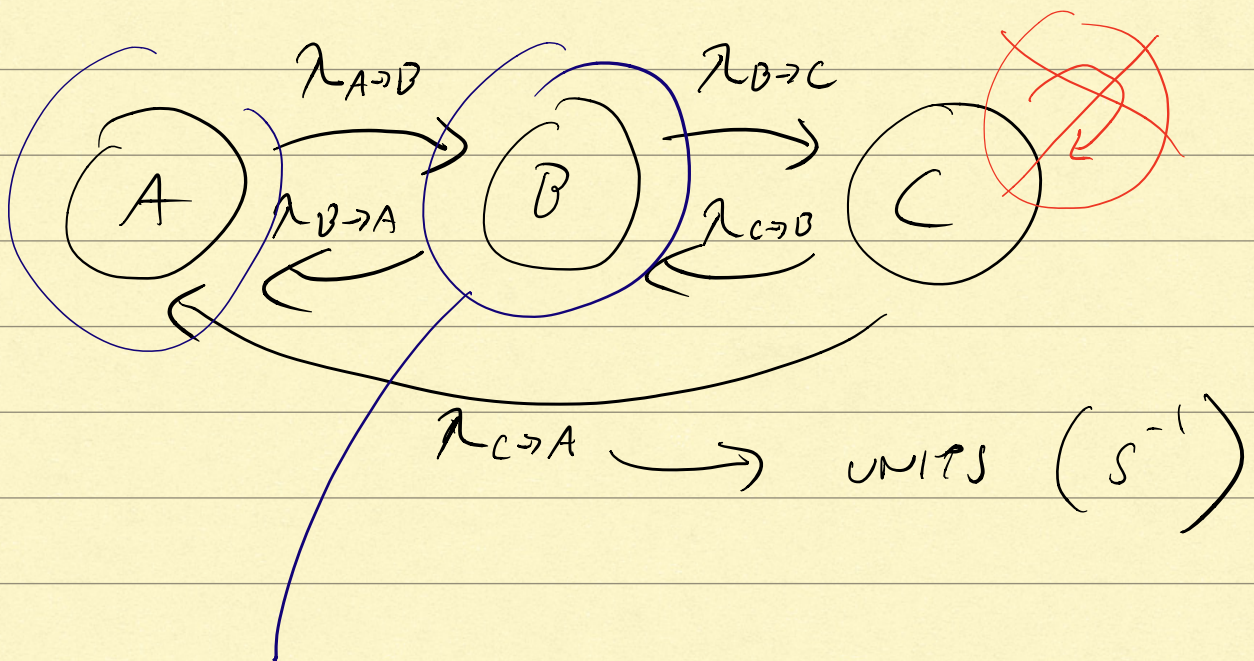
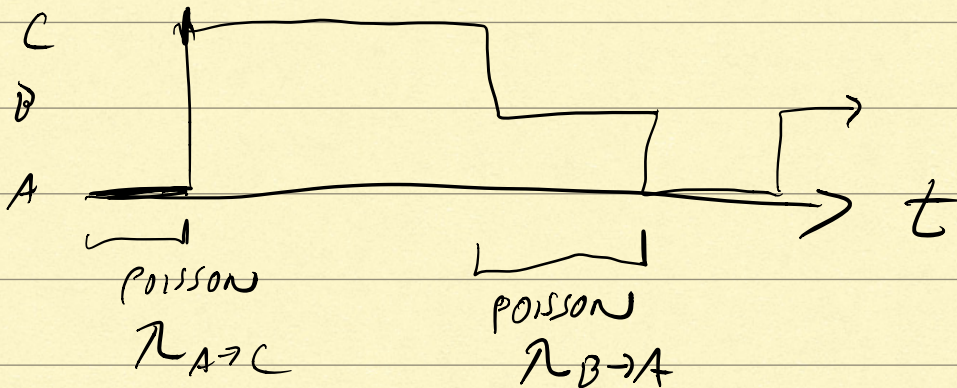


CONTINUOUS TIME MARKOV CHAINS

CONTINUOUS TIME STOCHASTIC PROCESS
WHERE STATE SPACE HAS N DISCRETE
STATES, AND TRANSITIONS BETWEEN
STATES ARE POISSON.



