

$$N(E) = \delta(E - E_0) \text{ theoretical.}$$

$$N(E) = \begin{cases} N_0 & E > E_0 \\ \emptyset & E \neq E_0 \end{cases}$$

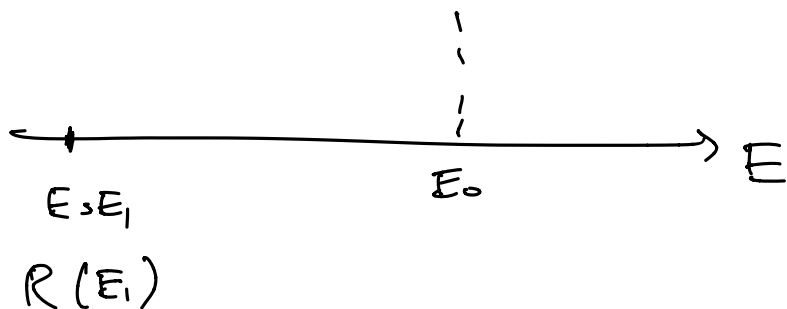
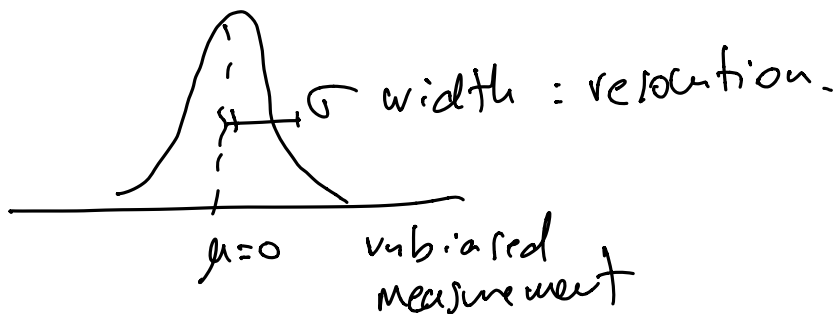
$$N(E) \longrightarrow R(E)$$

$$R(E) = \int_{-\infty}^{+\infty} N(E') G(E - E' | \mu = 0, \sigma) dE'$$

physics input

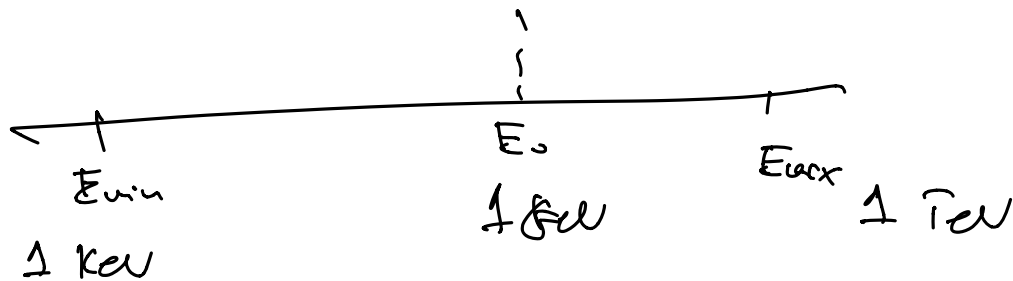
Detector resolution

Best case scenario: Gaussian.



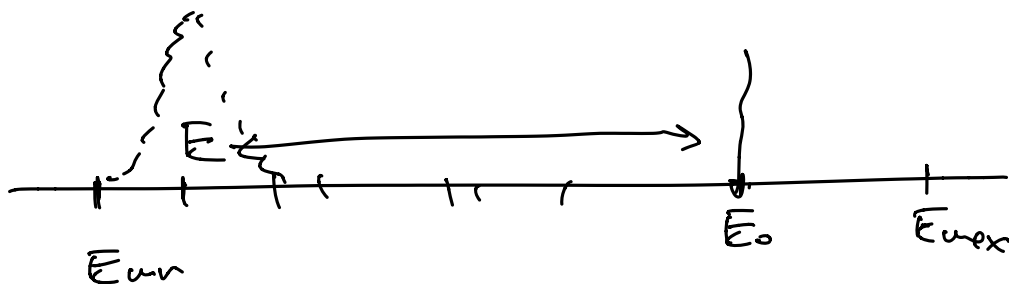
$$R(E) = \sum_{E_i} N(E_i) G(E-E_i | \mu=0, \sigma)$$

