores **Distributionally Robust Markov Games (RMGs)**. In an RMG, each agent learns a policy that maximizes its *worst-case* performance when the environment deviates from the training distribution.¹¹⁸ This is critical for ATLAS, ensuring its agents perform reliably when the "distribution" of research problems changes.
- **Stackelberg Games (2024):** This model is ideal for leader-follower dynamics.¹¹⁹ A 2024 paper ¹²⁰ applies "Stackelberg game-theoretic learning" to multi-robot collaborative assembly. This is a very strong analogue for the ATLAS Designer \rightarrow Critic relationship. The Designer (leader) makes a move (generates an artifact), and the Critic (follower) plays its best response (provides a critique). This can be used to find a "Stackelberg equilibrium," where the Designer anticipates the Critic's critique and produces a better initial artifact.
- **Mechanism Design:** A branch of game theory that *designs the rules of the game*. For ATLAS, this applies directly to the design of the **Auction-Based Task Allocation** (Section 1.3). The auction mechanism ²² is designed so that the self-interested, "bidding" behavior of the 40+ agents results in a globally efficient and truthful assignment.

Table 5.1: Adversarial Testing Frameworks for LLM-Agent Systems (2024)

Framework	Type	Attack Focus	Target Agent	Open Source
DeepTeam ¹¹³	Toolkit	Jailbreaking, PII Leakage,	General LLM, Chatbot, RAG	Yes ¹¹³

		Bias, Misinformation (40+ vulnerabilities)		
BrowserART ¹¹²	Test Suite	Harmful Behaviors (100 tasks, e.g., web-based attacks)	Browser Agents	Yes (via AgentSafety) ¹¹²
AATMF ¹¹⁴	Methodology	Prompt Subversion, Linguistic Evasion, Memory Manipulation (14 tactics)	General AI Systems	Yes ¹¹⁴
RedAgent ¹²²	Attack Generator	Context-aware Jailbreak Prompt Generation	Black-box LLMs	Yes (via AgentSafety) ¹²²

Part 2: Comparative Analysis of Frameworks, Tools, and Benchmarks

Section 6: Platforms, Libraries, and Testbeds

This section provides a comparative analysis of production-ready tools, research-prototype libraries, and benchmark datasets, offering recommendations for the "buy vs. build" decisions in the ATLAS/TURING architecture.

6.1 Multi-Agent Orchestration Platforms

The choice of orchestration framework is a fundamental architectural decision. The 2024-2025 landscape is dominated by a few key players.⁵⁴

- **LangGraph (2024):**
 - **Architecture:** A library from LangChain for building *stateful, multi-actor applications*.⁴⁵ Its key feature is treating workflows as *cyclical graphs* rather than DAGs.⁵⁴
 - **Pros:** Explicit, persistent state management (a central state object is passed and modified by each node). Native support for *cycles, branching, and human-in-the-loop*.⁴⁵ This is, by far, the best-suited framework for implementing the Designer \rightarrow Critic \rightarrow Refactorer loop.
 - **Cons:** Can be complex, requiring explicit definition of the graph, state schema, and conditional edges.⁵⁴
- **Microsoft AutoGen (2023/2024):**
 - **Architecture:** A generic *multi-agent conversation* framework.⁵⁴ Agents (e.g., UserProxyAgent, AssistantAgent) coordinate by sending and receiving *asynchronous messages*.⁵⁴
 - **Pros:** Highly flexible, good for "emergent" group chat behaviors, supports both autonomous and human-in-the-loop workflows.⁵⁴
 - **Cons:** The "conversation-driven" flow can be chaotic, difficult to debug, and get stuck in loops.⁵⁴ State management is less explicit than in LangGraph, as it is embedded in the message history.
- **CrewAI (2024):**
 - **Architecture:** A *role-based* framework.⁵⁴ The developer defines Agents (with roles, backstories, and goals), Tasks (with descriptions), and a Crew that executes them using a Process.⁵⁴
 - **Pros:** Extremely simple to get started, excellent for rapid prototyping, and enforces a clear, hierarchical structure.⁵⁴
 - **Cons:** The default "sequential" process is far too rigid for the dynamic needs of ATLAS.⁵⁴ It is not designed for complex, graph-based, or cyclical logic.
- **Swarm (OpenAI, 2024/2025):**
 - **Architecture:** This is currently experimental and not a production-ready framework.¹²³ The name, along with related research into swarm intelligence¹²⁵ and decentralized systems (see Section 7.7), suggests a future direction, but it is not a tool that can be adopted today.

Recommendation: A hybrid architecture is required.

1. **Level 1 (Task Scheduling):** Use **Prefect**⁴³ for high-level, dynamic task orchestration (as discussed in Section 2.3).
2. **Level 2 (Agent Coordination):** Use **LangGraph**⁴⁵ to build the internal, stateful, cyclical workflows (e.g., the dialectical chains) that are *triggered* by Prefect.

