# OncoSimulR: forward genetic simulation in asexual populations with arbitrary epistatic interactions and a focus on modeling tumor progression.

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# 1 Introduction

OncoSimulR is an individual-based forward-time genetic simulator for biallelic markers (wildtype vs. mutated) in asexually reproducing populations without spatial structure (perfect mixing). Its design emphasizes flexible specification of fitness and mutator effects.

OncoSimulR was originally developed to simulate tumor progression using several models of tumor progression with emphasis on allowing users to set restrictions in the accumulation of mutations as specified, for example, by Oncogenetic Trees (OT: Desper et al. 1999; Szabo and Boucher 2008) or Conjunctive Bayesian Networks (CBN: Beerenwinkel, Eriksson, and Sturmfels 2007; Gerstung et al. 2009; Gerstung et al. 2011), with the possibility of adding passenger mutations to the simulations and allowing for several types of sampling.

Since then, OncoSimulR has been vastly extended to allow you to specify other types of restrictions in the accumulation of genes, such as the XOR models of Korsunsky et al. (2014) or the "semimonotone" model of Farahani and Lagergren (2013). Moreover, different fitness effects related to the order in which mutations appear can also be incorporated, involving arbitrary numbers of genes. This is *very* different from "restrictions in the order of accumulation of mutations". With order effects, described in a recent cancer paper by Ortmann and collaborators (Ortmann et al. 2015), the effect of having both mutations "A" and "B" differs depending on whether "A" appeared before or after "B" (the actual case involves genes JAK2 and TET2).

More generally, OncoSimulR now also allows you to specify arbitrary epistatic interactions between arbitrary collections of genes and to model, for example, synthetic mortality or synthetic viability (again, involving an arbitrary number of genes, some of which might also depend on other genes, or show order effects with other genes). Moreover, it is possible to specify the above interactions in terms of modules, not genes. This idea is discussed in, for example, Raphael and Vandin (2015) and Gerstung et al. (2011): the restrictions encoded in, say, CBNs or OT can be considered to apply not to genes, but to modules, where each module is a set of genes (and the intersection between modules is the empty set) that performs a specific biological function. Modules, then, play the role of a "union operation" over the set of genes in a module. In addition, arbitrary numbers of genes without interactions (and with fitness effects coming from any distribution you might want) are also possible.

Mutator/antimutator genes, genes that alter the mutation rate of other genes (Gerrish et al. 2007, Tomlinson, Novelli, and Bodmer (1996)), can also be simulated with OncoSimulR and specified with most of the mechanisms above (you can have, for instance, interactions between mutator genes). And, with regards to mutation rates, different genes can have different mutation rates (regardless of the presence or not of other mutator/antimutator genes).

Simulations can be stopped as a function of total population size, number of mutated driver genes, or number of time periods. Simulations can also be stopped with a stochastic detection mechanism where the probability of detecting a tumor increases

with total population size. Simulations return the number of cells of every genotype/clone at each of the sampling periods and the genealogical relationships of all clones generated during the simulation. We can take samples from those data with single-cell or whole- tumor resolution, adding noise if we want.

The models so far implemented are all continuous time models, which are simulated using the BNB algorithm of Mather, Hasty, and Tsimring (2012). The core of the code is implemented in C++, providing for fast execution. To help with simulation studies, code to simulate random graphs of the kind often seen in CBNs, OTs, etc, is also available. Finally, OncoSimulR also allows for the generation of random fitness landscapes and the representation of fitness landscapes and provides some statistics of of evolutionary predictability.

## 1.1 Key features of OncoSimulR

As mentioned above, OncoSimulR is now a very general package for forward genetic simulation, with applicability well beyond tumor progression. This is a summary of some of the key features:

- You can specify arbitrary interactions between genes, with arbitrary fitness effects, with explicit support for:
  - Restrictions in the accumulations of mutations, as specified by Oncogenetic Trees (OTs), Conjunctive Bayesian Networks (CBNs), semimonotone progression networks, and XOR relationships.
  - Epistatic interactions, including, but not limited to, synthetic viability and synthetic lethality.
  - Order effects.
- You can add passenger mutations.
- You can add mutator/antimutator effects.
- Fitness and mutation rates can be gene-specific.
- More generally, you can add arbitrary numbers of non-interacting genes with arbitrary fitness effects.
- you can allow for deviations from the OT, CBN, semimonotone, and XOR models, specifying a penalty for such deviations (the  $s_h$  parameter).
- You can conduct multiple simulations, and sample from them with different temporal schemes and using both whole tumor or single cell sampling.
- You can stop the simulations using a flexible combination of conditions, from final time to number of drivers to population size, to fixation of certain genotypes, to a stochastic stopping mechanism that depends on size, etc.

- Right now, three different models are available, two that lead to exponential growth, one of them loosely based on Bozic et al. (2010), and another that leads to logistic-like growth, based on McFarland et al. (2013).
- You can use very large numbers of genes (e.g., see an example of 50000 in section 6.6.3).
- Simulations are generally very fast: I use C++ to implement the BNB algorithm (see sections 11.4 and 11.5 for more detailed comments on the usage of this algorithm).
- You can obtain the true sequence of events and the phylogenetic relationships between clones (see section 11.0.1 for the details of what we mean by "clone").
- You can generate random fitness landscapes (under the House of Cards, Rough Mount Fuji, or additive models, or combinations of the former) and use those landscapes as input to the simulation functions.
- You can plot fitness landscapes.
- You can obtain some basic measures of evolutionary predictability from the simulations.

The table below, modified from the table at the Genetics Simulation Resources (GSR) page provides a summary of the key features of OncoSimulR. (An explanation of the meaning of terms specific to the GSR table is available from https://popmodels.cancercontrol.cancer.gov/gsr/search/ or from the Genetics Simulation Resources table itself, by moving the mouse over each term).

Table 1: Key features of OncoSimulR. Modified from the original table from https://popmodels.cancercontrol. cancer.gov/gsr/packages/oncosimulr/#detailed .

Attribute Category	Attribute
Target	
Type of Simulated Data variations	Haploid DNA Sequence Biallelic Marker, Genotype or Sequencing Error
Simulation Method Type of Dynamical	Forward-time Continuous time
Model	Clause (ass 11.1)
Entities Tracked Input	Clones (see 11.1) Program specific (R data frames and matrices specifying genotypes' fitness, gene effects, and starting genotype)
Output	
Data Type	Genotype or Sequence, Individual Relationship (complete parent-child relationships between clones), Demographic (populations sizes of all clones at sampling times), Diversity Measures (LOD, POM, diversity of genotypes), Fitness
Sample Type	Random or Independent, Longitudinal, Other (proportional to population size)
<b>Evolutionary Features</b>	(1 1 )
Mating Scheme	Asexual Reproduction
Demographic	
Population Size	Exponential (two models), Logistic (McFarland et
Changes	al., 2013)
Fitness Components	
Birth Rate	Individually Determined from Genotype (models "Exp" and "McFL")
Death Rate	Individually Determined from Genotype (model "Bozic"), Influenced by Environment —population size (model "McFL")
Natural Selection	
Determinant	Single and Multi-locus, Fitness of Offspring, Environmental Factors (population size)
Models	Directional Selection, Multi-locus models, Epistasis, Random Fitness Effects
Mutation Models	Two-allele Mutation Model (wildtype, mutant), without back mutation
Events Allowed	Varying Genetic Features: change of individual mutation rates (mutator/antimutator genes)
Spatial Structure	No Spatial Structure (perfectly mixed and no migration)

Further details about the original motivation for wanting to simulate data this way in the context of tumor progression can be found in Diaz-Uriarte (2015), where additional comments about model parameters and caveats are discussed.

Are there similar programs? The Java program by Reiter et al. (2013) offers somewhat similar functionality to the previous version of OncoSimulR, but it is restricted to at most four drivers (whereas v.1 of OncoSimulR allowed for up to 64), you cannot use arbitrary CBNs or OTs (or XORs or semimonotone graphs) to specify restrictions, there is no allowance for passengers, and a single type of model (a discrete time Galton-Watson process) is implemented. The current functionality of OncoSimulR goes well beyond the previous version (and, thus, also the TPT of (Reiter et al. 2013)). We now allow you to specify all types of fitness effects in other general forward genetic simulators such as FFPopSim (Zanini and Neher 2012), and some that, to our knowledge (e.g., order effects) are not available from any genetics simulator. In addition, the "Lego system" to flexibly combine different fitness specifications is also unique; by "Lego system" I mean that we can combine different pieces and blocks, similarly to what we do with Lego bricks. (I find this an intuitive and very graphical analogy, which I have copied from Hothorn et al. (2006) and Hothorn et al. (2008)). In a nutshell, salient features of OncoSimulR compared to other simulators are the unparalleled flexibility to specify fitness and mutator effects, with modules and order effects as particularly unique, and the options for sampling and stopping the simulations, particularly convenient in cancer evolution models. Also unique in this type of software is the addition of functions for simulating fitness landscapes and assessing evolutionary predictability.

# 1.2 What kinds of questions is OncoSimulR suited for?

OncoSimulR can be used to address questions that span from the effect of mutator genes in cancer to the interplay between fitness landscapes and mutation rates. The main types of questions that OncoSimulR can help address involve combinations of:

- Simulating asexual evolution (the oncoSimul\* functions) where:
  - Fitness is:
    - \* A function of specific epistatic effects between genes
    - \* A function of order effects
    - \* A function of epistatic effects specified using DAGs/posets where these DAGs/posets:
      - · Are user-specified
      - · Generated randomly (simOGraph)
    - \* Any mapping between genotypes and fitness:
      - · User-specified
      - · Generated randomly from families of random fitness landscapes (rfitness)
  - Mutation rates can:
    - \* Vary between genes

- \* Be affected by other genes
- Examining times to evolutionarily or biomedically relevant events (fixation of genotypes, reaching a minimal size, acquiring a minimal number of driver genes, etc —specified with the stopping conditions to the oncoSimul\* functions).
- Using different sampling schemes (samplePop) that are related to:
  - Assessing genotypes from single-cell vs. whole tumor (or whole population)
     with the typeSample argument
  - Genotyping error (propError argument)
  - Timing of samples (timeSample argument)
  - and assessing the consequences of those on the observed genotypes and their diversity (sampledGenotypes) and any other inferences that depend on the observational process.
  - OncoSimulR returns the genotypes at each of the sampling points, so you are not restricted by what the samplePop function provides.
- Tracing the genealogical relationships of clones (plotClonePhylog) and assessing evolutionary predictability (LOD, POM).

Some specific questions that you can address with the help of OncoSimulR are discussed in section 1.3.

A quick overview of the main functions and their relationships is shown in the figure 1, where we use italics for the type/class of R object and courier for the name of the functions.

# 1.3 Examples of questions that can be addressed with OncoSimulR

Most of the examples in the rest of this vignette, starting with those in 1.6, focus on the mechanics. Here, we will illustrate some problems in cancer genomics and evolutionary genetics where OncoSimulR could be of help. This section does not try to provide an answer to any of these questions (those would be full papers by themselves) but simply to illustrate some kinds of questions where you can use OncoSimulR; of course, the possible uses of OncoSimulR are only limited by your ingenuity. Finally, I will only use short snippets of working code as we are limited by time of execution; for real work you would want to use many more scenarios and many more simulations, you would use appropriate statistical methods to compare the output of runs, etc, etc, etc.

## Load the package
library(OncoSimulR)

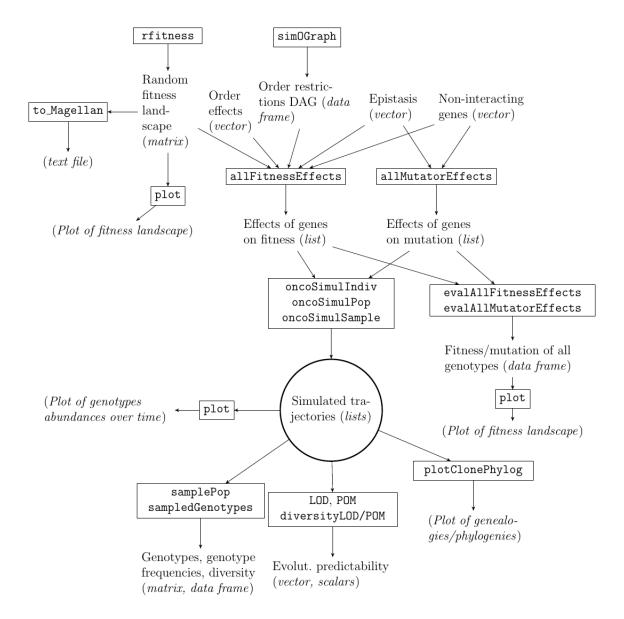


Figure 1: Relationships between the main functions in OncoSimulR.

#### 1.3.1 Recovering restrictions in the order of accumulation of mutations

This is a question that was addressed, for instance in Diaz-Uriarte (2015): do methods that try to infer restrictions in the order of accumulation of mutations (e.g., Szabo and Boucher (2008), Gerstung et al. (2009), Ramazzotti et al. (2015)) work well under different evolutionary models and with different sampling schemes? (This issue is also touched upon in section 12.2).

A possible way to examine that question would involve:

- generating random DAGs that encode restrictions;
- simulating cancer evolution using those DAGs;
- sampling the data and adding different levels of noise to the sampled data;
- running the inferential method;
- comparing the inferred DAG with the original, true, one.

```
## 1. Simulate a DAG
g1 <- simOGraph(4, out = "rT")
## 2. Simulate two evolutionary trajectories
s1 <- oncoSimulPop(10, allFitnessEffects(g1, drvNames = 1:4),
                   mc.cores = 2, ## adapt to your hardware
                   seed = NULL) ## for reproducibility of vignette
## 3. Sample those data uniformly, and add noise
d1 <- samplePop(s1, timeSample = "unif", propError = 0.1)</pre>
##
   Subjects by Genes matrix of 10 subjects and 4 genes.
##
## 4. You would now run the appropriate inferential method and
## compare observed and true
require(Oncotree)
## Loading required package: Oncotree
## Loading required package: boot
fit1 <- oncotree.fit(d1)</pre>
## Now, compare fitted and original. This is well beyond the
## scope of this document (and OncoSimulR itself).
```

# 1.3.2 Epistasis and predictability in rugged fitness landscapes in asexual populations

These questions encompass a wide range of specific issues that have been addressed in evolutionary genetics studies and which include from detailed analysis of simple models with a few uphill paths and valleys as in Weissman et al. (2009) or Ochs and Desai (2015), to questions that refer to larger, more complex fitness landscapes as in Szendro, Franke, et al. (2013) or Franke et al. (2011).

For the first case, we could specify the fitness landscape and run simulations until fixation (with argument fixation to oncoSimulPop—see more details in section 6.4 where we also use this same model). We would then examine the proportion of genotypes fixed under different scenarios. For instance, we can use the example from Ochs and Desai (2015) (we will see this example also in section 5.3, where we cover different ways of specifying fitness). And we can extend this example by adding mutator genes:

```
## Specify fitness effects.
## Numeric values arbitrary, but set the intermediate genotype en
## route to ui as mildly deleterious so there is a valley.
## As in Ochs and Desai, the ui and uv genotypes
## can never appear.
u \leftarrow 0.2; i \leftarrow -0.02; vi \leftarrow 0.6; ui \leftarrow uv \leftarrow -Inf
od <- allFitnessEffects(</pre>
    epistasis = c("u" = u, "u:i" = ui,
                   "u:v" = uv, "i" = i,
                   "v:-i" = -Inf, "v:i" = vi)
## For the sake of extending this example, also turn i into a
## mutator gene
odm <- allMutatorEffects(noIntGenes = c("i" = 50))</pre>
## How do mutation and fitness look like for each genotype?
evalAllGenotypesFitAndMut(od, odm, addwt = TRUE)
     Genotype Fitness MutatorFactor
## 1
            WT
                 1.000
## 2
             i
                 0.980
                                    50
## 3
                 1.200
                                     1
            u
## 4
             V
                 0.000
                                     1
## 5
         i, u
                 0.000
                                    50
## 6
         i, v
                 1.568
                                    50
## 7
                 0.000
                                     1
         u, v
                                    50
## 8 i, u, v
                 0.000
```

Ochs and Desai explicitly say "Each simulated population was evolved until either the uphill genotype or valley-crossing genotype fixed." So we will use fixation.

```
## Set a small initSize, as o.w. unlikely to pass the valley
initS <- 10</pre>
```

```
## The number of replicates is tiny, 10, for the sake of speed
## of creation of the vignette
od sim <- oncoSimulPop(10, od, muEF = odm,
                       fixation = c("u", "i, v"), initSize = initS,
                       model = "McFL",
                       mu = 1e-4, detectionDrivers = NA, finalTime = NA,
                       detectionSize = NA, detectionProb = NA,
                       onlyCancer = TRUE,
                       mc.cores = 2, ## adapt to your hardware
                       seed = NULL) ## for reproducibility
## What is the frequency of each final genotype?
sampledGenotypes(samplePop(od_sim))
##
    Subjects by Genes matrix of 10 subjects and 3 genes.
##
     Genotype Freq
## 1
         i, v
                 5
## 2
                 5
            u
##
    Shannon's diversity (entropy) of sampled genotypes: 0.6931
##
```

For the second set of questions, we would run simulations under random fitness landscapes with varied ruggedness, and would then examine the evolutionary predictability of the trajectories with measures such as "Lines of Descent" and "Path of the Maximum" (Szendro, Franke, et al. 2013) and the diversity of the sampled genotypes under different sampling regimes.

```
## Repeat the following loop for different combinations of whatever
## interests you, such as number of genes, or distribution of the
## c and sd (which affect how rugged the landscape is), or
## reference genotype or evolutionary model, or stopping criterion,
## sampling procedure, or ...
## 1. Generate a random fitness landscape, from the Rough Mount
      Fuji model, with g genes, and c ("slope" constant) and
##
##
      reference chosen randomly. Ask for a minimal number of
##
      accessible genotypes
g <- 6
c \leftarrow runif(1, 1/5, 5)
rl <- rfitness(g, c = c, min_accessible_genotypes = g)
## Plot it if you want; commented here as it takes long for a
## vignette
## plot(rl)
```

```
## Obtain landscape measures from Magellan. Export to Magellan
to_Magellan(rl, file = "rl1.txt")
## (Getting the statistics requires you to install Magellan,
## and that requires either calling the web app
## (http://wwwabi.snv.jussieu.fr/public/Magellan/) or
## asking Magellan's authors for the software. This is of course
## beyond the scope of the example and the package.
## 3. Simulate evolution in that landscape many times (here just 5)
simulrl <- oncoSimulPop(10, allFitnessEffects(genotFitness = rl),</pre>
                        keepPhylog = TRUE, keepEvery = 1,
                        initSize = 4000,
                        seed = NULL, ## for reproducibility
                        mc.cores = 2) ## adapt to your hardware
## 4. Obtain measures of evolutionary predictability
diversityLOD(LOD(simulrl))
## [1] 1.418
diversityPOM(POM(simulrl))
## [1] 1.643
sampledGenotypes(samplePop(simulrl, typeSample = "whole"))
##
    Subjects by Genes matrix of 10 subjects and 6 genes.
##
##
     Genotype Freq
## 1
            Α
## 2
         A, E
                 1
         A, F
                 2
## 3
## 4
         E. F
                 4
##
   Shannon's diversity (entropy) of sampled genotypes: 1.28
##
```

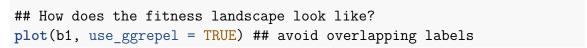
# 1.3.3 Epistatic interactions between drivers and passengers in cancer initiation

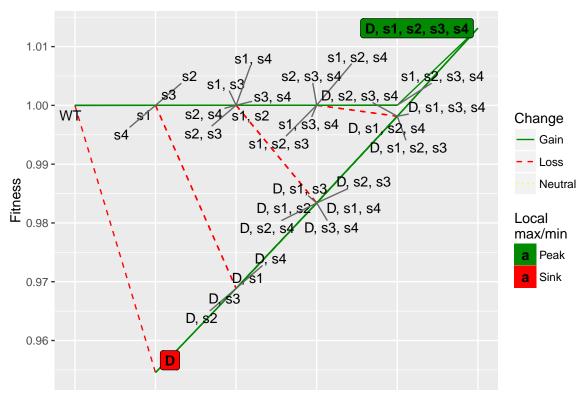
Bauer, Siebert, and Traulsen (2014) have examined the effects of epistatic relationships between drivers and passengers in cancer initiation. We could use their model as a starting point, and examine how likely cancer is to develop under different variations of their model and different evolutionary scenarios (e.g., initial sample size, mutation rates, evolutionary model, etc).

