

DISEÑO Y ANÁLISIS DE ALGORITMOS

Ramificación y poda

Maximum diversity problem

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1. Introducción

En esta práctica se implementaran algoritmos heurísticos y de ramificación y poda para el *Maximum diversity problem*. El programa se implementara en C++.

2. Algoritmos usados para resolver el problema

Para ello usaremos 4 tipos de algoritmos que iré explicando más adelante. Greedy, GRASP y Branch Bound.

2.1 Greedy

```
1: Elem = S;  
2: S = ∅;  
3: Obtener s c = centro(Elem);  
4: repeat  
5: Obtener el elemento s * ∈ Elem más alejado de s c ;  
6: S = S ∪ {s * };  
7: Elem = Elem - {s * };  
8: Obtener s c = centro(S);  
9: until (|S| = m)  
10: Devolver S;
```

2.2 GRASP

```
procedure grasp()  
1 InputInstance();  
2 for GRASP stopping criterion not satisfied →  
3 ConstructGreedyRandomizedSolution(Solution);  
4 LocalSearch(Solution);  
5 UpdateSolution(Solution, BestSolutionFound);  
6 rof;  
7 return(BestSolutionFound)  
end grasp;
```

```
procedure ConstructGreedyRandomizedSolution(Solution)  
1 Solution = {};
```

```

2 for Solution construction not done →
3 MakeRCL(RCL);
4 s = SelectElementAtRandom(RCL);
5 Solution = Solution ∪ {s};
6 AdaptGreedyFunction(s);
7 rof;
end ConstructGreedyRandomizedSolution;

```

2.3 Branch & Bound

```

1. Compute an initial lower bound  $LB$  with a heuristic algorithm
2. Make  $ActiveNodes = \{ \text{Initial node and its child nodes in the search tree} \}$ 
While ( $ActiveNodes \neq \emptyset$ )
    3. Take  $Node$  from  $ActiveNodes$ 
    If ( $Node$  is a leaf node)
        4. Compute the value  $z'$  of its associated solution
        If ( $z' > LB$ )
            5.  $LB = z'$ 
        6. Remove  $Node$  from  $ActiveNodes$ 
    Else
        7. Let  $Sel = \{s_1, s_2, \dots, s_k\}$  be the partial solution associated with  $Node$ 
        8. Compute  $d_{\max}(s_j)$  for  $j = 1, 2, \dots, k$  and  $z(v)$  as well as  $d_{\min}(v)$  for  $v \in V \setminus Sel$ 
        If ( $d_{\max}(s_j) < d_{\min}(v)$  for any  $j = 1, 2, \dots, k$  and  $v \in V \setminus Sel$ )
            9. Remove  $Node$  from  $ActiveNodes$ 
        Else
            10. Compute the upper bound  $z_1 + UB_{23}$  of  $Node$ 
            11. Let  $v_1^*, v_2^*, \dots, v_{m-k}^*$  be the vertices in  $V \setminus Sel$  with maximum  $z$ -values
            12. Compute the value  $z'$  of solution  $x = \{s_1, s_2, \dots, s_k, v_1^*, v_2^*, \dots, v_{m-k}^*\}$ 
            If ( $z' > LB$ )
                13.  $LB = z'$ 
            If ( $z_1 + UB_{23} < LB$ )
                14. Remove  $Node$  from  $ActiveNodes$ 
            Else If ( $z' < z_1 + UB_{23}$ )
                15.  $IUB = \max(z, z_1 + UB_{23}(v_1^*), z_1 + UB_{23}(v_2^*), \dots, z_1 + UB_{23}(v_{m-k}^*))$ 
                If ( $IUB < LB$ )
                    16. Remove  $Node$  from  $ActiveNodes$ 
            Else
                17. Add the child nodes of  $Node$  to  $ActiveNodes$ 

```

Fig. 6. Branch and bound algorithm pseudo-code.

4. Resultados obtenidos

En este apartado estaremos ejecutando los diferentes problemas con los algoritmos implementados.

Greedy

Problema	n	K	m	z	S	CPU
max_div_15_2.txt	15	2	5	73.5619	[8 6 3 10 1]	1.69827ms
max_div_15_2.txt	15	2	4	48.4139	[8 6 3 10]	1.20948ms
max_div_15_3.txt	15	3	5	94.7487	[11 8 4 10 13]	1.5821ms
max_div_15_3.txt	15	3	4	59.7638	[11 8 4 10]	1.26959ms
max_div_20_2.txt	20	2	5	61.2393	[17 18 8 2 12]	0.487891ms
max_div_20_2.txt	20	2	4	39.5682	[17 18 8 2]	0.392543ms
max_div_20_3.txt	20	3	5	92.8298	[12 13 7 2 16]	0.521287ms
max_div_20_3.txt	20	3	4	56.5347	[12 13 7 2]	0.418575ms
max_div_30_2.txt	30	2	5	80.9102	[8 27 1 10 12]	1.19503ms

max_div_30_2.txt	30	2	4	52.7712	[8 27 1 10]	0.987367ms
max_div_30_3.txt	30	3	5	99.5088	[16 6 23 13 14]	4.71543ms
max_div_30_3.txt	30	3	4	63.5184	[16 6 23 13]	5.05585ms

