

Notebook - Maratona de Programação

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1 Algoritmos

1.1 Mochila

```
int val[MAXN], peso[MAXN], dp[MAXN][MAXS]
3 int knapsack(int N, int M) // Objetos | Peso max
4 {
       for (i=0;i<=N;i++)</pre>
5
6
          for (j=0; j <= M; j++)</pre>
                if (i==0 || j==0)
                    dp[i][j] = 0;
10
                else if (peso[i-1] <= j)</pre>
11
                    dp[i][j] = max(val[i-1]+dp[i-1][j-
      peso[i-1]], dp[i-1][j]);
                    dp[i][j] = dp[i-1][j];
14
      }
16
17
      return dp[N][M];
```

1.2 Iterative-BS

```
1 int main()
       int l=1, r=N;
       int res=-1;
4
       while(1 <= r)</pre>
            int m = (1 + r)/2;
            if(!ver(m))
            {
10
                 1 = m+1;
11
            }
            else
13
14
            {
                 res = m:
15
            }
18
       cout << res << endl;</pre>
19
20
       return 0;
22 }
```

2 Grafos

2.1 BFS

```
1 //BFS (Breadth First Search) O(V+A)
3 vector < vector < int >> adj; // adjacency list
     representation
4 int n; // number of nodes
5 int s; // source vertex
7 queue < int > q;
8 vector<int> d(n, INF);
10 q.push(s);
used[s] = true;
12 while (!q.empty()) {
    int v = q.front();
13
      q.pop();
      for (int u : adj[v]) {
15
         if (d[u] > d[v] + 1) {
```

2.2 Find-bridges

```
1 #define vi vector<int>
3 vector < vector <int> > grafo;
4 vector < bool > visited;
5 vi t, low;
6 int timer=0;
8 void find_bridges(int v, int p=-1)
       visited[v] = true;
10
       t[v] = low[v] = timer++;
11
       for(int i=0;i<(int)grafo[v].size();i++)</pre>
12
13
14
           int vert = grafo[v][i];
           if(vert == p)
15
16
               continue;
           if (visited[vert])
17
18
               low[v] = min(low[v], t[vert]);
19
           {
20
                find_bridges(vert, v);
21
               low[v] = min(low[v], low[vert]);
22
               if(low[to] > t[v])
23
24
                    IS_BRIDGE(v, vert);
25
       }
27 }
28
29 int main()
30 {
31
       timer = 0;
       visited.assign(N+1, false);
32
33
       t.assign(N+1, 0);
       low.assign(N+1, 0);
34
35
       for(int i=0;i<N;i++)</pre>
36
           if(!visited[i])
37
               find_bridges(1);
39
       return 0;
41 }
```

2.3 Dijkstra

```
1 // Dijkstra - Shortest Path
3 #define pii pair<int, int>
4 #define vi vector<int>
5 #define vii vector< pair<int,int> >
6 #define INF 0x3f3f3f3f
8 vector < vii > grafo(N+1, vii());
9 vi distancia(N+1, INF);
10 priority_queue < pii, vii, greater <pii>> fila;
12 void dijkstra(int k)
13 {
14
      int dist, vert, aux;
      distancia[k]=0;
15
      fila.push(mp(k, 0));
17
      while(!fila.empty())
19
20
```

```
aux=fila.top().f;
                                                                      return A.dist < B.dist;</pre>
21
                                                               29
22
           fila.pop();
                                                               30 }
23
                                                               31
            for(auto v: grafo[aux])
                                                               32 void kruskal()
24
                                                               33 {
                vert=v.f:
                                                                       for (int i=1;i<=N;i++)</pre>
26
                                                               34
                dist=v.s;
                                                                           pai[i]=i;
                if (distancia[vert]>distancia[aux]+dist)
28
                                                               36
                                                                       for (int i=1;i<=M;i++)</pre>
                {
29
                                                               37
                     distancia[vert]=distancia[aux]+dist; 38
                                                                           cin >> grafo[i].A >> grafo[i].B >> grafo[i].
30
                     fila.push(mp(vert, distancia[vert]));
31
                                                                      sort(grafo+1, grafo+M+1, comp);
32
                }
                                                               40
           }
                                                               41
33
       }
                                                                      for(int i=1;i<M;i++)</pre>
34
                                                               42
35 }
                                                               43
                                                               44
                                                                           if (find(grafo[i].A)!=find(grafo[i].B))
37 int main()
                                                                           {
                                                               45
                                                                                join(grafo[i].A, grafo[i].B);
38 €
       for(int i=0; i<M; i++)</pre>
                                                                               soma+=grafo[i].dist;
39
                                                               47
40
                                                               48
            cin >> a >> b >> p;
                                                                      }
41
                                                               49
           grafo[a].pb(mp(b, p));
42
                                                               50
           grafo[b].pb(mp(a, p));
                                                               51
                                                                      cout << soma << endl;</pre>
                                                               52 }
44
45 }
                                                                  2.6
                                                                       DFS
  2.4 Floyd-Warshall
```

```
1 // Floyd Warshall
3 int dist[MAX][MAX];
5 void Floydwarshall()
6 {
       for(int k = 1;k <= n;k++)</pre>
            for(int i = 1;i <= n;i++)</pre>
                 for(int j = 1; j <= n; j++)</pre>
                      \texttt{dist[i][j] = min(dist[i][j], dist[i][}^{11}
10
       k] + dist[k][j]);
11 }
```

2.5 Kruskal

28 {

```
1 // Kruskal - Minimum Spanning Tree
3 typedef struct
4 {
       int A, B;
      int dist;
7 } vertice;
9 vertice grafo[MAX];
10 int pai[MAX];
11
12 int find(int X) // Union-Find
13 {
       if (pai[X] == X)
15
          return X;
16
17
          return pai[X]=find(pai[X]);
18 }
19
20 void join(int X, int Y)
21 {
22
       int paix = find(X);
       int paiy = find(Y);
23
       pai[paix]=paiy;
24
25 }
27 bool comp(vertice A, vertice B)
```

```
1 //DFS (Depth First Search) O(V+A)
3 void DFS(int x)
4 {
      for(int i=0; i<(int)vizinhos[x].size(); i++)</pre>
5
6
           int v = vizinhos[x][i];
           if (componente[v] == -1)
                componente[v] = componente[x];
10
               DFS(v);
12
           }
      }
13
14 }
```