There are several ways to specify their model, as we discuss in section 5.1. We will use one based on DAGs here:

```
K <- 4
sp <- 1e-5
```

```
sdp <- 0.015
sdplus \leftarrow 0.05
sdminus <- 0.1
cnt \langle -(1 + sdplus)/(1 + sdminus)
prod cnt <- cnt - 1
bauer <- data.frame(parent = c("Root", rep("D", K)),</pre>
                      child = c("D", paste0("s", 1:K)),
                      s = c(prod_cnt, rep(sdp, K)),
                      sh = c(0, rep(sp, K)),
                      typeDep = "MN")
fbauer <- allFitnessEffects(bauer)</pre>
(b1 <- evalAllGenotypes(fbauer, order = FALSE, addwt = TRUE))
##
                Genotype Fitness
## 1
                       WT
                           1.0000
## 2
                        D
                           0.9545
## 3
                       s1
                           1.0000
                       s2
## 4
                           1.0000
## 5
                       s3
                           1.0000
## 6
                       s4
                           1.0000
## 7
                   D, s1
                           0.9689
## 8
                   D, s2
                           0.9689
## 9
                   D, s3
                           0.9689
## 10
                   D, s4
                           0.9689
## 11
                  s1, s2
                           1.0000
## 12
                  s1, s3
                           1.0000
## 13
                  s1, s4
                           1.0000
                  s2, s3
## 14
                           1.0000
## 15
                  s2, s4
                           1.0000
## 16
                  s3, s4
                           1.0000
## 17
               D, s1, s2
                           0.9834
## 18
               D, s1, s3
                           0.9834
               D, s1, s4
## 19
                           0.9834
## 20
               D, s2, s3
                           0.9834
## 21
               D, s2, s4
                           0.9834
## 22
               D, s3, s4
                           0.9834
## 23
              s1, s2, s3
                           1.0000
## 24
              s1, s2, s4
                           1.0000
## 25
              s1, s3, s4
                           1.0000
## 26
              s2, s3, s4
                           1.0000
## 27
          D, s1, s2, s3
                           0.9981
## 28
          D, s1, s2, s4
                           0.9981
## 29
          D, s1, s3, s4
                           0.9981
## 30
          D, s2, s3, s4
                           0.9981
## 31
         s1, s2, s3, s4
                           1.0000
## 32 D, s1, s2, s3, s4
                           1.0131
```





Now run simulations and examine how frequently the runs do not end up in extinction (for real, you would of course increase the number of total populations, the range of initial population sizes, model, mutation rate, etc):

# 1.3.4 Epistatic interactions between drivers and passengers in cancer initiation

Instead of focusing on different models for epistatic interactions, you might want to examine the consequences of order effects (Ortmann et al. 2015). You would proceed as above, but using models that differ by, say, the presence or absence of order effects. Details on their specification are provided in section 3.7. Here is one particular model (you would, of course, want to compare this to models without

order effects or with other magnitudes and types of order effects):

```
## Order effects involving three genes.
## Genotype D, M has different fitness effects
## depending on whether M or D mutated first.
## Genotype F, D, M has different fitness
## depending on which of the order in which the genes
## mutated.
o3 <- allFitnessEffects(orderEffects = c(
                             "F > D > M" = -0.3,
                             "D > F > M" = 0.4,
                             "D > M > F" = 0.2,
                             "D > M"
                                          = 0.1,
                             "M > D"
                                         = 0.5)
## With the above specification, let's double check
## the fitness of the possible genotypes
(oeag <- evalAllGenotypes(o3, addwt = TRUE, order = TRUE))</pre>
##
       Genotype Fitness
## 1
             WT
                    1.00
## 2
              D
                    1.00
              F
## 3
                    1.00
                    1.00
## 4
              М
          D > F
## 5
                    1.00
## 6
          D > M
                    1.10
## 7
          F > D
                    1.00
## 8
          F > M
                    1.00
## 9
          M > D
                    1.50
## 10
          M > F
                    1.00
## 11 D > F > M
                    1.54
## 12 D > M > F
                    1.32
## 13 F > D > M
                    0.77
## 14 F > M > D
                    1.50
## 15 M > D > F
                    1.50
## 16 M > F > D
                    1.50
```

Now, run simulations and examine how frequently the runs do not end up in extinction. As above, for real, you would of course increase the number of total populations, the range of initial population sizes, mutation rate, etc:

#### 1.3.5 Effects of mutator and antimutator genes

The effects of mutator and antimutator genes have been examined both in cancer genetics (Nowak 2006, Tomlinson, Novelli, and Bodmer (1996)) and in evolutionary genetics (Gerrish et al. 2007), and are related to wider issues such as Muller's ratchet and the evolution of sex. There are, thus, a large range of questions related to mutator and antimutator genes.

One question addressed in Tomlinson, Novelli, and Bodmer (1996) concerns under what circumstances mutator genes are likely to play a role in cancer progression. For instance, Tomlinson, Novelli, and Bodmer (1996) find that an increased mutation rate is more likely to matter if the number of required mutations in driver genes needed to reach cancer is large and if the mutator effect is large.

We might want to ask, then, how long it takes before we reach cancer. This is stored in the component FinalTime of the output. We would specify different numbers and effects of mutator genes (argument muEF). We would also change the criteria for reaching cancer and in our case we can easily do that by specifying different numbers in detectionDrivers. Of course, we would also want to examine the effects of varying numbers of mutators, drivers, and possibly fitness consequences of mutators (below we assume mutators are neutral and we assume there are no additional genes with deleterious mutations, but this need not be so, of course; see also (Tomlinson, Novelli, and Bodmer 1996, Gerrish et al. (2007), McFarland, Mirny, and Korolev (2014))).

Let us run an example. For the sake of simplicity, we assume no epistatic interactions.

```
mt <- allMutatorEffects(noIntGenes = mutatorGenesVector)</pre>
```

Now, simulate using the fitness and mutator specification. We fix the number of drivers to cancer, and we stop when those numbers of drivers are reached. Since we only care about the time it takes to reach cancer, not the actual trajectories, we set keepEvery = NA:

(Incidentally, notice that it is easy to get OncoSimulR to throw an exception if you do not think twice about the mutator effects you are using and specify a huge mutation rate if all mutator genes are mutated: see @(tomlin-except).)

#### 1.4 Trade-offs and what is OncoSimulR not well suited for

OncoSimulR is designed for complex fitness specifications and selection scenarios and uses forward-time simulations; the types of questions where OncoSimulR can be of help are discussed in sections 1.2 and 1.3 and running time and space consumption of OncoSimulR are addressed in section 2. You should be aware that **coalescent simulations**, sometimes also called backward-time simulations, are much more efficient for simulating neutral data as well as some special selection scenarios (Yuan et al. 2012, Carvajal-Rodriguez (2010), Hoban, Bertorelle, and Gaggiotti (2011)).

In addition, since OncoSimulR allows you to specify fitness with arbitrary epistatic and order effects, as well as mutator effects, you need to learn the syntax of how to specify those effects and you might be paying a performance penalty if your scenario does not require this complexity. For instance, in the models in Beerenwinkel et al. (2007) or Bozic et al. (2010), the fitness of a genotype depends only on the total number of drivers mutated, but not on which drivers are mutated (and, thus, not on the epistatic interactions nor the order of accumulation of the drivers). This means that the syntax for specifying those fitness models could probably be a lot simpler (e.g., specify s per driver).

But it also means that code written for just that case could probably run much faster.

First, because fitness evaluation is easier. Second, and possibly much more important, because what we need to keep track of leads to much simpler and economic structures: we do not need to keep track of clones (where two cells are regarded as different clones if they differ anywhere in their genotype), but only of clone types as defined by the number of mutated drivers, and keeping track of clones can be expensive—see sections 2 and 11.1.

So for those cases where you do not need the full flexibility of OncoSimulR, special purpose software might be easier to use and faster to run. Of course, for some types of problems this special purpose software might not be available, though.

## 1.5 Steps in using OncoSimulR

Using this package will often involve the following steps:

- 1. Specify the fitness effects: sections 3 and 5.
- 2. Simulate cancer progression: section 6. You can simulate for a single subject or for a set of subjects. You will need to:
  - Decide on a model. This basically amounts to choosing a model with exponential growth ("Exp" or "Bozic") or a model with carrying capacity ("McFL"). If exponential growth, you can choose whether the the effects of mutations operate on the death rate ("Bozic") or the birth rate ("Exp")<sup>1</sup>.
  - Specify other parameters of the simulation. In particular, decide when to stop the simulation, mutation rates, etc.

Of course, at least for initial playing around, you can use the defaults.

3. Sample from the simulated data and do something with those simulated data (e.g., fit an OT model to them, examine diversity or time until cancer, etc). Most of what you do with the data, however, is outside the scope of this package and this vignette.

Before anything else, let us load the package in case it was not yet loaded. We also explicitly load *graph* and *igraph* for the vignette to work (you do not need that for your usual interactive work). And I set the default color for vertices in igraph.

```
library(OncoSimulR)
library(graph)
library(igraph)
igraph_options(vertex.color = "SkyBlue2")
```

To be explicit, what version are we running?

<sup>&</sup>lt;sup>1</sup>It is of course possible to do this with the carrying capacity (or gompertz-like) models, but there probably is little reason to do it. McFarland et al. (2013) discuss this has little effect on their results, for example. In addition, decreasing the death rate will more easily lead to numerical problems as shown in section 3.4.

```
packageVersion("OncoSimulR")
## [1] '2.5.3'
```

## 1.6 Two quick examples of fitness specifications

Following 1.5 we will run two very minimal examples. First a model with a few genes and **epistasis**:

```
## 1. Fitness effects: here we specify an
      epistatic model with modules.
sa <- 0.1
sb < -0.2
sab <- 0.25
sac < -0.1
sbc < -0.25
sv2 <- allFitnessEffects(epistasis = c("-A : B" = sb,</pre>
                                         "A : -B" = sa,
                                         "A : C" = sac,
                                         "A:B" = sab,
                                         "-A:B:C" = sbc),
                          geneToModule = c(
                               "A" = "a1, a2",
                               "B" = "b".
                               "C" = "c"),
                          drvNames = c("a1", "a2", "b", "c"))
evalAllGenotypes(sv2, addwt = TRUE)
##
          Genotype Fitness
## 1
                 WT
                      1.000
## 2
                 a1
                      1.100
## 3
                 a2
                      1.100
## 4
                  b
                      0.800
## 5
                  С
                      1.000
## 6
            a1, a2
                      1.100
              a1, b
## 7
                      1.250
## 8
             a1, c
                      0.990
             a2, b
## 9
                      1.250
## 10
             a2, c
                      0.990
## 11
              b, c
                      1.000
## 12
         a1, a2, b
                      1.250
## 13
         a1, a2, c
                      0.990
          a1, b, c
## 14
                      1.125
## 15
          a2, b, c
                      1.125
## 16 a1, a2, b, c
                      1.125
## 2. Simulate the data. Here we use the "McFL" model and set
```

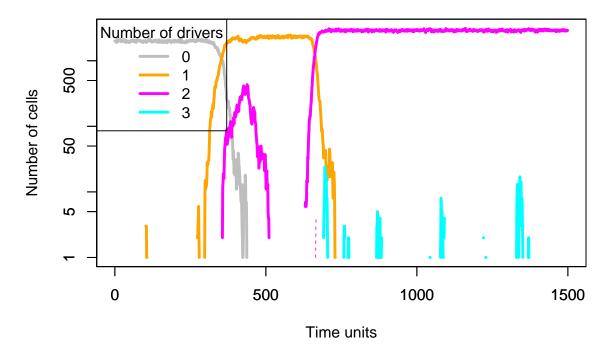
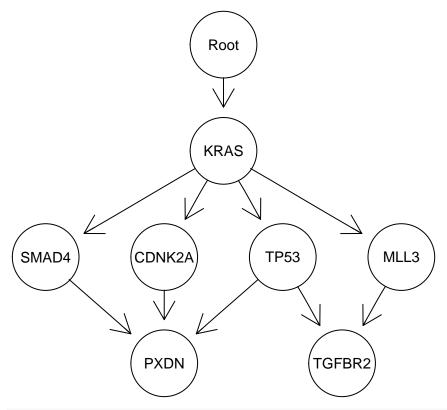


Figure 2: Plot of drivers of an epistasis simulation

As a second example, we will use a model where we specify **restrictions in the** order of accumulation of mutations using a DAG with the pancreatic cancer poset in Gerstung et al. (2011) (see more details in section 5.5):



## 2. Simulate from it. We change several possible options.

## 3. What genotypes and drivers we get? And play with limits
## to show only parts of the data. We also aggressively thin
## the data.

```
par(cex = 0.7)
plot(ep2, show = "genotypes", xlim = c(1000, 8000),
    ylim = c(0, 2400),
    thinData = TRUE, thinData.keep = 0.03)
```

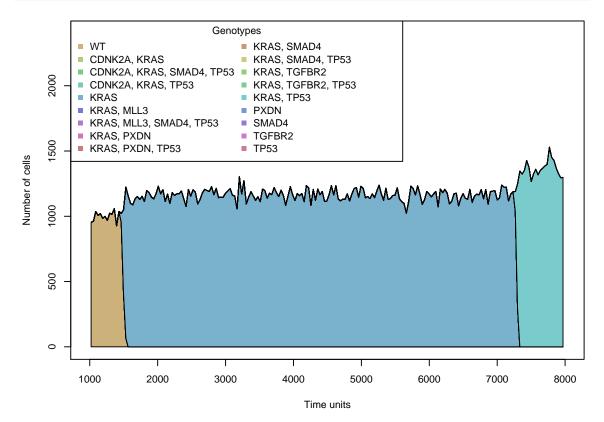


Figure 3: Plot of genotypes of a simulation from a DAG.

The rest of this vignette explores all of those functions and arguments in much more detail.

## 1.7 Citing OncoSimulR and other documentation

In R, you can do

```
citation("OncoSimulR")
##
## If you use OncoSimulR, please cite the OncoSimulR bioRxiv
## paper. A former version of OncoSimulR has been used in a
## large comparative study of methods to infer restrictions,
## published in BMC Bioinformatics; you might want to cite that
## too, if appropriate, such as when referring to using
## evolutionary simulations to assess oncogenetic tree methods
## performance.
##
```

```
## R Diaz-Uriarte. OncoSimulR: genetic simulation of cancer
## progression with arbitrary epistasis and mutator genes.
2016. bioRxiv, http://dx.doi.org/10.1101/069500.
##
## R Diaz-Uriarte. Identifying restrictions in the order of
accumulation of mutations during tumor progression:
## effects of passengers, evolutionary models, and sampling
## BMC Bioinformatics, 16(41), 2015.
```

which will tell you how to cite the package.

This is the URL for the bioRxiv paper: http://biorxiv.org/content/early/2016/08/14/069500.

#### 1.7.1 HTML and PDF versions of the vignette

A PDF version of this vignette is available from https://rdiaz02.github.io/OncoSimul/pdfs/OncoSimulR.pdf. And an HTML version from https://rdiaz02.github.io/OncoSimul/OncoSimulR.html. These files should correspond to the most recent, github version, of the package (i.e., they might include changes not yet available from the BioConductor package).

#### 1.8 Versions

In this vignette and the documentation I often refer to version 1 (v.1) and version 2 of OncoSimulR. Version 1 is the version available up to, and including, BioConductor v. 3.1. Version 2 of OncoSimulR is available starting from BioConductor 3.2 (and, of course, available too from development versions of BioC). So, if you are using the current stable or development version of BioConductor, or you grab the sources from GitHub (https://github.com/rdiaz02/OncoSimul) you are using what we call version 2. Please note that the functionality of version 1 will soon be removed.

# 2 Running time and space consumption of OncoSimulR

Time to complete the simulations and size of return objects (space consumption) depend on several, interacting factors. The usual rule of "experiment before launching a large number of simulations" applies, but here we will walk through several cases to get a feeling for the major factors that affect speed and size. Many of the comments on this section need to use ideas discussed in other places of this document. If you read this section first, you might want to come back after reading the relevant parts.

#### Speed will depend on:

- Your hardware, of course.
- The evolutionary model: using the "McFL" model is often slower (this model includes density dependence and is more complex).
- The granularity of how often you keep data (keepEvery argument). Note that the default, which is to keep as often as you sample (so that we preserve all history) can lead to very slow execution times.
- The mutation rate, because higher mutation rates lead to more clones, and more clones means we need to iterate over, well, more clones, and keep larger data structures.
- The fitness specification: more complex fitness specifications tend to be slightly slower but specially different fitness specifications can have radically different effects on the evolutionary trajectories, accessibility of fast growing genotypes and, generally, the evolutionary dynamics.
- The stopping conditions (detectionProb, detectionDrivers, detectionSize arguments) and whether or not simulations are run until cancer is reached (onlyCancer argument).

