

Orbital Mechanics Final Project



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Group 2163

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Interplanetary Mission – Preliminary Analysis

Jupiter – Earth – Venus

- Earliest departure date:
2025/08/01
- Latest arrival date:
2065/08/01

Selected ToFs:

	ToF1	ToF2
min	500	50
max	3000	1500

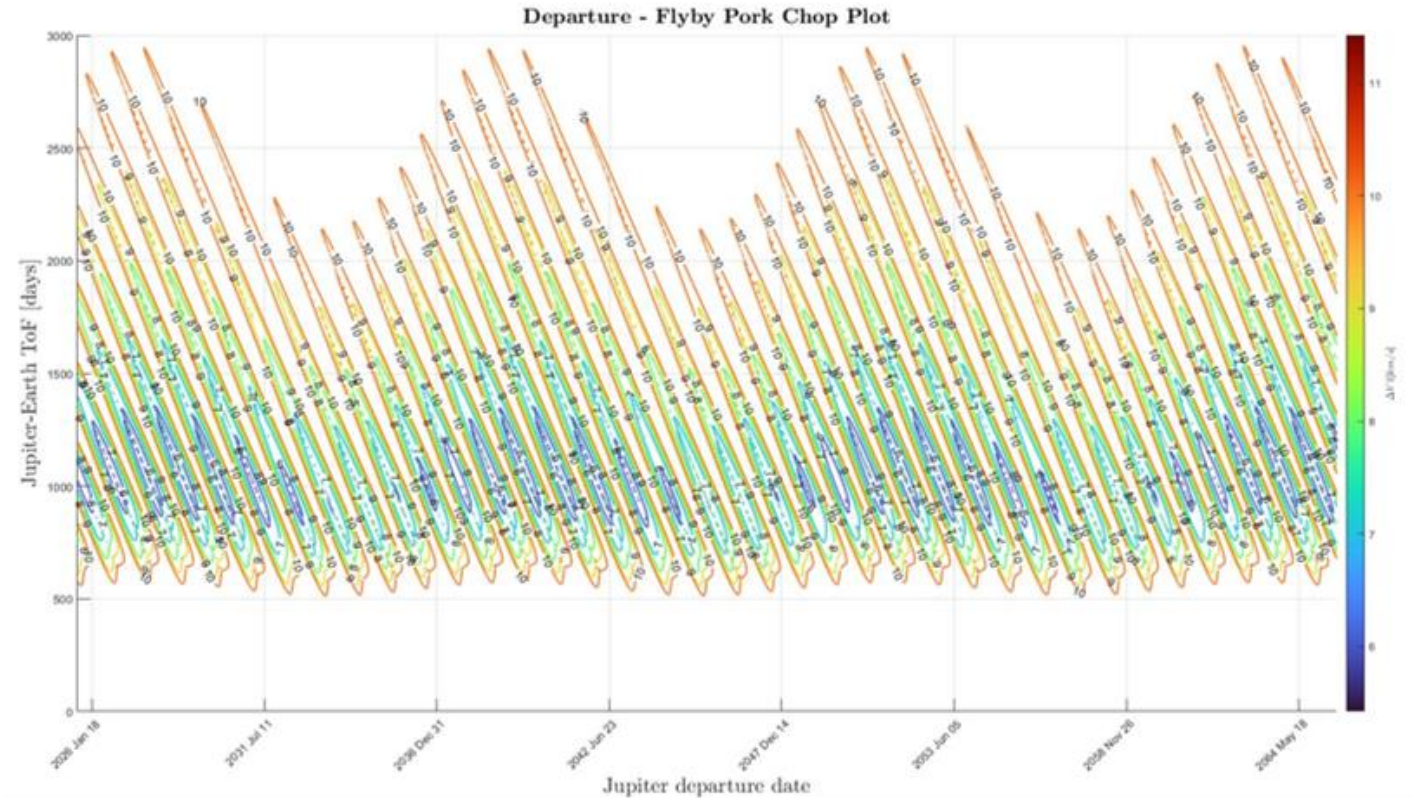


Figure 1: Departure – Flyby Pork Chop Plot



Interplanetary Mission – Preliminary Analysis

