

Movies

Train_Users

| | | | | | | | | |
|---|---|---|---|---|---|---|---|---|
| ◆ | ◆ | ? | ◆ | ◆ | ? | ◆ | ? | ◆ |
| ◆ | ◆ | ◆ | ? | ◆ | ◆ | ? | ◆ | ◆ |
| ◆ | ◆ | ? | ◆ | ◆ | ◆ | ◆ | ◆ | ◆ |
| ? | ◆ | ? | ? | ◆ | ? | ? | ◆ | ? |

n-by-m

Test_User

| | | | | | | | | |
|---|---|---|---|---|---|---|---|---|
| ◆ | ? | ◆ | ◆ | ? | ◆ | ◆ | ? | ◆ |
|---|---|---|---|---|---|---|---|---|

1-by-m

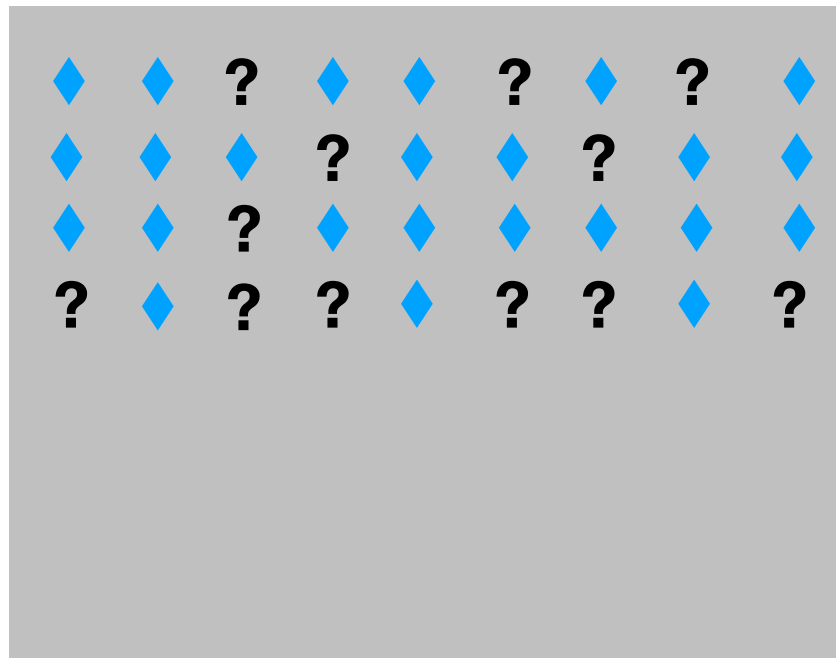
UBCF

- **Normalization:** Center each row for both train and test
- **Compute similarity** (cosine) between test and train
- **Find K nearest users** (i.e., users with highest similarities)
- **Compute the weighted average** of those K users ($K = 20$)

Movies

Similarity

Train_Users



n-by-m



n-by-1

Test_User



1-by-m

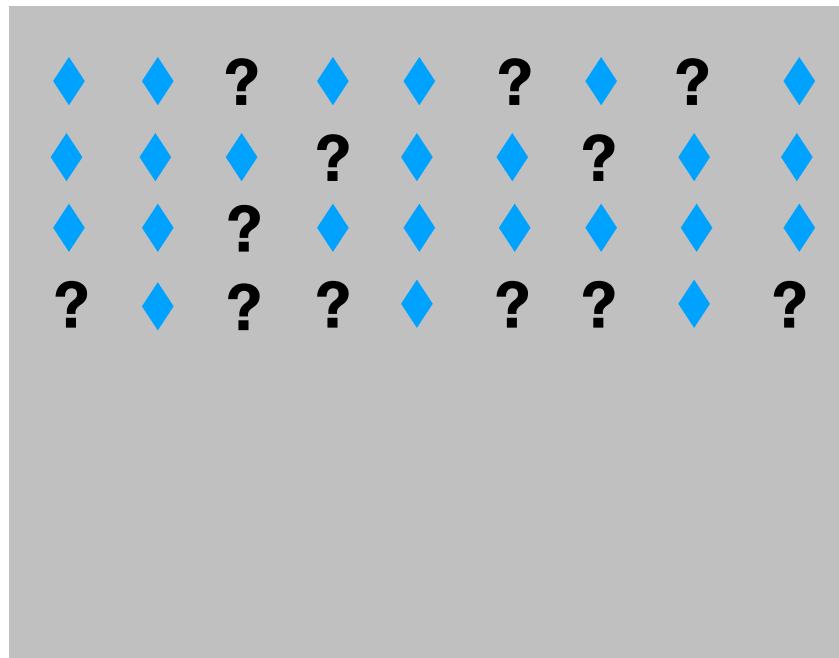
UBCF

- **Normalization:** Center each row for both train and test
- **Compute similarity** (cosine) between test and train
- **Find K nearest users** (i.e., users with highest similarities)
- **Compute the weighted average** of those K users (K = 20)