Size of returned objects will depend on:

- Any factor that affects the number of clones tracked/returned, in particular: initial sizes and stopping conditions, mutation rate, and how often you keep data (the keepEvery argument can make a huge difference here).
- Whether or not you keep the complete genealogy of clones (this affects slightly the size of returned object, not speed).

In the sections that follow, we go over several cases to understand some of the main settings that affect running time (or execution time) and space consumption (the size of returned objects). It should be understood, however, that many of the examples shown below do not represent typical use cases of OncoSimulR and are used only to identify what and how affects running time and space consumption. As we will see in most examples in this vignette, typical use cases of OncoSimulR involve hundreds to thousands of genes on population sizes up to  $10^5$  to  $10^7$ .

Note that most of the code in this section is not executed during the building of the vignette to keep vignette build time reasonable and prevent using huge amounts of RAM. All of the code, ready to be sourced and run, is available from the 'inst/miscell'

directory (and the summary output from some of the benchmarks is available from the 'miscell-files/vignette\_bench\_Rout' directory of the main OncoSimul repository at https://github.com/rdiaz02/OncoSimul).

# 2.1 Exp and McFL with "detectionProb" and pancreas example

To get familiar with some of they factors that affect time and size, we will use the fitness specification from section 1.6, with the detectionProb stopping mechanism (see 6.3.1). We will use the two main growth models (exponential and McFarland). Each model will be run with two settings of keepEvery. With keepEvery = 1 (runs exp1 and mc1), population samples are stored at time intervals of 1 (even if most of the clones in those samples later become extinct). With keepEvery = NA (runs exp2 and mc2) no intermediate population samples are stored, so clones that become extinct at any sampling period are pruned and only the existing clones at the end of the simulation are returned (see details in 11.1.1).

Will run 100 simulations. The results I show are for a laptop with an 8-core Intel Xeon E3-1505M CPU, running Debian GNU/Linux (the results from these benchmarks are available as data(benchmark\_1)).

```
## Specify fitness
pancr <- allFitnessEffects(</pre>
    data.frame(parent = c("Root", rep("KRAS", 4),
                    "SMAD4", "CDNK2A",
                    "TP53", "TP53", "MLL3"),
                child = c("KRAS", "SMAD4", "CDNK2A",
                    "TP53", "MLL3",
                    rep("PXDN", 3), rep("TGFBR2", 2)),
                s = 0.1,
               sh = -0.9,
               typeDep = "MN"),
    drvNames = c("KRAS", "SMAD4", "CDNK2A", "TP53",
                  "MLL3", "TGFBR2", "PXDN"))
Nindiv <- 100 ## Number of simulations run.
              ## Increase this number to decrease sampling variation
## keepEvery = 1
t_exp1 <- system.time(</pre>
    exp1 <- oncoSimulPop(Nindiv, pancr,</pre>
                             detectionProb = "default",
                             detectionSize = NA,
                             detectionDrivers = NA,
                             finalTime = NA,
                             keepEvery = 1,
```

```
model = "Exp",
                              mc.cores = 1))["elapsed"]/Nindiv
t_mc1 <- system.time(</pre>
    mc1 <- oncoSimulPop(Nindiv, pancr,</pre>
                             detectionProb = "default",
                             detectionSize = NA,
                             detectionDrivers = NA,
                             finalTime = NA,
                             keepEvery = 1,
                             model = "McFL",
                             mc.cores = 1))["elapsed"]/Nindiv
## keepEvery = NA
t_exp2 <- system.time(</pre>
    exp2 <- oncoSimulPop(Nindiv, pancr,</pre>
                              detectionProb = "default",
                              detectionSize = NA,
                              detectionDrivers = NA,
                              finalTime = NA,
                              keepEvery = NA,
                              model = "Exp",
                              mc.cores = 1))["elapsed"]/Nindiv
t_mc2 <- system.time(</pre>
    mc2 <- oncoSimulPop(Nindiv, pancr,</pre>
                             detectionProb = "default",
                             detectionSize = NA,
                             detectionDrivers = NA,
                             finalTime = NA,
                             keepEvery = NA,
                             model = "McFL",
                             mc.cores = 1))["elapsed"]/Nindiv
```

And we can obtain times, sizes of objects, and summaries of numbers of clones, iterations, and final times doing, for instance:

```
cat("\n\n\n t_exp1 = ", t_exp1, "\n")
object.size(exp1)/(Nindiv * 1024^2)
cat("\n\n")
summary(unlist(lapply(exp1, "[[", "NumClones")))
summary(unlist(lapply(exp1, "[[", "NumIter")))
summary(unlist(lapply(exp1, "[[", "FinalTime")))
summary(unlist(lapply(exp1, "[[", "TotalPopSize")))
```

The above runs yield the following:

Table 2: Benchmarks of Exp and McFL models using the default  $\tt detectionProb$  with two settings of  $\tt keepEvery$ .

	Elapsed Time, average per simulation (s)	Object Size, average per simulation (MB)	Number of Clones, median	Number of Iterations, median	Final Time, median	Total Population Size, median	Total Population Size, max.	keepEvery
exp1	0.001	0.037	2	253.5	252	1058	11046	1
mc1	0.737	3.855	12	816331	20406	696.5	979	1
$\mathbf{exp2}$	0.001	0.012	1	296	294	1021	21884	NA
mc2	0.696	0.014	1	694716	17366	692.5	888	NA

The above table shows that a naive comparison (looking simply at execution time) might conclude that the McFL model is much, much slower than the Exp model. But that is not the complete story: using the detectionProb stopping mechanism (see 6.3.1) will lead to stopping the simulations very quickly in the exponential model because as soon as a clone with fitness > 1 appears it starts growing exponentially. In fact, we can see that the number of iterations and the final time are much smaller in the Exp than in the McFL model. We will elaborate on this point below (section 2.2.1), when we discuss the setting for checkSizePEvery (here left at its default value of 20): checking the exiting condition more often (smaller checkSizePEvery) would probably be justified here (notice also the very large final times) and would lead to a sharp decrease in number of iterations and, thus, running time.

This table also shows that the keepEvery = NA setting, which was in effect in simulations exp2 and mc2, can make a difference especially for the McFL models, as seen by the median number of clones and the size of the returned object. Models exp2 and mc2 do not store any intermediate population samples so clones that become extinct at any sampling period are pruned and only the existing clones at the end of the simulation are returned. In contrast, models exp1 and mc1 store population samples at time intervals of 1 (keepEvery = 1), even if many of those clones eventually become extinct. We will return to this issue below as execution time and object size (which affects RAM usage) depend strongly on number of clones tracked.

We can run the exponential model again modifying the arguments of the detectionProb mechanism; in two of the models below (exp3 and exp4) no detection can take place unless populations are at least 100 times larger than the initial population size, and probability of detection is 0.1 with a population size 1,000 times larger than the initial one (PDBaseline = 5e4, n2 = 5e5). In the other two models (exp5 and exp6), no detection can take place unless populations are at least 1,000 times larger than the initial population size, and probability of detection is 0.1 with a population size 100,000 times larger than the initial one (PDBaseline = 5e5, n2 = 5e7). In runs exp3 and exp5 we set keepEvery = 1 and in runs exp4 and exp6 we set keepEvery = NA.

```
detectionProb = c(PDBaseline = 5e4,
                                                p2 = 0.1, n2 = 5e5,
                                                checkSizePEvery = 20),
                             detectionSize = NA,
                             detectionDrivers = NA,
                             finalTime = NA,
                             keepEvery = NA,
                             model = "Exp",
                             mc.cores = 1))["elapsed"]/Nindiv
t_exp5 <- system.time(</pre>
    exp5 <- oncoSimulPop(Nindiv, pancr,</pre>
                             detectionProb = c(PDBaseline = 5e5,
                                                p2 = 0.1, n2 = 5e7),
                             detectionSize = NA,
                             detectionDrivers = NA,
                             finalTime = NA,
                             keepEvery = 1,
                             model = "Exp",
                             mc.cores = 1))["elapsed"]/Nindiv
t_exp6 <- system.time(</pre>
    exp6 <- oncoSimulPop(Nindiv, pancr,</pre>
                             detectionProb = c(PDBaseline = 5e5,
                                                p2 = 0.1, n2 = 5e7),
                             detectionSize = NA,
                             detectionDrivers = NA,
                             finalTime = NA,
                             keepEvery = NA,
                             model = "Exp",
                             mc.cores = 1))["elapsed"]/Nindiv
```

Table 3: Benchmarks of Exp and McFL models modifying the default  ${\tt detectionProb}$  with two settings of  ${\tt keepEvery}$ .

	Elapsed Time,	Object Size,								
	average	average	Number			Total Pop-				
	per	per	of	Number of	Final	ulation	Total Pop-			
	simulation	simulation	Clones,	Iterations,	Time,	Size,	ulation			
	(s)	(MB)	median	median	median	median	Size, max.	keepEvery	PDBaseline	n2
exp3	0.01	0.41	14	2,754	1,890	6,798,358	2.7e + 08	1	50,000	5e+05
$\exp 4$	0.01	0.02	8	2,730	2,090	$7,\!443,\!812$	1.7e + 08	NA	50,000	5e + 05
exp5	0.84	0.91	34	54,332	2,026	1.4e + 09	$4.2e{+10}$	1	5e + 05	5e + 07
exp6	0.54	0.02	27	44,288	2,026	1.2e + 09	$3.3e{+}10$	NA	5e + 05	5e + 07

As above, keepEvery = NA (in exp4 and exp6) leads to much smaller object sizes and slightly smaller numbers of clones and execution times. Changing the exiting conditions (by changing detectionProb arguments) leads to large increases in number of iterations (in this case by factors of about 15x to 25x) and a corresponding increase in execution time.

In some of the runs of exp5 and exp6 we get the (recoverable) exception message from the C++ code: Recoverable exception ti set to DBL\_MIN. Rerunning, which is related to those simulations reaching total population sizes  $> 10^{10}$ ; we return to this below (section 2.4). You might also wonder why total and median population sizes are so large in these two runs, given the exiting conditions. One of the reasons is that we are using the default checkSizePEvery = 20, so the interval between successive checks of the exiting condition is large; this is discussed at greater length in section 2.2.1.

All the runs above used the default value onlyCancer = TRUE. This means that simulations will be repeated until the exiting conditions are reached (see details in section 6.3) and, therefore, any simulation that ends up in extinction will be repeated. This setting can thus have a large effect on the exponential models, because when the initial population size is not very large and we start from the wildtype, it is not infrequent for simulations to become extinct (when birth and death rates are equal and the population size is small, it is easy to reach extinction before a mutation in a gene that increases fitness occurs). But this is rarely the case in the McFarland model (unless we use really small initial population sizes) because of the dependency of death rate on total population size (see section 3.2.1).

The number of attempts until cancer was reached in the above models is shown in the Table 4 (the values can be obtained from any of the above runs doing, for instance, median(unlist(lapply(exp1, function(x) x\$other\$attemptsUsed)))):

Table 4.	Median	number	$\circ f$	attempts	until	cancer
Table 4.	median	Humber	OΙ	attempts	umum	cancer.

	Attempts	Attempts	Attempts		
	until	$\operatorname{until}$	$\operatorname{until}$		
	Cancer,	Cancer,	Cancer,		
	median	mean	max.	PDBaseline	n2
exp1	1	1.9	7	600	1,000
mc1	1	1	1	600	1,000
$\mathbf{exp2}$	2	2.2	16	600	1,000
mc2	1	1	1	600	1,000
$\exp 3$	6	7.7	40	50,000	5e + 05
$\exp 4$	6	8	39	50,000	5e + 05
${ m exp5}$	5	8.3	41	5e + 05	5e + 07
$\exp 6$	5	7.2	30	5e + 05	5e + 07

The McFL models finish in a single attempt. The exponential model simulations where we can exit with small population sizes (exp1, exp2) need many fewer attempts

to reach cancer than those where large population sizes are required (exp3 to exp6). There is no relevant different among those four, which is what we would expect: a population that has already reached a size of 50,000 cells from an initial population size of 500 is obviously a growing population where there is at least one mutant with positive fitness; thus, it unlikely to go extinct and therefore having to grow up to at least 500,000 will not significantly increase the risk of extinction.

We will now rerun all of the above models with argument onlyCancer = FALSE. The results are shown in Table 5 (note that the differences between this table and table 2 for the McFL models are due only to sampling variation).

Table 5: Benchmarks of models in Table 2 and 3 when run with  $\verb"onlyCancer" = FALSE$ .

	Elapsed Time, average per simulation (s)	Object Size, average per simulation (MB)	Number of Clones, median	Number of Iterations, median	Final Time, median	Total Population Size, median	Total Popula- tion Size, mean	Total Popula- tion Size, max.	keepEvery	PDBaseline	n2
exp1_noc	0.001	0.041	1.5	394	393	0	708	18,188	1	600	1,000
$mc1\_noc$	0.69	3.9	12	673,910	16,846	692	700	983	1	600	1,000
$\exp 2$ _noc	0.001	0.012	1	320	319	726	870	26,023	NA	600	1,000
$mc2\_noc$	0.65	0.014	1	628,683	15,716	694	704	910	NA	600	1,000
$exp3\_noc$	0.002	0.15	2	718	694	0	2,229,519	5.7e + 07	1	50,000	5e + 05
exp4_noc	0.002	0.013	0	600	599	0	3,122,765	1.3e + 08	NA	50,000	5e + 05
$exp5\_noc$	0.17	0.22	3	848	777	0	5.9e + 08	1.5e + 10	1	5e + 05	5e + 07
exp6_noc	0.068	0.013	0	784	716	0	4.1e + 08	$1.3e{+}10$	NA	5e + 05	5e+07

Now most simulations under the exponential model end up in extinction, as seen by the median population size of 0 (but not all, as the mean and max. population size are clearly away from zero). Consequently, simulations under the exponential model are now faster (and the size of the average return object is smaller). Of course, whether one should run simulations with onlyCancer = TRUE or onlyCancer = FALSE will depend on the question being asked (see, for example, section 1.3.3 for a question where we will naturally want to use onlyCancer = FALSE).

To make it easier to compare results with those of the next section, Table 6 shows all the runs so far.

Table 6: Benchmarks of all models in Tables 2, 3 and 5.

	Elapsed Time,											
	average	Object Size,				Total						
	per simu-	average per	Number of	Number of		Population	Total	Total				
	lation	simulation	Clones,	Iterations,	Final Time,	Size,	Population	Population				
	(s)	(MB)	median	median	median	median	Size, mean	Size, max.	keepEvery	PDBaseli	ine n2	onlyCancer
exp1	0.001	0.037	2	254	252	1,058	1,277	11,046	1	600	1,000	TRUE
mc1	0.74	3.9	12	816,331	20,406	696	702	979	1	600	1,000	TRUE
$\mathbf{exp2}$	0.001	0.012	1	296	294	1,021	1,392	21,884	NA	600	1,000	TRUE
mc2	0.7	0.014	1	694,716	$17,\!366$	692	698	888	NA	600	1,000	TRUE
$\mathbf{exp3}$	0.01	0.41	14	2,754	1,890	6,798,358	1.7e + 07	2.7e + 08	1	50,000	5e + 05	TRUE
$\exp 4$	0.009	0.016	8	2,730	2,090	7,443,812	1.5e + 07	1.7e + 08	NA	50,000	5e + 05	TRUE
${ m exp5}$	0.84	0.91	34	54,332	2,026	1.4e + 09	3.5e + 09	$4.2e{+}10$	1	5e + 05	5e + 07	TRUE
exp6	0.54	0.021	27	44,288	2,026	1.2e + 09	3.2e + 09	$3.3e{+}10$	NA	5e + 05	5e + 07	TRUE
exp1_noc	0.001	0.041	1.5	394	393	0	708	18,188	1	600	1,000	FALSE
mc1_noc	0.69	3.9	12	673,910	16,846	692	700	983	1	600	1,000	FALSE
$\exp 2$ _noc	0.001	0.012	1	320	319	726	870	26,023	NA	600	1,000	FALSE
$mc2\_noc$	0.65	0.014	1	628,683	15,716	694	704	910	NA	600	1,000	FALSE
$exp3\_noc$	0.002	0.15	2	718	694	0	$2,\!229,\!519$	5.7e + 07	1	50,000	5e + 05	FALSE
$\exp 4$ _noc	0.002	0.013	0	600	599	0	$3,\!122,\!765$	1.3e + 08	NA	50,000	5e + 05	FALSE
$\exp 5$ _noc	0.17	0.22	3	848	777	0	5.9e + 08	$1.5e{+10}$	1	5e + 05	5e + 07	FALSE
$\exp 6$ _noc	0.068	0.013	0	784	716	0	4.1e + 08	$1.3e{+10}$	NA	5e + 05	5e + 07	FALSE

#### **2.1.1** Changing fitness: s = 0.1 and s = 0.05

In the above fitness specification the fitness effect of each gene (when its restrictions are satisfied) is s=0.1 (see section 3.2 for details). Here we rerun all the above benchmarks using s=0.05 and results are shown below in Table 7; the results from these benchmarks are available as data(benchmark\_1\_0.05):

Table 7: Benchmarks of all models in Table 6 using s=0.05 (instead of s=0.1).

	Elapsed Time,											
	average	Object Size,				Total						
	per simu-	average per	Number of	Number of		Population	Total	Total				
	lation	simulation	Clones,	Iterations,	Final Time,	Size,	Population	Population				
	(s)	(MB)	median	median	median	median	Size, mean	Size, max.	keepEvery	PDBaseli	ine n2	${\rm only Cancer}$
exp1	0.002	0.043	2	316	315	1,104	1,181	3,176	1	600	1,000	TRUE
mc1	1.7	11	17	2e + 06	50,696	644	647	761	1	600	1,000	TRUE
$\mathbf{exp2}$	0.001	0.012	1	274	273	1,129	1,281	7,608	NA	600	1,000	TRUE
mc2	1.6	0.016	1	$1,\!615,\!197$	$40,\!376$	644	651	772	NA	600	1,000	TRUE
$\exp 3$	0.012	0.63	15	3,995	2,919	3,798,540	5,892,376	4.5e + 07	1	50,000	5e + 05	TRUE
$\exp 4$	0.011	0.017	9	4,288	3,276	$4,\!528,\!072$	$6,\!551,\!319$	3.2e + 07	NA	50,000	5e + 05	TRUE
${ m exp5}$	0.3	1.2	34	68,410	2,751	6.8e + 08	1e+09	8.2e + 09	1	5e + 05	5e + 07	TRUE
exp6	0.26	0.022	23	44,876	2,499	4.3e + 08	8.9e + 08	7.3e + 09	NA	5e + 05	5e + 07	TRUE
exp1_noc	0.001	0.039	2	310	308	0	522	2,239	1	600	1,000	FALSE
$mc1\_noc$	1.6	11	17	2e + 06	50,776	638	643	757	1	600	1,000	FALSE
$\exp 2$ _noc	0.001	0.012	0	340	336	0	599	3,994	NA	600	1,000	FALSE
$mc2\_noc$	1.7	0.017	1	2,102,439	$52,\!556$	645	650	740	NA	600	1,000	FALSE
$\exp 3$ _noc	0.002	0.11	2	618	615	0	150,978	6,093,498	1	50,000	5e + 05	FALSE
$\exp 4$ _noc	0.002	0.013	0	813	812	0	$558,\!225$	2.3e+07	NA	50,000	5e + 05	FALSE
$\exp 5$ _noc	0.031	0.23	3	917	914	0	1.1e + 08	3.7e + 09	1	5e + 05	5e + 07	FALSE
$\exp 6$ _noc	0.046	0.013	0	628	610	0	1.7e + 08	5.1e + 09	NA	5e + 05	5e + 07	FALSE

As expected, having a smaller s leads to slower processes in most cases, since it takes longer to reach the exiting conditions sooner. Particularly noticeable are the runs for the McFL models (notice the increases in population size and number of iterations—see also below).