$B \rightarrow C$ $\lambda_{B \rightarrow C}$
 $B \rightarrow A$ $\lambda_{B \rightarrow A}$

NEXT WONT $B \rightarrow X$ POISSON RATE $\lambda_{B \rightarrow C}$

$$+ \lambda_{B \rightarrow A}$$

PROBABILITY $B \rightarrow C$: $\frac{\lambda_{B \rightarrow C}}{\lambda_{B \rightarrow C} + \lambda_{B \rightarrow A}}$

$P_i(t)$ - PROBABILITY OF BEING IN STATE i AT TIME t

LET $\vec{P}(t) = \begin{bmatrix} P_1(t) \\ \vdots \\ P_N(t) \end{bmatrix}$ THEN

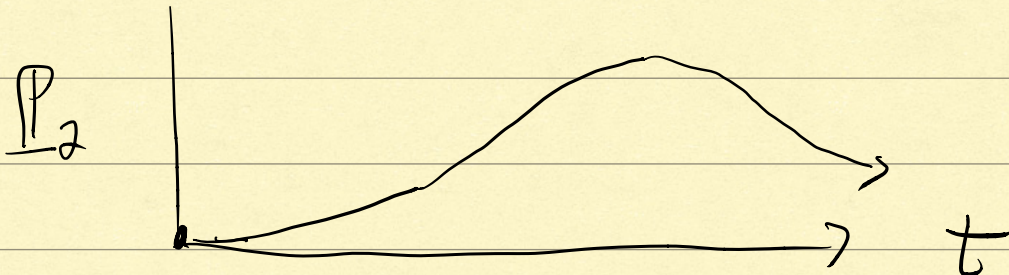
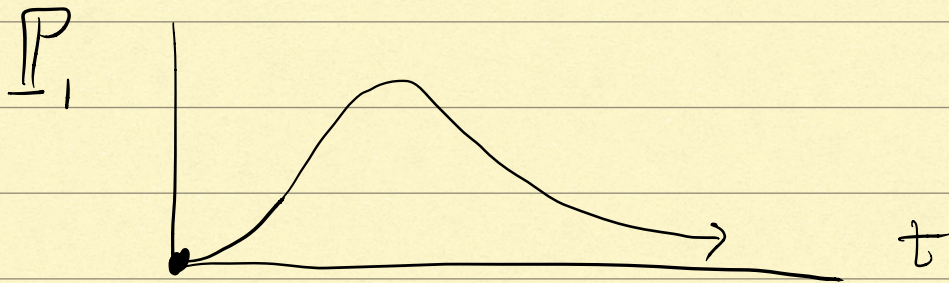
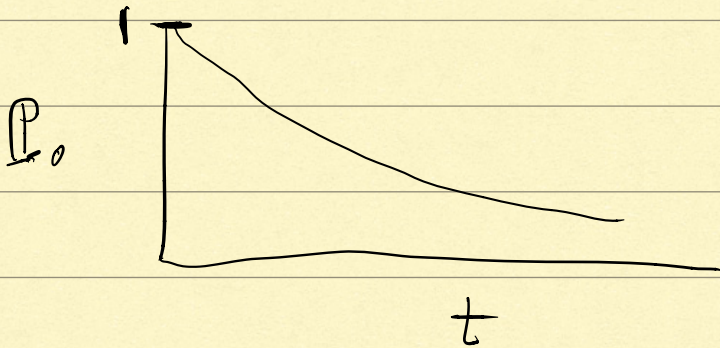
$$\frac{d}{dt} \vec{P}(t) = \begin{bmatrix} -\sum_i \lambda_{1 \rightarrow i} & & \lambda_{N \rightarrow 1} \\ \lambda_{1 \rightarrow 2} & \ddots & \\ & \ddots & \\ \lambda_{1 \rightarrow N} & & -\sum_i \lambda_{N \rightarrow i} \end{bmatrix} \cdot \vec{P}(t)$$

EX $N(t)$ - # OF POISSON EVENTS AT TIME t

MATRIX = $\begin{bmatrix} -\lambda & 0 & 0 & \ddots \\ \lambda & -\lambda & 0 & \\ 0 & \lambda & -\lambda & \\ & & & \ddots \end{bmatrix}$