$$E_i \in [E_{min}, E_{max}]$$



E_{min}, E_{max}
 best estimator of $-\infty$ best estimator of $+\infty$

$$E_{min} = E_0 - S \times \sigma, \quad E_{max} = E_0 + S \sigma$$



$$G(E-E_0) \quad E-E_0 \leq S\sigma$$

$$G(E-E_0) = e^{-\frac{(E-E_0)^2}{2\sigma^2}} \quad = \emptyset$$

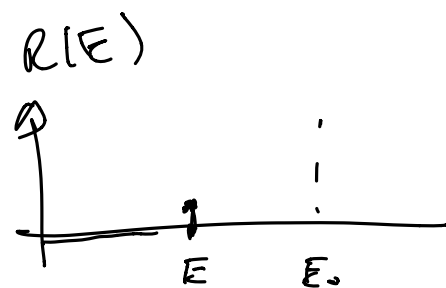
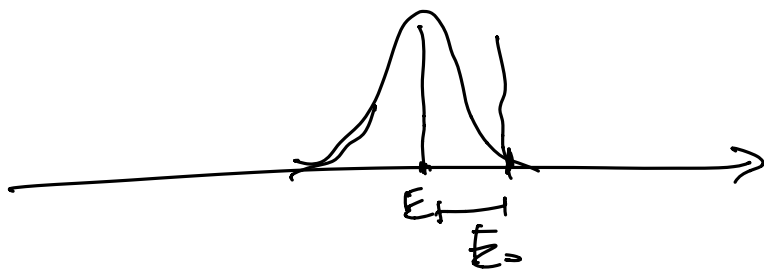
$$N(E) \neq 0 \quad E \leq E_0$$

$$E' \leq E_0$$

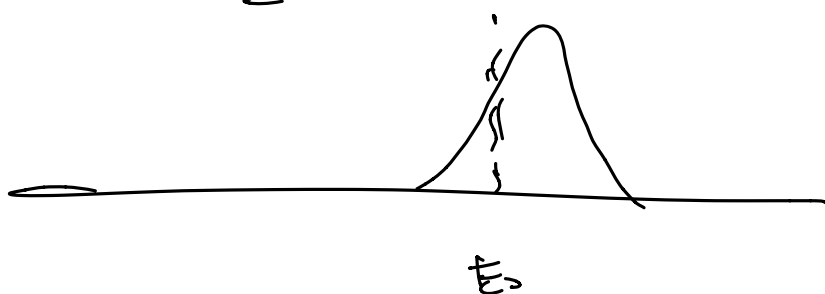
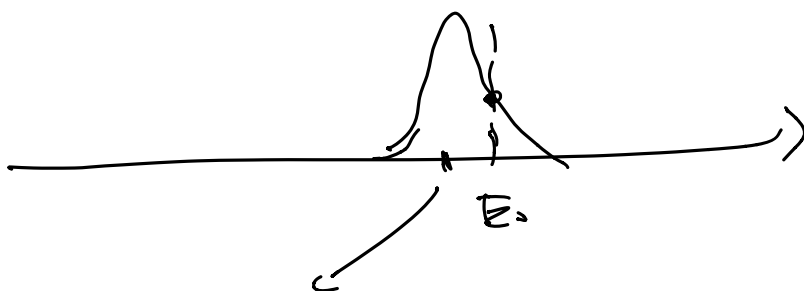
$$R(E) \simeq G(E-E_0) N(E_0)$$