GRASP

Problema	n	K	m	lter	L R C	z	S	CPU
max_div_15_2.txt	15	2	2	100	2	11.8592	[6 8]	9.93703ms
max_div_15_2.txt	15	2	2	100	3	11.8592	[6 8]	12.2435ms
max_div_15_2.txt	15	2	3	100	2	27.2313	[1 6 0]	24.5311ms
max_div_15_2.txt	15	2	3	100	3	27.2313	[1 0 6]	18.4703ms
max_div_15_2.txt	15	2	4	100	2	49.8268	[6 0 8 5]	39.5399ms

max_div_1 5_2.txt	15	2	4	100	3	49.76 33	[9 0 6 8]	41.8851 ms
max_div_1 5_2.txt	15	2	5	100	2	79.12 95	[6 8 0 5 3]	79.7236 ms
max_div_1 5_2.txt	15	2	5	100	3	78.93 46	[6 5 1 0 3]	84.8978 ms
max_div_1 5_3.txt	15	3	2	100	2	13.27 32	[11 8]	7.88421 ms
max_div_1 5_3.txt	15	3	2	100	3	13.27 32	[11 8]	7.33629 ms
max_div_1 5_3.txt	15	3	3	100	2	31.86 85	[11 4 6]	20.4185 ms
max_div_1 5_3.txt	15	3	3	100	3	31.86 85	[11 4 6]	19.722m s
max_div_1 5_3.txt	15	3	4	100	2	59.76 38	[8 10 4 11]	50.086m s
max_div_1 5_3.txt	15	3	4	100	3	59.76 38	[4 11 8 10]	50.3891 ms
max_div_1 5_3.txt	15	3	5	100	2	96.08 58	[8 11 3 4 13]	108.502 ms
max_div_1 5_3.txt	15	3	5	100	3	96.08 58	[13 3 8 11 4]	103.105 ms

max_div_2 0_2.txt	20	2	2	100	2	8.510 33	[17 18]	38.6212 ms
max_div_2 0_2.txt	20	2	2	100	3	8.510 33	[17 18]	14.9052 ms
max_div_2 0_2.txt	20	2	3	100	2	21.99 61	[17 8 18]	24.7779 ms
max_div_2 0_2.txt	20	2	3	100	3	21.99 61	[17 18 8]	23.6166 ms
max_div_2 0_2.txt	20	2	4	100	2	40.00 23	[1 18 2 8]	49.1495 ms
max_div_2 0_2.txt	20	2	4	100	3	40.00 23	[8 2 18 1]	52.1648 ms
max_div_2 0_2.txt	20	2	5	100	2	63.65 17	[17 18 8 1 13]	101.987 ms
max_div_2 0_2.txt	20	2	5	100	3	63.65 17	[13 8 18 1 17]	105.998 ms
max_div_2 0_3.txt	20	3	2	100	2	11.80 03	[13 12]	10.5786 ms
max_div_2 0_3.txt	20	3	2	100	3	11.80 03	[12 13]	9.78571 ms
max_div_2 0_3.txt	20	3	3	100	2	30.87 27	[13 12 7]	25.4742 ms

max_div_2 0_3.txt	20	3	3	100	3	30.87 27	[13 12 7]	27.9734 ms
max_div_2 0_3.txt	20	3	4	100	2	56.69 03	[12 13 16 2]	65.1883 ms
max_div_2 0_3.txt	20	3	4	100	3	56.69 03	[2 12 13 16]	64.176m s
max_div_2 0_3.txt	20	3	5	100	2	92.82 98	[12 2 16 13 7]	119.965 ms
max_div_2 0_3.txt	20	3	5	100	3	90.86 48	[16 2 12 13 8]	118.153 ms
max_div_3 0_2.txt	30	2	2	100	2	11.65 71	[8 27]	63.0623 ms
max_div_3 0_2.txt	30	2	2	100	3	11.65 71	[8 27]	51.0468 ms
max_div_3 0_2.txt	30	2	3	100	2	28.94 43	[8 27 1]	44.6917 ms
max_div_3 0_2.txt	30	2	3	100	3	27.59 43	[8 27 14]	32.8112 ms
max_div_3 0_2.txt	30	2	4	100	2	52.77 12	[8 1 10 27]	72.825m s
max_div_3 0_2.txt	30	2	4	100	3	52.77 12	[8 1 10 27]	69.4888 ms

max_div_3 0_2.txt	30	2	5	100	2	80.91 02	[12 8 10 1 27]	129.38m s
max_div_3 0_2.txt	30	2	5	100	3	80.06 75	[17 10 8 27 1]	121.755 ms
max_div_3 0_3.txt	30	3	2	100	2	13.07 37	[16 6]	67.4642 ms
max_div_3 0_3.txt	30	3	2	100	3	13.07 37	[6 16]	48.2569 ms
max_div_3 0_3.txt	30	3	3	100	2	34.29 05	[5 16 23]	47.9031 ms
max_div_3 0_3.txt	30	3	3	100	3	34.29 05	[5 16 23]	37.7643 ms
max_div_3 0_3.txt	30	3	4	100	2	63.70 2	[23 5 16 13]	87.3297 ms
max_div_3 0_3.txt	30	3	4	100	3	63.70 2	[23 5 16 13]	83.374m s
max_div_3 0_3.txt	30	3	5	100	2	99.59 2	[5 13 14 23 16]	149.611 ms
max_div_3 0_3.txt	30	3	5	100	3	99.50 89	[6 13 23 16 14]	153.469 ms

Branch & Bound

Problema	n	K	m	Strategy	z	S	CPU
max_div_15_2.txt	15	2	4	Minimum Level	49.8268	[0 5 6 8]	876.604 ms
max_div_15_3.txt	15	3	4	Minimum Level	59.7638	[4 8 10 11]	333.978 ms
max_div_20_2.txt	20	2	4	Minimum Level	40.0023	[1 2 8 18]	1535.62 ms
max_div_20_3.txt	20	3	4	Minimum Level	56.6903	[2 12 13 16]	776.42 ms
max_div_30_2.txt	30	2	4	Minimum Level	52.7712	[1 8 10 27]	5176.96 ms
max_div_30_3.txt	30	3	4	Minimum Level	63.702	[5 13 16 23]	5937.57 ms