Timer LM555

Threshold = $0.667 \times Vcc$

Astable comienza en 10:00m

Terminal 7 es descarga

$$Vcc = (Ra + Rb)i(t) + Vcapacitor$$

$$V capacitor = \frac{1}{c} \int_{0}^{\infty} i(t) dt$$

Despejando i(t)

$$\frac{Vcc}{s} = R_i(s) + \frac{i(s)}{cs} = i(s)\frac{(R+1)}{sc} = \dot{I}(s)\frac{Rcs+1}{sc}$$

Despejando i(s)

$$i(s) = \frac{Vccsc}{s}(Rc + 1)$$

Vcapacitor

$$\frac{1}{c}\int_{0}^{\infty}i(t)\,dt = \frac{V_{cc}}{R_{c}}\int_{0}^{\infty}e^{-\frac{t}{R}c}\,dt$$

Calculando la integral

$$Vcc(1-e^{-\frac{t}{Rc}})$$

$$\begin{split} Calcular \ t \ si \ vcc \ &= \frac{2Vcc}{3} \rightarrow \frac{2Vcc}{3} = Vcc \left(1 - e^{-\frac{t}{Rc}}\right) \rightarrow \frac{2}{3} = 1 - e^{-\frac{t}{Rc}} \rightarrow e^{-\frac{t}{Rc}} = 1 - \frac{2}{3} = \frac{1}{3} \\ &- \frac{t}{Rc} = \ln\left(\frac{1}{3}\right) \rightarrow t_{max} = -Rcln\left(\frac{1}{3}\right) \\ si \ Vcc \ &= \frac{Vcc}{3} \rightarrow -\frac{t}{Rc} = \ln\left(\frac{2}{3}\right) \\ t_{min} \ &= -Rcln\left(\frac{2}{3}\right) \end{split}$$

$$t_{max} = -Rcln\left(\frac{1}{3}\right)$$

$$t = t_{max} - t_{min}$$

$$t = -Rcln\left(\frac{1}{3}\right) + Rcln\left(\frac{2}{3}\right) = Rc\left(-ln\left(\frac{1}{3}\right) + ln\left(\frac{2}{3}\right)\right)$$
Tiempo de carga = $Rcln(2) = (R_a + R_b)c \ln(2)$

Tiempo de descarga

$$0 = Rbi(t) + \frac{1}{c} \int_{0}^{t} i(t) dt \rightarrow laplace \rightarrow 0 = Rbi(s) + \frac{1}{sc}i(s) = i(s)\left(Rb + \frac{1}{sc}\right)$$

Para la descarga

$$\frac{2}{3} = Vcce^{-\frac{t}{Rc}}$$

 $Despejando el tiempo_{min}$

$$\begin{split} &\ln\left(\frac{2}{3}\right) = -\frac{t}{Rbc} \to t_{min} = -RBcln\left(\frac{2}{3}\right) \to \ t_{max} = \ -Rbcln\left(\frac{1}{3}\right) \\ &t = t_{max} - t_{min} = -Rbcln\left(\frac{1}{3}\right) + Rbcln\left(\frac{2}{3}\right) = Rbcln(2) \end{split}$$

Periodo

$$T = (R_a + R_b)cln(2) + Rbcln(2) \rightarrow ln(2) c(R_a + R_b)$$

$$F = \frac{1}{T} \rightarrow 1/(ln(2) c(R_a + R_b) \rightarrow \frac{1.4426}{c(R_a + R_b)}$$

$$D = ciclo de trabajo = \frac{t_{bajo}}{T} \rightarrow \frac{t_{bajo}}{t_{alto} + t_{bajo}}$$

Ejemplo

$$D = \frac{Rbcln(2)}{(R_a + R_b)cln(2) + Rbcln(2)} \rightarrow \frac{\frac{cln(2)}{cln(2)}R_b}{R_a + R_b + R_b} = \frac{R_b}{R_a + 2R_b}$$

Las valores de Resistencias tienen que estar por encima de $1k\Omega$ para no hacer consumir al circuito corriente de mas

Ejercicio => Si c = 0.1μf,
$$R_a$$
 = 5kΩ, R_b =? y f = 1 khz → 4713.47 → 4.7 $kΩ$ ($R_a + R_b$) $_{max}$ = 20 $MΩ$ ($R_a + R_b$) $_{min}$ = 1 $KΩ$

Escriba aquí la ecuación.

 $Calcular\ para\ 1hz, 60hz\ y\ 5khz$

Calcular tambien D

$$Vcc = R_a i(t) + \frac{1}{c} \int_0^t i(t)dt$$

transformando Voltaje de capacitor por laplace
$$\frac{Vcc}{s} = R_a i(s) + \frac{1}{sc} i(s) = i(s) \left(R_a + \frac{1}{sc} \right)$$
$$\frac{Vcc}{s} = i(s) \frac{R_a cs + 1}{sc}$$

$$i(s) = \frac{Vcc}{s} \frac{sc}{R_a c s + 1} = \frac{\frac{cVcc}{R_a c}}{\frac{R_a c s + 1}{R_a c}} = \frac{Vcc}{R_a} \frac{1}{s + \frac{1}{R_a c}}$$

Antitransformada

$$i(t) = \frac{Vcc}{R_a} e^{-\frac{t}{R_a c}}$$

Voltaje en el capacitor

$$V capacitor = \frac{1}{c} \int_{0}^{t} i(t)dt = i(t) = \frac{Vcc}{R_a} e^{-\frac{t}{R_a c}}$$

$$V capacitor = -V cc e^{-\frac{t}{R_a c}} \bigg|_{0}^{t} = -V cc e^{-\frac{t}{R_a c}} + V cc e^{-\frac{0}{R_a c}}$$

$$V capacitor = V cc \left(1 - e^{-\frac{t}{R_a c}}\right)$$

$$\frac{2Vcc}{3} = Vcc \left(1 - e^{-\frac{t}{R_a c}}\right)$$

$$e^{-\frac{t}{R_a c}} = 1 - \frac{2}{3} = \frac{1}{3}$$

$$-\frac{t}{R_a c} = \ln\left(\frac{1}{3}\right)$$

$$t = -R_a c ln\left(\frac{1}{3}\right)$$

$$t = 1.1R_a c$$

para un tiempo de un segundo

$$c = 1\mu$$

$$R_a = \frac{t}{1.1c} = \frac{1}{1.1 * 1\mu} = 909k\Omega$$

Hacer de 500ms, 5s y 15s