6.2 Blackboard and Shared Memory Architectures

The 40+ agent system will be too large and complex to be managed by a single, monolithic LangGraph. A more scalable, flexible paradigm is the **Blackboard Architecture**, a classic AI pattern¹²⁶ being rediscovered for LLM agents.¹²⁷

- **Concept:** Agents do not communicate directly (peer-to-peer) or via a rigid graph (orchestrator). Instead, they communicate *indirectly* by reading and writing to a central, structured data store (the "blackboard").¹²⁶
- **Modern Relevance (2024/2025):**
 - MetaGPT (2024)¹²⁸ implements a "shared memory pool".¹²⁹
 - A 2025 paper¹²⁶ explicitly revives the blackboard architecture, distinguishing it from simple shared memory: in a true blackboard system, agents *autonomously* monitor the board and *decide* to contribute when a relevant request is posted. This contrasts with a shared-memory system where a central coordinator still *assigns* tasks.¹²⁶

This leads to a more sophisticated *hybrid architecture* recommendation:

- Use **LangGraph** for *small, well-defined, tactical* workflows (like the D-C-R loop) where the sequence is known but cyclical.
- Use a **Blackboard System** (which would need to be custom-built) for *high-level, strategic, emergent* coordination. For example:
 1. Literature Scout finishes its run and posts an "Artifact: New_Paper_Summary" to the blackboard.
 2. This post *triggers* all agents subscribed to that topic.
 3. A Hypothesis Generator autonomously pulls the summary, processes it, and posts a "Artifact: New_Hypothesis" to the board.
 4. This new post, in turn, triggers a Designer LangGraph team to spin up and begin working on the hypothesis.

This architecture is decentralized, flexible (new agents can be added at runtime by just subscribing to topics), and robust to agent failure. This connects to the SwarmSys decentralized model 130 and is a key topic for a novel contribution (Section 7.7).

6.3 MARL Platforms

For any research involving learning-based coordination (e.g., Sections 7.2, 7.5, 7.6), a dedicated MARL stack is necessary.

- **RLlib (from Ray):**
 - **Features:** A highly scalable, framework-agnostic library for RL.¹³¹ Its most critical feature for ATLAS is its built-in support for **hierarchical training**, with examples of a "manager" agent calling "worker" agents.¹³² It integrates directly with PettingZoo and OpenSpiel.¹³²
 - **Cons:** Notoriously complex and difficult to debug.¹³⁴
- **PettingZoo:**
 - **Features:** This is *not* a training library, but the *de facto standard API* for multi-agent environments (it is the multi-agent version of Gymnasium).¹³⁴
- **OpenSpiel (from DeepMind):**
 - **Features:** A framework for RL in *games*.¹³⁵ Its primary strength is its implementation of game-theoretic concepts, which is ideal for the research in Section 5.3 (e.g., Stackelberg games).¹³³

Recommendation: The MARL stack is clear: (1) Define the 40-agent ATLAS environment using the **PettingZoo** API.¹³⁴ (2) Use **RLlib** as the training backend, leveraging its hierarchical agent support.¹³²

6.4 Optimization Libraries (OR vs. ML)

- **OR Solvers (for QAP, Scheduling):**
 - Google OR-Tools: **Best open-source choice.** It is fast, Python-native, and has excellent, mature solvers for Constraint Programming (CP-SAT), scheduling (JSSP)²⁸, and routing (VRP), which are close cousins to QAP.¹⁰
 - Gurobi / CPLEX: **Best commercial choice.** These are the market leaders, known for "blazing speed" in solving large, complex MIPs (like QAP).¹⁰ They are available for free via academic licenses.
- **ML Solvers (for HPO, Evolution):**
 - Optuna: **Best for HPO.** A SOTA hyperparameter optimization framework that uses Bayesian methods (TPE).¹³⁷ It also includes samplers for evolutionary algorithms like CMA-ES.¹³⁹
 - Ray Tune: **Best for PBT.** The best-in-class, distributed implementation of Population-Based Training⁷⁶, which is essential for the PBT+Elo agent evolution

concept (Section 3.4).

- **DEAP: Best for pure Genetic Programming.** A classic, flexible framework for evolving *code* or *trees*.¹⁰⁵ This would be the library to use for the *Safe-EvoFlow* research gap (Section 7.4).

6.5 Benchmark Datasets

Validating novel research requires SOTA benchmarks.