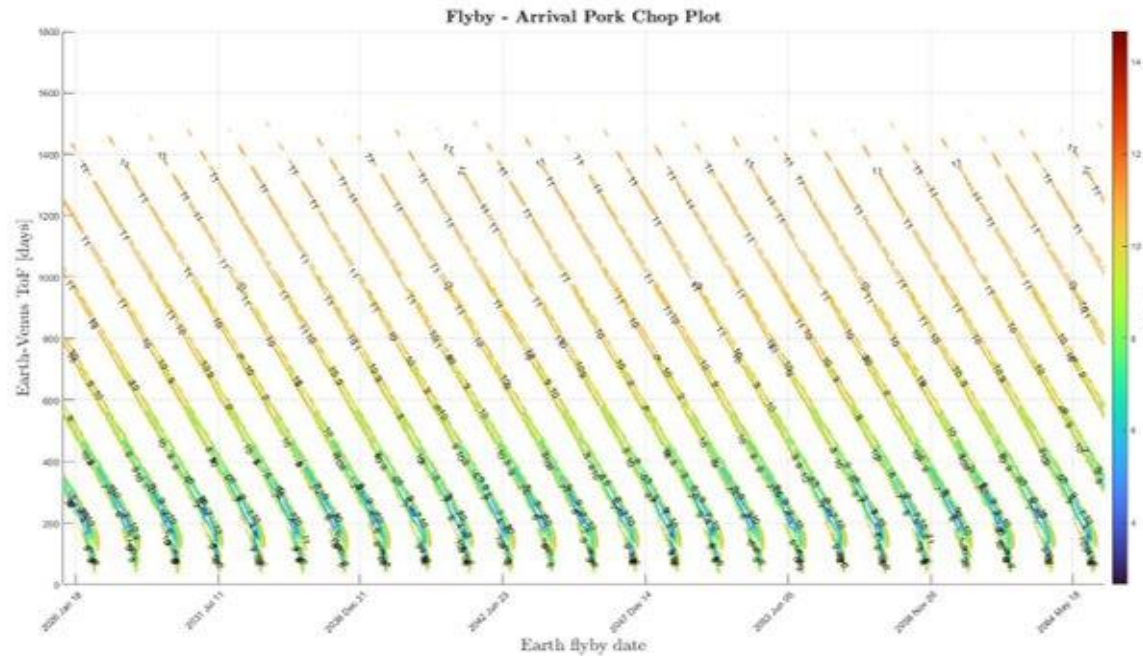


Figure 2: Flyby – Arrival Pork Chop Plot

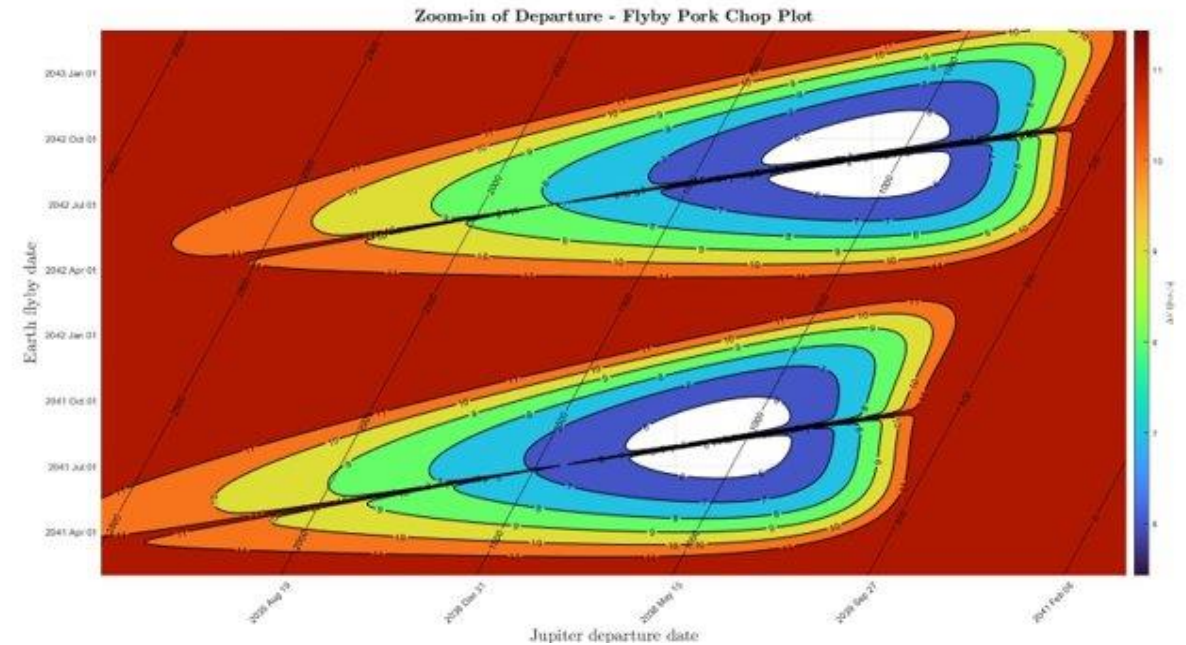


Figure 3: Zoomed Departure – Flyby Pork Chop Plot



Interplanetary Mission – Preliminary Analysis

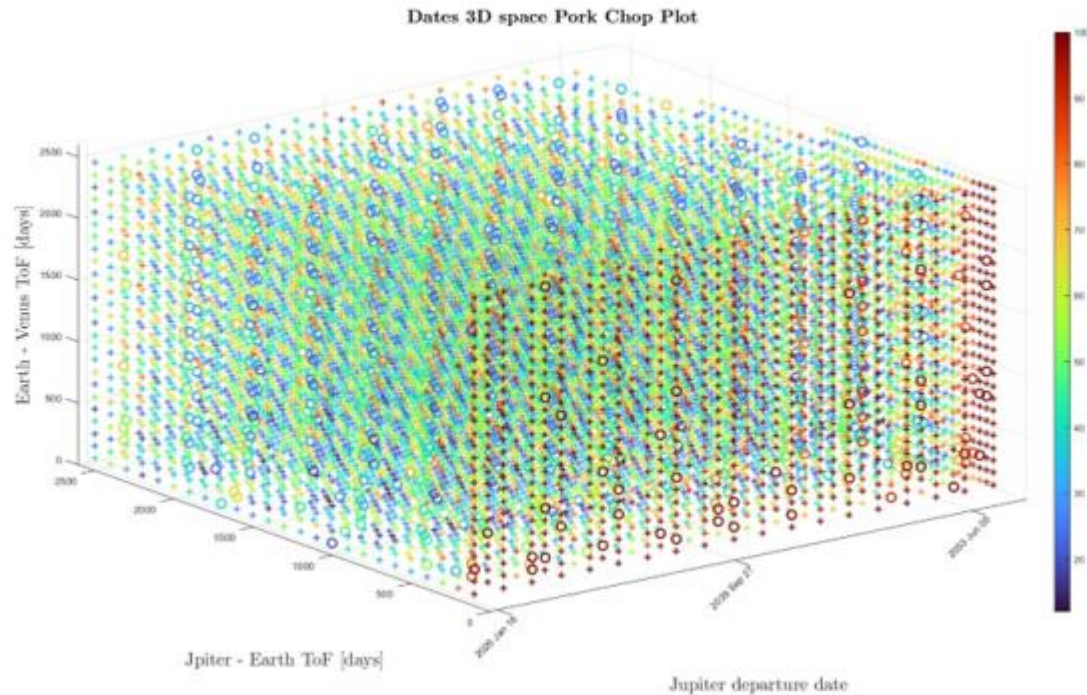


Figure 4: 3D Pork Chop Plot in ToFs space

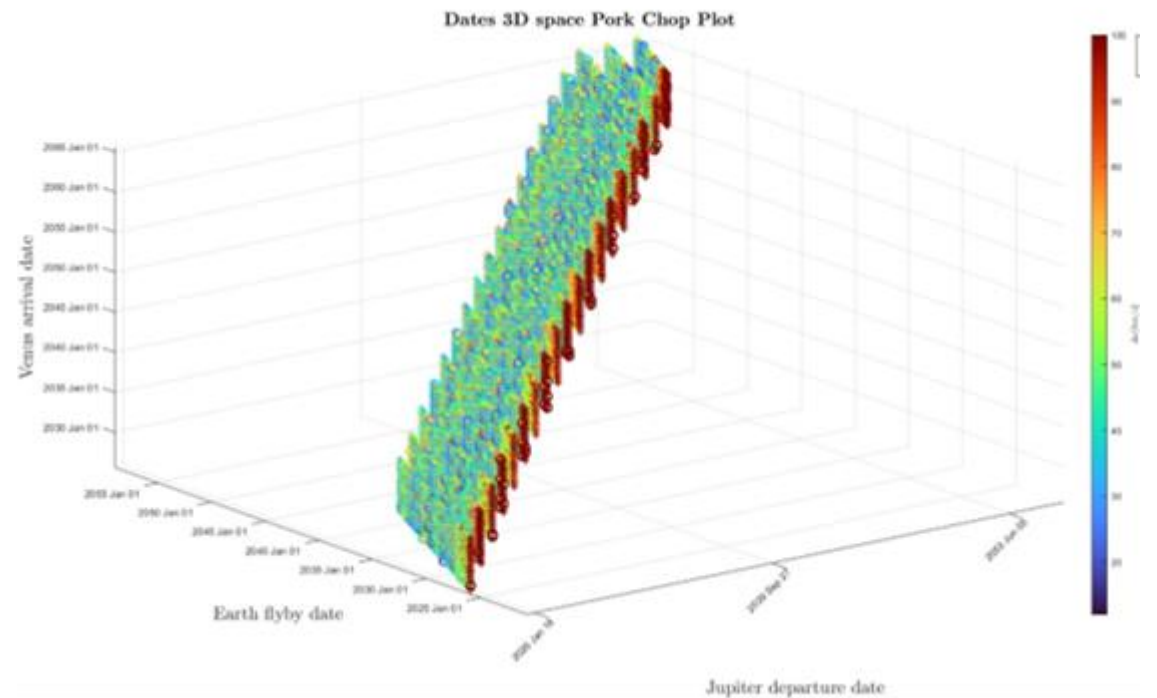
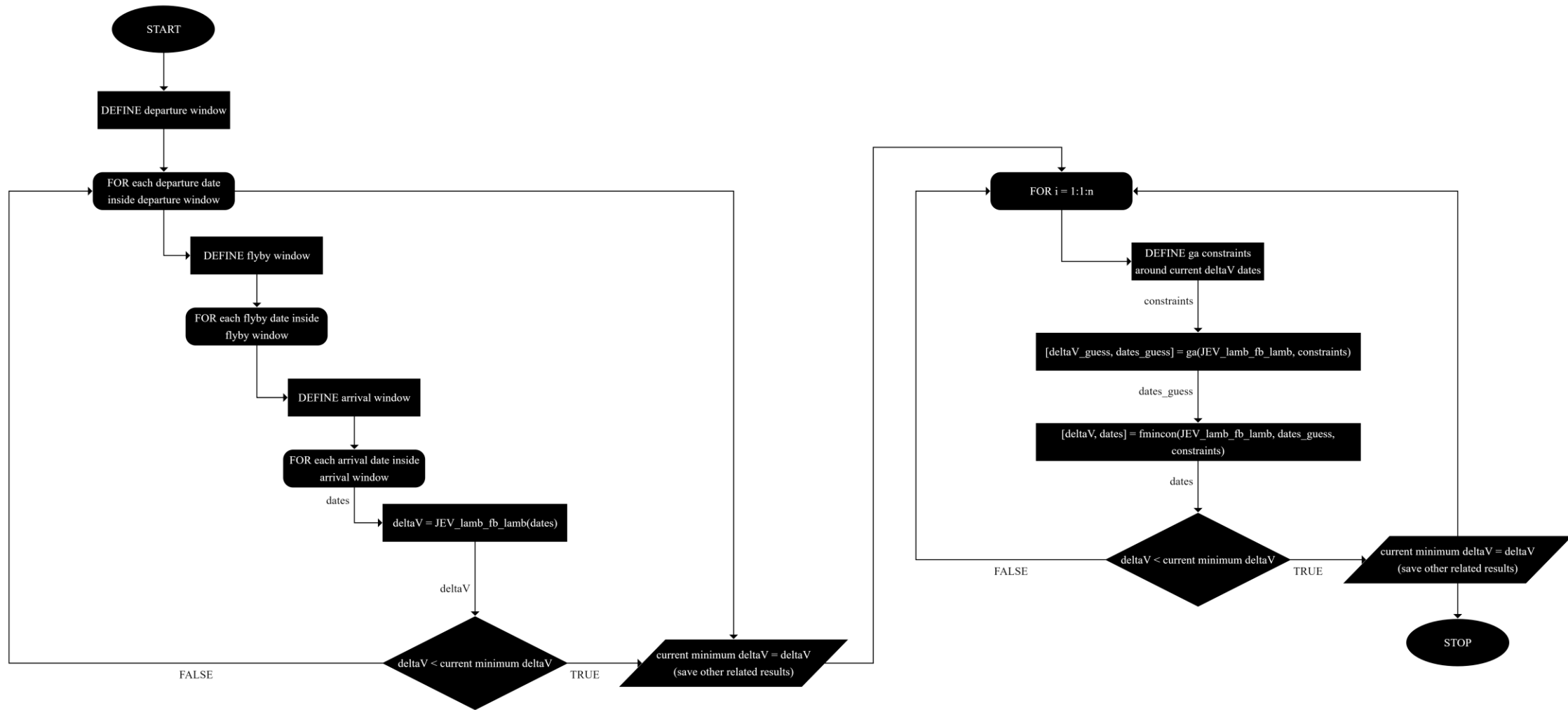


Figure 5: 3D Pork Chop Plot in dates space



Interplanetary Mission – Method 1

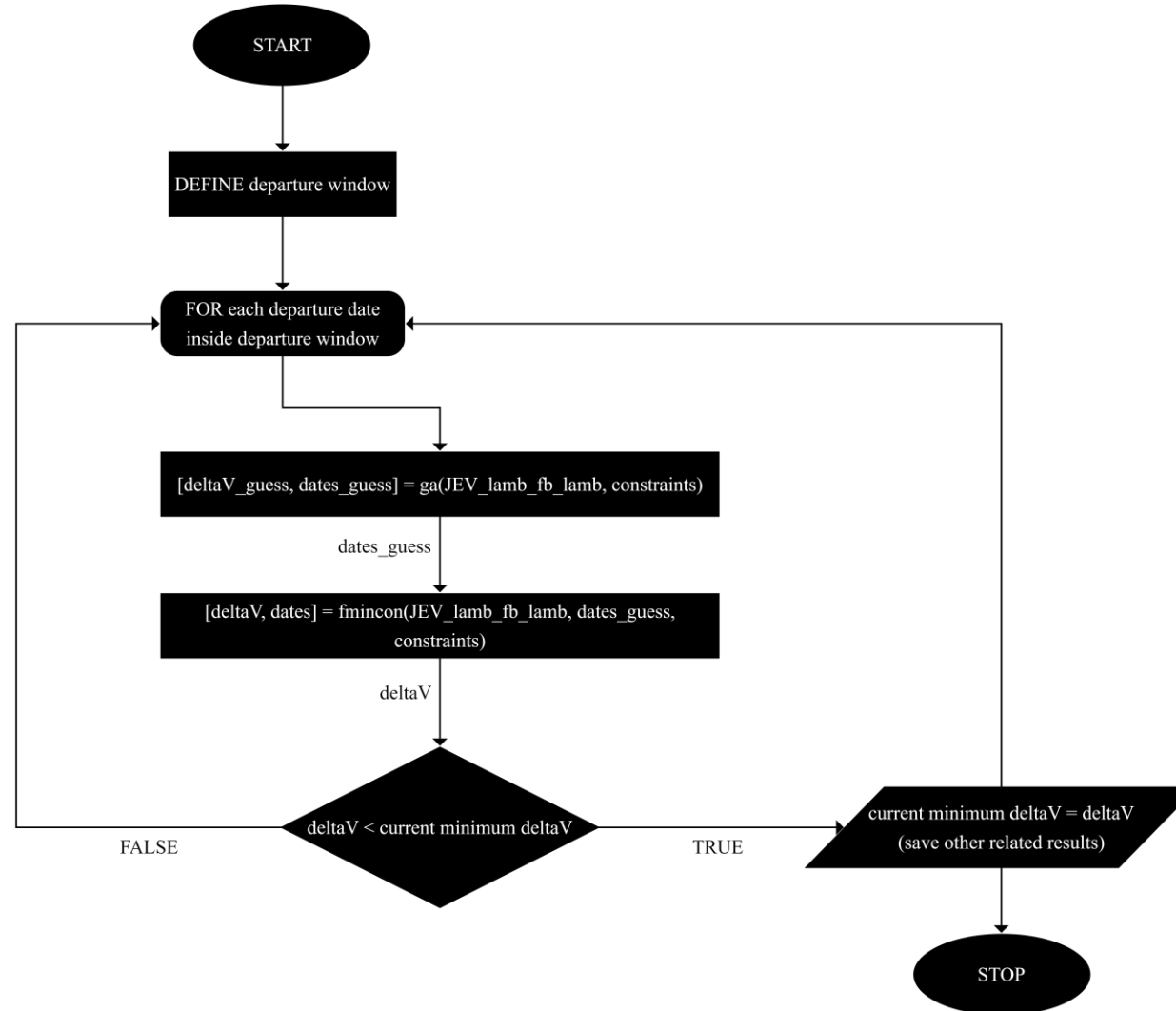


Interplanetary Mission – Method 1 Mesh Convergence

Discretization Grid	Departure window time step [days]	First ToF time step [days]	Second ToF time step [days]	Run time [sec]	Δv [km/sec]
250x75x75	58.4	33.3	33.3	1115	13.8063
250x100x100	58.4	25	15	2547	13.4847
250x150x150	58.4	16.7	10	4470	13.2796
300x150x150	48.6	16.7	10	7286	13.3454
300x200x200	48.6	12.5	7.5	9498	13.3211
350x200x200	41.7	12.5	7.5	12664	13.3311
350x250x250	41.7	10	6	15832	13.3046
400x250x250	36.5	10	6	17558	13.2169