Represent

```
1 // Grafos
_{\rm 3} // List of edges
       vector< pair<int, int> > arestas;
       arestas.push_back(make_pair(1, 2));
6
       arestas.push_back(make_pair(1, 3));
9 // Adjacency Matrix
10
      int grafo[10][10];
1.1
12
       grafo[1][2] = grafo[2][1] = 1;
13
       grafo[1][3] = grafo[3][1] = 2;
14
15
16 // Adjacency List
17
       vector < int > vizinhos[10];
18
19
20
       vizinhos[1].push_back(2);
       vizinhos[1].push_back(2);
  2.8
       \mathbf{Prim}
```

```
1 // Prim Algorithm
2 #define MAXN 10100
3 #define INFINITO 999999999
```

```
5 int n, m;
                                                              73
                                                                     cout << Prim() << endl;</pre>
6 int distancia[MAXN];
                                                              74
7 int processado[MAXN];
                                                              75
                                                                     return 0;
8 vector < pii > vizinhos [MAXN];
                                                              76 }
9
10 int Prim()
                                                                 3
                                                                      Geometria
11 {
       for(int i = 2;i <= n;i++) distancia[i] = INFINITO</pre>
                                                                3.1
       distancia[1] = 0;
13
14
       priority_queue < pii, vector <pii>, greater <pii> >
                                                               3 typedef struct
       fila.push( pii(distancia[1], 1) );
16
                                                              4 {
17
                                                                     int x, y;
       while (1)
                                                               6 } pnt;
19
           int davez = -1;
21
                                                              9 {
           while(!fila.empty())
22
                                                              10
23
                int atual = fila.top().second;
24
               fila.pop();
                                                              12
26
                                                              13
                                                                     return false:
                if (!processado[atual])
27
                                                              14 }
28
                                                              15
                    davez = atual;
29
                    break;
                                                              17 {
                }
31
                                                              18
           }
32
                                                              19
33
                                                                     if(val==0)
                                                              20
           if(davez == -1)
34
                                                                         return 0;
                                                              21
               break:
36
                                                                         return 1;
                                                              23
           processado[davez] = true;
38
           for(int i = 0;i < (int)vizinhos[davez].size() 25</pre>
                                                                         return 2;
39
       ;i++)
           {
40
41
                                                              29 {
                int dist = vizinhos[davez][i].first;
42
                                                              30
                int atual = vizinhos[davez][i].second;
43
                                                              31
44
                                                              32
                if( distancia[atual] > dist && !
45
                                                              33
       processado[atual])
                {
46
                                                              35
                    distancia[atual] = dist;
                    fila.push( pii(distancia[atual],
48
                                                              37
       atual));
                                                              38
                }
49
                                                              39
           }
50
                                                              40
                                                              41
52
                                                              42
       int custo_arvore = 0;
53
                                                              43
       for(int i = 1;i <= n;i++)</pre>
54
                                                              44
           custo_arvore += distancia[i];
55
                                                              45
56
57
       return custo arvore:
                                                              47
58 }
                                                              48
59
                                                              49
60 int main(){
                                                              50
                                                                     return false;
                                                              51
       cin >> n >> m;
62
                                                              52 }
      for(int i = 1:i <= m:i++){</pre>
64
65
           int x, y, tempo;
           cin >> x >> y >> tempo;
67
                                                             1 typedef struct
                                                              2 {
           vizinhos[x].pb( pii(tempo, y) );
69
                                                                     int x, y;
70
           vizinhos[y].pb( pii(tempo, x) );
                                                              4 } Point;
       }
71
```

72

Inter-Retas

```
1 // Intersection between lines
8 bool collinear(pnt p, pnt q, pnt r)
      if (q.x<=max(p.x,r.x) && q.x>=min(p.x,r.x) && q.y
      <=max(p.y,r.y) && q.y>=min(p.y,r.y))
          return true;
int orientation(pnt p, pnt q, pnt r)
      int val=(q.y-p.y)*(r.x-q.x)-(q.x-p.x)*(r.y-q.y);
       else if(val>0)
28 bool intersect(pnt p1, pnt q1, pnt p2, pnt q2)
      int o1 = orientation(p1, q1, p2);
      int o2 = orientation(p1, q1, q2);
      int o3 = orientation(p2, q2, p1);
      int o4 = orientation(p2, q2, q1);
      if (o1!=o2 and o3!=o4)
          return true;
      if(o1==0 && collinear(p1, p2, q1))
          return true;
      if(o2==0 && collinear(p1, q2, q1))
          return true;
      if(o3==0 && collinear(p2, p1, q2))
          return true;
      if(o4==0 && collinear(p2, q1, q2))
          return true;
```