Movies

Similarity

Train_Users



n-by-m



n-by-1

Test_User



1-by-m

UBCF

**Be careful
with NAs**

- **Normalization:** Center each row for both train and test
- **Compute similarity** (cosine) between test and train
- **Find K nearest users** (i.e., users with highest similarities)
- **Compute the weighted average** of those K users (K = 20)
- Some additional steps before output your prediction

— **Normalization:** Center each row for both train and test

```
> train = Rmat[1:500, ]  
> test = Rmat[501, ]  
  
> data = as(train, "matrix")  
> user.means = rowMeans(data, na.rm = TRUE)  
> data = data - user.means  
  
> newdata = as(Rmat[501, ], "matrix")  
> newuser.mean = mean(newdata, na.rm = TRUE)  
> newdata = newdata - newuser.mean
```

— **Normalization:** Center each row for both train and test

```
> train = Rmat[1:500, ]
> test = Rmat[501, ]

> data = as(train, "matrix")
> user.means = rowMeans(data, na.rm = TRUE)
> data = data - user.means

> newdata = as(Rmat[501, ], "matrix")
> newuser.mean = mean(newdata, na.rm = TRUE)
> newdata = newdata - newuser.mean
```

$$\frac{\sum_{i \in S} x_i y_i}{\sqrt{\sum_{i \in S} x_i^2} \sqrt{\sum_{i \in S} y_i^2}}$$

$$S = \{i : x_i \text{ and } y_i \neq NA\}$$

— **Compute similarity** (cosine)

```
> sim = rep(0, dim(data)[1])
> for(i in 1:length(sim))
+ {
+   tmp.y = as.vector(newdata)
+   ind.y = which(!is.na(tmp.y))
+   tmp.x = data[i, ]
+   ind.x = which(!is.na(tmp.x))
+   ind = intersect(ind.x, ind.y)
+   if (length(ind) > 0){
+     tmp.x = tmp.x[ind]
+     tmp.y = tmp.y[ind]
+     sim[i] = sum(tmp.x * tmp.y) / sqrt(sum(tmp.x^2) * sum(tmp.y^2))
+   }
+ }
```

— **Normalization:** Center each row for both train and test

```
> train = Rmat[1:500, ]
> test = Rmat[501, ]

> data = as(train, "matrix")
> user.means = rowMeans(data, na.rm = TRUE)
> data = data - user.means

> newdata = as(Rmat[501, ], "matrix")
> newuser.mean = mean(newdata, na.rm = TRUE)
> newdata = newdata - newuser.mean
```

$$\frac{\sum_{i \in S} x_i y_i}{\sqrt{\sum_{i \in S} x_i^2} \sqrt{\sum_{i \in S} y_i^2}}$$

$$S = \{i : x_i \text{ and } y_i \neq NA\}$$

— **Compute similarity (cosine)**

```
> sim = rep(0, dim(data)[1])
> for(i in 1:length(sim))
+ {
+   tmp.y = as.vector(newdata)
+   ind.y = which(!is.na(tmp.y))
+   tmp.x = data[i, ]
+   ind.x = which(!is.na(tmp.x))
+   ind = intersect(ind.x, ind.y)
+   if (length(ind) > 0){
+     tmp.x = tmp.x[ind]
+     tmp.y = tmp.y[ind]
+     sim[i] = sum(tmp.x * tmp.y) / sqrt(sum(tmp.x^2) * sum(tmp.y^2))
+   }
+ }
> sim = (1 + sim)/2
```

Don't forget the transformation

— **Normalization:** Center each row for both train and test

```
> train = Rmat[1:500, ]
> test = Rmat[501, ]

> data = as(train, "matrix")
> user.means = rowMeans(data, na.rm = TRUE)
> data = data - user.means

> newdata = as(Rmat[501, ], "matrix")
> newuser.mean = mean(newdata, na.rm = TRUE)
> newdata = newdata - newuser.mean
```

$$\frac{\sum_{i \in S} x_i y_i}{\sqrt{\sum_{i \in S} x_i^2} \sqrt{\sum_{i \in S} y_i^2}}$$

$$S = \{i : x_i \text{ and } y_i \neq NA\}$$

— **Compute similarity (cosine)**

```
> sim = rep(0, dim(data)[1])
> for(i in 1:length(sim))
+ {
+   tmp.y = as.vector(newdata)
+   ind.y = which(!is.na(tmp.y))
+   tmp.x = data[i, ]
+   ind.x = which(!is.na(tmp.x))
+   ind = intersect(ind.x, ind.y)
+   if (length(ind) > 0){
+     tmp.x = tmp.x[ind]
+     tmp.y = tmp.y[ind]
+     sim[i] = sum(tmp.x * tmp.y) / sqrt(sum(tmp.x^2) * sum(tmp.y^2))
+   }
+ }
> sim = (1 + sim)/2
```