Interplanetary Mission – Method 2



Interplanetary Mission – Method 2 Mesh Convergence

Departure discretization	Departure window Time step [days]	Run Time [sec]	Δv [km/sec]
175 sub-windows	83.5	3159	13.5385
200 sub-windows	73.1	5073	13.5084
225 sub-windows	65	6872	13.4163
250 sub-windows	58.4	6692	13.4229
300 sub-windows	48.7	8147	13.4158
500 sub-windows	29.2	12432	13.2534
600 sub-windows	24.3	16364	13.2702



Interplanetary Mission – Results

	Departure	Flyby	Arrival
Date	12/30/2040	11/21/2043	03/03/2045
Natural Flyby Δv		6.71739 [km/sec]	
Total Δv required		13.2169 [km/sec]	
Perigee passage altitude		301 [km]	
Time inside Earth SOI		138138 [sec]	



Interplanetary Mission – Results

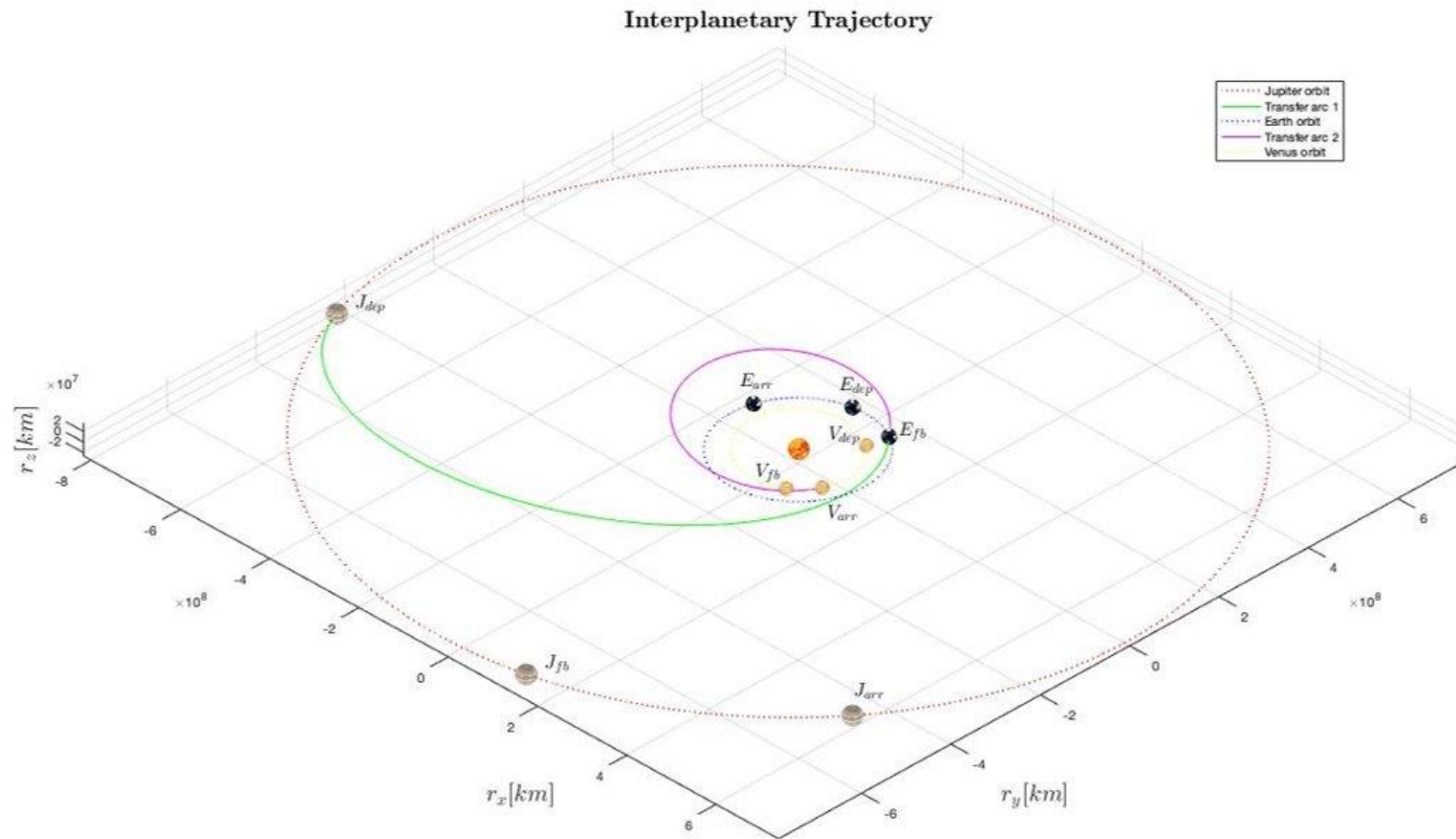


Figure 6: Interplanetary Trajectory



Interplanetary Mission – Results

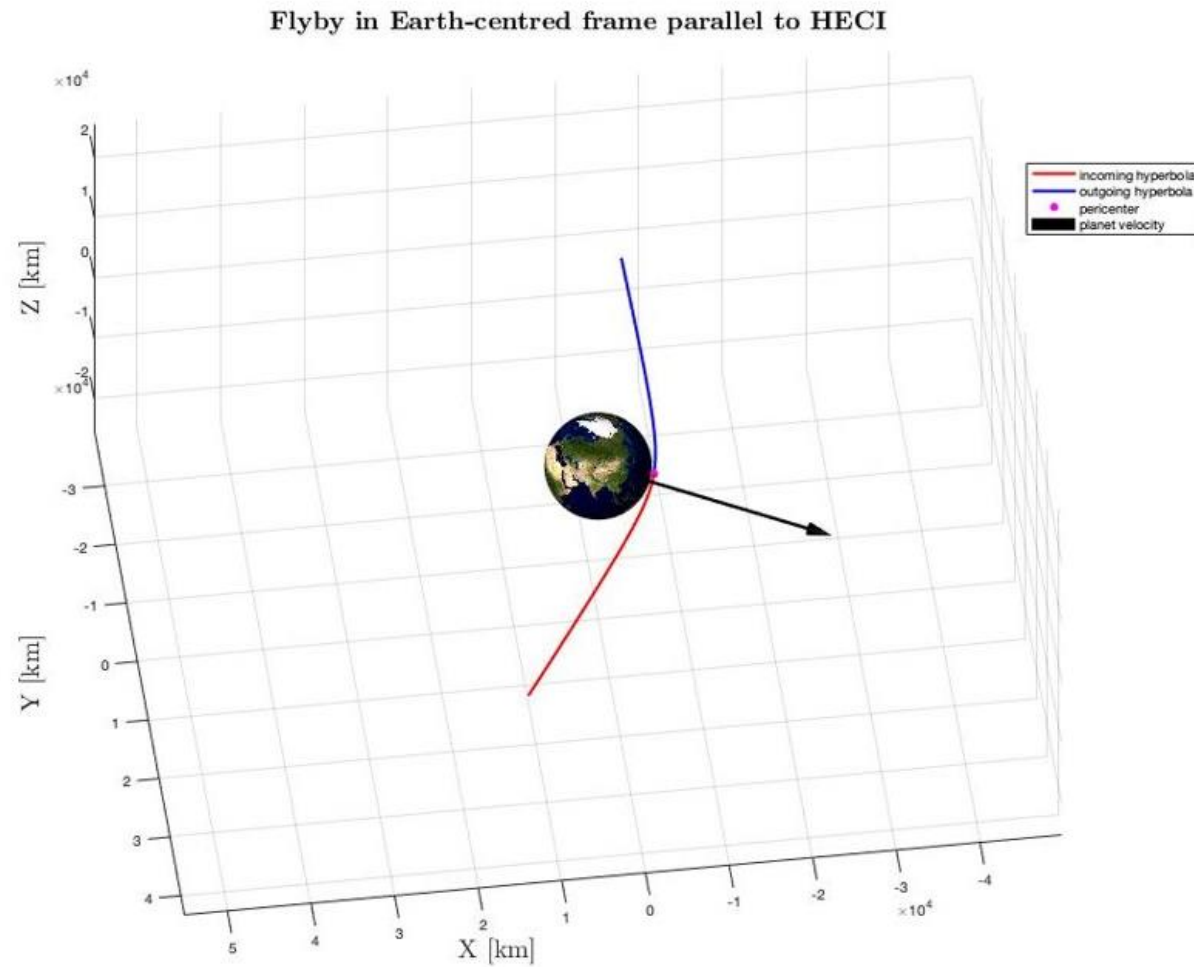


Figure 7: Flyby Trajectory



Planetary Mission – Objectives

Aim of the mission : Earth's observation

- Ground track estimation
- J2 and SRP perturbed orbit analysis
- Real satellite comparison