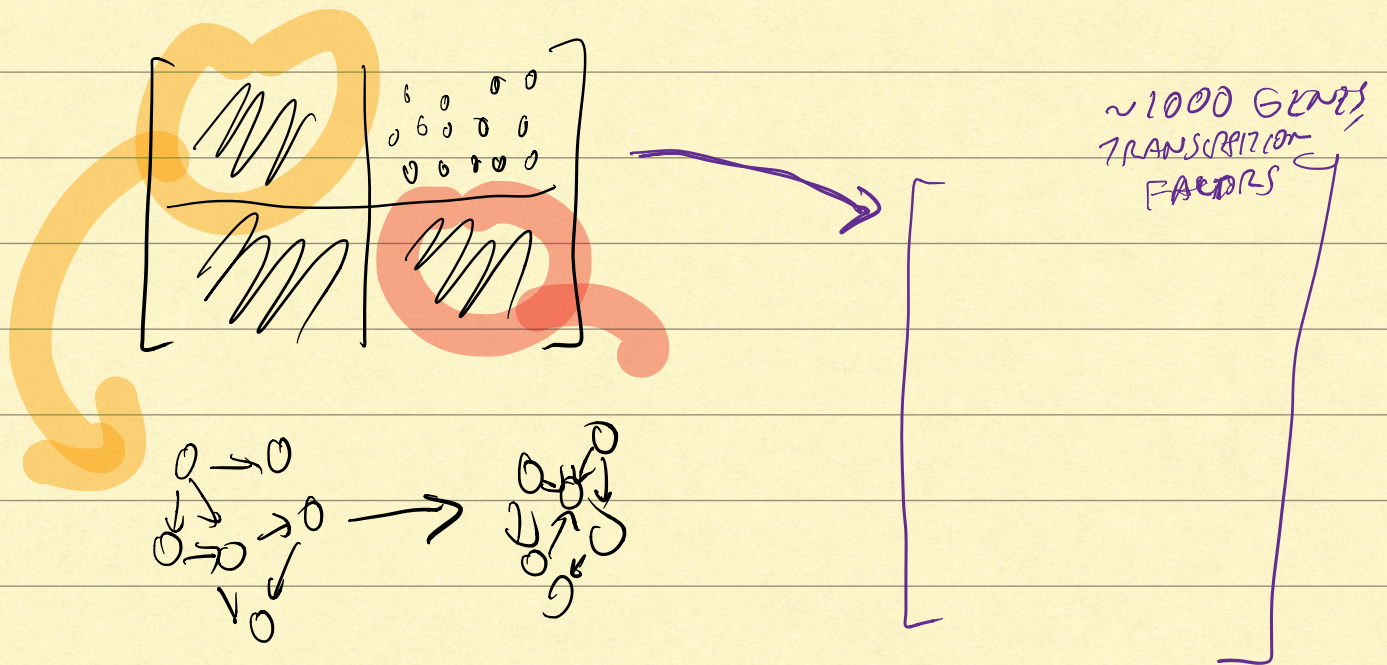
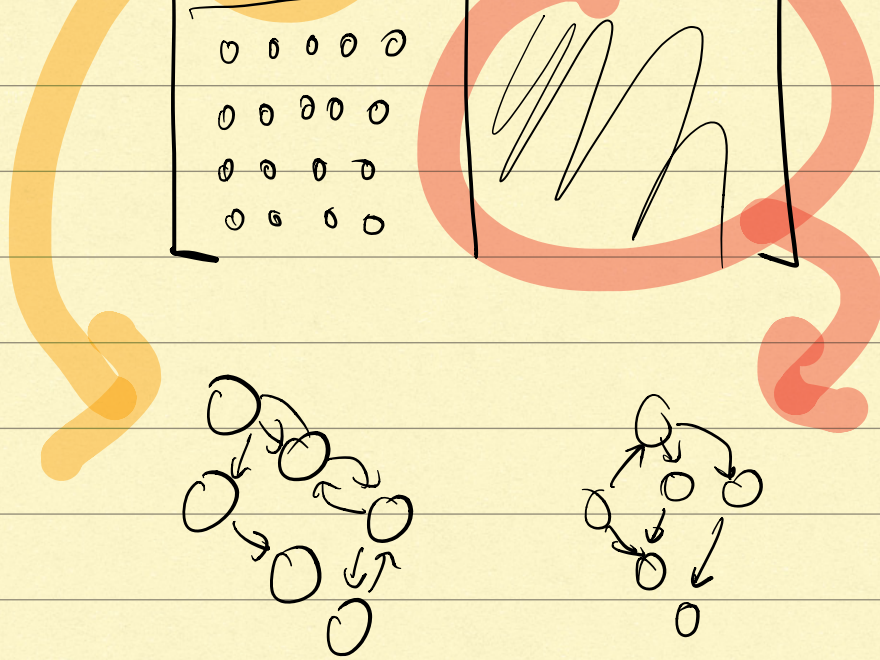
$$\begin{bmatrix} 0 & 0 & \lambda & -\lambda \\ 0 & 0 & 0 & \lambda & \dots \end{bmatrix}$$

$$\vec{P}(0) = \begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$



EX.

$$\left[\begin{array}{c|c} \text{[scribbles]} & \begin{matrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \end{matrix} \end{array} \right]$$



PS5

