

# Notebook - Maratona de Programação

# Tiago de Souza Fernandes

$\mathbf{S}$	umário			5.7 Verif-primo	
1	Algoritmos 1.1 Mochila	2 2 2		5.8 Crivo	12 12 12
<b>2</b>	Grafos	2		5.12 Kamenetsky	10
	2.1 BFS	2	6	6 Misc	13
	2.2 Find-bridges	2		6.1 LIS	13
	2.3 Dijkstra	2		6.2 Bitwise	13
	2.4 Floyd-Warshall	3	_		
	2.5 Kruskal	3	7	8	14
	2.6 DFS	3		7.1 KMP	
	2.7 Represent	3		7.2 Pal-int	
	2.8 Prim	4		7.3 Z-Func	14
3	Geometria	4			
	3.1 Inter-Retas	4			
	3.2 Inter-Retangulos	5			
	3.3 Analytic-Geometry	5			
4	ED	5			
	4.1 Range-query-bigger-than-k-BIT	5			
	4.2 Iterative-SegTree	6			
	4.3 Recursive-SegTree	7			
	4.4 Delta-Encoding	7			
	4.5 Seg-Tree-Farao	7			
	4.6 BIT-2D	8			
	4.7 BIT	8			
	4.8 Sparse-Table	9			
	4.9 Union-Find	9			
5	Math	9			
	5.1 Linear-Diophantine-Equation	9			
	5.2 Factorization-sqrt	9			
	5.3 Modular-Exponentiation	9			
	5.4 Miller-Habin	10			
	5.5 Inverso-Mult	11			
	5.6 Pollard Pho	11			

## 1 Algoritmos

#### 1.1 Mochila

```
1 int val[MAXN], peso[MAXN], dp[MAXN][MAXS]
3 int knapsack(int N, int M) // Objetos | Peso max
4 {
       for (i=0;i<=N;i++)</pre>
5
6
          for (j=0; j <= M; j++)</pre>
                if (i==0 || j==0)
                    dp[i][j] = 0;
10
                else if (peso[i-1] <= j)</pre>
11
                    dp[i][j] = max(val[i-1]+dp[i-1][j-
      peso[i-1]], dp[i-1][j]);
                    dp[i][j] = dp[i-1][j];
14
      }
16
17
      return dp[N][M];
```

#### 1.2 Iterative-BS

```
1 int main()
       int l=1, r=N;
       int res=-1;
4
       while(1 <= r)</pre>
            int m = (1 + r)/2;
            if(!ver(m))
            {
10
                1 = m+1;
11
            }
            else
13
14
            {
                res = m;
15
            }
18
       cout << res << endl;</pre>
20
       return 0;
22 }
```

#### 2 Grafos

#### 2.1 BFS

```
if (d[u] > d[v] + 1) {
17
                q.push(u);
18
                d[u] = d[v] + 1;
19
                //p[u] = v;
20
22
24 // Restore Path
25 if (!used[u]) {
       cout << "No path!";</pre>
27 } else {
       vector < int > path;
       for (int v = u; v != -1; v = p[v])
29
           path.push_back(v);
30
31
       reverse(path.begin(), path.end());
       cout << "Path: ";</pre>
32
33
       for (int v : path)
           cout << v << " ";
34
35 }
```

#### 2.2 Find-bridges

```
1 #define vi vector<int>
3 vector < vector < int > > grafo;
4 vector < bool > visited;
5 vi t, low;
6 int timer=0;
8 void find_bridges(int v, int p=-1)
9 {
10
       visited[v] = true;
       t[v] = low[v] = timer++;
11
       for(int i=0;i<(int)grafo[v].size();i++)</pre>
12
13
14
           int vert = grafo[v][i];
           if (vert == p)
15
                continue;
16
17
           if(visited[vert])
               low[v] = min(low[v], t[vert]);
18
           {
20
                find_bridges(vert, v);
22
                low[v] = min(low[v], low[vert]);
                if(low[to] > t[v])
23
                    IS_BRIDGE(v, vert);
24
           }
25
       }
27 }
28
29 int main()
30 {
       timer = 0;
31
       visited.assign(N+1, false);
32
33
       t.assign(N+1, 0);
34
       low.assign(N+1, 0);
35
       for(int i=0;i<N;i++)</pre>
           if(!visited[i])
37
                find_bridges(1);
38
39
40
       return 0;
41 }
```

### 2.3 Dijkstra

```
1 // Dijkstra - Shortest Path
2
3 #define pii pair<int, int>
4 #define vi vector<int>
5 #define vii vector< pair<int,int> >
6 #define INF 0x3f3f3f3f
```

```
return X:
                                                             1.5
8 vector < vii > grafo(N+1, vii());
                                                             16
                                                                    else
                                                                        return pai[X]=find(pai[X]);
9 vi distancia(N+1, INF);
                                                             17
10 priority_queue < pii, vii, greater <pii>> fila;
                                                             18 }
12 void dijkstra(int k)
                                                             20 void join(int X, int Y)
13 {
                                                             21 {
                                                                    int paix = find(X);
       int dist, vert, aux;
14
                                                             22
       distancia[k]=0;
                                                                    int paiy = find(Y);
15
                                                             23
                                                             24
                                                                    pai[paix]=paiy;
16
       fila.push(mp(k, 0));
                                                             25 }
17
       while(!fila.empty())
19
                                                             27 bool comp(vertice A, vertice B)
                                                             28 {
20
                                                                    return A.dist < B.dist;</pre>
21
           aux=fila.top().f;
                                                             29
           fila.pop();
                                                             30 }
22
23
           for(auto v: grafo[aux])
                                                             32 void kruskal()
24
                                                                    for(int i=1;i<=N;i++)</pre>
26
               vert=v.f;
                                                             34
                                                                       pai[i]=i;
               dist=v.s;
                                                             35
27
               if (distancia[vert]>distancia[aux]+dist)
                                                                    for(int i=1;i<=M;i++)</pre>
29
                    distancia[vert]=distancia[aux]+dist; 38
                                                                        cin >> grafo[i].A >> grafo[i].B >> grafo[i].
                    fila.push(mp(vert, distancia[vert]));
31
               }
                                                                    sort(grafo+1, grafo+M+1, comp);
32
                                                             40
           }
33
                                                             41
       }
                                                             42
                                                                    for(int i=1;i<M;i++)</pre>
34
35 }
                                                             43
                                                                         if(find(grafo[i].A)!=find(grafo[i].B))
                                                             44
37 int main()
                                                             45
38 {
                                                                             join(grafo[i].A, grafo[i].B);
                                                             46
39
       for(int i=0; i<M; i++)</pre>
                                                             47
                                                                             soma+=grafo[i].dist;
                                                                        }
40
                                                             48
           cin >> a >> b >> p;
41
                                                             49
           grafo[a].pb(mp(b, p));
42
                                                             50
                                                                    cout << soma << endl;</pre>
           grafo[b].pb(mp(a, p));
                                                             51
43
       }
                                                             52 }
44
45 }
                                                                     DFS
                                                               2.6
  2.4 Floyd-Warshall
                                                             1 //DFS (Depth First Search) O(V+A)
1 // Floyd Warshall
                                                             3 void DFS(int x)
3 int dist[MAX][MAX];
                                                              4 {
                                                                    for(int i=0; i<(int)vizinhos[x].size(); i++)</pre>
                                                             5
5 void Floydwarshall()
6 {
                                                                        int v = vizinhos[x][i];
       for(int k = 1; k <= n; k++)</pre>
                                                                        if (componente[v] == -1)
           for(int i = 1;i <= n;i++)</pre>
               for(int j = 1; j <= n; j++)</pre>
                                                                             componente[v] = componente[x];
                    dist[i][j] = min(dist[i][j], dist[i][11
                                                                             DFS(v);
      k] + dist[k][j]);
                                                                        }
                                                             12
                                                                    }
                                                             13
                                                             14 }
  2.5 Kruskal
                                                                     Represent
1 // Kruskal - Minimum Spanning Tree
                                                              1 // Grafos
3 typedef struct
                                                             3 // List of edges
       int A, B;
      int dist;
                                                                    vector< pair<int, int> > arestas;
7 } vertice;
                                                                    arestas.push_back(make_pair(1, 2));
                                                                    arestas.push_back(make_pair(1, 3));
9 vertice grafo[MAX];
10 int pai[MAX];
                                                             9 // Adjacency Matrix
                                                             10
12 int find(int X) // Union-Find
                                                                    int grafo[10][10];
                                                             11
```