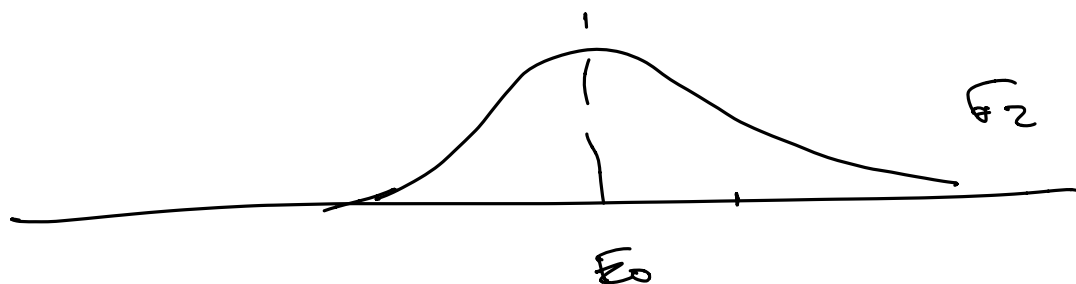
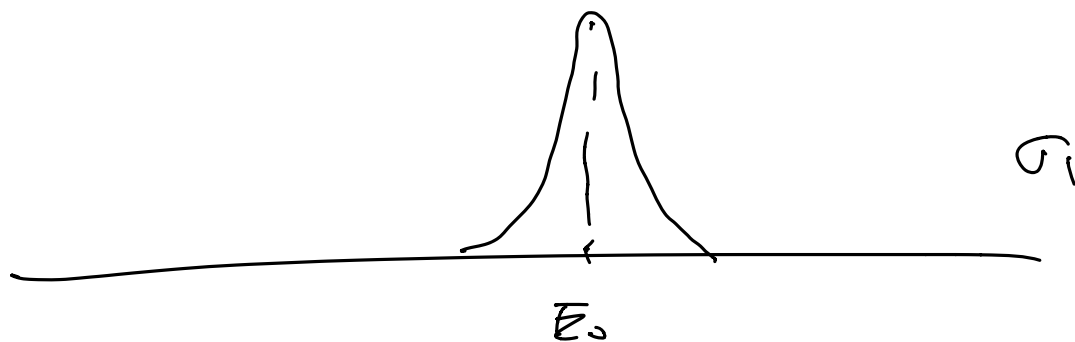
$$R(E) \simeq \emptyset.$$

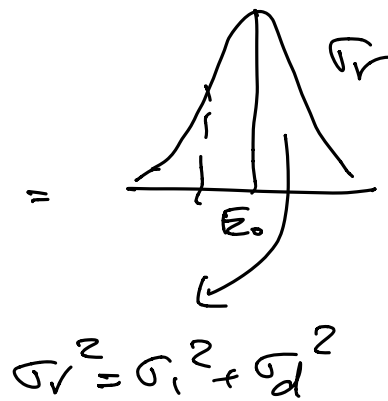


$$E - E_0 \approx 3\sigma \Rightarrow G \neq 0$$



$R(E)$



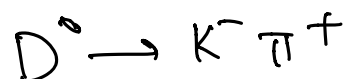


$$\underline{N \otimes G} \equiv \int_{-\infty}^{+\infty} N(E') G(E-E' | \mu=0, \sigma) dE'$$