- **Classical Benchmarks:** QAPLIB² (for assignment), TSPLIB (for routing), and JSSP Datasets²⁸ (for scheduling). These are necessary to validate any new *solvers* (e.g., the OC-QAP in Section 7.1).
- **SOTA Agent Workflow Benchmarks (2023-2025):** These are essential for validating the *agent architecture* itself.
 - AgentBench (2023)¹⁴¹: Evaluates reasoning and decision-making in 8 diverse environments (OS, DB, Knowledge Graph, Web).¹⁴¹
 - WebArena (2023)¹⁴¹: Focuses on realistic, multi-step web-based tasks (e-commerce, collaborative code development).¹⁴¹
 - GAIA (2023)¹⁴¹: The SOTA benchmark for "General AI Assistants." Requires long-horizon reasoning, multi-step tool use, and multimodality.¹⁴¹ This was used to validate EvoAgentX.⁹²
 - ToolBench / ToolLLM (2023)¹⁴¹: The largest benchmark for *tool use* and API calls (16,000+ APIs).¹⁴¹
 - ItineraryBench (2025)¹⁶: A new benchmark from Feb 2024 (v2 Jan 2025) for *dynamic, complex, multi-step* planning tasks.¹⁶

Key Gap ("ATLAS-Bench"):

There is no public benchmark for evaluating a multi-agent system on end-to-end autonomous scientific research. Anthropic has published a blog post on its internal multi-agent research system 143, but no public testbed exists.

The *first publication* from the ATLAS project could be the definition and open-sourcing of **"ATLAS-Bench: A Benchmark for Evaluating Autonomous Multi-Agent Scientific Research Systems."** This would be a high-impact contribution, defining a new testbed for the entire field.

Table 6.1: Multi-Agent Orchestration Framework Comparison (2024/2025)

Framework	Core Architecture	State Management	Key Pro	Key Con	Maintenance Status
LangGraph ⁴⁵	Stateful, Cyclical Graph	Explicit State Object	Best for loops, branching, state	More complex "boilerplate" ¹²³	Actively Maintained (2025) ⁵⁴
AutoGen ⁵⁴	Conversational (Async)	Message History	Flexible, "emergent" chat	Unstructured, can be chaotic ¹²³	Actively Maintained (2025) ⁵⁴
CrewAI ⁵⁴	Role-Based	Task-Based	Very simple, rapid prototyping ⁵⁵	Too rigid, default sequential ⁵⁴	Actively Maintained (2025) ⁵⁴
MetaGPT ¹²⁸	Blackboard-like	Shared Memory Pool ¹²⁹	Structured, role-based workflow	Less flexible than LangGraph	Actively Maintained (2024) ¹²⁸
OpenAI Swarm ¹²⁴	Decentralized (Swarm)	Unknown	(Theoretical) Scalability, Robustness	Experimental, not production-ready ¹²³	Experimental (2024) ¹²³

Table 6.2: Optimization and MARL Library Ecosystem for ATLAS

Library	Problem Type	License	Recommended Use Case in
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			ATLAS
Gurobi ¹⁰	MIP / QAP / Scheduling	Commercial (Free Academic)	(If licensed): SOTA solver for static QAP/Scheduling baselines.
Google OR-Tools ²⁸	CP / MIP / Scheduling / Routing	Apache 2.0	(Default): Open-source solver for assignment and scheduling heuristics.
Optuna ¹³⁷	Hyperparameter Optimization (HPO)	MIT	General HPO for all models and agents (e.g., prompts, temperatures).
Ray Tune ¹³⁸	Scalable HPO / PBT	Apache 2.0	Core component: Running the PBT+Elo system for agent evolution. ⁷⁶
DEAP ¹⁰⁵	Genetic Programming (GP)	LGPL-3.0	Research component: Backend for Safe-EvoFlow (Gap 7.4).
PettingZoo ¹³⁵	MARL Environment API	MIT	Core MARL component: Defining the 40-agent system as an RL environment.
RLlib (Ray) ¹³²	MARL Training	Apache 2.0	Core MARL component: Training algorithms for H-MARL (Gap

			7.6).
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Part 3: Research Gaps and Novel Contribution Opportunities

This section synthesizes the preceding analysis to identify seven high-impact, publishable research contributions. These are designed to be novel in the 2024-2025 research landscape and directly address the unique challenges of the ATLAS/TURING system.