12

13

grafo[1][2] = grafo[2][1] = 1;

13 **{** 

if(pai[X]==X)

```
grafo[1][3] = grafo[3][1] = 2;
                                                            58 }
14
15
16 // Adjacency List
                                                            60 int main(){
17
                                                            61
      vector < int > vizinhos[10];
                                                            62
                                                                   cin >> n >> m;
19
                                                            63
      vizinhos[1].push_back(2);
                                                                   for(int i = 1;i <= m;i++){</pre>
                                                            64
      vizinhos[1].push_back(2);
21
                                                            65
                                                                       int x, y, tempo;
                                                            66
  2.8 Prim
                                                            67
                                                                       cin >> x >> y >> tempo;
                                                            68
1 // Prim Algorithm
                                                            69
                                                                       vizinhos[x].pb( pii(tempo, y) );
2 #define MAXN 10100
                                                            70
                                                                       vizinhos[y].pb( pii(tempo, x) );
3 #define INFINITO 999999999
                                                            71
                                                            72
                                                                   cout << Prim() << endl;</pre>
                                                            73
5 int n, m;
6 int distancia[MAXN];
                                                            74
                                                                   return 0;
                                                            75
7 int processado[MAXN];
8 vector < pii > vizinhos [MAXN];
                                                            76 }
                                                               3
                                                                   Geometria
10 int Prim()
11 {
       for(int i = 2;i <= n;i++) distancia[i] = INFINITO</pre>
                                                              3.1
                                                                    Inter-Retas
       distancia[1] = 0;
13
                                                             1 // Intersection between lines
14
      priority_queue < pii, vector <pii>, greater <pii> >
15
                                                             3 typedef struct
      fila.push( pii(distancia[1], 1) );
                                                            4 {
16
                                                                   int x, y;
18
      while (1)
                                                             6 } pnt;
19
20
           int davez = -1;
                                                            8 bool collinear(pnt p, pnt q, pnt r)
                                                            9 {
21
           while(!fila.empty())
                                                                   if (q.x<=max(p.x,r.x) && q.x>=min(p.x,r.x) && q.y
                                                                   <=max(p.y,r.y) && q.y>=min(p.y,r.y))
           {
23
               int atual = fila.top().second;
                                                            11
                                                                       return true;
25
               fila.pop();
                                                            12
                                                                   return false;
26
                                                            13
               if(!processado[atual])
                                                            14 }
28
                                                            15
                    davez = atual;
                                                            int orientation(pnt p, pnt q, pnt r)
30
                   break:
                                                            17 {
               }
                                                                   int val=(q.y-p.y)*(r.x-q.x)-(q.x-p.x)*(r.y-q.y);
                                                            18
31
32
           }
                                                            19
                                                                   if(val==0)
33
                                                            20
34
           if(davez == -1)
                                                            21
                                                                       return 0;
                                                                   else if(val>0)
               break:
35
                                                            22
36
                                                            23
                                                                       return 1;
           processado[davez] = true;
37
                                                                   else
                                                                       return 2;
38
           for(int i = 0;i < (int)vizinhos[davez].size() 26 }</pre>
39
      ;i++)
                                                            28 bool intersect(pnt p1, pnt q1, pnt p2, pnt q2)
41
                                                            29 {
               int dist = vizinhos[davez][i].first;
                                                            30
                                                                   int o1 = orientation(p1, q1, p2);
42
               int atual = vizinhos[davez][i].second;
                                                            31
                                                                   int o2 = orientation(p1, q1, q2);
43
                                                                   int o3 = orientation(p2, q2, p1);
44
                                                            32
               if( distancia[atual] > dist && !
                                                                   int o4 = orientation(p2, q2, q1);
       processado[atual])
                                                            34
                                                                   if(o1!=o2 and o3!=o4)
               {
46
                                                            35
                    distancia[atual] = dist;
47
                                                            36
                                                                       return true;
                   fila.push( pii(distancia[atual],
                                                            37
48
       atual));
                                                            38
                                                                   if(o1==0 && collinear(p1, p2, q1))
                                                                       return true;
49
                                                            39
           }
50
                                                            40
      }
51
                                                            41
                                                                   if(o2==0 && collinear(p1, q2, q1))
52
                                                            42
                                                                       return true;
      int custo_arvore = 0;
53
                                                            43
                                                                   if(o3==0 && collinear(p2, p1, q2))
      for(int i = 1;i <= n;i++)</pre>
54
                                                            44
           custo_arvore += distancia[i];
                                                                       return true;
56
                                                            46
      return custo_arvore;
                                                            47
                                                                   if(o4==0 && collinear(p2, q1, q2))
```

```
return a.x*b.y - a.y*b.x;
          return true:
48
                                                         49
49
                                                         50 }
      return false;
50
                                                         51
                                                         52 // Dist entre dois pontos
51
52 }
                                                         53 double dist(point a, point b){
                                                                point c = sub(a, b);
                                                         54
      Inter-Retangulos
                                                                return sqrt(c.x*c.x + c.y*c.y);
  3.2
                                                         56 }
                                                         57
1 typedef struct
                                                         58 // Dist entre ponto e reta
2 {
                                                         59 double dist(point a, line b){
      int x, y;
                                                                double crs = cross(point(sub(a, b.fp)), point(sub
4 } Point;
                                                                (b.sp, b.fp)));
                                                                return abs(crs/dist(b.fp, b.sp));
6 bool doOverlap(Point 11, Point r1, Point 12, Point r2
7 {
                                                          64 // Area de um poligono (pontos ordenados por
      if (11.x>r2.x or 12.x>r1.x or 11.y<r2.y or 12.y<
                                                                adjacencia)
      r1.y)
                                                          65 double area(vector <point> p){
         return false;
                                                          66 double ret = 0;
10
      return true;
                                                          67
                                                              for(int i=2;i<(int)p.size();i++)</pre>
11 }
                                                                ret += cross(sub(p[i], p[0]), sub(p[i-1], p[0]))
  3.3 Analytic-Geometry
                                                          69 return abs(ret);
                                                         70 }
1 typedef struct Point
2 {
                                                            4
                                                                 ED
      double x, y;
      Point(int _x=0, int _y=0)
4
                                                            4.1
                                                                 Range-query-bigger-than-k-BIT
          x = _x; y = _y;
                                                          1 // C++ program to print the number of elements
                                                          _{\rm 2} // greater than k in a subarray of range L-R.
      void show()
                                                          3 #include <bits/stdc++.h>
9
                                                          4 using namespace std;
          cout << "x = " << x << endl;
          cout << "y = " << y << endl;
                                                          6 // Structure which will store both
12
                                                          _{7} // array elements and queries.
13
                                                          8 struct node {
14
15 } point;
                                                               int pos;
                                                          9
                                                                int 1:
                                                         10
17 typedef struct Line
                                                                int r;
                                                          11
18 {
                                                                int val;
                                                         12
      point fp, sp;
                                                         13 };
19
      Line(point _fp=0, point _sp=0)
                                                         15 // Boolean comparator that will be used
21
          fp=_fp;sp=_sp;
                                                         _{16} // for sorting the structural array.
      }
                                                         17 bool comp(node a, node b)
23
                                                         18 €
25 } line;
                                                                // If 2 values are equal the query will
                                                         19
                                                         20
                                                                // occur first then array element
27 point sum(point A, point B)
                                                                if (a.val == b.val)
                                                         21
                                                                    return a.l > b.l;
                                                         22
      return point(A.x+B.x, A.y+B.y);
                                                         23
30 }
                                                                // Otherwise sorted in descending order.
                                                         24
31
                                                         25
                                                                return a.val > b.val;
32 point sub(point A, point B)
                                                         26 }
33 €
                                                         27
      return point(A.x-B.x, A.y-B.y);
                                                         28 // Updates the node of BIT array by adding
                                                         _{29} // 1 to it and its ancestors.
35 }
                                                         30 void update(int* BIT, int n, int idx)
37 point neg(point A)
                                                         31 {
                                                                while (idx <= n) {</pre>
38 €
                                                         32
      return point(-A.x, -A.y);
                                                         33
                                                                    BIT[idx]++;
40 }
                                                                    idx += idx & (-idx);
                                                         34
                                                         35
42 // Produto Escalar
                                                         36 }
                                                         37 // Returns the count of numbers of elements
43 double dot(point a, point b){
      return a.x*b.x + a.y*b.y;
                                                         38 // present from starting till idx.
45 }
                                                         39 int query(int* BIT, int idx)
                                                          40 {
47 // Produto Vetorial
```