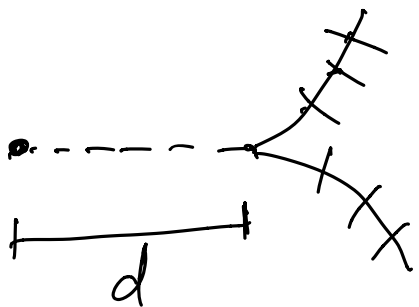
Lifetime of particles

unstable particles: lifetime τ

$$N(t) = N_0 e^{-t/\tau}$$



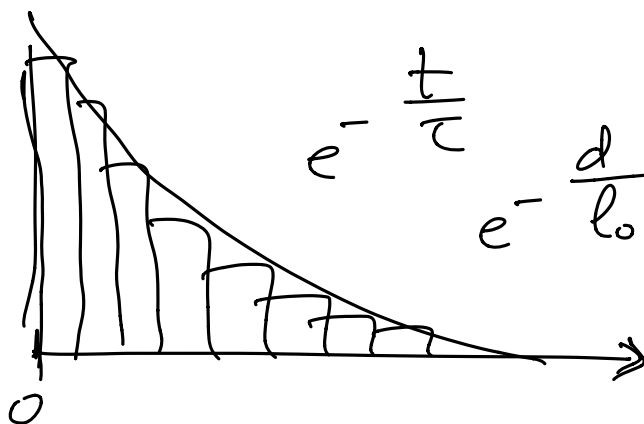
⊙ B



$$d = \beta \gamma c \tau$$

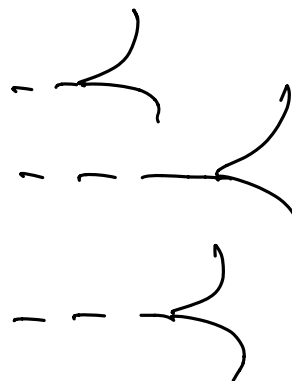
$\beta \gamma$ of D^0

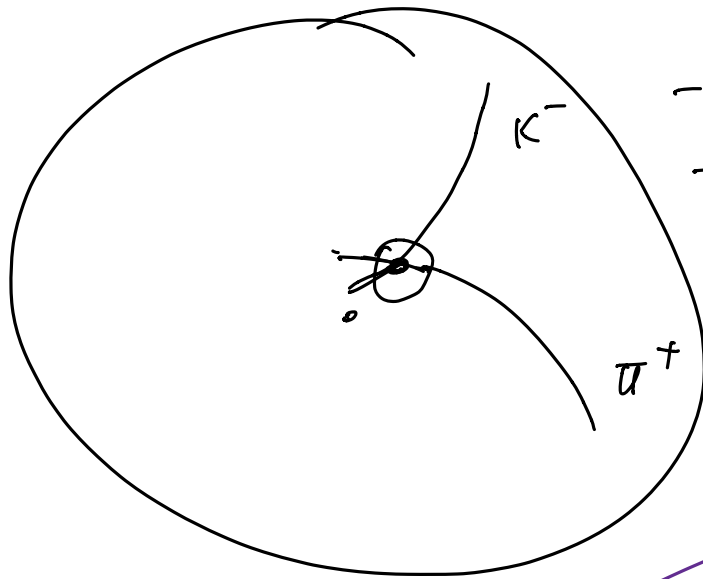
Experimentally \vec{p} for $K^- \pi^+$



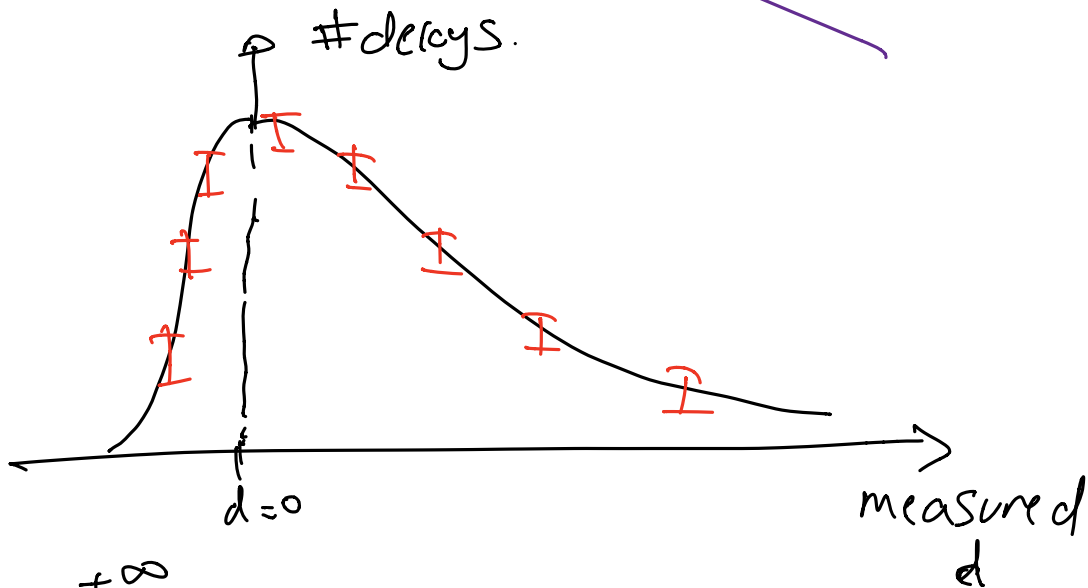
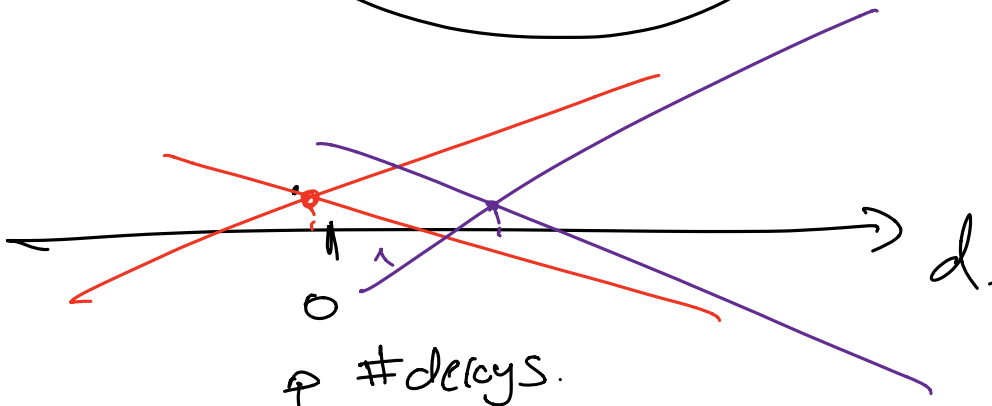
$$e^{-\frac{t}{\tau}}$$

