

You must submit your exam by **Friday Sep 13 at 17:00** following the instruction at <http://www.roma1.infn.it/people/rahatlou/cmp/>

### Bethe-Bloch formula

The [Bethe-Bloch formula](#) provides an accurate estimate of the average energy loss of relativistic particles due to ionisation ( $dE/dx$ ) in mater. The scope of this exercise is to simulate the distribution of  $dE/dx$  for protons in lead (Pb). The dimensions of the detector or not relevant for this exercise. You need to use the ROOT libraries.

1. Generate  $10^5$  protons with momentum in the range [300 MeV, 1000 TeV]
2. For each proton compute the average energy loss  $\langle dE/dx \rangle$  according to the Bethe-Bloch formula
3. The effective energy loss  $dE/dx$  for the particle must be extracted from a Gaussian distribution with mean of  $\langle dE/dx \rangle$  and a width of

$$10\% - 5\% \times \frac{\beta\gamma}{1000}$$

where  $\beta\gamma$  is that of the particle.

4. Make a 2D plot of  $dE/dx$  as a function of momentum for all protons using the [ROOT TH2F](#) class. Use appropriate binning, axis scale, and draw options to obtain a good-looking plot and save it as PDF.
5. Use the [ROOT TProfile](#) class to plot the mean  $dE/dx$  and its standard deviation in bins of momentum for all protons. Store a copy of the plot as a PDF file.

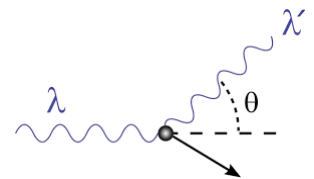
Provide instructions for compiling your code in the comments at the beginning of `_exam.cc` .

### Spectrum of Compton Scattering

Cesium-137 is a radioactive isotope which decays via beta emission (half life of 30.2 years) to a an excited metastable state of Barium  $^{137m}\text{Ba}$ . This state decays with a half-life of 153 seconds to the ground state  $^{137}\text{Ba}$  emitting a photon with energy  $E_0 = 662$  keV. We want to study the spectrum of  $^{137}\text{Cs}$  and the effect of Compton scattering.

6. Generate 10000 photons with energy  $E_0$ .
7. Each photon is detected with a NaI crystal which has a resolution of 3%. Use a Gaussian convolution and plot the distribution of detected energy  $E_i$  of all photons. Make sure reasonable binning are used for the histogram and labels and units are added. The expected distribution should be a Gaussian entered at  $E_0$ .
8. Assume that each photon has a 60% probability of undergoing Compton scattering in the crystal.
9. The energy  $E_f$  of the photon after the scattering is given by  

$$E_f = \frac{E_i}{1 + (E_i/m_e)(1 - \cos\theta)}$$
 where  $m_e$  is the mass of the electron (511 keV) and  $\theta$  is the angle of the photon after scattering as shown in the figure.



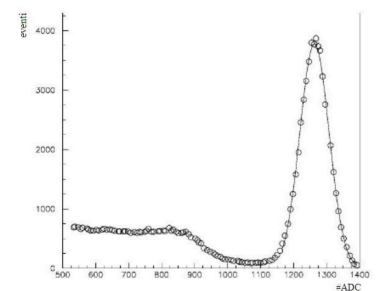
10. The angle  $\theta$  must be generated casually assuming that the differential cross section

$$\frac{d\sigma}{d\cos\theta} \propto 1 + \cos^2\theta$$

If you do not know how to do this, you can generate a flat distribution for  $\theta$  (with a penalty).

11. Plot the distribution of for all 10000 photons. You should still see a peak around  $E_0$  and a continuous distribution (a Fermi-Dirac shape) for  $E_f < 0$ .

Save a PDF file for each of the above 2 plots. Use comprehensions and dictionaries to implement the simulation and plotting the required plots. Define a function **Compton** (with proper arguments and return values) to simulate the scattering for each photon of energy  $E_i$  at each step for each particle.



Evaluation will be based on use of python features and data structures, comprehensions (instead of C-style for loops), dictionaries, NumPy objects, labels, units, and clarity of plots.