Inter-Retangulos

```
6 bool doOverlap(Point 11, Point r1, Point 12, Point r2 61 // Area de um poligono (pontos ordenados por
                                                               adjacencia)
                                                         62 double area(vector <point> p){
      if (11.x>r2.x or 12.x>r1.x or 11.y<r2.y or 12.y< 63 double ret = 0;
                                                         64 for(int i=2;i<(int)p.size();i++)
                                                              ret += cross(p[i] - p[0], p[i-1] - p[0])/2;
          return false:
9
                                                         65
      return true;
10
                                                             return abs(ret);
11 }
                                                         67 }
                                                         68 // Concavo ou Convexo
  3.3 Analytic-Geometry
                                                         69 double ccw(point a, point b, point c){
                                                         70 double ret = cross(b - a, c - b);
                                                             return ret < 0;</pre>
1 struct point
                                                         72 }
2 {
3
      double x, y;
      point(double _x=0, double _y=0) {
                                                           4
                                                                 ED
          x = _x; y = _y;
6
                                                                 Range-query-bigger-than-k-BIT
                                                            4.1
      void show(){
         cout << "x = " << x << endl;
                                                        1 // C++ program to print the number of elements
          cout << "y = " << y << endl;
                                                        2 // greater than k in a subarray of range L-R.
10
                                                          3 #include <bits/stdc++.h>
11
                                                          4 using namespace std;
12
13
      point operator+(const point &o) const{
         return {x + o.x, y + o.y};
                                                         6 // Structure which will store both
14
                                                         _{7} // array elements and queries.
1.5
      point operator - (const point &o) const{
                                                         8 struct node {
16
          return {x - o.x, y - o.y};
                                                               int pos;
                                                          9
                                                               int 1;
18
                                                         10
      bool operator == (const point &o) const{
          return (x == o.x and y == o.y);
20
                                                         12
                                                               int val;
                                                         13 };
21
22
                                                         14
23 };
                                                         15 // Boolean comparator that will be used
                                                         16 // for sorting the structural array.
                                                         17 bool comp(node a, node b)
25 struct line
26 {
                                                         18 €
27
      point fp, sp;
                                                         19
                                                                // If 2 values are equal the query will
      line(point _fp=0, point _sp=0){
                                                               // occur first then array element
                                                         20
                                                                if (a.val == b.val)
          fp=_fp;sp=_sp;
                                                         21
                                                                    return a.l > b.l;
30
                                                         22
                                                         23
                                                                // Otherwise sorted in descending order.
32 };
                                                         24
                                                                return a.val > b.val;
                                                         25
33
34 // Produto Escalar
                                                        26 }
35 double dot(point a, point b){
                                                         27
36
      return a.x*b.x + a.y*b.y;
                                                         28 // Updates the node of BIT array by adding
                                                         29 // 1 to it and its ancestors.
37 }
                                                         30 void update(int* BIT, int n, int idx)
39 // Produto Vetorial
                                                         31 {
40 double cross(point a, point b){
                                                         32
                                                                while (idx <= n) {</pre>
     return a.x*b.y - a.y*b.x;
                                                                   BIT[idx]++;
41
                                                         33
42 }
                                                                    idx += idx & (-idx);
                                                         34
                                                        35
_{44} // Dist entre dois pontos
                                                         36 }
45 double dist(point a, point b){
                                                         37 // Returns the count of numbers of elements
      point c = a - b;
                                                         38 // present from starting till idx.
      return sqrt(c.x*c.x + c.y*c.y);
                                                         39 int query(int* BIT, int idx)
47
48 }
                                                         40 {
                                                                int ans = 0;
                                                         41
50 // Colinearidade entre 3 pontos
                                                                while (idx) {
                                                         42
51 bool collinear(point a, point b, point c){
                                                         43
                                                                  ans += BIT[idx];
     return ((c.y - b.y)*(b.x - a.x) == (b.y - a.y)*(c.x44)
52
      -b.x));
                                                                    idx -= idx & (-idx);
53 }
                                                                }
                                                         46
                                                         47
                                                                return ans;
_{55} // Dist entre ponto e reta
                                                         48 }
56 double distr(point a, line b){
      double crs = cross(point(a - b.fp), point(b.sp - 50 // Function to solve the queries offline
                                                         _{\mbox{\scriptsize 51}} void solve
Query(int arr[], int n, int QueryL[],
      b.fp));
      return abs(crs/dist(b.fp, b.sp));
                                                                            int QueryR[], int QueryK[], int q)
                                                         52
59 }
                                                         53 {
                                                               // create node to store the elements
60
                                                         54
```

```
// and the queries
                                                                  int QueryK[] = { 6, 8 };
                                                          123
       node a[n + q + 1];
                                                          124
       // 1-based indexing.
                                                                  // number of queries
                                                          125
                                                                  int q = sizeof(QueryL) / sizeof(QueryL[0]);
                                                          126
       // traverse for all array numbers
                                                          127
       for (int i = 1; i <= n; ++i) {</pre>
                                                                  // Function call to get
                                                          128
           a[i].val = arr[i - 1];
                                                                  solveQuery(arr, n, QueryL, QueryR, QueryK, q);
                                                          129
           a[i].pos = 0;
                                                          130
           a[i].1 = 0;
                                                          131
                                                                  return 0;
           a[i].r = i;
                                                          132 }
                                                             4.2
                                                                  Iterative-SegTree
       // iterate for all queries
       for (int i = n + 1; i <= n + q; ++i) {</pre>
                                                           1 // Segment Tree Iterativa - Range maximum query
           a[i].pos = i - n;
           a[i].val = QueryK[i - n - 1];
                                                           3 #define N 100010
           a[i].l = QueryL[i - n - 1];
           a[i].r = QueryR[i - n - 1];
                                                           5 struct Segtree
                                                            6 {
                                                                  int t[2*N]={0};
       // In-built sort function used to
       // sort node array using comp function.
                                                           9
                                                                  void build()
       sort(a + 1, a + n + q + 1, comp);
                                                                  {
                                                           10
                                                           11
                                                                      for(int i=N-1; i>0; i--)
       // Binary Indexed tree with
                                                                          t[i]=max(t[i<<1], t[1<<1|1]);
                                                           12
       // initially 0 at all places.
                                                           13
       int BIT[n + 1];
                                                           14
                                                                  int query(int 1, int r)
                                                           15
       // initially 0
       memset(BIT, 0, sizeof(BIT));
                                                                      int ans=0:
                                                           17
                                                                      for(i+=N, r+=N; l<r; l>>=1, r>>=1)
                                                           18
       // For storing answers for each query( 1-based
                                                           19
                                                                      {
       indexing ).
                                                           20
       int ans[q + 1];
                                                                              ans=max(ans, t[1++]);
                                                                          if (r&1)
                                                           22
       // traverse for numbers and query
                                                                              ans=max(ans, t[--r]);
       for (int i = 1; i <= n + q; ++i) {
                                                                      }
                                                           24
           if (a[i].pos != 0) {
                                                           25
                                                                      return ans;
               // call function to returns answer for
                                                           27
       each query
               int cnt = query(BIT, a[i].r) - query(BIT,
                                                                  void update(int p, int value)
                                                           29
        a[i].1 - 1);
                                                           30
                                                                      for(t[p+=n]=value; p>1; p>>=1)
               // This will ensure that answer of each
                                                                          t[p>>1] = max(t[p], t[p^1]);
                                                           32
       query
               // are stored in order it was initially
                                                           34
       asked.
                                                           35 };
               ans[a[i].pos] = cnt;
                                                           37 int main()
           else {
                                                           38 {
               // a[i].r contains the position of the
                                                                  Segtree st;
                                                           39
               // element in the original array.
                                                           40
               update(BIT, n, a[i].r);
                                                                  for(int i=0;i<n;i++)</pre>
                                                           41
           }
                                                           42
                                                                      cin >> aux:
                                                           43
       // Output the answer array
                                                                      st.t[N+i] = aux; //Leaves are stored in
                                                           44
       for (int i = 1; i <= q; ++i) {</pre>
                                                                  continuous nodes with indices starting with {\tt N}
           cout << ans[i] << endl;</pre>
                                                           45
                                                           46
110 }
                                                           47
                                                                  st.build();
                                                           48
                                                                  x = st.query(inicio, fim);
112 // Driver Code
                                                                  st.update(ind, value);
                                                           49
113 int main()
                                                           50
114 {
                                                           51 }
       int arr[] = { 7, 3, 9, 13, 5, 4 };
       int n = sizeof(arr) / sizeof(arr[0]);
                                                                   Recursive-SegTree
       // 1-based indexing
       int QueryL[] = { 1, 2 };
                                                           1 // Segment Tree Recursiva - Range maximum query
       int QueryR[] = { 4, 6 };
                                                           3 vector < int > val(MAX, 0);
       // k for each query
                                                            4 vector < int > vet(N);
```