$$e^{-\frac{d}{\ell_0}}$$

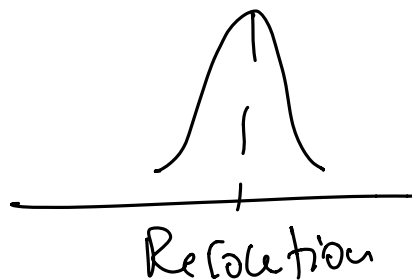
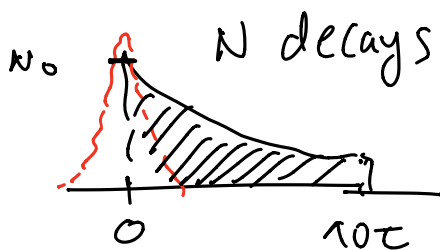




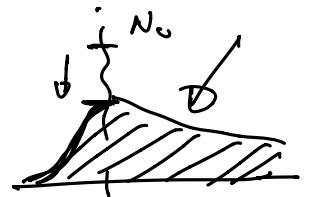
- First identify $K^- \pi^-$
- estimate decay vertex

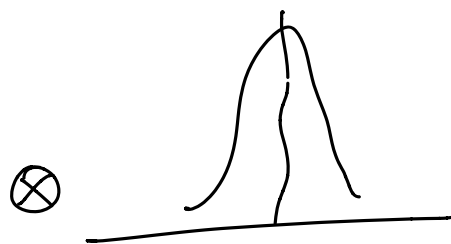
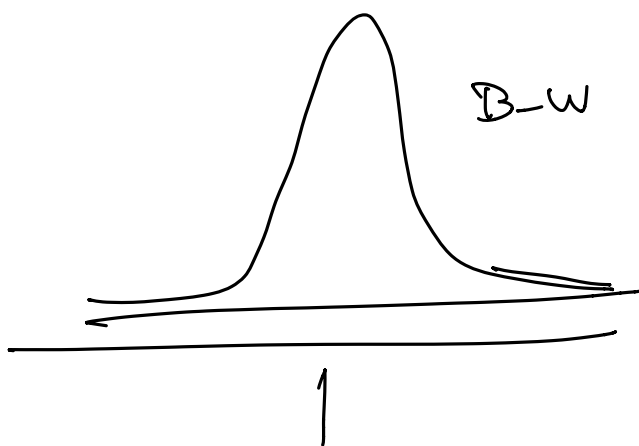
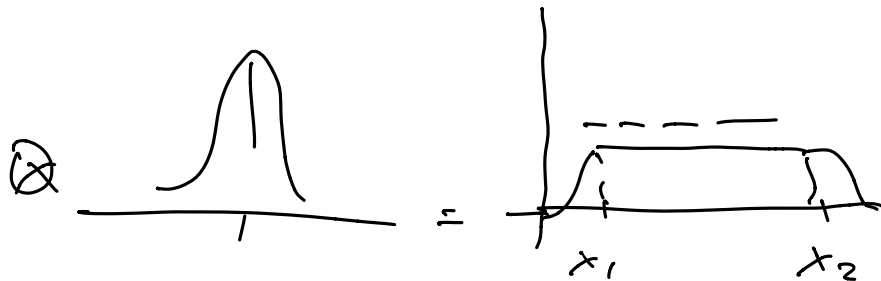
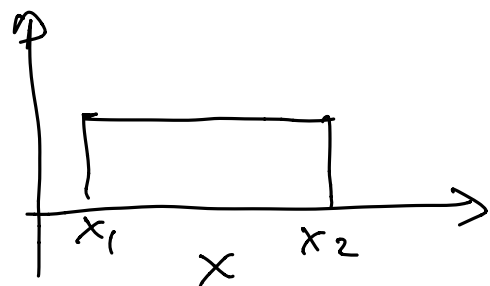
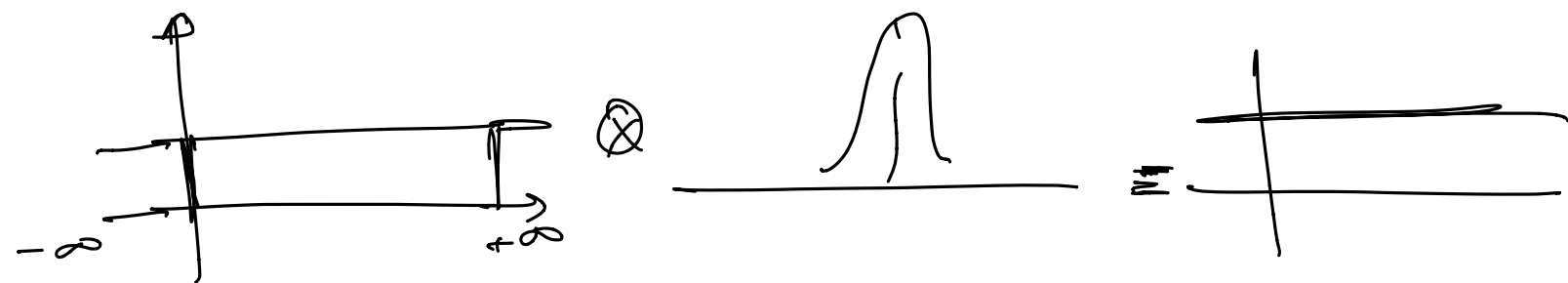