Table 7.1: Matrix of Novel Research Contributions

Gap ID	Research Gap	Problem Domain	Novel Contribution	Key Baselines	Target Venue	Feasibility
7.1	Contextual QAP	Agent-Task Assignment	OC-QAP : GNN-based heuristic solver	Static QAP ² , MAB ²⁹ , STRMAC ³³	AAAI, ICLR	Medium
7.2	Dialectical Chain	Workflow Scheduling	SSP-QC: Model loop as Stochastic Shortest Path	Fixed-loop, STRMAC ³³	AAMAS, NeurIPS	High
7.3	Hierarchical BwK	Resource Allocation	HBwK: Two-level (Team/Ag	Flat BwK-TS	ICML, AISTATS	High

		n	ent) bandit	⁶¹ , DORAL ⁶³		
7.4	Constrained Evolution	Architecture Search	Safe-Evo Flow: EvoFlow + constrained operators	EvoFlow ⁸⁴ , MASS ⁹⁵ , Safe MARL ¹⁰⁸	GECCO, IEEE TEVC	Medium
7.5	Adversarial Robustness	Robust Workflow Design	M2-WO: Bi-level min-max (Evo vs. RedAgent)	RobustFlow ¹¹⁰ , DeepTeam ¹¹³	NeurIPS, ICLR	Low-Medium
7.6	Meta-Control	MARL Orchestration	H-MARL: Meta-controller sets sub-agent goals	Flat MARL (RLlib) ¹³² , EvoAgent ⁸⁶	AAMAS, CoRL	Medium
7.7	Decentralized Swarm	Orchestration Architecture	Stigmergy-Blackboard: Emergent coordination	MetaGPT ¹³⁰ , LangGraph ⁴⁵ , SwarmSyS ¹³⁰	AAMAS, TAAS	Medium

7.1 Gap: Contextual QAP for Dynamic Agent Assignment

Existing Work: The Quadratic Assignment Problem (QAP)¹ is a powerful model for static assignment with synergies. However, its cost matrices are static. For dynamic assignment, the field has bifurcated: (1) simplified models like Contextual Multi-Armed Bandits (MABs)²⁹, which are dynamic but ignore quadratic synergies, or (2) dynamic routing frameworks like

TDAG¹⁶ and STRMAC³³, which are ad-hoc and do not formally optimize global assignment cost.

Specific Limitation: There is no unified framework for **Online Contextual QAP (OC-QAP)**, where the full $N \times M$ cost matrix $C_{ij}(s_t)$ (cost of agent i on task j) and the $N \times N$ flow matrix $F_{ik}(s_t)$ (synergy of agent i and k) are both functions of the dynamic system state s_t (e.g., agent load, agent confidence, task features). Solving a full QAP at every time-step t is intractable.

Novel Contribution Proposal: "A Deep Learning Framework for Online Contextual Quadratic Assignment (OC-QAP) in Multi-Agent Systems."

Formulation: This contribution frames the OC-QAP as a *learned heuristic* problem, bridging ML4CO¹¹ and dynamic assignment.

1. **State Representation:** At time t , the system state s_t (agents, tasks, context) is represented as a heterogeneous graph.
2. **Cost Prediction:** A Graph Neural Network (GNN) model G_{θ} is trained. It takes the state graph s_t as input and *predicts* the full set of QAP cost matrices: $(C(s_t), F(s_t)) = G_{\theta}(s_t)$.
3. **Fast Assignment:** These predicted, context-aware cost matrices are fed into a *fast* (but sub-optimal) QAP heuristic solver (e.g., Tabu Search from QAPSolver⁴ or a 2-Opt heuristic) to find the ϕ_t assignment for the current step.
4. **Training:** The GNN G_{θ} is trained via Reinforcement Learning. The "action" is the predicted cost matrix. The "reward" is the *downstream* task quality or system throughput achieved by the assignment ϕ_t . The GNN learns to *predict cost matrices that lead to good final solutions*.

Expected Novelty: This framework is the first to bridge the gap between static, high-synergy QAP and dynamic, low-synergy contextual MABs. It learns the *problem context* itself, rather than just learning a policy to solve a static problem.

Validation:

- **Baselines:** (1) Static QAP (solved once at $t=0$). (2) A greedy "best-agent" assignment (a contextual MAB²⁹). (3) A full "flat" MARL policy.¹³² (4) STRMAC³³ as a SOTA routing baseline.
- **Benchmark:** Run on a modified ItineraryBench¹⁷ or a new, custom ATLAS-Bench.

Target Venue: AAAI (bridges AI and OR), ICLR (representation learning for optimization).

Feasibility: Medium. Requires deep expertise in both GNNs and combinatorial optimization.

7.2 Gap: Confidence-Aware DAG Scheduling (The Dialectical Chain)

Existing Work: SOTA routing frameworks like STRMAC³³ and SelfOrg³² are "myopic"—they pick the best *next* agent. The "dialectical" pattern (Designer \rightarrow Critic \rightarrow Refactorer) is ubiquitous⁴⁶, and "Critic"⁴⁸ or "Dialectical Reasoning"⁴⁹ frameworks are emerging.

Specific Limitation: These frameworks do not formally optimize the *convergence* of the dialectical loop. The key decision ("Do we refactor again, or stop and validate?") is made by a simple heuristic (e.g., "stop at score > 0.9"). This can lead to infinite loops⁴⁶ or, more likely, premature stopping that results in a suboptimal artifact.