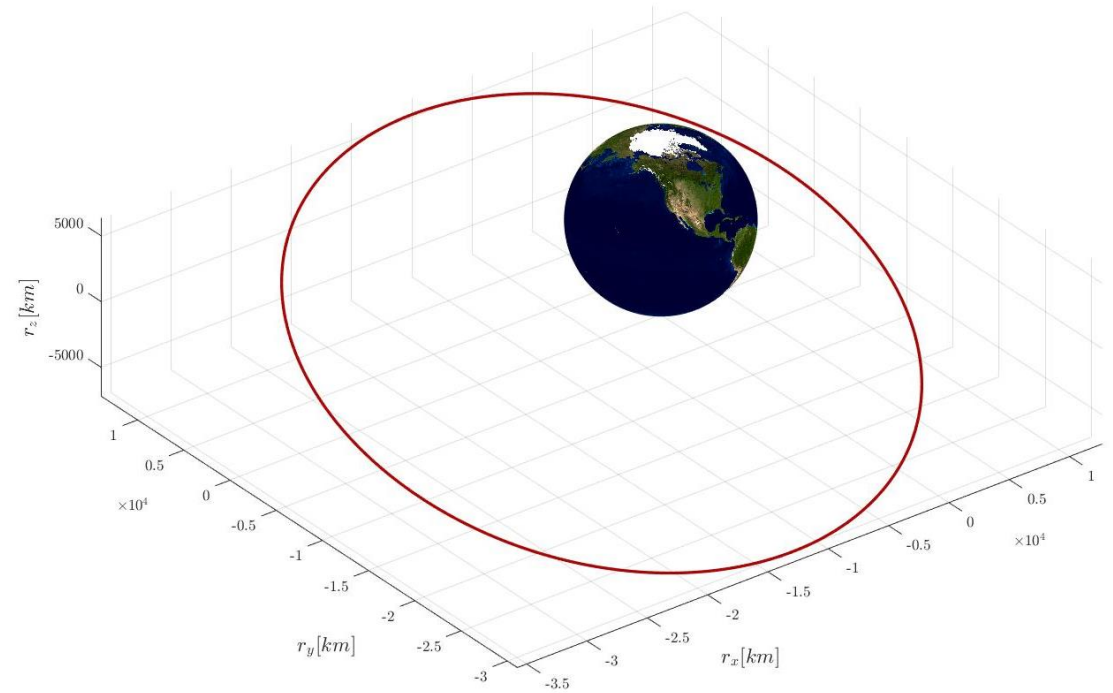


Figure 8: Nominal Orbit



Planetary Mission – Ground Tracks

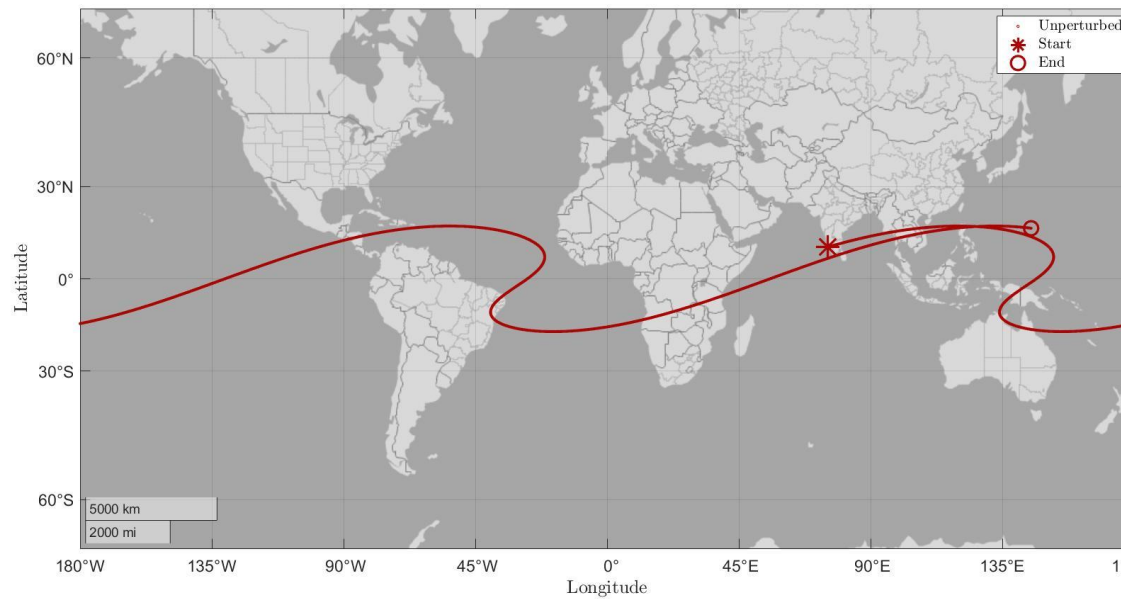


Figure 9: Unperturbed Ground track – 1 day

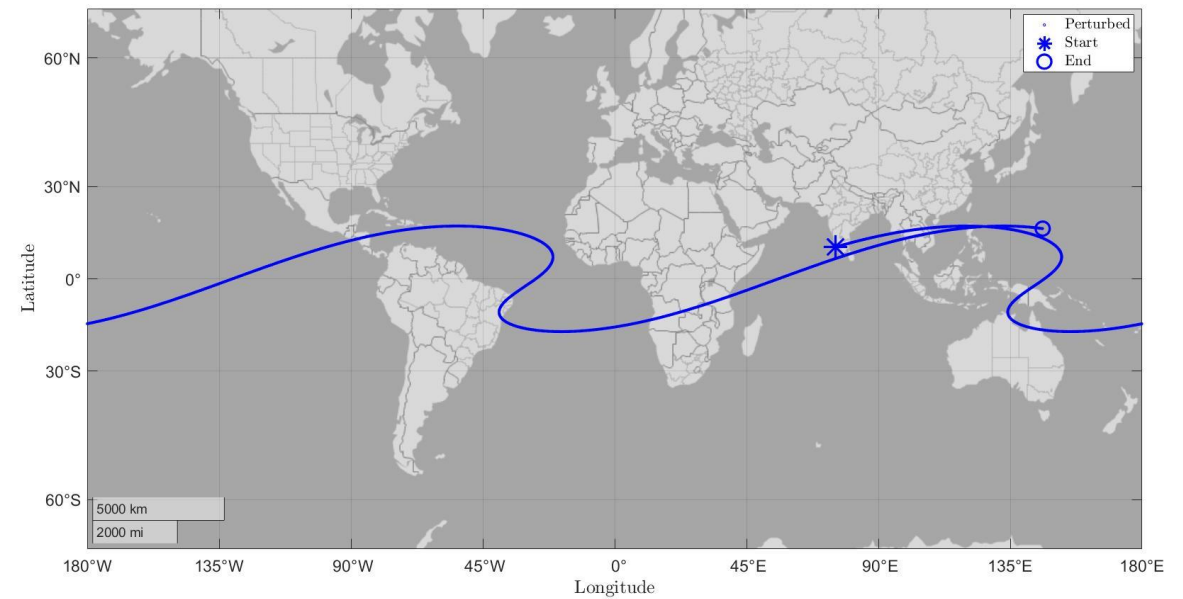


Figure 10: Perturbed Ground track – 1 day



Planetary Mission – Repeating Ground Tracks