55

56

57

58

60

62

63

65

66

67

68

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72

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80

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98 99

100

103

104

105

106

107

108

109

115

116

117

118

119

120

```
x = consulta(1, 1, N, inicio, fim);
                                                          76
6 void monta(int i, int j, int no)
                                                          78 }
7 {
      if(i==j)
8
                                                             4.4 Delta-Encoding
9
          val[no]=vet[i];
10
          return:
                                                           1 // Delta encoding
12
13
                                                           3 for(int i=0;i<q;i++)</pre>
      int esq = 2*no;
                                                           4 {
      int dir = 2*no+1;
15
                                                                 int l,r,x;
                                                           5
16
      int meio = (i+j)/2;
                                                                 cin >> 1 >> r >> x;
                                                           6
17
                                                                 delta[1] += x;
      monta(i, meio, esq);
18
                                                                 delta[r+1] = x;
19
      monta(meio+1, j, dir);
                                                           9 }
20
                                                          10
21
      val[no]=max(val[esq], val[dir]);
                                                          11 int atual = 0;
22 }
                                                          12
                                                          13 for (int i=0; i < n; i++)
24 void atualiza(int no, int i, int j, int pos, int
                                                          14 {
      novo_valor)
                                                                 atual += delta[i];
                                                          15
25 {
                                                          16
                                                                 v[i] += atual;
      if (i == i)
26
                                                          17 }
          val[no]=novo_valor;
28
                                                           4.5 Seg-Tree-Farao
      }else
29
30
          int esq = 2*no;
31
                                                           1 typedef struct
          int dir = 2*no+1;
                                                           2 {
          int meio = (i+j)/2;
33
                                                                 pii prefix, sufix, total, maximo;
34
                                                           4 } no;
           if (pos <= meio)</pre>
35
              atualiza(esq, i, meio, pos, novo_valor); 6 int noleft[MAX], noright[MAX]; //Guarda os valores
36
                                                                dos nos para que nao sejam calculados novamente
               atualiza(dir, meio+1, j, pos, novo_valor)
38
                                                                nas querys
                                                           7 int v[MAX];
39
                                                           8 no arvore[MAX];
          if (val[esq]>val[dir])
40
              val[no]=val[esq];
                                                          10 pii somar(pii a, pii b) // une pairs
41
42
                                                          11 {
43
               val[no]=val[dir];
                                                                 return mp(a.f+b.f, a.s+b.s);
                                                          12
      }
44
                                                          13 }
45 }
                                                          14
46
                                                          15 no une(no 1, no r)
47 int consulta(int no, int i, int j, int A, int B)
                                                          16 {
48 {
                                                                 if(1.total.s==0)
                                                          17
      if(i>B || j<A)</pre>
49
                                                                     return r;
          return -1;
                                                                  if(r.total.s==0)
                                                          19
      if(i>=A and j<=B)
51
                                                          20
                                                                    return 1;
          return val[no];
52
                                                          21
53
                                                          22
                                                                 no m;
      int esq = 2*no;
54
                                                          23
      int dir = 2*no+1;
                                                                 m.prefix = max(l.prefix, somar(l.total, r.prefix)
                                                          24
      int meio = (i+j)/2;
56
                                                                 ); //prefixo
                                                                 m.sufix = max(r.sufix, somar(r.total, l.sufix));
      int resp_esq = consulta(esq, i, meio, A, B);
58
                                                                 //sufixo
      int resp_dir = consulta(dir, meio+1, j, A, B);
59
                                                                 m.total = somar(1.total, r.total); //Soma de
60
                                                                 todos os elementos da subarvore
61
      if (resp dir==-1)
                                                                 m.maximo = max(max(1.maximo, r.maximo), somar(1.
62
          return resp_esq;
                                                                 sufix, r.prefix)); //Resultado para cada
63
      if (resp_esq==-1)
                                                                 subarvore
         return resp_dir;
64
                                                          28
65
                                                                 return m;
                                                          29
      if(resp_esq>resp_dir)
66
                                                          30 }
          return resp_esq;
                                                          31
68
                                                          32 no makenozero()
          return resp_dir;
69
                                                          33 {
70 }
                                                          34
71
                                                          35
                                                                 m.prefix=m.sufix=m.total=m.maximo=mp(0,0);
72 int main()
                                                                 return m;
                                                          36
73 {
                                                          37 }
      monta(1, N, 1);
75
      atualiza(1, 1, N, pos, valor);
                                                          39 no makeno(int k)
```

```
6 {
40 {
41
       no m;
                                                                   int resp=0;
       m.prefix=m.sufix=m.total=m.maximo=mp(k,1);
42
                                                             8
                                                                   for(int i=x;i>0;i-=i&-i)
       return m;
                                                             9
43
                                                                       for(int j=y;j>0;j-=j&-j)
44 }
                                                                            resp+=bit[i][j];
45
                                                            11
46 void monta(int n)
                                                            12
47 {
                                                                   return resp:
                                                            13
       if(noleft[n] == noright[n])
                                                            14 }
48
49
                                                            15
            arvore[n]=makeno(v[noleft[n]]);
                                                            16 void update(int x, int y, int delta)
50
51
            return:
                                                            17 {
       }
52
                                                            18
                                                                   for (int i=x;i<MAX;i+=i&-i)</pre>
                                                                       for (int j=y; j < MAX; j+=j&-j)</pre>
53
                                                            19
       int mid = (noleft[n]+noright[n])/2;
                                                                            bit[i][j]+=delta;
54
                                                            20
       noleft[2*n]=noleft[n]; noright[2*n]=mid;
55
                                                            21 }
56
       noleft[2*n+1]=mid+1; noright[2*n+1]=noright[n];
                                                            23 int query(int x1, y1, x2, y2)
57
58
       monta(2*n);
       monta(2*n+1);
                                                                   59
                                                            25
                                                                   (x1,y1);
60
       arvore[n]=une(arvore[2*n], arvore[2*n+1]);
61
                                                            26 }
62 }
                                                                    BIT
                                                               4.7
63
64 no busca(int n, int esq, int dir)
65 {
                                                            1 // (BIT) Fenwick Tree
       if(noleft[n]>=esq and noright[n]<=dir)</pre>
66
           return arvore[n];
67
                                                            3 int N, bit[MAX];
       if(noright[n] < esq or noleft[n] > dir)
68
           return makenozero();
69
                                                             5 int soma(int x)
70
                                                             6 {
       return une(busca(2*n, esq, dir),busca(2*n+1, esq,
71
                                                                   int resp=0;
        dir));
72 }
                                                                   // for(int i=x;i>0;i-=i&-i)
73
                                                                   //
                                                                         resp+=bit[i];
                                                            10
74 int main()
                                                            11
75 ₹
                                                                   while (x > 0)
                                                            12
76
       int T, N, Q, A, B;
                                                            13
77
       no aux;
                                                            14
                                                                       resp += bit[x];
78
                                                                       x = (x & -x);
                                                            15
79
       scanf("%d", &T);
                                                            16
80
                                                            17
       while (T--)
81
                                                            18
                                                                   return resp;
82
                                                            19 }
            scanf("%d", &N);
83
                                                            20
84
            for (int i=1;i<=N;i++)</pre>
                scanf("^{'}d", &v[i]); //Elementos da arvore ^{21} int query(int L, int R)
85
                                                            22 {
                                                                   return soma(R)-soma(L-1);
           noleft[1]=1; noright[1]=N;
87
                                                            24 }
           monta(1);
88
                                                            25
89
                                                            26 void update(int x, int v) // add v in x
           cin >> Q;
90
                                                            27 {
           while (Q--)
                                                                   // for(;x<=n;x+=x&-x)
                                                            28
           {
92
                                                                            bit[x] += v;
                                                                   //
                                                            29
                scanf("%d%d", &A, &B); //Intervalo da
93
                                                            30
       query
                                                                   while(x <= N)</pre>
                                                            31
                aux = busca(1, A, B);
94
                                                                   {
                                                            32
                printf("%d %d\n", aux.maximo.f, aux.
95
                                                                       bit[x] += v;
       maximo.s):
                                                                       x += (x & -x);
                                                            34
96
           }
                                                            35
       }
97
                                                            36 }
98
99
                                                                     Sparse-Table
       return 0:
100
101 }
                                                             1 // Precompute log2
   4.6 BIT-2D
                                                             2 int logv[MAXN+1];
                                                             3 \log v[1] = 0;
 1 // BIT 2D
                                                             4 for (int i = 2; i <= MAXN; i++)
                                                                   logv[i] = logv[i/2] + 1;
                                                             5
 3 int bit[MAX][MAX];
                                                             7 int st[MAXN][K];
 5 int sum(int x, int y)
```

```
9 void precompute(int N)
                                                                     return d:
                                                              13
10 {
                                                              14 }
       for (int i = 0; i < N; i++)</pre>
11
                                                              15
          st[i][0] = array[i];
12
                                                              16 bool find_any_solution(int a, int b, int c, int &x0,
                                                                     int &y0, int &g)
       int k = logv[N];
                                                              17 €
14
       for (int j = 1; j <= k; j++)
    for (int i = 0; i + (1 << j) <= N; i++)</pre>
                                                                     g = gcd(abs(a), abs(b), x0, y0);
                                                              18
                                                                     if (c % g)
16
                                                              19
               st[i][j] = max(st[i][j-1], st[i + (1 << (20))]
                                                                         return false;
       j - 1))][j - 1]);
                                                                     x0 *= c / g;
18 }
                                                                     y0 *= c / g;
20 int query(int L, int R)
                                                                     if (a < 0) x0 = -x0;
                                                              24
21 {
                                                                     if (b < 0) y0 = -y0;
       int j = logv[R - L + 1];
                                                                     return true;
       int minimum = min(st[L][j], st[R - (1 << j) + 1][27 }</pre>
       j]);
24 }
                                                              29 // All solutions
                                                              30 // x = x0 + k*b/g
       Union-Find
                                                              31 // y = y0 - k*a/g
  4.9
```

```
1 // Union-Find Functions
3 int pai[MAX], peso[MAX];
5 int find(int aux)
       if(pai[aux] == aux)
          return aux;
9
           return pai[aux]=find(pai[aux], pai);
10
11 }
12
13 void join(int x, int y)
14 {
       x = find(x);
15
      y = find(y);
16
17
       if (pesos[x] < pesos[y])</pre>
          pai[x] = y;
19
       else if(pesos[x]>pesos[y])
          pai[y] = x;
21
       else if(pesos[x] == pesos[y])
22
23
           pai[x] = y;
24
           pesos[y]++;
25
26
27 }
28
29 int main()
30 €
       for(int i=1;i<=N;i++)</pre>
31
           pai[i]=i;
32
```