Novel Contribution Proposal: "Optimizing Dialectical Agent Workflows as a Stochastic Shortest Path (SSP) Problem with Quality Gates."

Formulation: Model the D-C-R loop as a Markov Decision Process (MDP), specifically a Stochastic Shortest Path (SSP) problem.

- **States (\$S\$):** A tuple representing the artifact's state: (v, q) , where v is the artifact version (e.g., Code_v2) and $q \in [0, 1]$ is the Critic's last quality/confidence score.
- **Actions (\$A\$):** A set of actions available from any state: (Refactor, Validate, Stop_and_Archive).
- **Transitions (\$P\$):** A (learned) probabilistic transition function $P(s' \mid s, a)$. For example, $P((v+1, q') \mid (v, q), \text{Refactor})$ is the probability distribution over the *next* quality score q' given the current score q and the "Refactor" action. This model can be learned from execution history.
- **Costs (\$C\$):** A cost $C(s, a)$ associated with each action (e.g., Refactor cost = 10 API credits; Validate cost = 5).
- **Goal State:** Any state where $a = \text{Stop_and_Archive}$.
- **Objective:** Find an optimal policy $\pi^*: S \rightarrow A$ that minimizes the expected total cost to reach a goal state, while maximizing the final quality q at that state. This can be formulated as a standard SSP, solvable with Value Iteration or Q-Learning. The resulting policy π^* is the optimal confidence-aware scheduler.

Expected Novelty: This is the first formal, optimization-based model of the "dialectical agent loop," a ubiquitous but poorly understood pattern in agentic AI. It replaces a fragile heuristic with a provably optimal policy.

Validation:

- **Implementation:** Implement this policy as the conditional router in a LangGraph.⁴⁵
- **Baselines:** (1) A fixed-loop policy (e.g., "always refactor $k=3$ times"). (2) A naive threshold policy ("stop when $q > 0.9$ "). (3) An evolutionary baseline from EvoAgentX.⁸⁶

- **Metrics:** Measure (Final Quality, Total Cost) pairs and show the SSP policy dominates the baselines on the Pareto front.

Target Venue: AAMAS (Autonomous Agents and Multiagent Systems), NeurIPS (RL Applications).

Feasibility: High. The formulation is clear, builds on standard MDP/RL theory, and is highly practical.

7.3 Gap: Constrained Hierarchical Bandits for Agent Resource Allocation

Existing Work: Contextual Bandits with Knapsacks (BwK) ⁶¹ are the correct *class* of models. The 2025 LinCBwK9TS algorithm ⁶¹ is a SOTA *implementation*. Nascent 2025 preprints are just beginning to explore *bi-level* contextual bandits ⁶⁶ and delayed feedback. ⁶³

Specific Limitation: Standard BwK algorithms ⁶¹ treat all 40+ agents as a "flat" set of \$K\$ arms. This is inefficient and ignores the known, exploitable *hierarchical structure* of the ATLAS agents (e.g., the "Coding" team, the "Validation" team, the "Literature" team). The bi-level work ⁶⁶ is a starting point but is not fully developed for this team-based structure.

Novel Contribution Proposal: "Hierarchical Bandits with Knapsacks (HBwK): A Two-Level Approach for Team-Aware Multi-Agent Resource Allocation."

Formulation: Design a two-level MAB system based on the principles of hierarchical RL.

1. **Level 1 (Group-MAB):** This is a high-level **BwK** problem. The "arms" are the \$G\$ *agent groups* (e.g., "Designers", "Critics", "Scouts"). This MAB learns to allocate the *total system budget* (e.g., 1000 GPU-hours) among these groups. Its reward is the *aggregate quality* produced by the group.
2. **Level 2 (Agent-MABs):** This is a set of \$G\$ *independent Contextual BwK* problems (one for each group). Each group's MAB solves a *local* allocation problem (e.g., "How does the 'Designers' group spend its 200 GPU-hour budget (from Level 1) among its 3 individual agents, given the current task context \$x_t\$?").

Expected Novelty: This structure allows the system to learn *both* inter-group synergies (e.g., "we get more value by giving more budget to Critics right now") and intra-group performance (e.g., "Agent Critic-A is outperforming Critic-B on this task type"). It is a clear, formal extension of BwK ⁶¹ and bi-level bandits ⁶⁶ that is highly practical for any large-scale, team-based agent system.

Validation:

- **Implementation:** Implement using Contextual Thompson Sampling at both levels, building on the SOTA LinCBwK9TS.⁶¹
- **Baselines:** (1) A "flat" CBwK (all 40 agents in one pool). (2) A static, non-bandit allocation (e.g., equal budget per group). (3) A non-hierarchical, "per-agent" CBwK.
- **Metrics:** Measure cumulative reward (quality) and regret vs. total budget. Hypothesize that HBwK learns faster (lower regret) due to its superior structural prior.