Figure 11: Repeating Ground tracks – 10 day

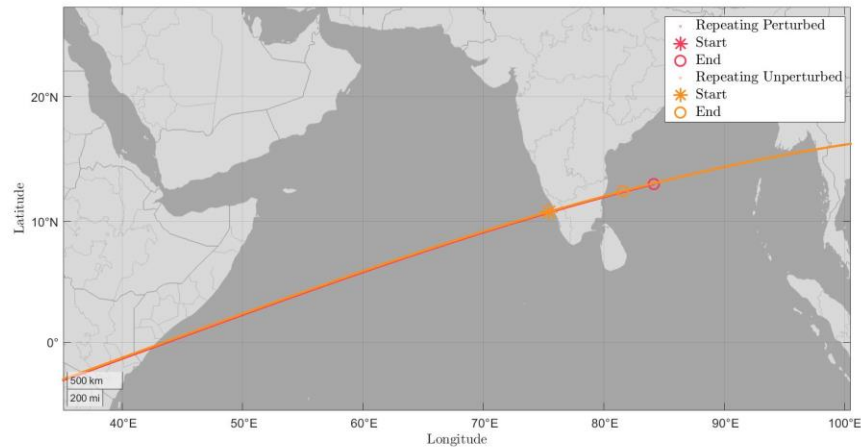


Figure 12: Repeating Ground tracks – 1 day

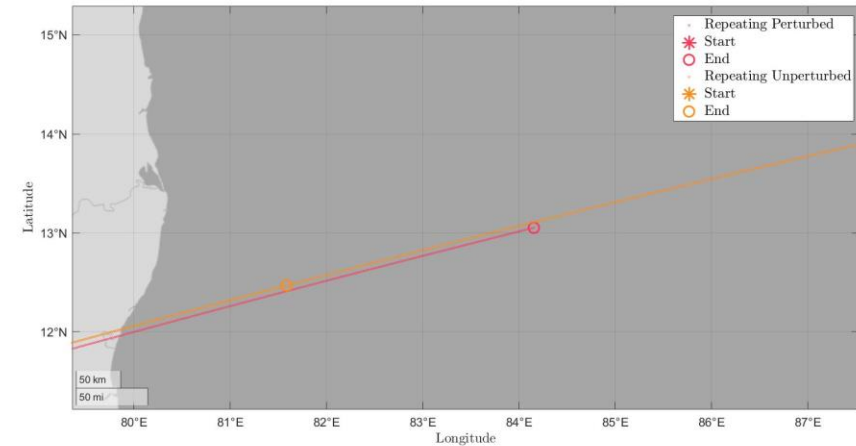


Figure 13: Repeating Ground tracks zoom-in – 1 day



Planetary Mission – Propagation

The evolution of Keplerian elements through two different methods:

- Gauss planetary equations
- Cartesian equation of motion

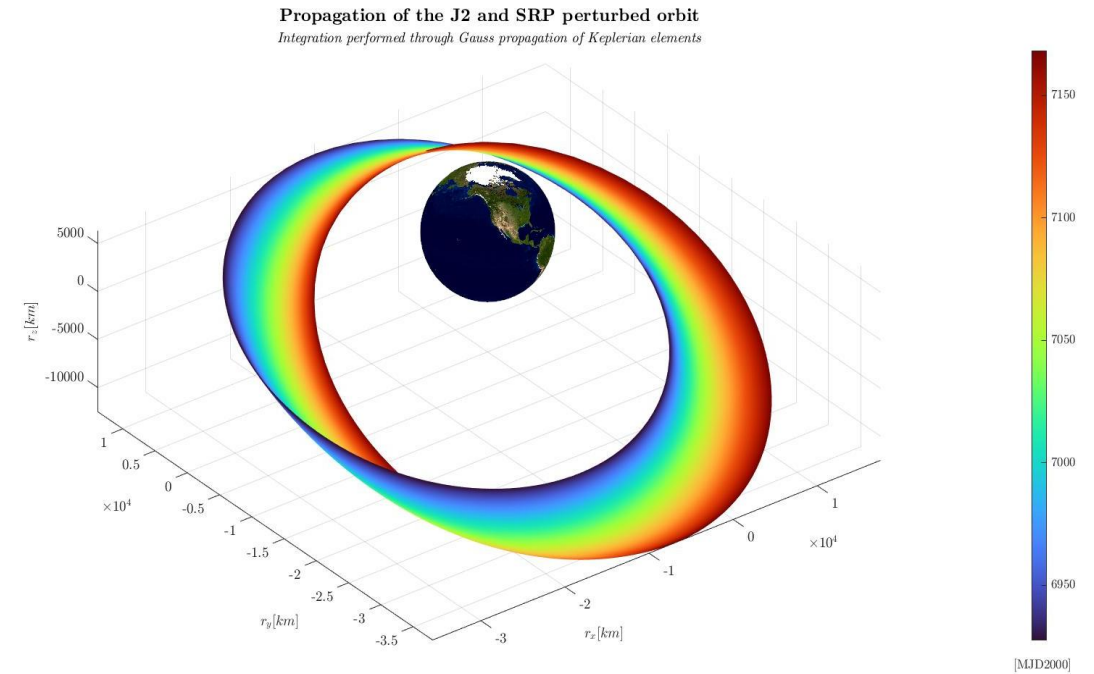


Figure 14: Perturbed Orbit



Planetary Mission – Propagation

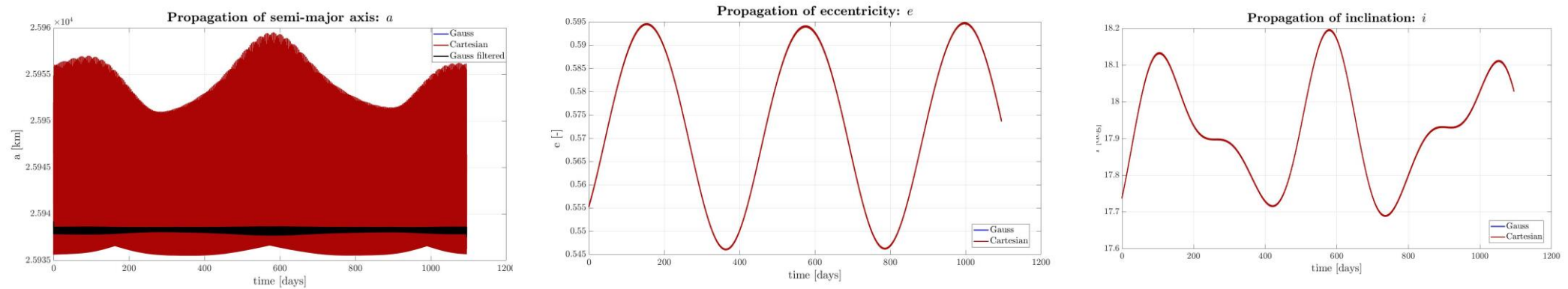


Figure 15: Evolution of Perturbed Orbit's Keplerian Elements

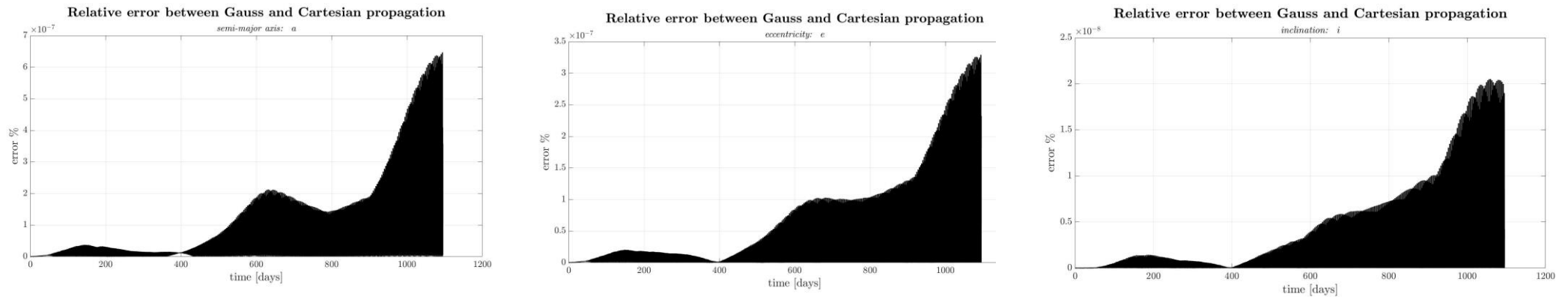


Figure 16: Evolution of Perturbed Orbit's Keplerian Elements – Error between direct integration and Gauss propagation



Planetary Mission – Propagation

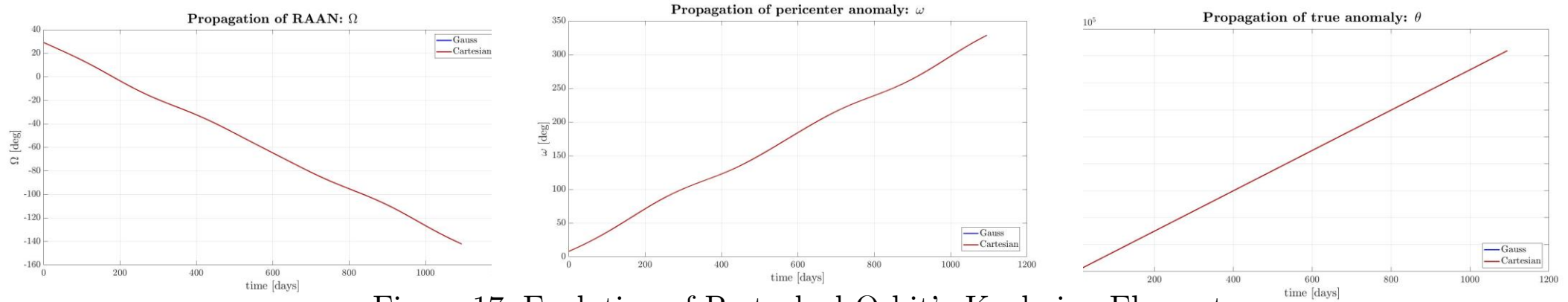


Figure 17: Evolution of Perturbed Orbit's Keplerian Elements

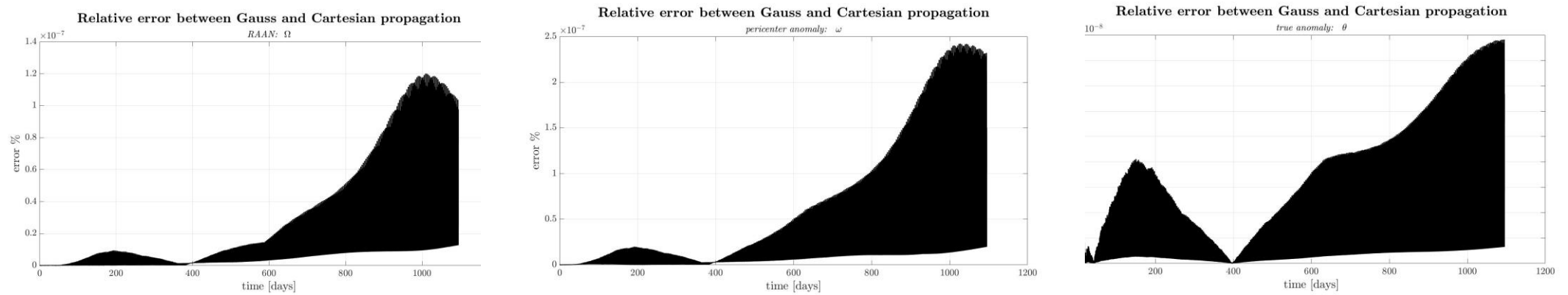


Figure 18: Evolution of Perturbed Orbit's Keplerian Elements – Error between direct integration and Gauss propagation