Don't forget the transformation

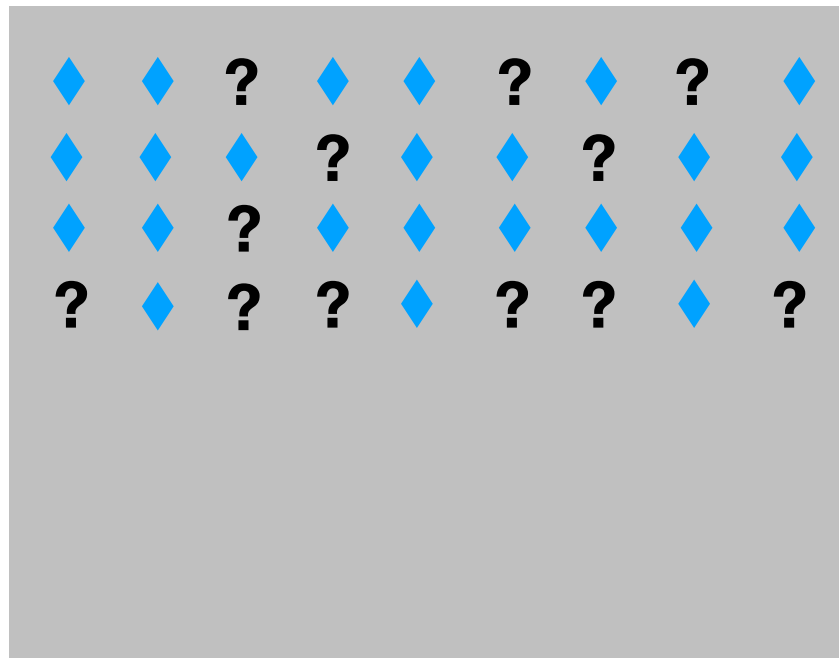
Alternative command

```
> sim1 = proxy::simil(data, newdata, method = "cosine")
> sim1 = (1 + sim1)/2
> sum((sim - sim1)^2)
[1] 3.37577e-29
```

Movies

Similarity

Train_Users



n-by-m



n-by-1

Test_User



1-by-m

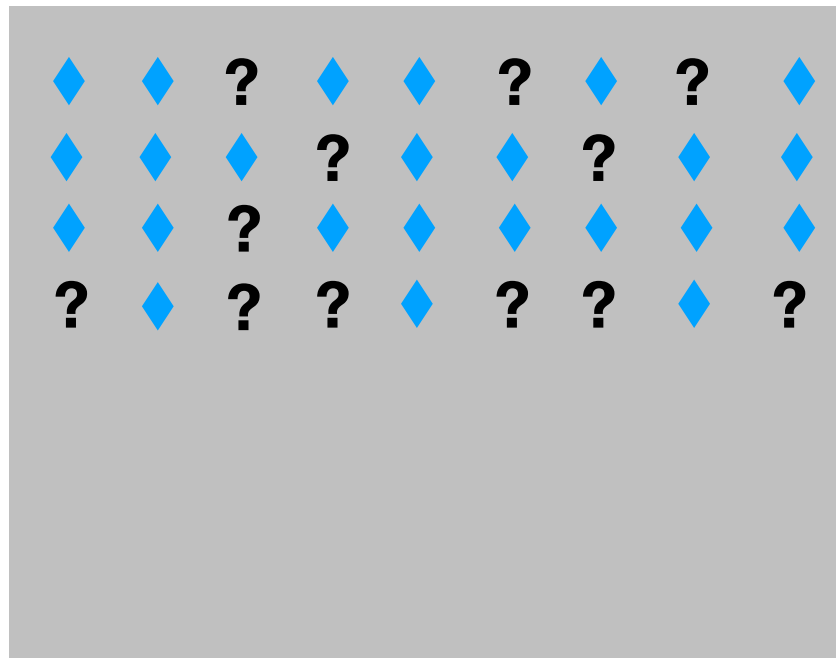
- Compute the weighted average of those K users (K = 20)

$$\text{mypred}[j] = \frac{\sum_{i \in S} s_i r_{ij}}{\sum_{i \in S} s_i} \quad S = \{i : s_i \text{ and } r_{ij} \text{ not NA}\}$$

Movies

Similarity

Train_Users



n-by-m



n-by-1

Test_User



1-by-m

Mypred



Some **additional steps** before output your prediction

1. Add back the mean of the test_user
2. Set infinite values to NA
3. Set movies watched by the test_user to NA