5 Math

33 }

5.1 Linear-Diophantine-Equation

```
1 // Linear Diophantine Equation
2 int gcd(int a, int b, int &x, int &y)
3 {
4     if (a == 0)
5     {
6         x = 0; y = 1;
7         return b;
8     }
9     int x1, y1;
10     int d = gcd(b%a, a, x1, y1);
11     x = y1 - (b / a) * x1;
12     y = x1;
```

5.2 Factorization-sqrt

```
1 // Factorization of a number in sqrt(n)
3 int main()
4 {
       11 N;
       vector < int > div;
6
       cin >> N;
       for(ll i=2;i*i<=N;i++)</pre>
10
11
12
            if(N\%i==0)
13
            {
                vet.pb(i);
                while(N%i==0)
15
                     N/=i;
16
17
            }
18
       if (N!=1)
19
           vet.pb(N);
20
21
       return 0:
22
23 }
```

5.3 Modular-Exponentiation

```
1 // Modular exponentiaion - (x^y)%mod in O(log y)
2 ll power(ll x, ll y, ll mod)
3 {
       11 \text{ res} = 1;
       x\%=mod;
       while(y)
8
            if (y&1)
9
               res=(res*x)%mod;
10
11
           y = y >> 1;
12
13
           x=(x*x)%mod;
14
15
       return res;
16 }
```