41

42

48 double cross(point a, point b){

int ans = 0;

while (idx) {

```
ans += BIT[idx]:
43
                                                            111
                                                            112 // Driver Code
44
           idx -= idx & (-idx);
                                                            113 int main()
45
                                                            114 {
46
                                                                    int arr[] = { 7, 3, 9, 13, 5, 4 };
       return ans;
48 }
                                                                    int n = sizeof(arr) / sizeof(arr[0]);
                                                            116
                                                            117
_{50} // Function to solve the queries offline
                                                                    // 1-based indexing
                                                            118
51 void solveQuery(int arr[], int n, int QueryL[],
                                                                    int QueryL[] = { 1, 2 };
                                                            119
                    int QueryR[], int QueryK[], int q)
                                                                    int QueryR[] = { 4, 6 };
                                                            120
53 {
                                                            121
54
       // create node to store the elements
                                                                    // k for each query
       // and the queries
                                                            123
                                                                    int QueryK[] = { 6, 8 };
       node a[n + q + 1];
56
                                                            124
       // 1-based indexing.
57
                                                                    // number of queries
                                                                    int q = sizeof(QueryL) / sizeof(QueryL[0]);
58
                                                            126
59
       // traverse for all array numbers
                                                            127
       for (int i = 1; i <= n; ++i) {</pre>
                                                                    // Function call to get
60
                                                            128
           a[i].val = arr[i - 1];
                                                                    solveQuery(arr, n, QueryL, QueryR, QueryK, q);
           a[i].pos = 0;
62
                                                            130
           a[i].1 = 0;
                                                            131
                                                                    return 0;
63
                                                            132 }
           a[i].r = i;
64
65
                                                                     Iterative-SegTree
                                                               4.2
       // iterate for all queries
67
       for (int i = n + 1; i <= n + q; ++i) {</pre>
68
                                                            1 // Segment Tree Iterativa - Range maximum query
            a[i].pos = i - n;
69
            a[i].val = QueryK[i - n - 1];
70
                                                             3 #define N 100010
            a[i].1 = QueryL[i - n - 1];
71
           a[i].r = QueryR[i - n - 1];
72
                                                              5 struct Segtree
                                                             6 {
74
                                                                    int t[2*N]={0};
       // In-built sort function used to
75
       // sort node array using comp function.
                                                                    void build()
                                                             9
       sort(a + 1, a + n + q + 1, comp);
77
                                                                        for(int i=N-1; i>0; i--)
                                                             11
       // Binary Indexed tree with
79
                                                                            t[i]=max(t[i<<1], t[1<<1|1]);
                                                             12
       // initially 0 at all places.
80
                                                             13
       int BIT[n + 1];
81
                                                             14
82
                                                                    int query(int 1, int r)
                                                             15
83
       // initially 0
                                                             16
       memset(BIT, 0, sizeof(BIT));
84
                                                                        int ans=0;
                                                             17
85
                                                                        for(i+=N, r+=N; 1<r; 1>>=1, r>>=1)
                                                             18
       // For storing answers for each query( 1-based
86
                                                             19
       indexing ).
                                                             20
                                                                             if (1&1)
       int ans[q + 1];
                                                                                 ans=max(ans, t[1++]);
                                                             21
88
                                                             22
                                                                             if(r&1)
       // traverse for numbers and query
                                                                                 ans=max(ans, t[--r]);
       for (int i = 1; i <= n + q; ++i) {</pre>
90
                                                             24
            if (a[i].pos != 0) {
91
                                                             25
92
                                                                        return ans;
                                                             26
                // call function to returns answer for
93
                int cnt = query(BIT, a[i].r) - query(BIT, 29
94
                                                                    void update(int p, int value)
        a[i].1 - 1);
                                                             30
95
                                                                        for(t[p+=n]=value; p>1; p>>=1)
                                                             31
                // This will ensure that answer of each
96
                                                                             t[p>>1] = max(t[p], t[p^1]);
       auerv
                                                             33
                // are stored in order it was initially
97
       asked.
                                                             35 };
98
                ans[a[i].pos] = cnt;
                                                             36
           }
99
                                                             37 int main()
                                                             38 €
                // a[i].r contains the position of the
                                                             39
                                                                    Segtree st;
                // element in the original array.
                                                             40
                update(BIT, n, a[i].r);
103
                                                                    for(int i=0;i<n;i++)</pre>
                                                             41
104
                                                             42
       }
                                                             43
                                                                        cin >> aux;
       // Output the answer array
106
                                                                        st.t[N+i]=aux; //Leaves are stored in
       for (int i = 1; i <= q; ++i) {
                                                                    continuous nodes with indices starting with \ensuremath{\mathtt{N}}
           cout << ans[i] << endl;</pre>
108
109
                                                             46
110 }
                                                                    st.build();
                                                             47
```

```
x = st.query(inicio, fim);
48
                                                           65
49
      st.update(ind, value);
                                                           66
                                                                  if (resp_esq>resp_dir)
50
                                                           67
                                                                     return resp_esq;
51 }
                                                           68
                                                           69
                                                                     return resp_dir;
  4.3 Recursive-SegTree
                                                          70 }
                                                          72 int main()
1 // Segment Tree Recursiva - Range maximum query
                                                           73 {
                                                           74
                                                                  monta(1, N, 1);
3 vector < int > val(MAX, 0);
                                                                  atualiza(1, 1, \mathbb{N}, pos, valor);
4 vector < int > vet(N);
                                                           75
                                                           76
                                                                  x = consulta(1, 1, N, inicio, fim);
6 void monta(int i, int j, int no)
                                                           77
      if(i==j)
                                                             4.4 Delta-Encoding
9
           val[no]=vet[i];
10
11
           return;
                                                          1 // Delta encoding
12
13
                                                           3 for(int i=0;i<q;i++)</pre>
      int esq = 2*no;
14
                                                           4 {
      int dir = 2*no+1;
15
                                                                 int 1,r,x;
      int meio = (i+j)/2;
                                                                 cin >> 1 >> r >> x;
17
                                                                  delta[1] += x;
      monta(i, meio, esq);
18
                                                                  delta[r+1] = x;
19
      monta(meio+1, j, dir);
                                                           9 }
20
                                                           10
      val[no]=max(val[esq], val[dir]);
21
                                                           11 int atual = 0:
22 }
                                                           12
                                                           13 for(int i=0;i<n;i++)</pre>
24 void atualiza(int no, int i, int j, int pos, int
                                                           14 {
      novo_valor)
                                                           15
                                                                  atual += delta[i];
25 {
                                                                  v[i] += atual;