Target Venue: ICML (International Conference on Machine Learning), AISTATS (AI and Statistics).

Feasibility: High. This is a very strong, clear, and publishable extension of existing SOTA bandit theory.

7.4 Gap: Constrained Evolutionary NAS for Safe Agentic Workflows

Existing Work: SOTA (2025) frameworks like EvoFlow⁸⁴, EvoAgentX⁸⁶, and MASS⁹⁵ are powerful tools for *auto-discovering* high-performance agent workflows.

Specific Limitation: These frameworks optimize primarily for performance and cost.⁸⁴ They lack a formal mechanism for enforcing hard *safety or validity constraints*. For example, the ATLAS system may have non-negotiable rules: "A Refactorer output *must* be followed by a Validator before Code_Archive," or "A Hypothesis *must* be logged by *both* Literature_Scout and Validator." An unconstrained evolution will produce many high-performing but *unsafe* or *invalid* workflows. EvoAgent⁹⁴ mentions constraints, but the mechanism is unclear and not the focus.

Novel Contribution Proposal: "Safe-EvoFlow: Constrained Evolutionary Optimization for Verifiable Agentic Workflows."

Formulation: This contribution extends an evolutionary framework (like EvoFlow⁸⁴) with formal principles from Constrained Optimization (CO) and Genetic Programming (GP).

1. **Representation:** Encode the workflow as a graph genome¹⁰⁰, as done in NADER.¹⁰⁰
2. **Constraints:** Define a formal *constraint language* for agent workflows. This could use Linear Temporal Logic (LTL) or simple graph-path rules (e.g., ALWAYS (Refactor -> (NOT Archive UNTIL Validator))).
3. **Constrained Operators:** Design *constraint-preserving* or *constraint-aware* genetic operators (mutation/crossover).⁸⁴
 - **Repair:** An invalid offspring (e.g., a mutation creates a Refactor -> Archive edge) is

- "repaired" by an algorithm to make it valid (e.g., by inserting a Validator node).
 - **Safe Operators:** A "Safe Add Edge" operator *refuses* to create a connection that violates a constraint.
- 4. **Multi-Objective Goal:** Use a Multi-Objective Evolutionary Algorithm (MOEA) like NSGA-II to optimize a vector: (Objective 1: Performance, Objective 2: Cost, Objective 3: Constraint_Violation_Penalty). This allows the system to find a Pareto front of solutions that trade off performance with constraint satisfaction, or to enforce constraints strictly (infinite penalty).

Expected Novelty: This is the first application of formal "safe evolution" / "safe genetic programming" to the *architecture* of LLM agent workflows. It moves beyond "safe MARL" (which optimizes a policy for a *fixed* architecture)¹⁰⁸ to optimizing the *architecture itself* for safety.

Validation:

- **Benchmark:** Define a set of 10-15 hard safety constraints for the ATLAS-Bench (from Gap 6.5).
- **Baselines:** Run standard EvoFlow⁸⁴ and MASS.⁹⁵
- **Metrics:** Show that Safe-EvoFlow finds a Pareto frontier where 100% of solutions are valid. Measure the performance/cost of the *best valid* solution found by the baselines vs. the Safe-EvoFlow frontier.

Target Venue: GECCO (Genetic and Evolutionary Computation Conference), IEEE Transactions on Evolutionary Computation (TEVC).

Feasibility: Medium. Requires deep expertise in genetic programming and constrained optimization, but the path is clear.

7.5 Gap: Adversarial Bi-Level Optimization for Agent Failure

Existing Work: Robustness is a major 2025 theme. RobustFlow (Sep 2025)¹¹⁰ uses bi-level optimization to make workflow *generation* robust to *input instruction* variations. Adversarial *testing* frameworks (DeepTeam¹¹³, BrowserART¹¹²) are for *post-design* validation.

Specific Limitation: No existing framework uses bi-level optimization¹¹¹ to design workflows that are robust to *agent failure* or *adversarial agent behavior* during *execution*. This includes a "lazy" Critic that passes all work, a "malicious" Refactorer that injects bugs, or a Literature Scout that simply dies (returns None).

Novel Contribution Proposal: "M2-WO: Min-Max Multi-Agent Workflow Optimization against

Adversarial Agent Failure."