5.4 Miller-Habin

```
1 #include <bits/stdc++.h>
2 #define mod 1000000007
3 #define Pi 3.14159265358979311599796346854
4 #define INF 0x3f3f3f3f
```

```
5 #define MAX 1000010
                                                                           if(b & 1)
                                                               77
6 #define f first
                                                               78
                                                                              ans = mul(ans, a, c);
7 #define s second
                                                                           a = mul(a, a, c);
                                                               79
8 #define 11 long long
                                                                           b /= 2;
                                                               80
9 #define pb push_back
                                                               81
                                                                       }
10 #define mp make_pair
                                                                       return ans:
                                                               82
11 #define pii pair<int, int>
                                                               83 }
12 #define vi vector<int>
                                                               84
13 #define vii vector< pii >
                                                               85 bool rabin(ll n)
14 #define sws ios_base::sync_with_stdio(false);cin.tie(86 {
      NULL)
                                                                       if (n <= 1)</pre>
                                                               87
15 #define forn(i, n) for(int i=0; i<(int)(n); i++)
                                                               88
                                                                           return 1;
                                                                       if(n <= 3)
16 #define mdc(a, b) (__gcd((a), (b)))
                                                               89
17 #define mmc(a, b) (((a)/_{-g}cd(a, b)) * b)
                                                                           return 1;
                                                               90
_{18} #define endl '\n'
                                                               91
19 #define teto(a, b) (a+b-1)/b
                                                                       11 s=0, d=n-1;
                                                               92
                                                               93
                                                                       while (d\%2==0)
21 using namespace std;
                                                                       {
                                                               94
                                                                           d/=2;
23 ll llrand()
                                                               96
                                                                           s++;
24 {
                                                               97
       11 tmp = rand();
25
                                                               98
       return (tmp << 31) | rand();</pre>
                                                               99
                                                                       for(int k = 0; k < 64*4; k++)
26
27 }
                                                              100
                                                                           11 a = (11rand()\%(n - 3)) + 2;
28
                                                                           11 x = fexp(a, d, n);
29 ll add(ll a, ll b, ll c)
                                                               102
                                                                           if (x != 1 and x != n-1)
30 €
                                                              103
       return (a + b)%c;
                                                                           {
31
                                                              104
32 }
                                                              105
                                                                                for(int r = 1; r < s; r++)</pre>
                                                                                Ł
33
                                                              106
34 ll mul(ll a, ll b, ll c)
                                                                                    x = mul(x, x, n);
                                                               107
                                                                                    if(x == 1)
35 €
                                                              108
       11 \text{ ans} = 0;
                                                              109
                                                                                        return 0;
36
37
       while(b)
                                                              110
                                                                                    if(x == n-1)
                                                                                        break;
       {
38
                                                              111
            if(b & 1)
39
               ans = add(ans, a, c);
                                                                                if(x != n-1)
40
                                                              113
           a = add(a, a, c);
                                                                                    return 0;
41
                                                              114
           b /= 2;
                                                              115
                                                                           }
42
       }
                                                              116
43
44
       return ans;
                                                              117
45 }
                                                                       return 1;
                                                              118
                                                              119 }
47 ll rho(ll n)
                                                              120
                                                              121
48 {
49
       ll x, c, y, d, k;
                                                              122 int main()
       int i;
                                                              123 €
50
       do{
                                                              124
                                                                       //sws;
                                                                       //freopen("input.txt", "r", stdin);
//freopen("output.txt", "w", stdout);
           i = 1;
52
                                                              125
53
           x = llrand()%n;
                                                              126
           c = llrand()%n;
54
                                                              127
           y = x, k = 4;
                                                                       11 N, resp;
55
                                                              128
           do{
                                                              129
                                                                       vector<ll> div;
                if(++i == k)
57
                                                              130
                {
                                                              131
                                                                       cin >> N;
58
                     y = x;
                                                                       resp = N;
59
                                                              132
                    k *= 2;
60
                                                              133
                }
                                                                       while(N>1 and !rabin(N))
                                                              134
                x = add(mul(x, x, n), c, n);
62
                                                              135
                                                                       {
                d = \_\_gcd(abs(x - y), n);
                                                                           11 d = rho(N);
63
                                                               136
           }
64
                                                              137
                                                                           if(!rabin(d))
           while(d == 1);
                                                              138
                                                                               continue;
65
       }
                                                              139
                                                                           div.pb(d);
66
       while(d == n);
                                                                           while (N\%d==0)
                                                              140
67
                                                               141
                                                                               N/=d;
       return d:
69
                                                              142
70 }
                                                                       if(N!=resp and N!=1)
                                                              143
                                                              144
                                                                           div.pb(N);
72 ll fexp(ll a, ll b, ll c)
                                                              145
73 {
                                                               146
       ll ans = 1;
                                                                       if (div.empty())
74
                                                              147
       while(b)
                                                                           cout << resp << endl;</pre>
75
                                                               148
76
       {
                                                               149
```

```
150
                                                              46
            for(int i=0;i<(int)div.size();i++)</pre>
                                                              47
                                                                              x = add(mul(x, x, n), c, n);
                                                                              d = \_gcd(abs(x - y), n);
                resp = __gcd(resp, div[i]);
152
                                                              48
                                                                          }
                                                              49
            cout << resp << endl;</pre>
                                                              50
                                                                          while(d == 1);
                                                              51
                                                                     while(d == n);
                                                              52
       return 0;
157
                                                              53
                                                              54
                                                                     return d;
158
159 }
                                                              55 }
                                                              56
   5.5 Inverso-Mult
                                                              57 int main()
                                                              58 {
                                                                     srand(time(0));
 _{1} // ax + my = 1, e gcd(a, m) = 1 para existir solucao _{60}^{\circ\circ}
 2 // outra forma de escrever: a*x = 1 (mod m)
                                                                     11 N;
                                                              61
 3 int x, y;
                                                                     cin >> N;
 4 int g = gcd(a, m, x, y);
                                                              63
 5 if (g != 1)
                                                                     11 \text{ div} = \text{rho}(N);
       cout << "No solution!";</pre>
                                                                     cout << div << " " << N/div << endl;
                                                              65
 7 else
                                                              66
 8 {
                                                              67
       x = (x\%m + m) \% m;
 9
                                                              68
                                                                     // Finding all divisors
       cout << x << endl;
10
                                                              69
11 }
                                                                     vector < 11 > div;
                                                              70
                                                              71
   5.6 Pollard-Rho
                                                                     while(N>1 and !rabin(N))
                                                              72
                                                                     {