                                                           16
      if(i==j)
26
                                                           17 }
           val[no]=novo_valor;
28
                                                            4.5 Seg-Tree-Farao
29
30
          int esq = 2*no;
                                                           1 typedef struct
31
          int dir = 2*no+1;
                                                           2 {
          int meio = (i+j)/2;
                                                                 pii prefix, sufix, total, maximo;
33
                                                           3
                                                           4 } no;
35
           if (pos <= meio)</pre>
              atualiza(esq, i, meio, pos, novo_valor); 6 int noleft[MAX], noright[MAX]; //Guarda os valores
36
                                                                dos nos para que nao sejam calculados novamente
                                                                 nas querys
               atualiza(dir, meio+1, j, pos, novo_valor)
38
                                                           7 int v[MAX];
                                                            8 no arvore[MAX]:
39
40
           if (val[esq]>val[dir])
                                                           10 pii somar(pii a, pii b) // une pairs
41
              val[no]=val[esq];
                                                           11 {
42
               val[no]=val[dir];
                                                                  return mp(a.f+b.f, a.s+b.s);
43
                                                           12
      }
                                                           13 }
44
45 }
                                                           14
                                                           15 no une(no l. no r)
46
47 int consulta(int no, int i, int j, int A, int B)
                                                           16 {
48 {
                                                                  if(1.total.s==0)
                                                           17
      if(i>B || j<A)</pre>
49
                                                           18
                                                                     return r:
          return -1;
                                                                  if(r.total.s==0)
51
      if(i>=A \text{ and } j<=B)
                                                           20
                                                                     return 1;
          return val[no];
                                                           21
52
53
                                                           22
                                                                  no m;
      int esq = 2*no;
54
                                                           23
      int dir = 2*no+1;
                                                                  m.prefix = max(l.prefix, somar(l.total, r.prefix)
                                                                  ); //prefixo
      int meio = (i+j)/2;
56
                                                                  m.sufix = max(r.sufix, somar(r.total, 1.sufix));
58
      int resp_esq = consulta(esq, i, meio, A, B);
                                                                 //sufixo
      int resp_dir = consulta(dir, meio+1, j, A, B);
                                                                 m.total = somar(1.total, r.total); //Soma de
59
                                                                  todos os elementos da subarvore
      if(resp_dir==-1)
                                                                  m.maximo = max(max(1.maximo, r.maximo), somar(1.
61
                                                           27
          return resp_esq;
                                                                  sufix, r.prefix)); //Resultado para cada
      if (resp_esq==-1)
63
                                                                  subarvore
          return resp_dir;
64
                                                           28
```

```
return m:
29
                                                             99
30 }
                                                             100
                                                                    return 0;
                                                             101 }
31
32 no makenozero()
                                                                       BIT-2D
33 {
                                                                4.6
34
       no m:
       m.prefix=m.sufix=m.total=m.maximo=mp(0,0);
35
                                                              1 // BIT 2D
       return m:
36
37 }
                                                              3 int bit[MAX][MAX];
38
39 no makeno(int k)
                                                              5 int sum(int x, int y)
40 {
                                                              6 {
41
       no m;
                                                                     int resp=0;
       m.prefix=m.sufix=m.total=m.maximo=mp(k,1);
42
43
       return m;
                                                                    for(int i=x;i>0;i-=i&-i)
                                                              9
44 }
                                                                         for(int j=y;j>0;j-=j&-j)
                                                             10
45
                                                                             resp+=bit[i][j];
                                                              11
46 void monta(int n)
                                                             12
47 {
                                                                    return resp;
                                                             13
       if(noleft[n] == noright[n])
48
                                                             14 }
49
50
           arvore[n]=makeno(v[noleft[n]]);
                                                             16 void update(int x, int y, int delta)
           return:
51
                                                             17 {
       }
52
                                                             18
                                                                     for(int i=x;i<MAX;i+=i&-i)</pre>
53
                                                                         for (int j=y; j < MAX; j += j & - j)</pre>
                                                             19
       int mid = (noleft[n]+noright[n])/2;
54
                                                             20
                                                                             bit[i][j]+=delta;
       noleft[2*n]=noleft[n]; noright[2*n]=mid;
55
                                                             21 }
       noleft[2*n+1]=mid+1; noright[2*n+1]=noright[n];
56
                                                             22
57
                                                             23 int query(int x1, y1, x2, y2)
       monta(2*n):
58
                                                             24 {
       monta(2*n+1);
59
                                                                     return sum(x2,y2) - sum(x2,y1) - sum(x1,y2) + sum
60
                                                                     (x1,y1);
       arvore[n] = une(arvore[2*n], arvore[2*n+1]);
61
62 }
63
                                                                4.7
                                                                     \operatorname{BIT}
64 no busca(int n, int esq, int dir)
65 {
66
       if (noleft[n] >= esq and noright[n] <= dir)</pre>
                                                             1 // (BIT) Fenwick Tree
67
           return arvore[n];
       if(noright[n] < esq or noleft[n] > dir)
68
                                                              3 int N, bit[MAX];
69
           return makenozero();
70
                                                              5 int soma(int x)
       return une(busca(2*n, esq, dir),busca(2*n+1, esq, 6 {
71
        dir));
                                                                     int resp=0;
72 }
73
                                                                    // for(int i=x;i>0;i-=i&-i)
                                                              9
74 int main()
                                                              10
                                                                    //
                                                                        resp+=bit[i];
75 {
       int T, N, Q, A, B;
76
                                                             12
                                                                     while (x > 0)
77
       no aux;
                                                             13
                                                                     {
78
                                                                         resp += bit[x];
                                                             14
       scanf("%d", &T);
79
                                                                         x = (x & -x);
                                                             16
       while (T--)
81
                                                             17
82
                                                             18
                                                                    return resp;
           scanf("%d", &N);
83
                                                             19 }
           for(int i=1;i<=N;i++)</pre>
84
               scanf("%d", &v[i]); //Elementos da arvore 21 int query(int L, int R)
85
86
                                                             22 {
           noleft[1]=1;noright[1]=N;
                                                                     return soma(R)-soma(L-1);
                                                             23
88
           monta(1);
                                                             24 }
89
                                                             25
           cin >> Q;
                                                             26 void update(int x, int v) // add v in x
90
           while (Q--)
91
                                                             27 {
92
                                                                     // for(;x<=n;x+=x&-x)
                                                             28
                scanf("%d%d", &A, &B); //Intervalo da
93
                                                                        bit[x] += v;
                                                             29
       query
                                                             30
94
               aux = busca(1, A, B);
                                                                    while(x <= N)</pre>
                                                             31
               printf("%d %d\n", aux.maximo.f, aux.
95
                                                                    {
                                                             32
       maximo.s);
                                                                         bit[x] += v;
                                                             33
           }
96
                                                                         x += (x & -x);
                                                             34
       }
97
                                                                    }
                                                             35
98
                                                             36 }
```

