

[Brief Review\*]

# Interior Product, Lie derivative and Wilson Line in the $KBc$ Subsector of Open String Field Theory

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$KBc$  algebra has been described classical solutions like tachyon condensation and multi-Dp branes. These solutions have singularities as  $K$  approaches 0, but reproduce the exact energies expected by string theory.  $K$ ,  $B$  and  $c$  are defined thorough

$$K = \int_{-i\infty}^{i\infty} \frac{dz}{2\pi i} T(z), \quad B = \int_{-i\infty}^{i\infty} \frac{dz}{2\pi i} b(z), \quad c = c(0), \quad (1)$$

where  $T$  is the energy-momentum tensor,  $b$  is the anti-ghost field, and  $c$  is the ghost field. These operators are supposed to be in the sliver frame, which is the region related to the radial coordinate  $\xi$  by  $z = (2/\pi) \arctan \xi$  (see [1] for the review).  $K$ ,  $B$  and  $c$  satisfies the following relations with the BRST operator  $Q_B$ :

$$[K, B] = 0, \quad \{B, c\} = 1, \quad B^2 = 0, \quad c^2 = 0, \quad (2)$$

$$Q_B K = 0, \quad Q_B B = K, \quad Q_B c = cKc. \quad (3)$$

We addressed how to emerge Chan-Paton factors around the multi-Dp brane solution found by Murata and Schnabl [2]. Comparing with the action with Chan-Paton factors, the fluctuation  $\Delta\Psi$  around the solution of  $N$  branes is expected to expanded by the modified form of vertex operators  $V_a^\dagger \mathcal{O}_F(k) V_b$  with some operators  $V_a$  ( $a = 1, \dots, N$ ) carrying no ghost. Then we find that the question becomes whether there exist  $N$  operators  $V_a$  satisfying

$$V_a(\overleftarrow{Q}_B + \Psi_0) = 0 \quad \text{and} \quad V_a V_b^\dagger = \delta_{ab}, \quad (4)$$

where  $\Psi_0$  is the solution of  $N$  branes and  $A\overleftarrow{Q}_B = -(-1)^{|A|}Q_B A$ . The similar equation for the former can be seen in Wilson lines of gauge theories, and the formal resemblance between SFT and Chern-Simons theory has been known, so we are driven to find the correspondence of Wilson line in SFT.

In the process to find this, we established the  $KBc$  manifold, which includes infinite sets of distinct  $(K, B, c)$ , of course satisfying  $KBc$  algebra, as its points. On the manifold, we succeeded in finding the interior product, Lie derivative and Lie bracket. The Lie derivative gives infinitesimal deformations in the space of solutions. By using the interior product, we finally obtained a candidate for the SFT Wilson line. However, the task to solve (4) is still left, and the information about  $KBc$  manifold may be not enough. For example, formulas for the interior product and the Lie derivative in the SFT side are slightly different from in the Chern-Simons side.

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## References

- [1] Y. Okawa, *Analytic methods in open string field theory*, *Prog. Theor. Phys.* **128** (2012) 1001.
- [2] M. Murata and M. Schnabl, *On Multibrane Solutions in Open String Field Theory*, *Prog. Theor. Phys. Suppl.* **188** (2011) 50 [1103.1382].