                                                              73
                                                              74
                                                                          11 d = rho(N);
 1 // Pollard Rho Algorithm
                                                                          if(!rabin(d))
                                                              75
                                                                              continue;
                                                              76
 3 #include <bits/stdc++.h>
                                                                          div.pb(d);
 4 #define 11 long long
                                                              77
                                                              78
                                                                          while (N\%d==0)
 6 using namespace std;
                                                              79
                                                                             N/=d;
                                                              80
                                                                     if(N!=resp and N!=1)
 8 ll llrand()
                                                              81
                                                                          div.pb(N);
                                                              82
 9 {
                                                              83
 10
       11 tmp = rand();
        return (tmp << 31) | rand();</pre>
                                                              84
                                                                     return 0;
11
                                                              85
12 }
                                                              86 }
13
 14 ll add(ll a, ll b, ll c)
                                                                       Verif-primo
                                                                 5.7
15 {
       return (a + b)%c;
16
17 }
                                                               1 // prime verification sqrt(N)
18
19 ll mul(ll a, ll b, ll c)
                                                               3 bool eh_primo(long long N)
20 {
21
       11 \text{ ans} = 0;
                                                                     if(N==2)
                                                               5
       while(b)
22
                                                                         return true;
                                                               6
23
                                                                     else if (N==1 \text{ or } N\%2==0)
            if(b & 1)
24
                                                                         return false;
              ans = add(ans, a, c);
25
                                                                      for(long long i=3;i*i<=N;i+=2)</pre>
            a = add(a, a, c);
                                                                         if(N\%i==0)
                                                              10
            b /= 2;
27
                                                              11
                                                                             return false;
       }
28
                                                                     return true;
                                                              12
29
        return ans;
                                                              13 }
30 }
                                                                 5.8 Crivo
32 ll rho(ll n)
33 {
                                                              1 // Sieve of Eratosthenes
34
        ll x, c, y, d, k;
        int i;
35
36
        do{
                                                              3 int N;
           i = 1;
                                                              4 vector < bool > primos (100010, true);
37
           x = 11rand()%n;
                                                               5 cin >> N;
38
           c = llrand()%n;
39
            y = x, k = 4;
                                                               7 primos[0]=false;
40
            do{
                                                               8 primos[1]=false;
41
                if(++i == k)
42
                                                              10 for(int i=2;i<=N;i++)</pre>
                     y = x;
                                                              if (primos[i])
44
                     k *= 2;
                                                                         for(int j=i+i; j<=N; j+=i)</pre>
45
                                                              12
```

```
primos[j]=false;
                                                              62
                                                              63
                                                                     FFT(in,out,step*2,size/2,dir);
  5.9 Formulas
                                                                     FFT(in+step,out+size/2,step*2,size/2,dir);
                                                              64
                                                              65
                                                                     for(int i=0;i<size/2;++i)</pre>
                                                              66
1 int sum_x2(11 N)
                                                                          cpx even=out[i];
                                                              67
2 {
                                                                          cpx odd=out[i+size/2];
                                                              68
       return (2*N*N*N + 3*N*N + N)/6;
3
                                                                          out[i] = even+EXP(i*step,dir)*odd;
                                                              69
4 }
                                                                          out[i+size/2] = even+EXP((i+size/2)*step,dir)*
                                                              70
                                                                     odd;
         FFT-golfbot
  5.10
                                                              71
                                                              72 }
1 #include <bits/stdc++.h>
                                                              73
                                                              74 int main()
3 using namespace std;
                                                              75 {
                                                                     for(int i=0;i<=N;++i)</pre>
                                                              76
5 \text{ const int } N = (1 << 19);
                                                              77
                                                                          coss[i] = cos(two_pi*i/N);
6 const double two_pi = 4 * acos(0);
                                                              78
                                                                          sins[i]=sin(two_pi*i/N);
                                                              79
                                                                     }
8 struct cpx
                                                              80
                                                                     while(cin >> n) // Numero de tacadas possiveis
                                                              81
9 {
       cpx(){}
                                                              82
10
                                                                          fill(x,x+N+100,0);
       cpx(double aa): a(aa){}
                                                              83
                                                                          fill(a,a+N+100,0);
12
       cpx(double aa,double bb):a(aa),b(bb){}
                                                                          for (int i=0; i < n; ++i)</pre>
                                                              85
       double a;
       double b;
                                                              86
14
                                                                              cin >> p; // Distancia das tacadas
       double modsq(void) const
                                                              87
15
                                                                              x[p]=1;
                                                              88
16
                                                                          }
                                                              89
           return a*a+b*b:
17
                                                                          for (int i=0;i<N+100;++i)</pre>
18
       }
                                                              90
                                                              91
       cpx bar(void) const
19
                                                                              b[i]=cpx(x[i],0);
                                                              92
20
                                                                          }
                                                              93
21
           return cpx(a,-b);
       }
                                                              94
                                                                          cin >> m; // Querys
22
                                                                          for (int i=0; i < m; ++i)</pre>
                                                              95
23 };
                                                              96
24
                                                                              cin >> a[i]; // Distancia da query
25 cpx b[N+100];
                                                              97
                                                              98
26 cpx c[N+100];
                                                                          FFT(b,B,1,N,1);
                                                              99
27 cpx B[N+100];
                                                                          for (int i=0; i < N; ++i)</pre>
                                                             100
28 cpx C[N+100];
                                                                              C[i]=B[i]*B[i];
29 int a[N+100];
                                                                          FFT(C,c,1,N,-1);
30 int x[N+100];
                                                                          for (int i=0;i<N;++i)</pre>
                                                             103
31 double coss[N+100], sins[N+100];
                                                             104
                                                                              c[i]=c[i]/N;
32 int n,m,p;
                                                                          int cnt=0;
                                                             105
33
                                                             106
                                                                          for (int i=0;i<m;++i)</pre>
34 cpx operator +(cpx a,cpx b)
                                                                              if(c[a[i]].a>0.5 || x[a[i]])
35 {
                                                                                  cnt++:
       return cpx(a.a+b.a,a.b+b.b);
36
                                                                          cout << cnt << endl;</pre>
37 }
                                                             109
                                                             110
                                                                     }
38
                                                             111
                                                                     return 0;
39 cpx operator *(cpx a,cpx b)
                                                             112 }
40 {
       return cpx(a.a*b.a-a.b*b.b,a.a*b.b+a.b*b.a);
41
                                                                         Modular-Factorial
42 }
43
44 cpx operator /(cpx a,cpx b)
                                                               1 // C++ program to comput n! % p using Wilson's
45 {
                                                                     Theorem
       cpx r = a*b.bar();
                                                               2 #include <bits/stdc++.h>
46
       return cpx(r.a/b.modsq(),r.b/b.modsq());
                                                               3 using namespace std;
48 }
                                                               5 int power(int x, unsigned int y, int p)
49
50 cpx EXP(int i,int dir)
                                                               6 {
                                                                     int res = 1;
51 {
52
       return cpx(coss[i],sins[i]*dir);
                                                                     x = x \% p;
53 }
                                                                     while (y > 0)
                                                              10
55 void FFT(cpx *in,cpx *out,int step,int size,int dir) 11
                                                                          if (y & 1)
56 {
                                                              12
       if(size<1) return;</pre>
                                                                              res = (res * x) % p;
57
       if(size==1)
58
                                                              14
                                                                          y = y >> 1;