#### 4.8 Sparse-Table 3 **{** 4 if (a == 0) { 5 1 // Precompute log2 x = 0; y = 1;6 1 int logv[MAXN+1]; return b; $3 \log v[1] = 0;$ 4 for (int i = 2; i <= MAXN; i++) 8 9 int x1, y1; logv[i] = logv[i/2] + 1;int d = gcd(b%a, a, x1, y1); 10 x = y1 - (b / a) \* x1;11 7 int st[MAXN][K]; 12 y = x1;return d: 13 9 void precompute(int N) 14 } 10 { 15 for (int i = 0; i < N; i++)</pre> 11 16 bool find\_any\_solution(int a, int b, int c, int &x0, st[i][0] = array[i]; 12 int &y0, int &g) 13 17 { int k = logv[N]; 14 18 g = gcd(abs(a), abs(b), x0, y0);for (int j = 1; j <= k; j++)</pre> 15 if (c % g) 19 for (int i = 0; i + (1 << j) <= N; i++)</pre> 16 return false; st[i][j] = max(st[i][j-1], st[i + (1 << (20))]17 21 j - 1))][j - 1]); x0 \*= c / g;22 18 } y0 \*= c / g;23 if (a < 0) x0 = -x0;24 20 int query(int L, int R) if (b < 0) y0 = -y0; 21 { return true; int j = logv[R - L + 1]; 22 int minimum = min(st[L][j], st[R - (1 << j) + 1][27 }</pre> 23 j]); 29 // All solutions 24 } $_{30}$ // x = x0 + k\*b/g 31 // y = y0 - k\*a/g**Union-Find** 4.95.2 Factorization-sqrt 1 // Union-Find Functions 1 // Factorization of a number in sqrt(n) 3 int pai[MAX], peso[MAX]; 3 int main() 5 int find(int aux) 4 { 6 € 5 if(pai[aux] == aux) vector < int > div; return aux; cin >> N; return pai[aux]=find(pai[aux], pai); 10 11 } for(11 i=2;i\*i<=N;i++)</pre> 10 11 13 void join(int x, int y) if(N%i==0)12 13 x = find(x);15 vet.pb(i); y = find(y); 14 16 while (N%i==0)15 17 N/=i: 16 if (pesos[x] < pesos[y])</pre> 18 } 17 pai[x] = y;18 else if(pesos[x]>pesos[y]) 20 if(N!=1)21 pai[y] = x;19 vet.pb(N); 20 else if(pesos[x] == pesos[y]) 22 21 { 23 22 return 0; pai[x] = y;24 23 } pesos[y]++; 25 26 **Modular-Exponentiation** 27 } 28 29 int main() 1 // Modular exponentiaion - (x^y)%mod in O(log y) 30 { 2 ll power(ll x, ll y, ll mod) for (int i=1; i <= N; i++)</pre> 31 3 **{** 32 pai[i]=i; 4 11 res = 1;33 } x%=mod;5 5 Math while(y) { if (y&1) Linear-Diophantine-Equation res=(res\*x)%mod; 10