Planetary Mission – HF Filtering

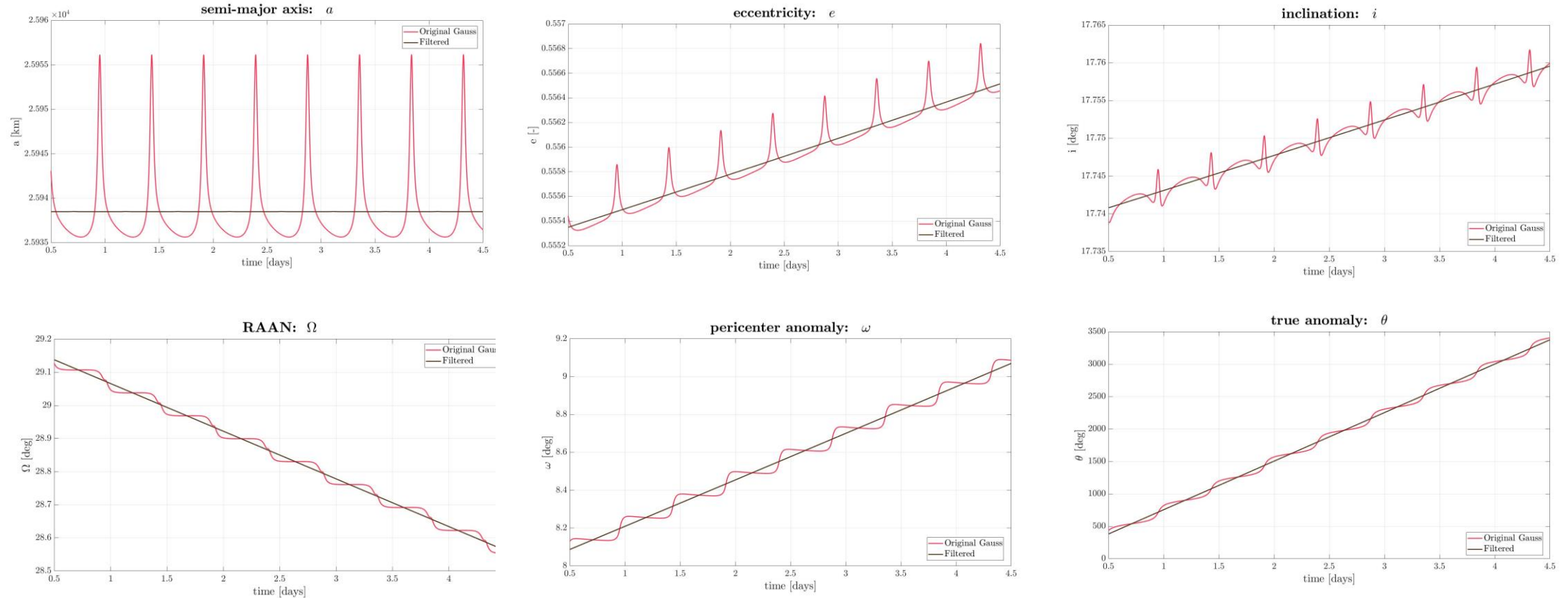


Figure 19: Filtering of Keplerian Elements



Planetary Mission – Real Satellite Comparison

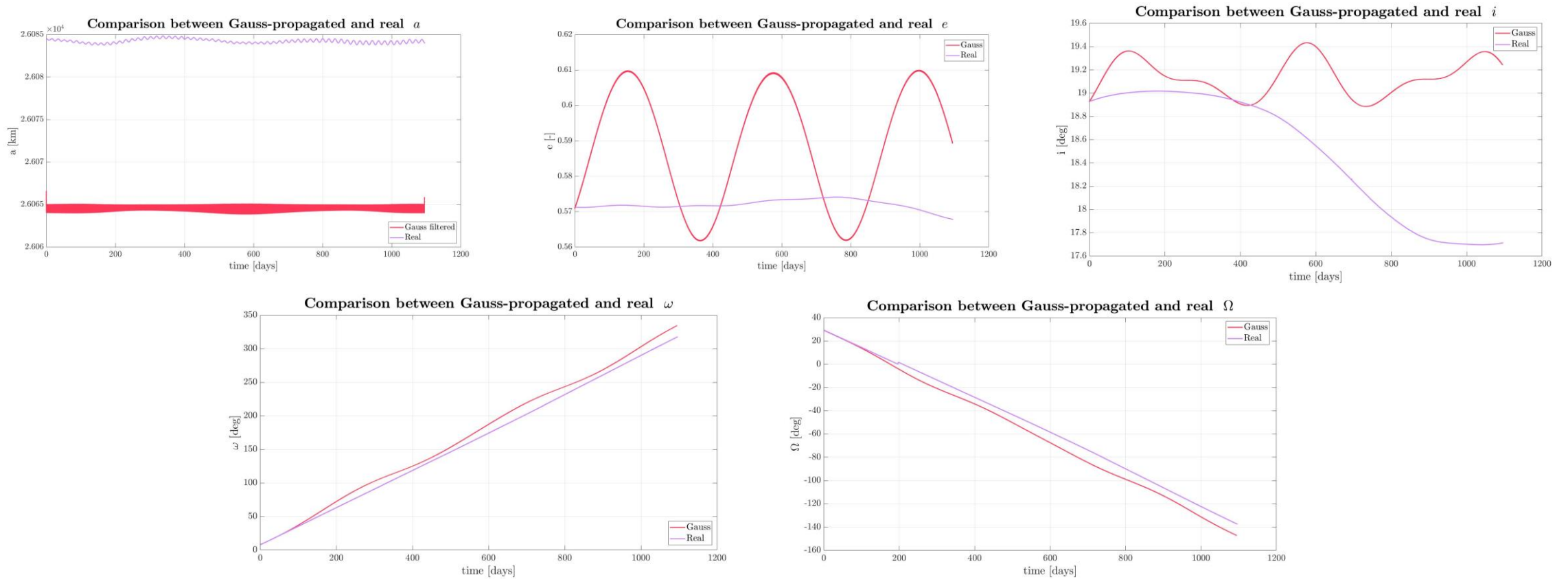
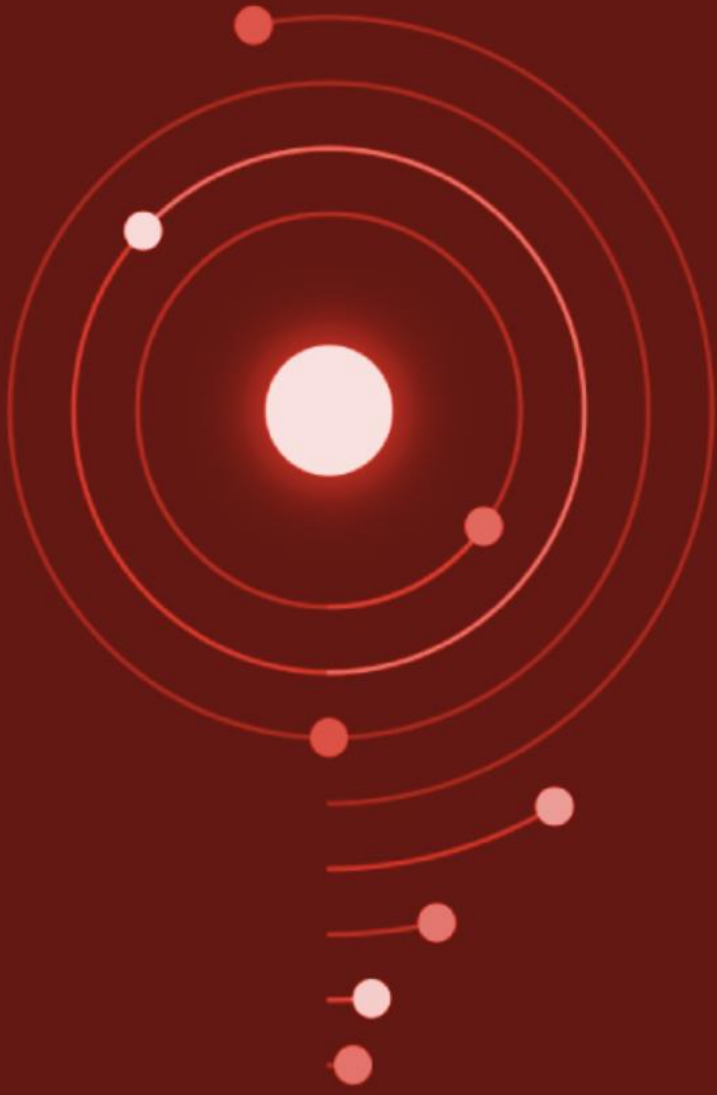


Figure 20: Comparison of Kepler Element's Propagation with a Real Satellite





Thank you for your attention

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