That is not the case, however, for exp5 and exp6 (and exp5\_noc and exp6\_noc). When running with s=0.05 the simulations exit at a later time (see column "Final Time") but they exit with smaller population sizes. Here we have an interaction between sampling frequency, speed of growth of the population, mutation events and number of clones. In populations that grow much faster mutation events will happen more often (which will trigger further iterations of the algorithm); in addition, more new clones will be created, even if they only exist for short times and become extinct by the following sampling period (so they are not reflected in the pops.by.time matrix). These differences are proportionally larger the larger the rate of growth of the population. Thus, they are larger between, say, the exp5 at s=0.1 and s=0.05 than between the exp4 at the two different s: the exp5 exit conditions can only be satisfied at much larger population sizes so at populations sizes when growth is much faster (recall we are dealing with exponential growth).

Recall also that with the default settings in detectionProb, we assess the exiting condition every 20 time periods (argument checkSizePEvery); this means that for fast growing populations, the increase in population size between successive checks of the exit conditions will be much larger (this phenomenon is also discussed in section 2.2.1).

Thus, what is happening in the exp5 and exp6 with s=0.1 is that close to the time the exit conditions could be satisfied, they are growing very fast, accumulating mutants, and incurring in additional iterations. They exit sooner in terms of time periods, but they do much more work before arriving there.

The setting of checkSizePEvery is also having a huge effect on the McFL model simulations (the number of iterations is  $> 10^6$ ). Even more than in the previous section, checking the exiting condition more often (smaller checkSizePEvery) would probably be justified here (notice also the very large final times) and would lead to a sharp decrease in number of iterations and, thus, running time.

The moral here is that in complex simulations like this, the effects of some parameters (s in this case) might look counter-intuitive at first. Thus the need to "experiment before launching a large number of simulations".

#### 2.2 Several "common use cases" runs

Let us now execute some simulations under more usual conditions. We will use seven different fitness specifications: the pancreas example, two random fitness landscapes, and four sets of independent genes (200 to 4000 genes) with fitness effects randomly drawn from exponential distributions:

```
pancr <- allFitnessEffects(</pre>
    data.frame(parent = c("Root", rep("KRAS", 4),
                   "SMAD4", "CDNK2A",
                   "TP53", "TP53", "MLL3"),
               child = c("KRAS", "SMAD4", "CDNK2A",
                   "TP53", "MLL3",
                   rep("PXDN", 3), rep("TGFBR2", 2)),
               s = 0.1,
               sh = -0.9,
               typeDep = "MN"),
    drvNames = c("KRAS", "SMAD4", "CDNK2A", "TP53",
                 "MLL3", "TGFBR2", "PXDN"))
## Random fitness landscape with 6 genes
## At least 50 accessible genotypes
rfl6 <- rfitness(6, min_accessible_genotypes = 50)
attributes(rf16)$accessible genotypes ## How many accessible
rf6 <- allFitnessEffects(genotFitness = rf16)</pre>
## Random fitness landscape with 12 genes
## At least 200 accessible genotypes
rfl12 <- rfitness(12, min_accessible_genotypes = 200)
attributes(rf112) $accessible genotypes ## How many accessible
rf12 <- allFitnessEffects(genotFitness = rf112)</pre>
## Independent genes; positive fitness from exponential distribution
## mean around 0.1, and negative from exponential with mean around
## 0.02. Half of genes positive fitness effects, half negative.
ng <- 200
re 200 <- allFitnessEffects(noIntGenes = c(rexp(ng/2, 10),
                                            -rexp(ng/2, 50))
ng <- 500
re 500 <- allFitnessEffects(noIntGenes = c(rexp(ng/2, 10),
                                            -rexp(ng/2, 50))
ng <- 2000
re 2000 <- allFitnessEffects(noIntGenes = c(rexp(ng/2, 10),
                                             -rexp(ng/2, 50))
```

#### 2.2.1 Common use cases, set 1.

We will use the Exp and the McFL models, run with different parameters. The script is provided as 'benchmark\_2.R', under '/inst/miscell', with output in the 'miscell-files/vignette\_bench\_Rout' directory of the main OncoSimul repository at https://github.com/rdiaz02/OncoSimul. The data are available as data(benchmark\_2).

For the Exp model the call will be

```
oncoSimulPop(Nindiv,
    fitness,
    detectionProb = NA,
    detectionSize = 1e6,
    initSize = 500,
    detectionDrivers = NA,
    keepPhylog = TRUE,
    model = "Exp",
    errorHitWallTime = FALSE,
    errorHitMaxTries = FALSE,
    finalTime = 5000,
    onlyCancer = FALSE,
    mc.cores = 1,
    sampleEvery = 0.5,
    keepEvery = 1)
```

And for McFL:

```
finalTime = 5000,
max.wall.time = 10,
onlyCancer = FALSE,
mc.cores = 1,
keepEvery = 1)
```

For the exponential model we will stop simulations when the populations have > 10<sup>6</sup> cells (simulations start from 500 cells). For the McFarland model we will use the detectionProb mechanism (see section 6.3.1 for details); we could have used as stopping mechanism detectionSize = 2 \* initSize (which would be basically equivalent to reaching cancer, as argued in (McFarland et al. 2013)) but we want to provide further examples under the detectionProb mechanism. We will start from 1000 cells, not 500 (starting from 1000 we almost always reach cancer in a single execution).

Why not use the detectionProb mechanism with the Exp models? Because it can be hard to intuitively understand what are reasonable settings for the parameters of the detectionProb mechanism when used in a population that is growing exponentially, especially if different genes have very different effects on fitness and we are using fitness specifications that are so different (compare the fitness landscape of six genes, the pancreas specification, and the fitness specification with 4000 genes with fitness effects drawn from an exponential distribution —re\_4000). In contrast, the detectionProb mechanism might be simpler to reason about in a population that is growing under a model of carrying capacity with possibly large periods of stasis. Let us emphasize that it is not that the detectionProb mechanism does not make sens with the Exp model; it is simply that the parameters might need finer adjustment for them to make sense, and in these benchmarks we are dealing with widely different fitness specifications.

Note also that we specify checkSizePEvery = 4 (instead of the default, which is 20). Why? Because the fitness specifications where fitness effects are drawn from exponential distributions (re\_200 to re\_4000 above) include many genes (well, up to 4000) some of them with possibly very large effects. In these conditions, simulations will run very fast in the sense of "units of time". If we check exiting conditions every 20 units the population could have increased size several orders of magnitude in between checks (this is also discussed in sections 6.3.1 and 2.1.1). You can verify this by running the script with other settings for checkSizePEvery (and being aware that large settings might require you to wait for a long time). To ensure that populations have really grown, we have increased the setting of PDBaseline so that no simulation can be considered for stopping unless its size is 1.4 times larger than initSize.

In all cases we use keepEvery = 1 and keepPhylog = TRUE. Finally, we run all models with errorHitWallTime = FALSE and errorHitMaxTries = FALSE so that we can see results even if stopping conditions are not met.

The results of the benchmarks, using 100 individual simulations, are shown in Table 8.

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Table 8: Benchmarks under some common use cases, set 1.

		Elapsed Time,	Object Size,	Number	NI 1 C	D: 1	TD 4 1	m . 1	T + 1
		average per simulation	average per simulation	of  Clones,	Number of Iterations,	Final Time,	Total Population	Total Population	Total Population
Model	Fitness	(s)	(MB)	median	median	median	Size, median	Size, mean	Size, max.
Exp	pancr	0.002	0.12	3	1,397	697	0	164,222	1,053,299
McFL	pancr	0.12	0.56	8	2e + 05	5,000	1,037	1,144	1,938
$\operatorname{Exp}$	rf6	0.002	0.064	6	783	391	1e+06	594,899	1,309,497
McFL	rf6	0.019	0.071	3	23,297	582	1,884	1,975	4,636
$\operatorname{Exp}$	rf12	0.01	0.13	4	1,178	542	0	287,669	1,059,141
McFL	rf12	0.14	0.82	18	2e + 05	5,000	1,252	1,295	1,695
$\operatorname{Exp}$	$re\_200$	0.013	0.67	230	1,185	223	1,060,944	859,606	1,536,242
McFL	$re\_200$	0.018	0.22	47	9,679	240	2,166	2,973	29,301
$\operatorname{Exp}$	$re\_500$	0.09	2.7	771	2,732	152	1,068,732	959,026	1,285,522
McFL	$re\_500$	0.024	0.44	91	7,056	172	2,148	2,578	8,234
$\operatorname{Exp}$	$re\_2000$	0.91	29	3,376	7,412	70	1,163,990	1,143,041	1,741,492
McFL	$re\_2000$	0.031	1.9	186	3,546	80	2,870	3,704	13,248
$\operatorname{Exp}$	$re\_4000$	3.3	113	7,088	12,216	52	1,217,568	1,309,185	2,713,200
m McFL	$re\_4000$	0.063	6.5	326	2,731	52	4,592	13,601	729,611

In most cases, simulations run reasonably fast (under 0.1 seconds per individual simulation) and the return objects are small. I will only focus on a few cases.

The McFL model with random fitness landscape rf12 and with pancr does not satisfy the conditions of detectionProb in most cases: its median final time is 5000, which was the maximum final time specified. This suggests that the fitness landscape is such that it is unlikely that we will reach population sizes > 1400 (remember we increase the setting for PDBaseline) before 5000 time units. There is nothing particular about using a fitness landscape of 12 genes and other runs in other 12-gene random fitness landscapes do not show this pattern. However, complex fitness landscapes might be such that genotypes of high fitness (those that allow reaching a large population size quickly) are not easily accessible<sup>2</sup> so reaching them might take a long time. This does not affect the exponential model in the same way because, well, because there is exponential growth in that model: any genotype with fitness > 1 will grow exponentially (of course, at possibly very different rates). You might want to play with the script and modify the call to rfitness (using different values of reference and c, for instance) to have simpler paths to a maximum or modify the call to oncoSimulPop (with, say, finalTime to much larger values). Some of these issues are related to more general questions about fitness landscapes and accessibility (see section 1.3.2 and references therein).

You could also set onlyCancer = TRUE. This might make sense if you are interested in only seeing simulations that "reach cancer" (where "reach cancer" means reaching a state you define as a function of population size or drivers). However, if you are exploring fitness landscapes, onlyCancer = TRUE might not always be reasonable as reaching a particular population size, for instance, might just not be possible under some fitness landscapes (this phenomenon is of course not restricted to random fitness landscapes —see also section 2.3.4).

As we anticipated above, the detectionProb mechanism has to be used with care: some of the simulations run in very short "time units", such as those for the fitness specifications with 2000 and 4000 genes. Having used a checkSizePEvery = 20 probably would not have made sense.

Finally, it is interesting that in the cases examined here, the two slowest running simulations are from "Exp", with fitnesses re\_2000 and re\_4000 (and the third slowest is also Exp, under re\_500). These are the cases with the largest number of clones. Why? In the "Exp" model there is no competition, and fitness specifications re\_2000 and re\_4000 have genomes with many genes with positive fitness contributions. It is thus very easy to obtain, from the wildtype ancestor, a large number of clones all of which have birth rates > 1 and, thus, clones that are unlikely to become extinct.

<sup>&</sup>lt;sup>2</sup>By easily accessible I mean that there are many, preferably short, paths of non-decreasing fitness from the wildtype to this genotype. See definitions and discussion in, e.g., Franke et al. (2011).

#### 2.2.2 Common use cases, set 2.

We will now rerun the simulations above changing the following:

- finalTime is set to 25000.
- onlyCancer is set to TRUE.
- The "Exp" models will stop when population size  $> 10^5$ .

This is in script 'benchmark\_3.R', under '/inst/miscell', with output in the 'miscell-files/vignette\_bench\_Rout' directory of the main OncoSimul repository at https://github.com/rdiaz02/OncoSimul. The data are available as data(benchmark\_3).

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Table 9: Benchmarks under some common use cases, set 2.

Model	Fitness	Elapsed Time, average per simulation (s)	Object Size, average per simulation (MB)	Number of Clones, median	Number of Iterations, median	Final Time, median	Total Population Size, median	Total Population Size, mean	Total Population Size, max.
Exp	pancr	0.012	0.32	10	3,480	1,718	1e+05	1e+05	108,805
McFL	pancr	0.41	1.7	14	4e + 05	9,955	1,561	1,555	1,772
$\operatorname{Exp}$	rf6	0.003	0.058	4	866	430	$107,\!492$	109,774	$135,\!257$
McFL	rf6	0.033	0.12	4	35,216	880	2,003	2,010	3,299
$\operatorname{Exp}$	rf12	0.012	0.098	9	1,138	561	1e + 05	1e+05	112,038
McFL	rf12	0.17	0.76	16	1e + 05	$2,\!511$	1,486	1,512	1,732
$\operatorname{Exp}$	$re\_200$	0.004	0.39	106	723	252	1e + 05	$105,\!586$	122,338
McFL	$re\_200$	0.026	0.33	61	13,484	335	1,830	2,049	3,702
$\operatorname{Exp}$	$re\_500$	0.007	0.61	168	490	117	110,311	$112,\!675$	134,860
McFL	$re\_500$	0.018	0.33	70	$5,\!157$	126	2,524	3,455	19,899
$\operatorname{Exp}$	$re\_2000$	0.046	5.7	651	1,078	68	106,340	109,081	153,146
McFL	$re\_2000$	0.029	1.8	186	3,444	80	2,837	4,009	37,863
$\operatorname{Exp}$	$re\_4000$	0.1	19	1,140	1,722	51	111,256	113,499	168,958
McFL	$re\_4000$	0.057	6.7	325	3,081	60	3,955	8,892	$265,\!183$

Since we increased the maximum final time and forced runs to "reach cancer" the McFL run with the pancreas fitness specification takes a bit longer because it also has to do a larger number of iterations. Interestingly, notice that the median final time is close to 10000, so the runs in 2.2.1 with maximum final time of 5000 would have had a hard time finishing with onlyCancer = TRUE.

Forcing simulations to "reach cancer", and just random differences between the random fitness landscape also affect the McFL run under rf12: final time is below 5000 and the median number of iterations is about half of what was above.

Finally, by stopping the Exp simulations at  $10^5$ , simulations with re\_2000 and re\_4000 finish now in much shorter times (but they still take longer than their McFL counterparts) and the number of clones created is much smaller.

#### 2.3 Can we use a large number of genes?

Yes. In fact, in OncoSimulR there is no pre-set limit on genome size. However, large numbers of genes can lead to unacceptable memory usage or running time. We discuss several examples next that illustrate some of the major issues to consider. Another example with 50,000 genes is shown in section 6.6.3.

We have seen in 2.1 and 2.2.1 that for the Exp model, benchmark results using detectionProb require a lot of care and can be misleading. Here, we will fix initial and final population sizes. Moreover, to avoid the confounding factor of the onlyCancer = TRUE argument, we will set it to FALSE, so we measure directly the time of individual runs.

#### 2.3.1 Exponential model with 10,000 and 50,000 genes

#### 2.3.1.1 Exponential, 10,000 genes, example 1

We will start with 10000 genes and an exponential model, where we stop when the population grows over 1e6 individuals:

```
t_e_10000
##
      user
            system elapsed
##
     4.368
              0.196
                      4.566
summary(e_10000)[, c(1:3, 8, 9)]
     NumClones TotalPopSize LargestClone FinalTime NumIter
## 1
          5017
                     1180528
                                    415116
                                                  143
                                                          7547
## 2
          3726
                     1052061
                                    603612
                                                  131
                                                         5746
## 3
          4532
                     1100721
                                    259510
                                                  132
                                                         6674
## 4
                     1283115
                                    829728
                                                   99
          4150
                                                          6646
## 5
          4430
                     1139185
                                    545958
                                                  146
                                                         6748
print(object.size(e 10000), units = "MB")
## 863.9 Mb
```

Each simulation takes about 1 second but note that the number of clones for most simulations is already over 4000 and that the size of the return object is close to 1 GB (a more detailed explanation of where this 1 GB comes from is deferred until section 2.3.6.1).

#### 2.3.1.2 Exponential, 10,000 genes, example 2

We can decrease the size of the return object if we use the **keepEvery = NA** argument (this setting was explained in detail in section 2.1):

```
t e 10000b
##
            system elapsed
      user
     5.484
             0.100
                      5.585
##
summary(e 10000b)[, c(1:3, 8, 9)]
     NumClones TotalPopSize LargestClone FinalTime NumIter
                                    727989
                                                  91
## 1
          2465
                     1305094
                                                         6447
```

```
## 2
           2362
                      1070225
                                     400329
                                                   204
                                                           8345
## 3
           2530
                      1121164
                                     436721
                                                   135
                                                           8697
## 4
           2593
                      1206293
                                     664494
                                                   125
                                                           8149
## 5
           2655
                      1186994
                                     327835
                                                   191
                                                           8572
print(object.size(e 10000b), units = "MB")
## 488.3 Mb
```

#### 2.3.1.3 Exponential, 50,000 genes, example 1

Let's use 50,000 genes. To keep object sizes reasonable we use keepEvery = NA. For now, we also set mutationPropGrowth = FALSE so that the mutation rate does not become really large in clones with many mutations but, of course, whether or not this is a reasonable decision depends on the problem; see also below.

```
ng <- 50000
u <- allFitnessEffects(noIntGenes = c(rep(0.1, ng/2), rep(-0.1, ng/2)))
t e 50000 <- system.time(
    e_50000 <- oncoSimulPop(5,
                             model = "Exp",
                             mu = 1e-7,
                             detectionSize = 1e6,
                             detectionDrivers = NA,
                             detectionProb = NA,
                             keepPhylog = TRUE,
                             onlyCancer = FALSE,
                             keepEvery = NA,
                             mutationPropGrowth = FALSE,
                             mc.cores = 1
                             ))
t e 50000
##
      user
            system elapsed
##
   44.192
             1.684 45.891
summary(e 50000)[, c(1:3, 8, 9)]
     NumClones TotalPopSize LargestClone FinalTime NumIter
## 1
          7367
                     1009949
                                   335455
                                               75.00
                                                       18214
## 2
          8123
                     1302324
                                   488469
                                               63.65
                                                       17379
          8408
                                               72.57
## 3
                     1127261
                                   270690
                                                       21144
## 4
          8274
                     1138513
                                   318152
                                               80.59
                                                       20994
## 5
                                               70.00
          7520
                     1073131
                                   690814
                                                       18569
print(object.size(e 50000), units = "MB")
```

```
## 7598.6 Mb
```

Of course, simulations now take longer and the size of the return object is over 7 GB (we are keeping over 7000 clones, even if when we prune all those that went extinct).