Formulation: This is a true "adversarial training" for workflow architectures, formulated as a bi-level min-max game ¹¹¹:

- **Outer Loop (Proposer / Minimizer):** An optimizer (e.g., EvoFlow ⁸⁴ or MASS ⁹⁵) proposes a workflow architecture W . Its goal is to $\min_W \text{Loss}(W)$.
- **Inner Loop (Adversary / Maximizer):** A "Red Team" policy π_{adv} tries to *break* W . This adversary can be a trained RL agent (like RedAgent ¹¹²).
 - **Action Space:** $\text{Action} \in \{\text{Corrupt}(\text{Agent}_i, \text{mode}), \text{Delay}(\text{Agent}_j), \text{Kill}(\text{Agent}_k)\}$.
 - **Objective:** The adversary learns $\pi_{\text{adv}}^* = \arg\max_{\pi} \text{Final_Error}(W, \pi)$.
- **Fitness:** The Outer Loop's fitness for W is its *worst-case* performance: the minimized error from the inner loop's π_{adv}^* .

Expected Novelty: This system will learn to discover architectures that are inherently robust. For example, it might evolve *redundancy* (e.g., "always run two Critics in parallel and check for consensus"), *self-healing* (e.g., "evolve a 'meta-agent' that re-routes around a node that returns None"), or *stronger validation* (e.g., "evolve a workflow where the Validator is given more compute resources").

Validation:

- **Baselines:** (1) RobustFlow ¹¹⁰ (robust to input, not failure). (2) A non-robust EvoFlow baseline. ⁸⁴
- **Experiment:** After training, take the best workflows from all baselines. Perform "ablation attacks" (e.g., kill 1, 2, 3 agents at random).
- **Metrics:** Show that M2-WO produces workflows with significantly lower performance degradation when agents fail.

Target Venue: NeurIPS (Adversarial ML, Optimization), ICLR.

Feasibility: Low-to-Medium. This is a very ambitious, high-risk, high-reward, PhD-level project. The computational cost of the inner loop (training an adversary π_{adv}^* for every candidate workflow W) is immense.

7.6 Gap: Hierarchical MARL for Meta-Control

Existing Work: MARL frameworks (RLlib ¹³², PettingZoo ¹³⁵) provide the tools. RLlib has nominal support for "hierarchical training". ¹³² However, most H-MARL is applied to robotics

(e.g., "walk" sub-policy, "navigate" meta-policy). Separately, EvoAgentX⁸⁶ and MASS⁹⁵ use *external, offline* optimizers to *design* the workflow.

Specific Limitation: There is a lack of *online, two-level* RL systems where a *meta-controller* agent learns to *orchestrate* a team of *sub-agents* that are *also* learning. Applying H-MARL to *abstract agent coordination* is a novel frontier. 2025 preprints¹⁴⁵ explicitly identify hierarchical control and meta-learning as a key unexplored direction for multi-agent coordination.

Novel Contribution Proposal: "A Hierarchical MARL Framework for Meta-Control of Agentic Research Teams."

Formulation: A two-level H-MARL system, implemented using RLLib's hierarchical agent support¹³².

1. **Meta-Controller (Level 1):** A single RL agent that operates at a slow timescale (e.g., one action per research "stage").
 - **State:** The overall research progress (e.g., "Hypothesis A: validated; Hypothesis B: pending").
 - **Actions:** *Strategic* decisions (e.g., "Assign Team_Coding to Hypothesis_A," "Set objective for Team_Coding to 'Maximize_Readability'").
2. **Sub-Agents (Level 0):** Multiple MARL teams (e.g., Team_Coding = {Designer, Critic, Refactorer}). These agents operate at a fast timescale.
 - **State:** The local artifact (e.g., Code_v2).
 - **Action:** Execute the task (e.g., Critic runs).
 - **Reward:** Their reward is shaped by the *meta-controller's objective* (e.g., a "Readability_Score" from the Validator).

Expected Novelty: This directly implements a "manager" agent that learns how to *manage* other agents. It bridges the gap between EvoAgentX⁸⁶ (offline design) and RLLib¹³² (flat MARL), creating an *online, adaptive* hierarchy that can respond to changing research priorities.

Validation:

- **Implementation:** Build in RLLib¹³² with the environment defined in PettingZoo.¹³⁴
- **Baselines:** (1) A "flat" 40-agent MARL system. (2) A hand-crafted, non-learning script (the STRMAC³³ or EvoAgentX⁸⁶ winner). (3) A non-learning meta-controller (e.g., round-robin).
- **Metrics:** Show that H-MARL achieves higher long-term reward (better research output) and adapts more quickly to *dynamic* changes in the meta-task (e.g., "a new high-priority paper was just published").

Target Venue: AAMAS, CoRL (Conference on Robot Learning - for the H-MARL theory).

Feasibility: Medium. H-MARL is notoriously difficult to get to converge, but the RLLib tooling

provides a strong foundation.

7.7 Gap: Decentralized Swarm Orchestration via Stigmergy

Existing Work: Most popular agent frameworks are *centralized* or *graph-based*. MetaGPT¹²⁸, LangGraph⁴⁵, and AutoGen⁵⁵ all rely on explicit message passing or a pre-defined graph structure.¹³⁰ Centralized orchestration is a bottleneck and a single point of failure.