$$\text{Decay}(x) = \int_{-\infty}^{+\infty} \text{Real Decay}(x') G(x-x' | \mu=0, \sigma) dx'$$



=





$$\frac{1}{(E - E_0)^2 + \Gamma^2}$$

Detector with resolution 10%
 total energy of 3 GeV = E_0

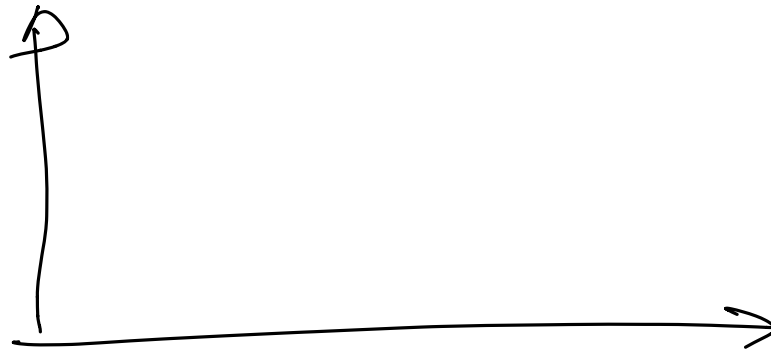
$$\sigma = 10\% \times E_0 = 300 \text{ MeV} = 0.3 \text{ GeV}$$

3 ± 0.1 ERROR



⊗

G ()



Draw THIF before and after

THIF h1 ("h1", "before conv", ---)

THIF h2 ("h2", "after conv", ---)

h1.Draw()

h2.Draw("same")