#### 2.3.2 Exponential, example 4: 50,000 genes

What if we had not pruned?

```
ng <- 50000
u <- allFitnessEffects(noIntGenes = c(rep(0.1, ng/2), rep(-0.1, ng/2)))
t_e_50000np <- system.time(
    e_50000np <- oncoSimulPop(5,
                               model = "Exp",
                               mu = 1e-7,
                               detectionSize = 1e6,
                               detectionDrivers = NA,
                               detectionProb = NA,
                               keepPhylog = TRUE,
                               onlyCancer = FALSE,
                               keepEvery = 1,
                               mutationPropGrowth = FALSE,
                               mc.cores = 1
                               ))
t_e_50000np
    user system elapsed
## 42.316
            2.764 45.079
summary(e_50000np)[, c(1:3, 8, 9)]
     NumClones TotalPopSize LargestClone FinalTime NumIter
##
## 1
         13406
                     1027949
                                   410074
                                               71.97
                                                       19469
## 2
         12469
                     1071325
                                   291852
                                               66.00
                                                       17834
## 3
         11821
                     1089834
                                   245720
                                               90.00
                                                       16711
## 4
                                               77.61
         14008
                     1165168
                                   505607
                                                       19675
## 5
         14759
                     1074621
                                   205954
                                               87.68
                                                       20597
print(object.size(e 50000np), units = "MB")
## 12748.4 Mb
```

The main effect is not on execution time but on object size (it has grown by 5 GB).

#### 2.3.2.1 Exponential, 50,000 genes, example 2

What about the mutationPropGrowth setting? We will rerun the example in 2.3.1.3

leaving keepEvery = NA but with the default mutationPropGrowth:

```
ng <- 50000
u <- allFitnessEffects(noIntGenes = c(rep(0.1, ng/2), rep(-0.1, ng/2)))
t_e_50000c <- system.time(</pre>
    e 50000c <- oncoSimulPop(5,
                              model = "Exp",
                              mu = 1e-7,
                              detectionSize = 1e6,
                              detectionDrivers = NA,
                              detectionProb = NA,
                              keepPhylog = TRUE,
                              onlyCancer = FALSE,
                              keepEvery = NA,
                              mutationPropGrowth = TRUE,
                              mc.cores = 1
                              ))
t_e_50000c
      user
            system elapsed
## 84.228
            2.416 86.665
summary(e 50000c)[, c(1:3, 8, 9)]
     NumClones TotalPopSize LargestClone FinalTime NumIter
##
## 1
         11178
                     1241970
                                    344479
                                               84.74
                                                        27137
## 2
         12820
                     1307086
                                               91.94
                                                       33448
                                    203544
## 3
         10592
                     1126091
                                   161057
                                               83.81
                                                       26064
## 4
                                               65.68
         11883
                     1351114
                                   148986
                                                       25396
## 5
         10518
                     1101392
                                   253523
                                               99.79
                                                       26082
print(object.size(e 50000c), units = "MB")
## 10904.9 Mb
```

As expected (because the mutation rate per unit time is increasing in the fastest growing clones), we have many more clones, larger objects, and longer times of execution here: we almost double the time and the size of the object increases by almost 3 GB.

What about larger population sizes or larger mutation rates? The number of clones starts growing fast, which means much slower execution times and much larger return objects (see also the examples below).

#### 2.3.3 McFarland model with 50,000 genes; the effect of keepEvery

We show an example of McFarland's model with 50,000 genes in section 6.6.3. We will show here a few more examples with those many genes but with a different fitness specification and changing several other settings.

#### 2.3.3.1 McFarland, 50,000 genes, example 1

Let's start with mutationPropGrowth = FALSE and keepEvery = NA:

```
ng <- 50000
u <- allFitnessEffects(noIntGenes = c(rep(0.1, ng/2), rep(-0.1, ng/2)))
t mc 50000 nmpg <- system.time(
    mc_50000_nmpg <- oncoSimulPop(5,</pre>
                                   model = "McFL",
                                   mu = 1e-7,
                                   detectionSize = 1e6,
                                   detectionDrivers = NA,
                                   detectionProb = NA,
                                   keepPhylog = TRUE,
                                   onlyCancer = FALSE,
                                   keepEvery = NA,
                                   mutationPropGrowth = FALSE,
                                   mc.cores = 1
                                   ))
t mc 50000 nmpg
    user system elapsed
   30.46
##
             0.54
                     31.01
summary(mc_50000_nmpg)[, c(1:3, 8, 9)]
##
     NumClones TotalPopSize LargestClone FinalTime NumIter
## 1
          1902
                     1002528
                                   582752
                                               284.2
                                                       31137
## 2
          2159
                     1002679
                                   404858
                                               274.8
                                                       36905
## 3
          2247
                     1002722
                                   185678
                                               334.5
                                                       42429
## 4
          2038
                     1009606
                                   493574
                                               218.4
                                                       32519
## 5
          2222
                     1004661
                                   162628
                                               291.0
                                                       38470
print(object.size(mc 50000 nmpg), units = "MB")
## 2057.6 Mb
```

We are already dealing with 2000 clones.

#### 2.3.3.2 McFarland, 50,000 genes, example 2

Setting keepEvery = 1 (i.e., keeping track of clones with an interval of 1):

```
t_mc_50000_nmpg_k <- system.time(
    mc 50000 nmpg k <- oncoSimulPop(5,
                                     model = "McFL",
                                     mu = 1e-7,
                                     detectionSize = 1e6,
                                     detectionDrivers = NA,
                                     detectionProb = NA,
                                     keepPhylog = TRUE,
                                     onlyCancer = FALSE,
                                     keepEvery = 1,
                                     mutationPropGrowth = FALSE,
                                     mc.cores = 1
                                     ))
t_mc_50000_nmpg_k
      user
            system elapsed
             1.712 31.714
##
    30.000
summary(mc_50000_nmpg_k)[, c(1:3, 8, 9)]
     NumClones TotalPopSize LargestClone FinalTime NumIter
##
## 1
          8779
                     1000223
                                   136453
                                               306.7
                                                       38102
## 2
          7442
                     1006563
                                   428150
                                               345.3
                                                       35139
## 3
          8710
                     1003509
                                   224543
                                               252.3
                                                       35659
          8554
                                               273.7
## 4
                     1002537
                                   103889
                                                       36783
## 5
          8233
                     1003171
                                   263005
                                               301.8
                                                       35236
print(object.size(mc 50000 nmpg k), units = "MB")
## 8101.4 Mb
```

Computing time increases slightly but the major effect is seen on the size of the return object, that increases by a factor of about 4x, up to 8 GB, corresponding to the increase in about 4x in the number of clones being tracked (see details of where size comes from in section 2.3.6.1).

#### 2.3.3.3 McFarland, 50,000 genes, example 3

We will set keepEvery = NA again, but we will now increase detection size by a factor of 3:

```
ng <- 50000
u <- allFitnessEffects(noIntGenes = c(rep(0.1, ng/2), rep(-0.1, ng/2)))
t_mc_50000_nmpg_3e6 <- system.time(
    mc_50000_nmpg_3e6 <- oncoSimulPop(5,</pre>
```

```
u,
                                       model = "McFL",
                                       mu = 1e-7,
                                       detectionSize = 3e6,
                                       detectionDrivers = NA,
                                       detectionProb = NA,
                                       keepPhylog = TRUE,
                                       onlyCancer = FALSE,
                                       keepEvery = NA,
                                       mutationPropGrowth = FALSE,
                                       mc.cores = 1
                                       ))
t mc 50000 nmpg 3e6
      user system elapsed
    77.240
             1.064 78.308
summary(mc_50000_nmpg_3e6)[, c(1:3, 8, 9)]
##
     NumClones TotalPopSize LargestClone FinalTime NumIter
## 1
          5487
                    3019083
                                   836793
                                              304.5
                                                      65121
## 2
                                              286.3
          4812
                    3011816
                                   789146
                                                      53087
## 3
          4463
                    3016896
                                  1970957
                                              236.6
                                                      45918
## 4
          5045
                                              360.3
                    3028142
                                   956026
                                                      63464
## 5
          4791
                    3029720
                                   916692
                                              358.1
                                                      55012
print(object.size(mc_50000_nmpg_3e6), units = "MB")
## 4759.3 Mb
```

Compared with the first run (2.3.3.1) we have approximately doubled computing time, number of iterations, number of clones, and object size.

#### 2.3.3.4 McFarland, 50,000 genes, example 4

Let us use the same detectionSize = 1e6 as in the first example (2.3.3.1), but with 5x the mutation rate:

```
keepPhylog = TRUE,
                                        onlyCancer = FALSE,
                                        keepEvery = NA,
                                        mutationPropGrowth = FALSE,
                                        mc.cores = 1
                                        ))
t mc 50000 nmpg 5mu
      user system elapsed
## 167.332
             1.796 169.167
summary(mc_50000_nmpg_5mu)[, c(1:3, 8, 9)]
##
     NumClones TotalPopSize LargestClone FinalTime NumIter
          7963
                     1004415
                                    408352
## 1
                                               99.03
                                                        57548
## 2
          8905
                     1010751
                                    120155
                                              130.30
                                                        74738
## 3
          8194
                     1005465
                                    274661
                                               96.98
                                                        58546
## 4
          9053
                     1014049
                                    119943
                                              112.23
                                                        75379
## 5
          8982
                     1011817
                                     95047
                                               99.95
                                                        76757
print(object.size(mc 50000 nmpg 5mu), units = "MB")
## 8314.4 Mb
```

The number of clones we are tracking is about 4x the number of clones of the first example (2.3.3.1), and roughly similar to the number of clones of the second example (2.3.3.2), and size of return object is similar to that of the second example. But computing time has increased by a factor of about 5x and iterations have increased by a factor of about 2x. Iterations increase because mutation is more frequent; in addition, at each sampling period each iteration needs to do more work as it needs to loop over a larger number of clones and this larger number includes clones that are not shown here, because they are pruned (they are extinct by the time we exit the simulation —again, pruning is discussed with further details in 11.1.1).

#### 2.3.3.5 McFarland, 50,000 genes, example 5

Finally, let's run the above example but with keepEvery = 1:

```
keepEvery = 1,
                                          mutationPropGrowth = FALSE,
                                          mc.cores = 1
                                          ))
t mc 50000 nmpg 5mu k
##
            system elapsed
      user
## 174.404
             5.068 179.481
summary(mc_50000_nmpg_5mu_k)[, c(1:3, 8, 9)]
##
     NumClones TotalPopSize LargestClone FinalTime NumIter
## 1
         25294
                     1001597
                                    102766
                                               123.4
                                                        74524
## 2
         23766
                     1006679
                                    223010
                                               124.3
                                                        71808
## 3
         21755
                     1001379
                                               114.8
                                    203638
                                                        62609
## 4
         24889
                     1012103
                                    161003
                                               119.3
                                                        75031
## 5
         21844
                     1002927
                                    255388
                                               108.8
                                                        64556
print(object.size(mc_50000_nmpg_5mu_k), units = "MB")
## 22645.8 Mb
```

We have already seen these effects before in section 2.3.3.2: using keepEvery = 1 leads to a slight increase in execution time. What is really affected is the size of the return object which increases by a factor of about 3x (and is now over 20GB). That 3x corresponds, of course, to the increase in the number of clones being tracked. This, by the way, also allows us to understand the comment above, where we said that in these two cases (where we have increased mutation rate) at each iteration we need to do more work as at every update of the population the algorithm needs to loop over a much larger number of clones (even if many of those are eventually pruned).

#### 2.3.3.6 McFarland, 50,000 genes, example 6

Finally, we will run the example in section 2.3.3.1 with the default of mutationPropGrowth = TRUE:

```
keepPhylog = TRUE,
                               onlyCancer = FALSE,
                              keepEvery = NA,
                              mutationPropGrowth = TRUE,
                              mc.cores = 1
                               ))
t mc 50000
      user
            system elapsed
## 303.352
             2.808 306.223
summary(mc_50000)[, c(1:3, 8, 9)]
##
     NumClones TotalPopSize LargestClone FinalTime NumIter
                                               210.9
         13928
                     1010815
## 1
                                    219814
                                                        91255
## 2
         12243
                     1003267
                                    214189
                                                178.1
                                                        67673
## 3
         13880
                     1014131
                                    124354
                                                161.4
                                                        88322
## 4
                                                205.7
         14104
                     1012941
                                     75521
                                                        98583
## 5
         12428
                     1005594
                                    232603
                                                167.4
                                                        70359
print(object.size(mc_50000), units = "MB")
## 12816.6 Mb
```

Note the huge increase in computing time (related of course to the huge increase in number of iterations) and in the size of the return object: we have gone from having to track about 2000 clones to tracking over 12000 clones even when we prune all clones without descendants.

#### **2.3.4** Examples with s = 0.05

A script with the above runs but using s=0.05 instead of s=0.1 is available from the repository ('miscell-files/vignette\_bench\_Rout/large\_num\_genes\_0.05.Rout'). I will single out a couple of cases here.

First, we repeat the run shown in section 2.3.3.5:

```
mutationPropGrowth = FALSE,
                                         mc.cores = 1
                                         ))
t mc 50000 nmpg 5mu k
            system elapsed
      user
             5.164 310.711
## 305.512
summary(mc 50000 nmpg 5mu k)[, c(1:3, 8, 9)]
     NumClones TotalPopSize LargestClone FinalTime NumIter
## 1
         61737
                    1003273
                                   104460
                                           295.8731
                                                     204214
## 2
         65072
                    1000540
                                   133068 296.6243
                                                    210231
print(object.size(mc 50000 nmpg 5mu k), units = "MB")
## 24663.6 Mb
```

Note we use only two replicates, since those two already lead to a 24 GB return object as we are tracking more than 60,000 clones, more than twice those with s = 0.1. The reason for the difference in number of clones and iterations is of course the change from s = 0.1 to s = 0.05: under the McFarland model to reach population sizes of  $10^6$  starting from an equilibrium population of 500 we need about 43 mutations (whereas only about 22 are needed if  $s = 0.1^3$ ).

Next, let us rerun 2.3.3.1:

```
t mc 50000 nmpg <- system.time(
    mc_50000_nmpg <- oncoSimulPop(5,</pre>
                                    u,
                                    model = "McFL",
                                    mu = 1e-7,
                                    detectionSize = 1e6,
                                    detectionDrivers = NA,
                                    detectionProb = NA,
                                    keepPhylog = TRUE,
                                    onlyCancer = FALSE,
                                    keepEvery = NA,
                                    mutationPropGrowth = FALSE,
                                    mc.cores = 1
                                    ))
t_mc_50000_nmpg
      user system elapsed
## 111.236
             0.596 111.834
summary(mc 50000 nmpg)[, c(1:3, 8, 9)]
```

<sup>&</sup>lt;sup>3</sup>Given the dependence of death rates on population size in McFarland's model (\section 3.2.1), if all mutations have the same fitness effects we can calculate the equilibrium population size (where birth and death rates are equal) for a given number of mutated genes:  $K * (e^{(1+s)^p} - 1)$  where K is the initial equilibrium size, s the fitness effect of each mutation and p the number of mutated genes.

```
##
     NumClones TotalPopSize LargestClone FinalTime NumIter
## 1
          2646
                     1000700
                                   217188
                                             734.475
                                                      108566
## 2
          2581
                     1001626
                                             806.500
                                                      107296
                                   209873
## 3
          2903
                     1001409
                                   125148
                                             841.700
                                                     120859
## 4
                                             906.300
          2310
                     1000146
                                   473948
                                                       91519
## 5
          2704
                     1001290
                                   448409
                                             838.800
                                                      103556
print(object.size(mc 50000 nmpg), units = "MB")
## 2638.3 Mb
```

Using s = 0.05 leads to a large increase in final time and number of iterations. However, as we are using the keepEvery = NA setting, the increase in number of clones tracked and in size of return object is relatively small.

## 2.3.5 The different consequences of keepEvery = NA in the Exp and McFL models

We have seen that keepEvery = NA often leads to much smaller return objects when using the McFarland model than when using the Exp model. Why? Because in the McFarland model there is strong competition and there can be complete clonal sweeps so that in extreme cases a single clone might be all that is left after some time. This is not the case in the exponential models.

Of course, the details depend on the difference in fitness effects between different genotypes (or clones). In particular, we have seen several examples where even with keepEvery=NA there are a lot of clones in the McFL models. In those examples many clones had identical fitness (the fitness effects of all genes with positive fitness is the same, and ditto for the genes with negative fitness effects), so no clone ends up displacing all the others.

#### 2.3.6 Are we keeping the complete history (genealogy) of the clones?

Yes we are if we run with keepPhylog = TRUE, regardless of the setting for keepEvery. As explained in section 11.1, OncoSimulR prunes clones that never had a population size larger than zero at any sampling period (so they are not reflected in the pops.by.time matrix in the output). And when set keepEvery = NA we are telling OncoSimulR to discard any sampling period except the very last one.

keepPhylog operates differently: it records the exact time at which a clone appeared and the clone that gave rise to it. This information is kept regardless of whether or not those clones appear in the pops.by.time matrix.

Keeping the complete genealogy might be of limited use if the pops.by.time matrix only contains the very last period. However, you can use plotClonePhylog and ask to be shown only clones that exist in the very last period.