Specific Limitation: The concept of **stigmergy**—indirect coordination via modifications to a shared environment¹⁴⁸—is underdeveloped for LLM agents.

- **SwarmSys (Oct 2025):** This is the first SOTA paper¹⁴⁹ to propose a "decentralized swarm-inspired" framework.¹³⁰ However, it uses specific, pre-defined roles ("Explorer," "Worker," "Validator").¹³⁰
- **Blackboard (2025):** The more *general* blackboard concept¹²⁶ (where *any* agent can subscribe to *any* task) has been proposed but not, to our knowledge, implemented and benchmarked against centralized orchestrators.

Novel Contribution Proposal: "Stigmergic Coordination of LLM Agents via a Unified Blackboard Architecture."

Formulation: Design and implement a pure *blackboard system*¹²⁶ as a general-purpose coordination mechanism.

1. **Blackboard:** A structured, shared database (e.g., Redis, MongoDB) where tasks and artifacts are posted with "Topics" or "Tags" (e.g., Topic:New_Hypothesis, Status:Pending_Review).
2. **Agents:** 40+ fully autonomous, "daemon-like" agents. Each agent's policy is defined by:
 - **Subscription:** The set of topics/tags it *listens* to (e.g., Critic subscribes to Status:Pending_Review).
 - **Action:** When triggered, it pulls the artifact, processes it, and *posts a new artifact* back to the board (e.g., Topic:New_Hypothesis, Status:Review_Complete, Score:0.8).
3. **Coordination:** Coordination is *emergent* and *indirect*.¹⁴⁸ There is no central orchestrator.
4. **Optimization:** The "optimization problem" is now to (a) learn the optimal *subscription* policy for each agent and (b) learn the optimal *prioritization* policy (if 10 tasks are on the board, which does an agent pick?).

Expected Novelty: This contrasts *directly* with the centralized, fixed-pipeline approach of MetaGPT¹³⁰ and the graph-based approach of LangGraph.⁴⁵ It is a completely different *paradigm* for multi-agent coordination, based on swarm intelligence.¹⁵²

Validation:

- **Implementation:** Build the blackboard framework (this is a significant engineering task).
- **Baselines:** (1) A rigid, pre-defined LangGraph⁴⁵ workflow. (2) MetaGPT.¹³⁰ (3) The SwarmSys framework.¹³⁰
- **Hypothesis:** The stigmergic system will be (a) slower for simple, linear tasks but (b) far more *robust* to agent failure (as any available Critic can pick up a Pending_Review task) and (c) more *flexible* (new agents can be added at runtime without *any* system redesign).

Target Venue: AAMAS, ACM Transactions on Autonomous and Adaptive Systems (TAAS).

Feasibility: Medium. Requires building a custom framework, but the concepts are well-established in classical AI.

Concluding Remarks and Architectural Synthesis

The analysis presented in this report provides a comprehensive roadmap for both the *implementation* and *research publication* phases of the ATLAS/TURING project. The 40+ agent system is not a single optimization problem but a *hierarchy* of them, requiring a hybrid, multi-layered architecture.

The recommended SOTA architecture synthesizes the findings as follows:

- **Task Orchestration: Prefect**⁴³ manages high-level, business-logic tasks (e.g., "start research project").
- **Strategic Coordination: A Blackboard System**¹²⁶ (as proposed in Gap 7.7) manages high-level, event-driven coordination between agent *teams* in a flexible, decentralized manner.
- **Tactical Coordination: LangGraph**⁴⁵ is used by individual teams to execute their internal, stateful, and *cyclical* logic (e.g., the Designer-Critic loop, formally optimized as an SSP per Gap 7.2).
- **Resource Allocation: A Hierarchical Bandits with Knapsacks (HBwK)** system (per Gap 7.3) manages the compute/API budget, allocating it first to *teams* and then to *individual agents*.⁶⁶
- **Agent Performance Evolution: A Population-Based Training (PBT)** scheduler from Ray Tune⁷⁶ continuously evolves agent hyperparameters (prompts, models), using an internal **Elo Rating System**⁸¹ (fed by Validator votes) as its fitness function.
- **Architecture Evolution: A Safe-EvoFlow** optimizer (per Gap 7.4) runs in the background, evolving the *topologies* of the LangGraph and Blackboard-subscription policies to discover better coordination patterns.⁸⁴

- **System Robustness:** A **DeepTeam**-powered ¹¹³ "Red Team" subsystem continuously generates attacks, serving as the inner loop for an **M2-WO** bi-level optimizer (per Gap 7.5) to ensure the evolved architectures are robust to failure.

This architecture is modular, adaptive, and self-optimizing. Each component is grounded in SOTA 2024/2025 research and provides a direct path to a novel, publishable contribution.

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