ME 499/599: Computer Programming for Mechanical Systems

Winter 2015

Lab 5: Complex Stuff

Purpose

The goal of this lab is to introduce you to classes in Python, and to give you some practice writing them.

Preparation

Remind yourself about complex numbers. Read chapters 15 and 16 in the textbook.

Assignment

- 1. Write a class circle, whose constructor takes a single argument, representing the radius. Put the class definition in a file called circle.py
- 2. Write a member function, called area, for the class that returns the area of the circle.
- 3. Write a member function, called diameter, that returns the circle diameter. Write a member function, called circumference that returns the circumference of the circle.
- 4. Now we're going to write a class for complex numbers. Start by writing a class called <code>complex</code> that takes two arguments, representing the real and imaginary parts of a complex number. Put the class definition in a file called <code>complex.py</code>, and call the member variables <code>re</code> and <code>im</code>. You should make these arguments optional, and default to something sensible if they are missing. Check that your code does the right thing in response to the following:

```
a = Complex(1.0, 2.3) # 1 + 2.3i

b = Complex(2) # 1 + 0i

c = Complex() # 0 + 0i
```

5. Implement the __str__() function, so that

```
a = Complex(1, 2)
b = Complex(1, -2)
print a
print b
```

works and prints out

```
(1 + 2i)
(1 - 2i)
```

6. Implement addition, such that the following works:

```
a = Complex(1, 2)
b = Complex(3, 4)
print a + b
print a + 1
print 1 + a
```

and prints out

```
(4 + 6i)
(2 + 2i)
(2 + 2i)
```

Once you have addition working, implement subtraction. This should look a lot like addition.

- 7. Now, implement multiplication and division. Verify that everything works as expected.
- 8. Finally, implement the complex conjugate:

```
a = Complex(1, 2)
print ~a
```

should print out

```
(1 - 2i)
```

9. OK. Let's use your new class. Write a new function that calculates the roots of a quadratic function. You should call it like this:

roots(1, 2, 3)

and it should return a list of all of the roots of the function. Sometimes these will be real numbers, sometimes the will be complex. Sometimes there will be two roots, and sometimes there will be one, or zero, depending on the values you pass in. You should deal with all of these cases.

Grading

If you use the built-in complex number implementation in your code, you will get zero points for this lab. The goal of this lab is for you to write your own code for complex numbers. You can, however, use the built-in implementation to test your own code. Turn the code into TEACH, as usual.

There are 29 points available in this lab.

- 1. 2 points for a correctly-defined circle class. 1 point each for the area, diameter, and circumference functions. 1 point for extra code (outside of the class) that tests your class code. [6 points total]
- 2. 2 points for a correctly-defined complex number class. 1 point for handling fewer than 2 arguments in the constructor. [3 points total]
- 3. 1 point for correctly implementing __str__. 1 point for dealing correctly with a negative imaginary term. [2 points total]
- 4. 1 point for being able to add two complex numbers correctly. 1 point for being to add a complex to a number. 1 point for being able to add a number to a complex. 1 point for being able to do all three for subtraction. 1 point for code that checks the correctness of the functions. [5 points total]
- 5. 1 point for being able to multiply two complex numbers correctly. 1 point for being to multiply a complex by a number. 1 point for being able to multiply a number by a complex. 1 point for being able to do all three for division. 1 point for code that checks the correctness of the functions. [5 points total]
- 6. 1 point for the complex conjugate. [1 point]
- 7. 1 point for a well-defined roots function. 1 point for handling two real roots.2 points for handling 1 complex roots. 1 point for handling the 1 root case.1 point for handling the zero root case. 1 point for code that tests your function. [7 points total]

Thoughts

- 1. Support for complex numbers already exists in Python (of course). However, for the purposes of this lab, were going to assume that it doesn't and we're going to write out own code. You could, however, use the built-in implementation to test the correctness of your own implementation, if you like.
- 2. There seems like a lot of code to write this week. It's actually less that you think since once you figure out how the operators work, most of the functions look more-or-less the same.
- 3. We're going to ask you do implement a bunch of mathematical functions without telling you how. All of these can be implemented as special class member functions, which are listed here. Only implement the ones you need.
- 4. Addition and multiplication of complex numbers both commute. This means that you can define one version of the function in terms of another. For example, the function <code>__radd__</code> should call the function <code>__add__</code>.
- 5. Some of the functions, like addition, will have different types in the second argument for different calls. The right way to deal with this is through duck typing. Assume it's a Complex number, and do the calculation. Wrap this in a try-except block, and deal with the non-Complex case (where it's a number) in the except block.

The Rules

Everything you do for this lab should be your own work. Don't look up the answers on the web, or copy them from any other source. You can look up general information about Python on the web, but no copying code you find there. Read the code, close the browser, then write your own code.

Page written by Bill Smart.