For instance, in run 2.3.1.3 we could have looked at the information stored about the genealogy of clones by doing:

```
head(e 50000[[1]]$other$PhylogDF)
##
     parent child
                     time
## 1
             3679 0.8402
## 2
             4754 1.1815
            20617 1.4543
## 3
## 4
            15482 2.3064
## 5
             4431 3.7130
## 6
            41915 4.0628
tail(e 50000[[1]]$other$PhylogDF)
##
                                                                 child time
                             parent
                                                   3679, 20282, 22359 75.0
## 20672
                        3679, 20282
## 20673
                                            3679, 17922, 22346, 35811 75.0
                3679, 17922, 22346
## 20674
                         2142, 3679
                                                    2142, 3679, 25838 75.0
## 20675
                3679, 17922, 19561
                                            3679, 17922, 19561, 43777 75.0
## 20676 3679, 15928, 19190, 20282 3679, 15928, 19190, 20282, 49686 75.0
                                             2142, 3679, 16275, 24201 75.0
## 20677
                 2142, 3679, 16275
```

where each row corresponds to one event of appearance of a new clone, the column labeled "parent" are the mutated genes in the parent, and the column labeled "child" are the mutated genes in the child.

And we could plot the clones that have a population size of at least one in the last period doing:

```
plotClonePhylog(e_50000[[1]]) ## plot not shown
```

What is the cost of keep the clone genealogies? In terms of time it is minor. In terms of space, and as shown in the example above, we can end up storing a data frame with tends of thousands of rows and three columns (two factors, one float). In the example above the size of that data frame is approximately 2 MB for a single simulation. This is much smaller than the pops.by.time or Genotypes matrices, but it can quickly build up if you routinely launch, say, 1000 simulations via oncoSimulPop. That is why the default is keepPhylog = FALSE as this information is not needed as often as that in the other two matrices (pops.by.time and Genotypes).

#### 2.3.6.1 Interlude: where is that 1 GB coming from?

In section 2.3.1.1 we have seen an apparently innocuous simulation producing a return object of almost 1 GB. Where is that coming from? It means that each simulation produced almost 200 MB of output.

Let us look at one simulation in more detail:

```
mu = 1e-7,
                      detectionSize = 1e6,
                      detectionDrivers = NA,
                      detectionProb = NA,
                      keepPhylog = TRUE,
                      onlyCancer = FALSE,
                      mutationPropGrowth = TRUE
summary(r1)[c(1, 8)]
##
     NumClones FinalTime
## 1
          3887
                       345
print(object.size(r1), units = "MB")
## 160 Mb
sizes <- lapply(r1, function(x) object.size(x)/(1024^2))
sort(unlist(sizes), decreasing = TRUE)[1:2]
## Genotypes pops.by.time
##
         148.28
                        10.26
dim(r1$Genotypes)
## [1] 10000 3887
```

The above shows the reason: the **Genotypes** matrix is a 10,000 by 3,887 integer matrix (with a 0 and 1 indicating not-mutated/mutated for each gene in each genotype) and in R integers use 4 bytes each. The pops.by.time matrix is 346 by 3,888 (the 1 in 346 = 345 + 1 comes from starting at 0 and going up to the final time, both included; the 1 in 3888 = 3887 + 1 is from the column of time) double matrix and doubles use 8 bytes<sup>4</sup>.

### 2.4 Population sizes $\geq 10^{10}$

We have already seen examples where population sizes reach  $10^8$  to  $10^{10}$ , as in Tables 3, 5, 7. What about even larger population sizes?

The C++ code will unconditionally alert if population sizes exceed  $4*10^{15}$  as in those cases loosing precision (as we are using doubles) would be unavoidable, and we would also run into problems with the generation of binomial random variates (code that illustrates and discusses this problem is available in file "example-binom-problems.cpp", in directory "/inst/miscell"). However, well before we reach  $4*10^{15}$  we loose precision from other sources. One of the most noticeable ones is that when we reach population sizes around  $10^{11}$  the C++ code will often alert us by throwing exceptions with the message Recoverable exception ti set to

 $<sup>^4</sup>$ These matrices do not exist during most of the execution of the C++ code; they are generated right before returning from the C++ code.

DBL\_MIN. Rerunning.; I throw this exception because  $t_i$ , the random variable for time to next mutation, is less than DBL\_MIN, the minimum representable floating-point number. This happens because, unless we use really tiny mutation rates, the time to a mutation starts getting closer to zero as population sizes grow very large. It might be possible to ameliorate these problems somewhat by using long doubles (instead of doubles) or special purpose libraries that provide more precision. However, this would make it harder to run the same code in different operating systems and would likely decrease execution speed on the rest of the common scenarios for which OncoSimulR has been designed.

The following code shows some examples where we use population sizes of  $10^{10}$  or larger. Since we do not want simulations in the exponential model to end because of extinction, I use a fitness specification where all genes have a positive fitness effect and we start all simulations from a large population (to make it unlikely that the population will become extinct before cells mutate and start increasing in numbers). We set the maximum running time to 10 minutes. We keep the genealogy of the clones and use keepEvery = 1.

```
ng <- 50
u <- allFitnessEffects(noIntGenes = c(rep(0.1, ng)))</pre>
```

```
t_mc_k_50_1e11 <- system.time(
    mc_k_50_1e11 <- oncoSimulPop(5,</pre>
                                  u,
                                  model = "McFL",
                                  mu = 1e-7,
                                  detectionSize = 1e11,
                                  initSize = 1e5,
                                  detectionDrivers = NA,
                                  detectionProb = NA,
                                  keepPhylog = TRUE,
                                  onlyCancer = FALSE,
                                  mutationPropGrowth = FALSE,
                                  keepEvery = 1,
                                  finalTime = 5000,
                                  mc.cores = 1,
                                  max.wall.time = 600
                                  ))
## Recoverable exception ti set to DBL MIN. Rerunning.
## Recoverable exception ti set to DBL_MIN. Rerunning.
t_mc_k_50_1e11
## user system elapsed
## 613.612
             0.040 613.664
summary(mc k 50 1e11)[, c(1:3, 8, 9)]
```

```
##
    NumClones TotalPopSize LargestClone FinalTime NumIter
## 1
         5491 100328847809 44397848771 1019.950 942764
## 2
         3194 100048090441 34834178374
                                          789.675 888819
## 3
         5745 100054219162 24412502660
                                          927.950 929231
## 4
         4017 101641197799 60932177160
                                          750.725 480938
## 5
         5393 100168156804 41659212367
                                          846.250 898245
## print(object.size(mc k 50 1e11), units = "MB")
## 177.8 Mb
```

We get to  $10^{11}$ . But notice the exception with the warning about  $t_i$ . Notice also that this takes a long time and we run a very large number of iterations (getting close to one million in some cases).

Now the exponential model with detectionSize = 1e11:

```
t_exp_k_50_1e11 <- system.time(
    exp k 50 1e11 <- oncoSimulPop(5,
                                   u,
                                   model = "Exp",
                                   mu = 1e-7,
                                   detectionSize = 1e11,
                                   initSize = 1e5,
                                   detectionDrivers = NA,
                                   detectionProb = NA,
                                   keepPhylog = TRUE,
                                   onlyCancer = FALSE,
                                   mutationPropGrowth = FALSE,
                                   keepEvery = 1,
                                   finalTime = 5000,
                                   mc.cores = 1,
                                   max.wall.time = 600,
                                   errorHitWallTime = FALSE,
                                   errorHitMaxTries = FALSE
                                   ))
## Recoverable exception ti set to DBL MIN. Rerunning.
## Hitted wall time. Exiting.
## Recoverable exception ti set to DBL MIN. Rerunning.
## Recoverable exception ti set to DBL MIN. Rerunning.
## Recoverable exception ti set to DBL_MIN. Rerunning.
## Hitted wall time. Exiting.
## Recoverable exception ti set to DBL MIN. Rerunning.
## Recoverable exception ti set to DBL MIN. Rerunning.
## Recoverable exception ti set to DBL_MIN. Rerunning.
## Recoverable exception ti set to DBL MIN. Rerunning.
## Recoverable exception ti set to DBL MIN. Rerunning.
```

```
## Hitted wall time. Exiting.
## Hitted wall time. Exiting.
t exp k 50 1e11
##
       user
              system
                      elapsed
## 2959.068
               0.128 2959.556
try(summary(exp k 50 1e11)[, c(1:3, 8, 9)])
     NumClones TotalPopSize LargestClone FinalTime NumIter
## 1
          6078
                65172752616
                             16529682757
                                           235.7590 1883438
## 2
          5370 106476643712
                             24662446729
                                           232.0000 2516675
## 3
          2711
                21911284363
                             17945303353
                                           224.8608
                                                     543698
## 4
          2838
                13241462284
                               2944300245
                                           216.8091
                                                     372298
## 5
                76166784312
                             10941729810
                                          240.0217 1999489
          7289
print(object.size(exp k 50 1e11), units = "MB")
## 53.5 Mb
```

Note that we almost reached max.wall.time (600 \* 5 = 3000). What if we wanted to go up to  $10^{12}$ ? We could not do it in 10 minutes. We could set max.wall.time to a value larger than 600 to allow us to reach larger sizes but then we would be waiting for a possibly unacceptable time for simulations to finish. Moreover, this would eventually fail as simulations would keep hitting the  $t_i$  exception without ever being able to complete. Finally, even if we were very patient, hitting that  $t_i$  exception should make us worry about possible biases in the samples.

# 2.5 A summary of some determinants of running time and space consumption

To summarize this section, we have seen:

- Both McFL and Exp can be run in short times over a range of sizes for the detectionProb mechanism using a complex fitness specification with a small number of genes. These are the typical or common use cases of OncoSimulR.
- The keepEvery argument can have a large effect on time in the McFL models and specially on object sizes. If only the end result of the simulation is to be used, you should set keepEvery = NA.
- The distribution of fitness effects and the fitness landscape can have large effects on running times. Sometimes these are intuitive and simple to reason about, sometimes they are not as they interact with other factors (e.g., stopping mechanism, numbers of clones, etc). In general, there can be complex interactions between different settings, from mutation rate to fitness effects to initial size. As usual, test before launching a massive simulation.
- Simulations start to slow down and lead to a very large object size when we keep track of around 6000 to 10000 clones. Anything that leads to these patterns

will slow down the simulations.

• OncoSimulR needs to keep track of genotypes (or clones), not just numbers of drivers and passengers, because it allows you to use complex fitness and mutation specifications that depend on specific genotypes. The keepEvery = NA is an approach to keep the minimal history needed, but it is unavoidable that during the simulations we might be forced to deal with many thousands of different clones.

## 3 Specifying fitness effects

OncoSimulR uses a standard continuous time model, where individual cells divide, die, and mutate with rates that can depend on genotype and population size; over time the abundance of the different genotypes changes by the action of selection (due to differences in net growth rates between genotypes), drift, and mutation. As a result of a mutation in a pre-existing clone new clones arise, and the birth rate of a newly arisen clone is determined at the time of its emergence as a function of its genotype. Simulations can use an use exponential growth model or a model with carrying capacity that follows McFarland et al. (2013). For the exponential growth model, the death rate is fixed at one whereas in the model with carrying capacity death rate increases with population size. In both cases, therefore, fitness differences between genotypes in a given population at a given time are due to differences in the mapping between genotype and birth rate. There is second exponential model (called "Bozic") where birth rate is fixed at one, and genotype determines death rate instead of birth rate (see details in 3.2). So when we discuss specifying fitness effects or the effects of genes on fitness, we are actually referring to specifying effects on birth (or death) rates, which then translate into differences in fitness (since the other rate, death or birth, is either fixed, as in the Exp and Bozic models, or depends on the population size). This is also shown in Table 1, in the rows for "Fitness components", under "Evolutionary Features".

#### 3.1 Introduction to the specification of fitness effects

With OncoSimulR you can specify different types of effects on fitness:

- A special type of epistatic effect that is particularly amenable to be represented as a graph. In this graph, having, say, "B" be a child of "A" means that a mutation in B can only accumulate if a mutation in A is already present. This is what OT (Desper et al. 1999; Szabo and Boucher 2008), CBN (Beerenwinkel, Eriksson, and Sturmfels 2007; Gerstung et al. 2009; Gerstung et al. 2011), progression networks (Farahani and Lagergren 2013), and other similar models (Korsunsky et al. 2014) generally mean. Details are provided in section 3.5. Note that this is not an order effect (discussed below): the fitness of a genotype from this DAGs is a function of whether or not the restrictions in the graph are satisfied, not the historical sequence of how they were satisfied.
- Effects where the order in which mutations are acquired matters, as illustrated in section 3.7. There is, in fact, empirical evidence of these effects (Ortmann et al. 2015). For instance, the fitness of genotype "A, B" would differ depending on whether A or B was acquired first (or, as in the actual example in (Ortmann et al. 2015), the fitness of the mutant with JAK2 and TET2 mutated will depend on which of the genes was mutated first).
- General epistatic effects (e.g., section 3.10), including synthetic viability (e.g., section 3.8) and synthetic lethality/mortality (e.g., section 3.9).

- Genes that have independent effects on fitness (section 3.3).
- Modules (see section 3.6) allow you to specify any of the above effects (except those for genes without interactions, as it would not make sense there) in terms of modules (sets of genes), not individual genes. We will introduce them right after 3.5, and we will continue using them thereafter.

A guiding design principle of OncoSimulR is to try to make the specification of those effects as simple as possible but also as flexible as possible. Thus, there are two main ways of specifying fitness effects:

- Combining different types of effects in a single specification. For instance, you can combine epistasis with order effects with no interaction genes with modules. What you would do here is specify the effects that different mutations (or their combinations) have on fitness (the fitness effects) and then have OncoSimulR take care of combining them as if each of these were lego pieces. We will refer to this as the **lego system of fitness effects**. (As explained above, I find this an intuitive and very graphical analogy, which I have copied from Hothorn et al. (2006) and Hothorn et al. (2008)).
- Explicitly passing to OncoSimulR a mapping of genotypes to fitness. Here you specify the fitness of each genotype. We will refer to this as the **explicit** mapping of genotypes to fitness.

Both approaches have advantages and disadvantages. Here I emphasize some relevant differences.

- With the lego system you can specify huge genomes with an enormous variety of interactions, since the possible genotypes are not constructed in advance. You would not be able to do this with the explicit mapping of genotypes to fitness if you wanted to, say, construct that mapping for a modest genotype of 500 genes (you'd have more genotypes than particles in the observable Universe).
- For many models/data you often intuitively start with the fitness of the genotypes, not the fitness consequences of the different mutations. In these cases, you'd need to do the math to specify the terms you want if you used the lego system.
- Sometimes you already have a moderate size genotype → fitness mapping and you certainly do not want to do the math by hand: here the lego system would be painful to use.
- But sometimes we do think in terms of "the effects on fitness of such and such mutations are" and that immediately calls for the lego system, where you focus on the effects, and let OncoSimulR take care of doing the math of combining.
- If you want to use order effects, you must use the lego system (at least for now).
- If you want to specify modules, you must use the lego system (the explicit mapping of genotypes is, by its very nature, ill-suited for this).

• The lego system might help you see what your model really means: in many cases, you can obtain fairly succinct specification of complex fitness models with just a few terms. Similarly, depending on what your emphasis is, you can often specify the same fitness landscape in several different ways.

Regardless of the route, you need to get that information into OncoSimulR's functions. The main function we will use is allFitnessEffects: this is the function in charge of reading the fitness specifications. We also need to discuss how, what, and where you have to pass to allFitnessEffects.

#### 3.1.1 Explicit mapping of genotypes to fitness

Conceptually, the simplest way to specify fitness is to specify the mapping of all genotypes to fitness explicitly. An example will make this clear. Let's suppose you have a simple two-gene scenario, so a total of four genotypes, and you have a data frame with genotypes and fitness, where genoytpes are specified as character vectors, with mutated genes separated by commas:

```
m4 \leftarrow data.frame(G = c("WT", "A", "B", "A, B"), F = c(1, 2, 3, 4))
```

Now, let's give that to the allFitnessEffects function:

```
fem4 <- allFitnessEffects(genotFitness = m4)</pre>
```

## Column names of object not Genotype and Fitness. Renaming them assuming that is

(The message is just telling you what the program guessed you wanted.)

That's it. You can plot that fitnessEffects object

#### plot(fem4)



In this case, that plot is not very interesting (compare with the plot(pancr) we

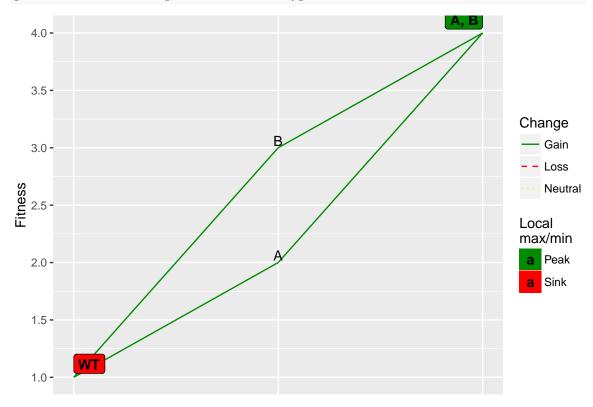
saw in 1.6 or the plots in 3.5).

You can also check what OncoSimulR thinks the fitnesses are, with the evalAllGenotypes function that we will use repeatedly below (of course, here we should see the same fitnesses we entered):

```
evalAllGenotypes(fem4, addwt = TRUE)
## Genotype Fitness
## 1 WT 1
## 2 A 2
## 3 B 3
## 4 A, B 4
```

And you can plot the fitness landscape:

#### plotFitnessLandscape(evalAllGenotypes(fem4))



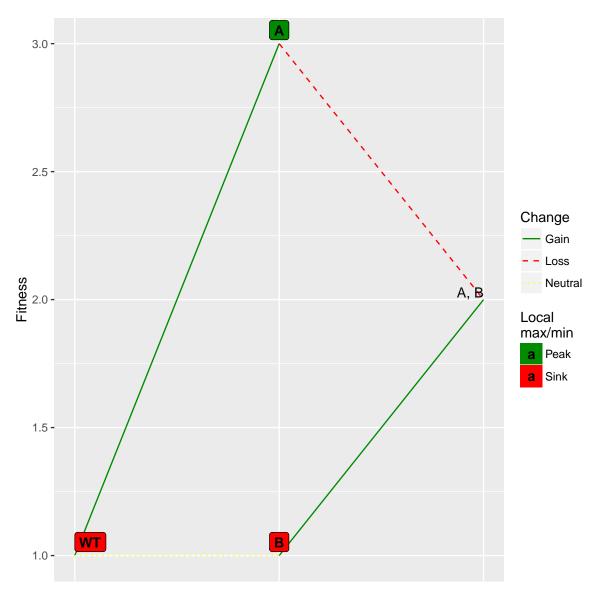
To specify the mapping you can also use a matrix (or data frame) with g+1 columns; each of the first g columns contains a 1 or a 0 indicating that the gene of that column is mutated or not. Column g+1 contains the fitness values. And you do not even need to specify all the genotypes (we will assume that the missing genotypes have fitness 1):

```
m6 <- cbind(c(1, 1), c(1, 0), c(2, 3))
fem6 <- allFitnessEffects(genotFitness = m6)
## Number of genotypes less than 2^L. Missing genotype will be set to 1
## Setting/resetting gene names because one or more are missing. If this is not wha
evalAllGenotypes(fem6, addwt = TRUE)</pre>
```

```
## Genotype Fitness
## 1 WT 1
## 2 A 3
## 3 B 1
## 4 A, B 2
plot(fem6)
```



plotFitnessLandscape(evalAllGenotypes(fem6))



This way of giving a fitness specification to OncoSimulR might be ideal if you directly generate random mappings of genotypes to fitness (or random fitness landscapes), as we will do in section 9.