           out [0] = in [0];
                                                                          x = (x * x) % p;
60
                                                              16
           return:
                                                              17
61
```

```
AND -
                                                                                   a&b
                                                                                         // The result is 00000001
      return res:
18
19 }
                                                                   (1)
                                                                                         // The result is 00001101
                                                                  OR. -
                                                                                   alb
20
                                                            6
21 int modInverse(int a, int p)
                                                                   (13)
                                                                                         // The result is 00001100
22 {
                                                                  XOR -
                                                                                   a^b
       return power(a, p-2, p);
                                                                   (12)
23
                                                                                   ~a
                                                                                         // The result is 11111010
24 }
                                                                  NOT -
                                                                  (250)
25
26 int modFact(int n, int p)
                                                                                  b<<1 // The result is 00010010
                                                                  Left shift -
27 {
                                                                   (18)
                                                                  Right shift - b > 1 // The result is 00000100
       if (p \le n)
28
                                                           10
29
           return 0;
                                                                  (4)
30
       int res = (p - 1);
                                                                  // Exchange two int variables
31
                                                           12
32
                                                           13
       for(int i = n + 1; i < p; i++)</pre>
33
                                                           14
                                                                       b^=a;
34
          res = (res * modInverse(i, p)) % p;
                                                           15
                                                                       a^=b;
       return res;
35
                                                           16
36 }
                                                           17
                                                                  // Even or Odd
37
                                                           18
38 int main()
                                                           19
                                                                       (x & 1)? printf("Odd"): printf("Even");
39 {
                                                           20
       int n = 25, p = 29;
40
                                                           21
       cout << modFact(n, p);</pre>
                                                                  // Turn on the j-th bit
41
                                                           22
       return 0;
42
                                                           23
43 }
                                                           24
                                                                       int S = 34; //(100010)
                                                                       int j = 3;
                                                           25
  5.12 Kamenetsky
                                                           26
                                                           27
                                                                       S = S | (1 << j);
                                                           28
1 // Number of digits in n! O(1)
                                                                  // Turn off the j-th bit
                                                           29
                                                           30
3 #define Pi 3.14159265358979311599796346854
                                                                       int S = 42; //(101010)
                                                           31
4 #define Eul 2.71828182845904509079559829842
                                                           32
                                                                      int j = 1;
                                                           33
6 long long findDigits(int n)
                                                                       S &= ~(1<<j)
                                                           34
7 {
                                                           35
       double x;
8
                                                                       S == 40 //(101000)
                                                           36
9
                                                           37
       if (n < 0)
10
                                                                  // Check the j-th element
                                                           38
          return 0;
                                                           39
       if (n == 1)
12
                                                                       int S = 42; //(101010)
                                                           40
           return 1;
                                                                       int j = 3;
                                                           41
14
                                                           42
      x = ((n * log10(n / euler) + log10(2 * Pi * n))
                                                                       T = S & (1 << j); // T = 0
                                                           43
       /2.0));
16
                                                                  // Least significant bit (lsb)
                                                           45
       return floor(x) + 1;
17
18 }
                                                                       int lsb(int x)
                                                           47
                                                           48
                                                                       {
       Misc
                                                           49
                                                                           return x&-x;
                                                           50
                                                           51
  6.1 LIS
                                                                  // Exchange o j-th element
                                                           52
                                                           53
                                                                       S ^= (1<<j)
                                                           54
nultiset < int > S;
2 for(int i = 0; i < n; i++){</pre>
                                                                  // Position of the first bit on
      auto it = S.upper_bound(vet[i]); // low for inc
                                                           57
4
       if(it != S.end())
                                                                       T = (S & (-S))
                                                           58
          S.erase(it):
5
                                                                       T -> 4 bit ligado //(1000)
                                                           59
      S.insert(vet[i]);
6
                                                           60
7 }
                                                           61
                                                                  // Most significant digit of N
8 // size of the lis
                                                           62
9 int ans = S.size();
                                                           63
                                                                       double K = log10(N);
                                                           64
  6.2 Bitwise
                                                                       K = K - floor(K);
                                                           65
                                                           66
                                                                       int X = pow(10, K);
1 // Bitwise
                                                           67
                                                                  // Number of digits in N
2
       unsigned char a = 5, b = 9; // a = (00000101), b 69
                                                                       X =floor(log10(N)) + 1;
       = (00001001)
```

```
int divisor = 1;
72
      // Power of two
                                                           6
73
                                                           7
                                                                 while(n/divisor >= 10)
          bool isPowerOfTwo(int x)
                                                                     divisor *= 10;
74
                                                           8
75
           {
                                                           9
                                                                 while (n != 0)
76
               return x && (!(x&(x-1)));
                                                          10
          }
                                                                 {
77
                                                          11
                                                                     int leading = n / divisor;
                                                          12
                                                                     int trailing = n % 10;
       Strings
                                                          13
                                                          14
                                                                     if(leading != trailing)
                                                          15
  7.1 KMP
                                                                         return false;
                                                          16
                                                          17
                                                                     n = (n \% divisor)/10;
vector<int> preffix_function(const string &s){
                                                          18
                                                          19
      int n = s.size(); vector<int> b(n+1);
      b[0] = -1; int i = 0, j = -1;
                                                                     divisor = divisor/100;
                                                          20
                                                          21
      while(i < n){
          while(j >= 0 && s[i] != s[j]) j = b[j];
                                                                 return true;
                                                          23
          b[++i] = ++j;
6
                                                          24 }
      return b;
                                                             7.3 Z-Func
9 }
10 void kmp(const string &t, const string &p){
      vector < int > b = preffix_function(p);
11
                                                          vector < int > z_algo(const string &s)
      int n = t.size(), m = p.size();
12
      int j = 0;
13
                                                                 int n = s.size();
      for(int i = 0; i < n; i++){</pre>
                                                                 int L = 0, R = 0;
          while(j >= 0 && t[i] != p[j]) j = b[j];
                                                                 vector < int > z(n, 0);
1.5
16
          j++;
                                                                 for(int i = 1; i < n; i++)</pre>
          if (j == m) {
17
18
                                                           8
                                                                     if(i <= R)</pre>
               j = b[j];
                                                                         z[i] = min(z[i-L], R - i + 1);
          }
20
                                                                     while (z[i]+i < n && s[z[i]+i] == s[z[i]])
                                                          10
      }
21
                                                          11
                                                                         z[i]++;
22 }
                                                                     if(i+z[i]-1 > R)
                                                          12
                                                                     {
                                                          13
  7.2 Pal-int
                                                          14
                                                                         L = i;
```

15

16

17

18

19 }

}

return z;

}

1 bool ehpalindromo(ll n)

return false;

if(n<0)

2 {

3

4

R = i + z[i] - 1;

14