11

12

13

y = y >> 1;

x=(x\*x)%mod;

1 // Linear Diophantine Equation

2 int gcd(int a, int b, int &x, int &y)

```
}
                                                                    while (d == n):
14
                                                             67
15
      return res;
                                                             68
16 }
                                                                    return d:
                                                             69
                                                             70 }
  5.4 Miller-Habin
                                                             71
                                                             72 ll fexp(ll a, ll b, ll c)
1 #include <bits/stdc++.h>
                                                             73 {
                                                                    ll ans = 1:
2 #define mod 100000007
                                                             74
                                                                    while(b)
3 #define Pi 3.14159265358979311599796346854
                                                             75
                                                             76
                                                                    {
4 #define INF 0x3f3f3f3f
                                                                         if(b & 1)
5 #define MAX 1000010
                                                             77
6 #define f first
                                                             78
                                                                            ans = mul(ans, a, c);
                                                                         a = mul(a, a, c);
7 #define s second
                                                             79
                                                                         b /= 2;
8 #define 11 long long
                                                             80
                                                                    }
9 #define pb push_back
                                                             81
                                                             82
                                                                    return ans;
10 #define mp make_pair
11 #define pii pair<int, int>
                                                             83 }
12 #define vi vector <int>
                                                             84
                                                             85 bool rabin(ll n)
13 #define vii vector< pii >
14 #define sws ios_base::sync_with_stdio(false);cin.tie(86 {
      NULL)
                                                                    if (n <= 1)</pre>
                                                             87
15 #define forn(i, n) for(int i=0; i<(int)(n); i++)</pre>
                                                                       return 1;
                                                             88
16 #define mdc(a, b) (__gcd((a), (b)))
                                                                    if(n \le 3)
                                                             89
17 #define mmc(a, b) (((a)/_{gcd}(a, b)) * b)
                                                                        return 1;
18 #define endl '\n'
                                                             91
                                                             92
                                                                    ll s=0, d=n-1;
19 #define teto(a, b) (a+b-1)/b
                                                                    while (d\%2==0)
                                                             93
                                                                    {
                                                             94
21 using namespace std;
                                                             95
                                                                         d/=2:
                                                                         s++:
23 ll llrand()
                                                             96
                                                                    }
                                                             97
24 {
25
       11 tmp = rand();
                                                             98
                                                             99
                                                                    for(int k = 0; k < 64*4; k++)
       return (tmp << 31) | rand();</pre>
26
27 }
                                                            100
                                                                         11 a = (11rand()\%(n - 3)) + 2;
                                                            101
                                                                         11 x = fexp(a, d, n);
29 ll add(ll a, ll b, ll c)
                                                                         if (x != 1 and x != n-1)
                                                            103
       return (a + b)%c;
                                                            104
31
32 }
                                                                             for(int r = 1; r < s; r++)
                                                            106
33
34 ll mul(ll a, ll b, ll c)
                                                            107
                                                                                  x = mul(x, x, n);
                                                                                 if(x == 1)
                                                            108
                                                                                     return 0;
       11 \text{ ans} = 0;
                                                            109
36
       while(b)
                                                            110
                                                                                  if(x == n-1)
37
                                                                                     break;
                                                            111
38
                                                            112
                                                                             }
           if(b & 1)
39
                                                                             if (x != n-1)
40
               ans = add(ans, a, c);
                                                            113
           a = add(a, a, c);
                                                                                  return 0;
41
                                                                         }
42
           b /= 2;
                                                            115
                                                            116
                                                                    }
      }
43
                                                            117
44
       return ans;
                                                                    return 1;
45 }
                                                            118
                                                            119 }
46
                                                            120
47 ll rho(ll n)
                                                            121
48 {
                                                            122 int main()
49
       ll x, c, y, d, k;
                                                            123 {
50
       int i;
                                                            124
                                                                    //sws:
       do{
51
                                                                    //freopen("input.txt", "r", stdin);
           i = 1;
                                                            125
                                                                    //freopen("output.txt", "w", stdout);
                                                            126
           x = llrand()%n;
53
           c = llrand()%n;
                                                            127
54
                                                            128
                                                                    11 N, resp;
55
           y = x, k = 4;
                                                            129
                                                                    vector<ll> div;
           do{
56
                if(++i == k)
                                                            130
                                                            131
                                                                    cin >> N;
                {
58
                                                                    resp = N;
                    y = x;
                                                            132
59
                    k *= 2;
                                                            133
60
                                                                    while(N>1 and !rabin(N))
                                                            134
61
                                                            135
                x = add(mul(x, x, n), c, n);
                                                            136
                                                                         11 d = rho(N);
                d = \_gcd(abs(x - y), n);
63
                                                                         if(!rabin(d))
                                                            137
                                                                            continue;
           while(d == 1);
                                                            138
65
       }
                                                            139
                                                                         div.pb(d);
66
```

```
while (N\%d==0)
                                                                      do{
140
                                                               36
141
                N/=d;
                                                               37
                                                                           i = 1;
                                                                           x = llrand()%n;
142
                                                               38
       if(N!=resp and N!=1)
                                                                           c = llrand()%n;
143
                                                               39
                                                                           y = x, k = 4;
            div.pb(N);
                                                               40
                                                                           do{
145
                                                               41
                                                                               if(++i == k)
                                                               42
        if(div.empty())
                                                                               Ł
147
                                                               43
          cout << resp << endl;</pre>
                                                                                    y = x;
148
                                                               44
149
        else
                                                                                    k *= 2;
        {
150
                                                               46
            for(int i=0;i<(int)div.size();i++)</pre>
151
                                                               47
                                                                               x = add(mul(x, x, n), c, n);
               resp = __gcd(resp, div[i]);
                                                                               d = \_gcd(abs(x - y), n);
                                                               48
                                                                           }
                                                               49
153
            cout << resp << endl;</pre>
                                                                           while(d == 1);
154
                                                               50
155
                                                               51
                                                               52
                                                                      while(d == n);
        return 0;
157
                                                               53
                                                                       return d;
                                                               54
                                                               55 }
159 }
                                                               56
   5.5 Inverso-Mult
                                                               57 int main()
                                                               58 €
                                                                       srand(time(0));
 _1 // ax + my = 1, e gcd(a, m) = 1 para existir solucao _{60}^{\circ\circ}
 _2 // outra forma de escrever: a*x = 1 (mod m)
                                                               61
                                                                      11 N;
 3 int x, y;
                                                                      cin >> N;
                                                               62
 4 int g = gcd(a, m, x, y);
                                                               63
 5 if (g != 1)
                                                               64
                                                                      11 \text{ div} = \text{rho(N)};
       cout << "No solution!";</pre>
                                                                      cout << div << " " << N/div << endl;</pre>
                                                               65
 7 else
                                                               66
 8 {
                                                               67