We will see an example of this way of passing fitness again in 5.1, where will compare it with the lego system.

#### 3.1.2 How to specify fitness effects with the lego system

An alternative general approach followed in many genetic simulators is to specify how particular combinations of alleles modify the wildtype genotype or the genotype that contains the individual effects of the interacting genes (e.g., see equation 1 in the supplementary material for FFPopSim (Zanini and Neher 2012)). For example, if we specify that a mutation in "A" contributes 0.04, a mutation in "B" contributes 0.03, and the double mutation "A:B" contributes 0.1, that means that the fitness of the "A, B" genotype (the genotype with A and B mutated) is that of the wildtype

(1, by default), plus (actually, times —see section 3.2— but plus on the log scale) the effects of having A mutated, plus (times) the effects of having B mutated, plus (times) the effects of "A:B" both being mutated.

We will see below that with the "lego system" it is possible to do something very similar to the explicit mapping of section 3.1.1. But this will sometimes require a more cumbersome notation (and sometimes also will require your doing some math). We will see examples in sections 3.10.1, 3.10.2 and 3.10.3 or the example in 5.4.2. But then, if we can be explicit about (at least some of) the mappings  $genotype \rightarrow fitness$ , how are these procedures different? When you use the "lego system" you can combine both a partial explicit mapping of genotypes to fitness with arbitrary fitness effects of other genes/modules. In other words, with the "lego system" OncoSimulR makes it simple to be explicit about the mapping of specific genotypes, while also using the "how this specific effects modifies previous effects" logic, leading to a flexible specification. This also means that in many cases the same fitness effects can be specified in several different ways.

Most of the rest of this section is devoted to explaining how to combine those pieces. Before that, however, we need to discuss the fitness model we use.

#### 3.2 Numeric values of fitness effects

We evaluate fitness using the usual (Zanini and Neher 2012; Gillespie 1993; Beerenwinkel, Eriksson, and Sturmfels 2007; Datta et al. 2013) multiplicative model: fitness is  $\Pi(1+s_i)$  where  $s_i$  is the fitness effect of gene (or gene interaction) i. In all models except Bozic, this fitness refers to the growth rate (the death rate being fixed to  $1^5$ ). The original model of McFarland et al. (2013) has a slightly different parameterization, but you can go easily from one to the other (see section 3.2.1).

For the Bozic model (Bozic et al. 2010), however, the birth rate is set to 1, and the death rate then becomes  $\prod (1 - s_i)$ .

#### 3.2.1 McFarland parameterization

In the original model of McFarland et al. (2013), the effects of drivers contribute to the numerator of the birth rate, and those of the (deleterious) passengers to the denominator as:  $\frac{(1+s)^d}{(1-s_p)^p}$ , where d and p are, respectively, the total number of drivers and passengers in a genotype, and here the fitness effects of all drivers is the same (s) and that of all passengers the same too  $(s_p)$ . However, we can map from this ratio to the usual product of terms by using a different value of  $s_p$ , that we will call  $s_{pp} = -s_p/(1+s_p)$  (see McFarland (2014), his eq. 2.1 in p.9). This reparameterization applies to v.2. In v.1 we use the same parameterization as in the original one in McFarland et al. (2013).

<sup>&</sup>lt;sup>5</sup>You can change this if you really want to.

For death rate, we use the expression that McFarland et al. (2013) (see their p. 2911) use "(...) for large cancers (grown to  $10^6$  cells)":  $D(N) = \log(1 + N/K)$  where K is the initial equilibrium population size. As the authors explain, for large N/K the above expression "(...) recapitulates Gompertzian dynamics observed experimentally for large tumors".

By default, OncoSimulR uses a value of  $K = initSize/(e^1 - 1)$  so that the starting population is at equilibrium.

#### 3.2.2 No viability of clones and types of models

For all models where fitness affects directly the birth rate (all except Bozic), if you specify that some event (say, mutating gene A) has  $s_A \leq -1$ , if that event happens then birth rate becomes zero. This is taken to indicate that the clone is not even viable and thus disappears immediately without any chance for mutation<sup>6</sup>.

Models based on Bozic, however, have a birth rate of 1 and mutations affect the death rate. In this case, a death rate larger than birth rate, *per se*, does not signal immediate extinction and, moreover, even for death rates that are a few times larger than birth rates, the clone could mutate before becoming extinct<sup>7</sup>.

In general, if you want to identify some mutations or some combinations of mutations as leading to immediate extinction (i.e., no viability), of the affected clone, set it to  $-\infty$  as this would work even if how birth rates of 0 are handled changes. Most examples below evaluate fitness by its effects on the birth rate. You can see one where we do it both ways in Section 3.8.2.

#### 3.3 Genes without interactions

This is a simple scenario. Each gene i has a fitness effect  $s_i$  if mutated. The  $s_i$  can come from any distribution you want. As an example let's use three genes. We know there are no order effects, but we will also see what happens if we examine genotypes as ordered.

<sup>&</sup>lt;sup>6</sup>This is a shortcut that we take because we think that it is what you mean. Note, however, that technically a clone with birth rate of 0 might have a non-zero probability of mutating before becoming extinct because in the continuous time model we use mutation is not linked to reproduction. In the present code, we are not allowing for any mutation when birth rate is 0. There are other options, but none which I find really better. An alternative implementation makes a clone immediately extinct if and only if any of the  $s_i = -\infty$ . However, we still need to handle the case with  $s_i < -1$  as a special case. We either make it identical to the case with any  $s_i = -\infty$  or for any  $s_i > -\infty$  we set  $(1 + s_i) = \max(0, 1 + s_i)$  (i.e., if  $s_i < -1$  then  $(1 + s_i) = 0$ ), to avoid obtaining negative birth rates (that make no sense) and the problem of multiplying an even number of negative numbers. I think only the second would make sense as an alternative.

<sup>&</sup>lt;sup>7</sup>We said "a few times". For a clone of population size 1 —which is the size at which all clones start from mutation—, if death rate is, say, 90 but birth rate is 1, the probability of mutating before becoming extinct is very, very close to zero for all reasonable values of mutation rate}. How do we signal immediate extinction or no viability in this case? You can set the value of  $s = -\infty$ .

```
ai1 <- evalAllGenotypes(allFitnessEffects(
   noIntGenes = c(0.05, -.2, .1)), order = FALSE)</pre>
```

We can easily verify the first results:

```
ai1
##
     Genotype Fitness
## 1
                 1.050
## 2
            2
                0.800
## 3
            3
                1.100
## 4
         1, 2
                0.840
## 5
         1, 3
                1.155
## 6
         2, 3
                0.880
      1, 2, 3
                0.924
all(ai1[, "Fitness"] == c((1 + .05), (1 - .2), (1 + .1),
       (1 + .05) * (1 - .2),
       (1 + .05) * (1 + .1),
```

```
(1 - .2) * (1 + .1),

(1 + .05) * (1 - .2) * (1 + .1)))

## [1] TRUE
```

And we can see that considering the order of mutations (see section 3.7) makes no difference:

```
(ai2 <- evalAllGenotypes(allFitnessEffects(</pre>
    noIntGenes = c(0.05, -.2, .1)), order = TRUE,
    addwt = TRUE))
##
       Genotype Fitness
## 1
              WT
                   1.000
## 2
               1
                   1.050
## 3
               2
                   0.800
               3
## 4
                   1.100
          1 > 2
## 5
                   0.840
          1 > 3
## 6
                   1.155
## 7
          2 > 1
                   0.840
          2 > 3
## 8
                   0.880
## 9
          3 > 1
                   1.155
          3 > 2
## 10
                   0.880
## 11 1 > 2 > 3
                   0.924
## 12 1 > 3 > 2
                   0.924
## 13 2 > 1 > 3
                   0.924
## 14 2 > 3 > 1
                   0.924
## 15 3 > 1 > 2
                   0.924
## 16 3 > 2 > 1
                   0.924
```

(The meaning of the notation in the output table is as follows: "WT" denotes the wild-type, or non-mutated clone. The notation x > y means that a mutation in "x"

happened before a mutation in "y". A genotype  $x > y \_ z$  means that a mutation in "x" happened before a mutation in "y"; there is also a mutation in "z", but that is a gene for which order does not matter).

And what if I want genes without interactions but I want modules (see section 3.6)? Go to section 3.11.

#### 3.4 Numerical issues with death rates of 0 in Bozic model

As we mentioned above (section 3.8.2) death rates of 0 can lead to trouble when using Bozic's model:

```
i1 <- allFitnessEffects(noIntGenes = c(1, 0.5))</pre>
evalAllGenotypes(i1, order = FALSE, addwt = TRUE,
                 model = "Bozic")
##
     Genotype Death_rate
## 1
           WT
## 2
            1
                     0.0
            2
                     0.5
## 3
## 4
         1, 2
                      0.0
i1 b <- oncoSimulIndiv(i1, model = "Bozic")</pre>
## Warning in nr oncoSimul.internal(rFE = fp, birth = birth, death
## = death, : You are using a Bozic model with the new restriction
## specification, and you have at least one s of 1. If that gene is
## mutated, this will lead to a death rate of 0 and the simulations
## will abort when you get a non finite value.
##
   DEBUG2: Value of rnb = nan
##
##
##
   DEBUG2: Value of m = 1
##
    DEBUG2: Value of pe = 0
##
##
    DEBUG2: Value of pm = 1
##
##
##
   this is spP
##
   popSize = 1
##
   birth = 1
##
##
   death = 0
   W = 1
##
## R = 1
## mutation = 1e-10
## timeLastUpdate = 92.052
    absfitness = -inf
##
## numMutablePos =0
```

```
##
## Unrecoverable exception: Algo 2: retval not finite. Aborting.
```

Of course, there is no problem in using the above with other models:

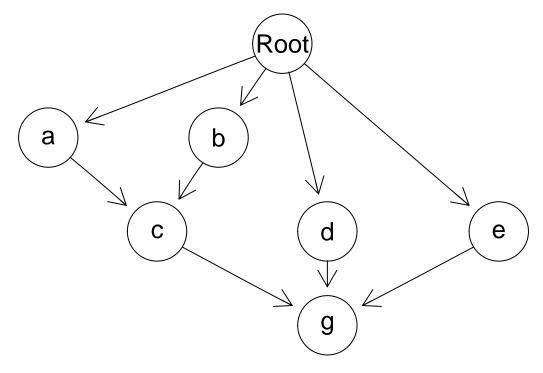
```
evalAllGenotypes(i1, order = FALSE, addwt = TRUE,
                  model = "Exp")
##
     Genotype Fitness
## 1
           WT
                   1.0
## 2
            1
                   2.0
## 3
            2
                   1.5
         1, 2
                   3.0
## 4
i1 e <- oncoSimulIndiv(i1, model = "Exp")</pre>
summary(i1_e)
##
     NumClones TotalPopSize LargestClone MaxNumDrivers MaxDriversLast
## 1
                   411464448
                                  3.59e+08
##
     NumDriversLargestPop TotalPresentDrivers FinalTime NumIter
## 1
                                               0
                                                        386
                                                                538
     HittedWallTime HittedMaxTries errorMF minDMratio minBMratio
##
## 1
                              FALSE
                                                   5e+05
                                                               5e+05
              FALSE
                                           NA
##
     OccurringDrivers
## 1
```

# 3.5 Using DAGs: Restrictions in the order of mutations as extended posets

#### 3.5.1 AND, OR, XOR relationships

The literature on Oncogenetic trees, CBNs, etc, has used graphs as a way of showing the restrictions in the order in which mutations can accumulate. The meaning of "convergent arrows" in these graphs, however, differs. In Figure 1 of Korsunsky et al. (2014) we are shown a simple diagram that illustrates the three basic different meanings of convergent arrows using two parental nodes. We will illustrate it here with three. Suppose we focus on node "g" in the following figure (we will create it shortly)

```
data(examplesFitnessEffects)
plot(examplesFitnessEffects[["cbn1"]])
```



- In relationships of the type used in Conjunctive Bayesian Networks (CBN) (e.g., Gerstung et al. 2009), we are modeling an AND relationship, also called CMPN by Korsunsky et al. (2014) or monotone relationship by Farahani and Lagergren (2013). If the relationship in the graph is fully respected, then "g" will only appear if all of "c", "d", and "e" are already mutated.
- Semimonotone relationships *sensu* Farahani and Lagergren (2013) or **DMPN** *sensu* Korsunsky et al. (2014) are **OR** relationships: "g" will appear if one or more of "c", "d", or "e" are already mutated.
- XMPN relationships (Korsunsky et al. 2014) are XOR relationships: "g" will be present only if exactly one of "c", "d", or "e" is present.

Note that Oncogenetic trees (Desper et al. 1999; Szabo and Boucher 2008) need not deal with the above distinctions, since the DAGs are trees: no node has more than one incoming connection or more than one parent<sup>8</sup>.

To have a flexible way of specifying all of these restrictions, we will want to be able to say what kind of dependency each child node has on its parents.

#### 3.5.2 Fitness effects

Those DAGs specify dependencies and, as explained in Diaz-Uriarte (2015), it is simple to map them to a simple evolutionary model: any set of mutations that does not conform to the restrictions encoded in the graph will have a fitness of 0. However, we might not want to require absolute compliance with the DAG. This means we

<sup>&</sup>lt;sup>8</sup>OTs and CBNs have some other technical differences about the underlying model they assume, such as the exponential waiting time in CBNs. We will not discuss them here.

might want to allow deviations from the DAG with a corresponding penalization that is, however, not identical to setting fitness to 0 (again, see Diaz-Uriarte 2015). This we can do by being explicit about the fitness effects of the deviations from the restrictions encoded in the DAG. We will use below a column of s for the fitness effect when the restrictions are satisfied and a column of sh when they are not. (See also 3.2 for the details about the meaning of the fitness effects).

That way of specifying fitness effects makes it also trivial to use the model in Hjelm, Höglund, and Lagergren (2006) where all mutations might be allowed to occur, but the presence of some mutations increases the probability of occurrence of other mutations. For example, the values of sh could be all small positive ones (or for mildly deleterious effects, small negative numbers), while the values of s are much larger positive numbers.

#### 3.5.3 Extended posets

In version 1 of this package we used posets in the sense of Beerenwinkel, Eriksson, and Sturmfels (2007) and Gerstung et al. (2009), as explained in section 12.1 and in the help for poset. Here, we continue using two columns, that specify parents and children, but we add columns for the specific values of fitness effects (both s and sh—i.e., fitness effects for what happens when restrictions are and are not satisfied) and for the type of dependency as explained in section 3.5.1.

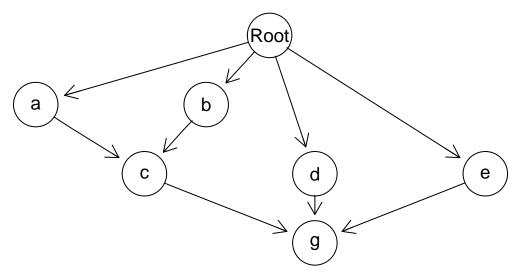
We can now illustrate the specification of different fitness effects using DAGs.

#### 3.5.4 DAGs: A first conjunction (AND) example

(We skip one letter, just to show that names need not be consecutive or have any particular order.)

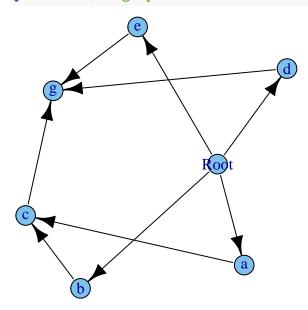
We can get a graphical representation using the default "graphNEL"

```
plot(cbn1)
```



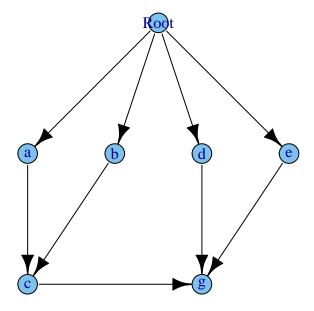
or one using "igraph":

### plot(cbn1, "igraph")



Since we have a parent and children, the reingold.tilford layout is probably the best here, so you might want to use that:

library(igraph) ## to make the reingold.tilford layout available
plot(cbn1, "igraph", layout = layout.reingold.tilford)



And what is the fitness of all genotypes?

```
gfs <- evalAllGenotypes(cbn1, order = FALSE, addwt = TRUE)
gfs[1:15,]
##
      Genotype Fitness
             WT
## 1
                    1.00
## 2
                    1.10
              a
## 3
                    1.10
              b
## 4
                    0.10
              С
## 5
              d
                    1.10
## 6
                    1.10
              е
## 7
              g
                    0.10
## 8
              b
                    1.21
           a,
## 9
              С
                    0.11
           a,
## 10
           a, d
                    1.21
## 11
                    1.21
              е
## 12
                    0.11
           a, g
## 13
           b, c
                    0.11
## 14
           b, d
                    1.21
## 15
           b, e
                    1.21
```

You can verify that for each genotype, if a mutation is present without all of its dependencies present, you get a (1-0.9) multiplier, and you get a (1+0.1) multiplier for all the rest with its direct parents satisfied. For example, genotypes "a", or "b", or "d", or "e" have fitness (1+0.1), genotype "a, b, c" has fitness  $(1+0.1)^3$ , but genotype "a, c" has fitness (1+0.1)(1-0.9) = 0.11.

#### 3.5.5 DAGs: A second conjunction example

Let's try a first attempt at a somewhat more complex example, where the fitness consequences of different genes differ.

If you try this, you'll get an error. There is an error because the "sh" varies within a child, and we do not allow that for a poset-type specification, as it is ambiguous. If you need arbitrary fitness values for arbitrary combinations of genotypes, you can specify them using epistatic effects as in section 3.10 and order effects as in section 3.7.

Why do we need to specify as many "s" and "sh" as there are rows (or a single one, that gets expanded to those many) when the "s" and "sh" are properties of the child node, not of the edges? Because, for ease, we use a data.frame.

We fix the error in our specification. Notice that the "sh" is not set to -1 in these examples. If you want strict compliance with the poset restrictions, you should set sh=-1 or, better yet,  $sh=-\infty$  (see section 3.2.2), but having an sh>-1 will lead to fitnesses that are >0 and, thus, is a way of modeling small deviations from the poset (see discussion in Diaz-Uriarte 2015).