       x = (x\%m + m) \% m;
 9
                                                                      // Finding all divisors
                                                               68
       cout << x << endl;</pre>
10
                                                               69
 11 }
                                                                      vector<ll> div;
                                                               70
                                                               71
   5.6 Pollard-Rho
                                                                      while(N>1 and !rabin(N))
                                                               72
                                                               73
                                                                      {
                                                                           11 d = rho(N);
 1 // Pollard Rho Algorithm
                                                               74
                                                                           if(!rabin(d))
                                                               75
 3 #include <bits/stdc++.h>
                                                               76
                                                                               continue;
                                                                           div.pb(d);
 4 #define 11 long long
                                                               77
                                                                           while (N\%d==0)
                                                               78
 6 using namespace std;
                                                               79
                                                                              N/=d;
                                                               80
                                                               81
                                                                      if(N!=resp and N!=1)
 8 ll llrand()
                                                                           div.pb(N);
 9 {
                                                               82
       11 tmp = rand();
 10
                                                                      return 0;
11
        return (tmp << 31) | rand();</pre>
                                                               84
                                                               85
12 }
                                                               86 }
13
14 ll add(ll a, ll b, ll c)
                                                                        Verif-primo
15 €
        return (a + b)%c;
17 }
                                                                1 // prime verification sqrt(N)
18
19 ll mul(ll a, ll b, ll c)
                                                                3 bool eh_primo(long long N)
20 {
                                                                4 {
       11 \text{ ans} = 0;
                                                                      if(N==2)
                                                                5
       while(b)
22
                                                                6
                                                                          return true;
23
                                                                      else if (N==1 \text{ or } N\%2==0)
            if(b & 1)
24
                                                                          return false;
               ans = add(ans, a, c);
25
                                                                      for(long long i=3;i*i<=N;i+=2)</pre>
                                                                9
            a = add(a, a, c);
                                                                         if(N\%i==0)
                                                               10
            b /= 2;
27
                                                                               return false;
                                                               11
        }
                                                               12
                                                                      return true;
29
        return ans;
                                                               13 }
30 }
31
                                                                  5.8 Crivo
32 ll rho(ll n)
33 {
                                                                1 // Sieve of Eratosthenes
        ll x, c, y, d, k;
34
       int i;
35
```

```
return cpx(coss[i],sins[i]*dir);
3 int N:
                                                              52
4 vector < bool > primos (100010, true);
                                                              53 }
5 cin >> N;
                                                              54
                                                              55 void FFT(cpx *in,cpx *out,int step,int size,int dir)
7 primos [0] = false;
                                                              56 {
8 primos[1]=false;
                                                                     if(size<1) return:</pre>
                                                              57
                                                                     if(size==1)
                                                              58
10 for (int i=2; i <= N; i++)
                                                                     Ł
                                                              59
                                                                         out [0] = in [0];
       if(primos[i])
11
                                                              60
           for(int j=i+i; j<=N; j+=i)</pre>
                                                              61
                                                                         return;
               primos[j]=false;
13
                                                              62
                                                              63
                                                                     FFT(in,out,step*2,size/2,dir);
        Formulas
  5.9
                                                              64
                                                                     FFT(in+step,out+size/2,step*2,size/2,dir);
                                                                     for(int i=0;i<size/2;++i)</pre>
                                                              65
                                                              66
                                                                     {
1 int sum_x2(11 N)
                                                                         cpx even=out[i];
                                                              67
2 {
                                                              68
                                                                         cpx odd=out[i+size/2];
       return (2*N*N*N + 3*N*N + N)/6;
                                                                         out[i] = even+EXP(i*step,dir)*odd;
                                                              69
4 }
                                                              70
                                                                         out[i+size/2] = even+EXP((i+size/2)*step,dir)*
                                                                     odd:
         FFT-golfbot
  5.10
                                                              71
                                                              72 }
                                                              73
1 #include <bits/stdc++.h>
                                                              74 int main()
                                                              75 {
3 using namespace std;
                                                              76
                                                                     for(int i=0;i<=N;++i)</pre>
5 const int N = (1<<19);</pre>
                                                              77
                                                                         coss[i]=cos(two_pi*i/N);
6 const double two_pi = 4 * acos(0);
                                                              78
                                                                         sins[i]=sin(two_pi*i/N);
                                                              79
8 struct cpx
                                                              80
                                                                     while(cin >> n) // Numero de tacadas possiveis
                                                              81
9 {
                                                                     {
       cpx(){}
                                                              82
10
                                                                         fill(x,x+N+100,0);
                                                              83
       cpx(double aa): a(aa){}
       cpx(double aa, double bb):a(aa),b(bb){}
                                                              84
                                                                         fill(a,a+N+100,0);
12
                                                                         for (int i=0;i<n;++i)</pre>
       double a;
                                                              85
       double b;
14
                                                                              cin >> p; // Distancia das tacadas
       double modsq(void) const
                                                              87
                                                              88
                                                                              x[p]=1;
16
                                                                         }
                                                              89
           return a*a+b*b;
17
                                                                         for (int i=0;i<N+100;++i)</pre>
                                                              90
       }
                                                              91
                                                                         {
       cpx bar(void) const
19
                                                                              b[i]=cpx(x[i],0);
                                                              92
20
                                                                         }
                                                              93
21
            return cpx(a,-b);
                                                              94
                                                                         cin >> m; // Querys
22
                                                                         for (int i=0; i < m; ++i)</pre>
                                                              95
23 };
                                                              96
24
                                                                              cin >> a[i]; // Distancia da query
25 cpx b[N+100];
                                                              97
26 cpx c[N+100];
                                                                         FFT(b,B,1,N,1);
27 cpx B[N+100];
                                                             99
                                                             100
                                                                         for (int i=0;i<N;++i)</pre>
28 cpx C[N+100];
                                                             101
                                                                             C[i]=B[i]*B[i];
29 int a[N+100];
                                                                         FFT(C,c,1,N,-1);
30 int x[N+100];
                                                             102
                                                                         for (int i=0; i < N; ++i)</pre>
31 double coss[N+100], sins[N+100];
                                                             103
                                                                              c[i]=c[i]/N;
                                                             104
32 int n,m,p;
                                                                          int cnt=0;
33
                                                                          for (int i=0;i<m;++i)</pre>
                                                             106
34 cpx operator +(cpx a,cpx b)
                                                                              if(c[a[i]].a>0.5 || x[a[i]])
35 {
                                                                                  cnt++:
       return cpx(a.a+b.a,a.b+b.b);
                                                             108
36
                                                                         cout << cnt << endl;</pre>
37 }
                                                             109
                                                                     }
                                                             110
38
                                                             111
                                                                     return 0:
39 cpx operator *(cpx a,cpx b)
                                                             112
40 {
       return cpx(a.a*b.a-a.b*b.b,a.a*b.b+a.b*b.a);
41
                                                                5.11 Modular-Factorial
42 }
43
44 cpx operator /(cpx a,cpx b)
                                                              1 // C++ program to comput n! % p using Wilson's
45 {
                                                                     Theorem
       cpx r = a*b.bar();
46
                                                              2 #include <bits/stdc++.h>
       return cpx(r.a/b.modsq(),r.b/b.modsq());
                                                              3 using namespace std;
47
48 }
                                                              5 int power(int x, unsigned int y, int p)
50 cpx EXP(int i,int dir)
                                                              6 {
51 {
                                                                     int res = 1;
```

#### x = x % p;8 9 while (y > 0)10 11 if (y & 1) res = (res \* x) % p; 13 14 y = y >> 1; 1.5 x = (x \* x) % p;16 } 17 return res; 18 19 } 20 21 int modInverse(int a, int p) 22 { return power(a, p-2, p); 23 24 } 25 26 int modFact(int n, int p) 27 { $if (p \le n)$ 28 29 return 0; 30 int res = (p - 1); 32 for(int i = n + 1; i < p; i++)</pre> 33 res = (res \* modInverse(i, p)) % p; 34 return res; 35 36 } 37 38 int main() 39 € int n = 25, p = 29; 40 41 cout << modFact(n, p);</pre> return 0; 42 43 } 5.12 Kamenetsky 1 // Number of digits in n! O(1) 3 #define Pi 3.14159265358979311599796346854 4 #define Eul 2.71828182845904509079559829842 6 long long findDigits(int n) 7 { double x; 9 if (n < 0)return 0; 11 if (n == 1) 12 13 return 1; 14 x = ((n \* log10(n / euler) + log10(2 \* Pi \* n))/2.0)); 16 return floor(x) + 1; 17 18 } Misc 6

#### 6.1 LIS

```
1 multiset < int > S;
2 for (int i = 0; i < n; i++) {
3    auto it = S.upper_bound(vet[i]); // low for inc
4    if (it != S.end())
5         S.erase(it);
6    S.insert(vet[i]);
7 }
8 // size of the lis
9 int ans = S.size();</pre>
```

#### 6.2 Bitwise

```
1 // Bitwise
       unsigned char a = 5, b = 9; // a = (00000101), b
3
       = (00001001)
 4
       AND -
                       a&b
                             // The result is 00000001
 5
       (1)
                             // The result is 00001101
       OR -
                       alb
 6
       (13)
       XOR -
                             // The result is 00001100
                       a^b
       (12)
                       ~a
                             // The result is 11111010
       иот -
       (250)
                       b<<1 // The result is 00010010
 9
       Left shift -
       (18)
       Right shift - b >> 1 // The result is 00000100
       (4)
       // Exchange two int variables
12
13
           a^=b;
14
           b^=a:
15
           a^=b;
16
17
       // Even or Odd
18
19
           (x & 1)? printf("Odd"): printf("Even");
20
21
       // Turn on the j-th bit
22
23
           int S = 34; //(100010)
24
           int j = 3;
25
           S = S | (1 << j);
27
28
       // Turn off the j-th bit
29
30
           int S = 42; //(101010)
31
           int j = 1;
32
           S &= ~(1<<j)
34
35
           S == 40 //(101000)
36
37
       // Check the j-th element
38
39
40
           int S = 42; //(101010)
           int j = 3;
41
42
           T = S & (1 << j); // T = 0
44
       // Least significant bit (lsb)
45
46
47
           int lsb(int x)
48
                return x&-x;
49
           7
51
       // Exchange o j-th element
52
53
           S = (1 << j)
54
       // Position of the first bit on
56
           T = (S & (-S))
58
           T -> 4 bit ligado //(1000)
59
61
       // Most significant digit of N
62
63
           double K = log10(N);
64
```

```
K = K - floor(K);
65
66
           int X = pow(10, K);
67
      // Number of digits in N
68
           X =floor(log10(N)) + 1;
70
      // Power of two
72
73
           bool isPowerOfTwo(int x)
           {
75
76
               return x && (!(x&(x-1)));
           }
77
```

### Strings

#### 7.1 KMP

```
vector<int> preffix_function(const string &s){
      int n = s.size(); vector<int> b(n+1);
      b[0] = -1; int i = 0, j = -1;
      while(i < n){</pre>
          while(j >= 0 && s[i] != s[j]) j = b[j];
          b[++i] = ++j;
      }
      return b;
9 }
void kmp(const string &t, const string &p){
      vector < int > b = preffix_function(p);
      int n = t.size(), m = p.size();
12
      int j = 0;
13
14
      for(int i = 0; i < n; i++){</pre>
          while (j \ge 0 \&\& t[i] != p[j]) j = b[j];
15
           j++;
          if (j == m) {
17
18
19
               j = b[j];
          }
20
21
      }
22 }
```

#### 7.2 Pal-int

1 bool ehpalindromo(ll n)

```
2 {
3
       if(n<0)
          return false;
4
5
       int divisor = 1;
       while(n/divisor >= 10)
7
           divisor *= 10;
8
9
       while (n != 0)
10
11
           int leading = n / divisor;
12
13
           int trailing = n % 10;
14
           if(leading != trailing)
15
               return false;
16
17
           n = (n \% divisor)/10;
18
19
           divisor = divisor/100;
       }
21
22
23
       return true;
24 }
 7.3 Z-Func
vector <int> z_algo(const string &s)
      int n = s.size();
       int L = 0, R = 0;
       vector < int > z(n, 0);
       for(int i = 1; i < n; i++)</pre>
           if(i <= R)</pre>
               z[i] = min(z[i-L], R - i + 1);
10
           while (z[i]+i < n \&\& s[z[i]+i] == s[z[i]])
               z[i]++;
11
12
           if(i+z[i]-1 > R)
           {
13
14
               L = i;
               R = i + z[i] - 1;
15
           }
```

16

17

18 19 } }

return z;