Note that for those nodes that depend only on "Root" the type of dependency is irrelevant.

We could get graphical representations but the figures would be the same as in the example in section 3.5.4, since the structure has not changed, only the numeric values.

What is the fitness of all possible genotypes? Here, order of events *per se* does not matter, beyond that considered in the poset. In other words, the fitness of genotype "a, b, c" is the same no matter how we got to "a, b, c". What matters is whether or not the genes on which each of "a", "b", and "c" depend are present or not (I only show the first 10 genotypes)

```
gcbn2 <- evalAllGenotypes(cbn2, order = FALSE)</pre>
gcbn2[1:10, ]
##
      Genotype Fitness
## 1
                   1.010
              а
## 2
              b
                   1.020
## 3
                   0.100
              С
## 4
              d
                   1.030
## 5
                   1.040
              е
## 6
                   0.050
              g
## 7
           a, b
                   1.030
## 8
           a, c
                   0.101
## 9
           a, d
                   1.040
## 10
                   1.050
           a, e
```

Of course, if we were to look at genotypes but taking into account order of occurrence of mutations, we would see no differences

```
gcbn2o <- evalAllGenotypes(cbn2, order = TRUE, max = 1956)
gcbn2o[1:10, ]
##
      Genotype Fitness
## 1
                  1.010
              a
## 2
                  1.020
              b
                  0.100
## 3
              С
## 4
              d
                  1.030
                  1.040
## 5
              е
## 6
                  0.050
              g
## 7
                  1.030
         a > b
## 8
         a > c
                  0.101
## 9
         a > d
                  1.040
## 10
         a > e
                  1.050
```

(The max = 1956 is there so that we show all the genotypes, even if they are more than 256, the default.)

You can check the output and verify things are as they should. For instance:

```
all.equal(
    gcbn2[c(1:21, 22, 28, 41, 44, 56, 63), "Fitness"],
    c(1.01, 1.02, 0.1, 1.03, 1.04, 0.05,
        1.01 * c(1.02, 0.1, 1.03, 1.04, 0.05),
        1.02 * c(0.10, 1.03, 1.04, 0.05),
        0.1 * c(1.03, 1.04, 0.05),
        1.03 * c(1.04, 0.05),
        1.04 * 0.05,
        1.01 * 1.02 * 1.1,
        1.01 * 0.1 * 0.05,
        1.03 * 1.04 * 0.05,
        1.01 * 1.02 * 1.1 * 0.05,
```

```
1.03 * 1.04 * 1.2 * 0.1, ## notice this

1.01 * 1.02 * 1.03 * 1.04 * 1.1 * 1.2

))
## [1] TRUE
```

A particular one that is important to understand is genotype with mutated genes "c, d, e, g":

```
gcbn2[56, ]
## Genotype Fitness
## 56 c, d, e, g 0.1285
all.equal(gcbn2[56, "Fitness"], 1.03 * 1.04 * 1.2 * 0.10)
## [1] TRUE
```

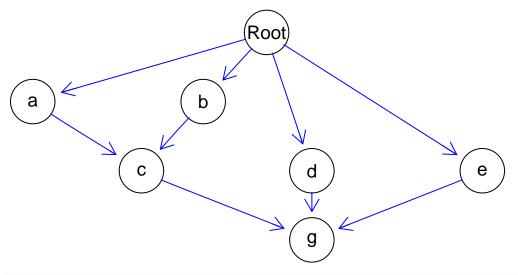
where "g" is taken as if its dependencies are satisfied (as "c", "d", and "e" are present) even when the dependencies of "c" are not satisfied (and that is why the term for "c" is 0.9).

#### 3.5.6 DAGs: A semimonotone or "OR" example

We will reuse the above example, changing the type of relationship:

It looks like this (where edges are shown in blue to denote the semimonotone relationship):

```
plot(smn1)
```



gsmn1 <- evalAllGenotypes(smn1, order = FALSE)</pre>

Having just one parental dependency satisfied is now enough, in contrast to what happened before. For instance:

```
gcbn2[c(8, 12, 22), ]
      Genotype Fitness
## 8
          a, c
                 0.101
## 12
          b, c
                 0.102
## 22 a, b, c
                 1.133
gsmn1[c(8, 12, 22),]
##
      Genotype Fitness
## 8
                 1.111
          a, c
## 12
          b, c
                 1.122
## 22 a, b, c
                 1.133
gcbn2[c(20:21, 28),]
      Genotype Fitness
##
## 20
          d, g 0.05150
## 21
          e, g 0.05200
## 28 a, c, g 0.00505
gsmn1[c(20:21, 28),]
      Genotype Fitness
##
## 20
                 1.236
          d, g
## 21
                 1.248
          e, g
## 28
                 1.333
       a, c, g
```

#### 3.5.7 An "XMPN" or "XOR" example

Again, we reuse the example above, changing the type of relationship:

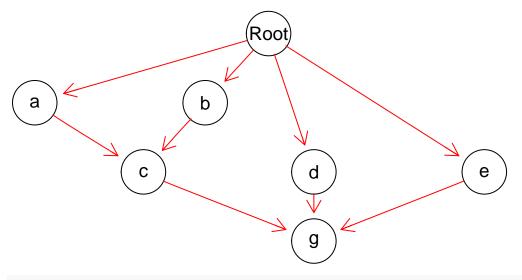
```
x1 <- data.frame(parent = c(rep("Root", 4), "a", "b", "d", "e", "c"),</pre>
```

```
child = c("a", "b", "d", "e", "c", rep("g", 3)),
    s = c(0.01, 0.02, 0.03, 0.04, 0.1, 0.1, rep(0.2, 3)),
    sh = c(rep(0, 4), c(-.9, -.9), rep(-.95, 3)),
    typeDep = "XMPN")

xor1 <- allFitnessEffects(x1)</pre>
```

It looks like this (edges in red to denote the "XOR" relationship):

#### plot(xor1)



```
gxor1 <- evalAllGenotypes(xor1, order = FALSE)</pre>
```

Whenever "c" is present with both "a" and "b", the fitness component for "c" will be (1-0.1). Similarly for "g" (if more than one of "d", "e", or "c" is present, it will show as (1-0.05)). For example:

```
gxor1[c(22, 41), ]
## Genotype Fitness
## 22 a, b, c 0.10302
## 41 d, e, g 0.05356
c(1.01 * 1.02 * 0.1, 1.03 * 1.04 * 0.05)
## [1] 0.10302 0.05356
```

However, having just both "a" and "b" is identical to the case with CBN and the monotone relationship (see sections 3.5.5 and 3.5.6). If you want the joint presence of "a" and "b" to result in different fitness than the product of the individual terms, without considering the presence of "c", you can specify that using general epistatic effects (section 3.10).

We also see a very different pattern compared to CBN (section 3.5.5) here:

```
gxor1[28, ]
## Genotype Fitness
## 28 a, c, g 1.333
```

```
1.01 * 1.1 * 1.2
## [1] 1.333
```

as exactly one of the dependencies for both "c" and "g" are satisfied.

But

```
gxor1[44,]

## Genotype Fitness

## 44 a, b, c, g 0.1236

1.01 * 1.02 * 0.1 * 1.2

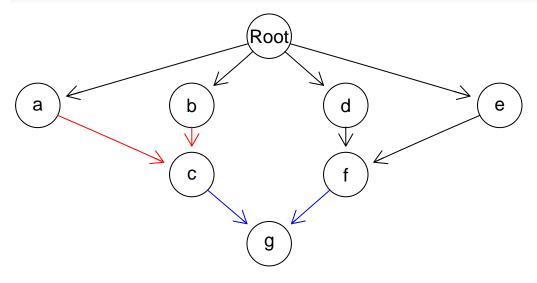
## [1] 0.1236
```

is the result of a 0.1 for "c" (and a 1.2 for "g" that has exactly one of its dependencies satisfied).

#### 3.5.8 Posets: the three types of relationships

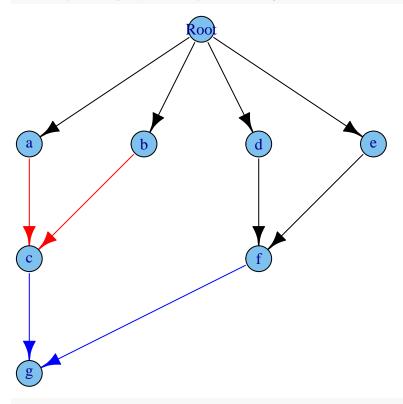
This is how it looks like:

#### plot(fp3)



We can also use "igraph":

#### plot(fp3, "igraph", layout.reingold.tilford)



gfp3 <- evalAllGenotypes(fp3, order = FALSE)</pre>

Let's look at a few:

```
gfp3[c(9, 24, 29, 59, 60, 66, 119, 120, 126, 127),]
##
                  Genotype Fitness
## 9
                      a, c 1.111000
## 24
                      d, f 0.051500
## 29
                   a, b, c 0.103020
## 59
                   c, f, g 0.006500
## 60
                   d, e, f 1.285440
## 66
                a, b, c, f 0.005151
## 119
             c, d, e, f, g 0.167107
## 120
          a, b, c, d, e, f 0.132426
          b, c, d, e, f, g 1.874943
## 127 a, b, c, d, e, f, g 0.172154
c(1.01 * 1.1, 1.03 * .05, 1.01 * 1.02 * 0.1, 0.1 * 0.05 * 1.3,
  1.03 * 1.04 * 1.2, 1.01 * 1.02 * 0.1 * 0.05,
  0.1 * 1.03 * 1.04 * 1.2 * 1.3,
 1.01 * 1.02 * 0.1 * 1.03 * 1.04 * 1.2,
 1.02 * 1.1 * 1.03 * 1.04 * 1.2 * 1.3,
 1.01 * 1.02 * 1.03 * 1.04 * 0.1 * 1.2 * 1.3
## [1] 1.111000 0.051500 0.103020 0.006500 1.285440 0.005151 0.167107
```

#### ## [8] 0.132426 1.874943 0.172154

As before, looking at the order of mutations makes no difference (look at the test directory to see a test that verifies this assertion).

#### 3.6 Modules

As already mentioned, we can think in all the effects of fitness in terms not of individual genes but, rather, modules. This idea is discussed in, for example, Raphael and Vandin (2015), Gerstung et al. (2011): the restrictions encoded in, say, the DAGs can be considered to apply not to genes, but to modules, where each module is a set of genes (and the intersection between modules is the empty set). Modules, then, play the role of a "union operation" over sets of genes. Of course, if we can use modules for the restrictions in the DAGs we should also be able to use them for epistasis and order effects, as we will see later (e.g., 3.7.2).

#### 3.6.1 What does a module provide

Modules can provide very compact ways of specifying relationships when you want to, well, model the existence of modules. For simplicity suppose there is a module, "A", made of genes "a1" and "a2", and a module "B", made of a single gene "b1". Module "B" can mutate if module "A" is mutated, but mutating both "a1" and "a2" provides no additional fitness advantage compared to mutating only a single one of them. We can specify this as:

```
s < -0.2
sboth <- (1/(1 + s)) - 1
m0 <- allFitnessEffects(data.frame(</pre>
    parent = c("Root", "Root", "a1", "a2"),
    child = c("a1", "a2", "b", "b"),
    s = s
    sh = -1,
    typeDep = "OR"),
                         epistasis = c("a1:a2" = sboth))
evalAllGenotypes(m0, order = FALSE, addwt = TRUE)
##
      Genotype Fitness
             WT
                   1.00
## 1
## 2
             a1
                   1.20
             a2
## 3
                   1.20
## 4
             b
                   0.00
## 5
        a1, a2
                   1.20
## 6
         a1, b
                   1.44
## 7
         a2, b
                   1.44
## 8 a1, a2, b
                   1.44
```

Note that we need to add an epistasis term, with value "sboth" to capture the idea of "mutating both"al" and "a2" provides no additional fitness advantage compared to mutating only a single one of them"; see details in section 3.10.

Now, specify it using modules:

```
s < -0.2
m1 <- allFitnessEffects(data.frame(</pre>
    parent = c("Root", "A"),
    child = c("A", "B"),
    s = s
    sh = -1,
    typeDep = "OR"),
                          geneToModule = c("Root" = "Root",
                                            "A" = "a1, a2",
                                            "B" = "b1"))
evalAllGenotypes(m1, order = FALSE, addwt = TRUE)
##
       Genotype Fitness
              WT
## 1
                    1.00
## 2
                    1.20
              a1
## 3
              a2
                    1.20
                    0.00
## 4
              b1
                    1.20
## 5
         a1, a2
## 6
         a1, b1
                    1.44
## 7
         a2, b1
                    1.44
## 8 a1, a2, b1
                    1.44
```

This captures the ideas directly. The typing savings here are small, but they can be large with modules with many genes.

#### 3.6.2 Specifying modules

How do you specify modules? The general procedure is simple: you pass a vector that makes explicit the mapping from modules to sets of genes. We just saw an example. There are several additional examples such as 3.6.3, 3.7.2, 3.10.4.

It is important to note that, once you specify modules, we expect all of the relationships (except those that involve the non interacting genes) to be specified as modules. Thus, all elements of the epistasis, posets (the DAGs) and order effects components should be specified in terms of modules. But you can, of course, specify a module as containing a single gene (and a single gene with the same name as the module).

What about the "Root" node? If you use a "restriction table", that restriction table (that DAG) must have a node named "Root" and in the mapping of genes to module there **must** be a first entry that has a module and gene named "Root", as we saw above with <code>geneToModule = c("Root" = "Root", ....</code> We force you to do this to be explicit about the "Root" node. This is not needed (thought it does not hurt) with other fitness specifications. For instance, if we have a model with two modules,

one of them with two genes (see details in section 3.11) we do not need to pass a "Root" as in

```
fnme <- allFitnessEffects(epistasis = c("A" = 0.1,
                                          "B" = 0.2),
                           geneToModule = c("A" = "a1, a2",
                                              "B" = "b1"))
evalAllGenotypes(fnme, order = FALSE, addwt = TRUE)
       Genotype Fitness
##
## 1
             WT
                    1.00
## 2
              a1
                    1.10
## 3
              a2
                    1.10
                    1.20
## 4
             b1
## 5
         a1, a2
                    1.10
## 6
         a1, b1
                    1.32
## 7
         a2, b1
                    1.32
## 8 a1, a2, b1
                    1.32
```

but it is also OK to have a "Root" in the geneToModule:

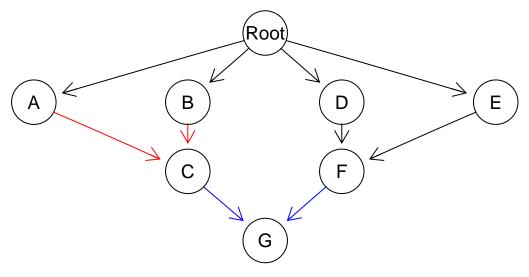
```
fnme2 <- allFitnessEffects(epistasis = c("A" = 0.1,</pre>
                                           "B" = 0.2),
                            geneToModule = c(
                                "Root" = "Root",
                                "A" = "a1, a2",
                                "B" = "b1"))
evalAllGenotypes(fnme, order = FALSE, addwt = TRUE)
##
       Genotype Fitness
## 1
              WT
                    1.00
## 2
              a1
                    1.10
## 3
              a2
                    1.10
## 4
              b1
                    1.20
## 5
         a1, a2
                    1.10
## 6
         a1, b1
                    1.32
## 7
         a2, b1
                    1.32
## 8 a1, a2, b1
                    1.32
```

## 3.6.3 Modules and posets again: the three types of relationships and modules

We use the same specification of poset, but add modules. To keep it manageable, we only add a few genes for some modules, and have some modules with a single gene. Beware that the number of genotypes is starting to grow quite fast, though. We capitalize to differentiate modules (capital letters) from genes (lowercase with a number), but this is not needed.

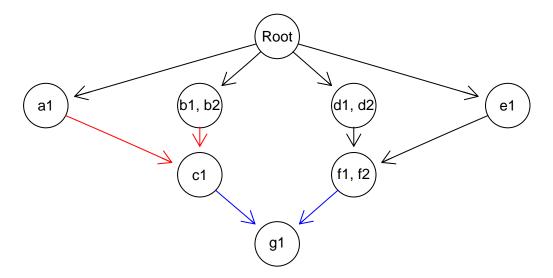
By default, plotting shows the modules:

#### plot(fp4m)

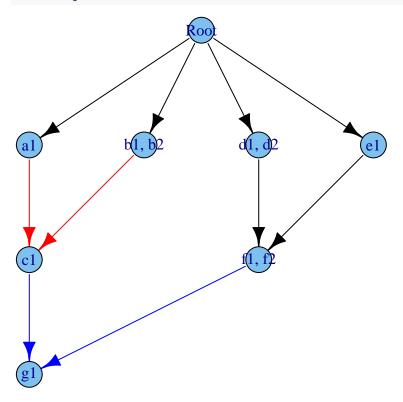


but we can show the gene names instead of the module names:

```
plot(fp4m, expandModules = TRUE)
```



or



We obtain the fitness of all genotypes in the usual way:

```
gfp4 <- evalAllGenotypes(fp4m, order = FALSE, max = 1024)</pre>
```

Let's look at a few of those:

```
## 12
                        a1, b2
                                1.0302
## 20
                        b1, b2
                                1.0200
## 21
                        b1, c1
                                1.1220
## 40
                        c1, g1
                                0.1300
                        d1, d2
## 41
                                1.0300
## 46
                        d2, e1
                                1.0712
                        e1, f1
## 50
                                0.0520
## 55
                        f2, g1
                                0.0650
## 64
                    a1, b2, c1
                                0.1030
## 92
                    b1, b2, c1
                                1.1220
## 155
                    c1, f2, g1
                                0.0065
                    d1, d2, f1
## 157
                                0.0515
## 163
                    d1, f1, f2
                                0.0515
               d1, d2, e1, f2
## 372
                                1.2854
## 632
           d1, d2, e1, f1, f2
                                1.2854
## 828 b2, c1, d1, e1, f2, g1
                                1.8749
c(1.01 * 1.02, 1.02, 1.02 * 1.1, 0.1 * 1.3, 1.03,
  1.03 * 1.04, 1.04 * 0.05, 0.05 * 1.3,
  1.01 * 1.02 * 0.1, 1.02 * 1.1, 0.1 * 0.05 * 1.3,
  1.03 * 0.05, 1.03 * 0.05, 1.03 * 1.04 * 1.2, 1.03 * 1.04 * 1.2,
  1.02 * 1.1 * 1.03 * 1.04 * 1.2 * 1.3
    [1] 1.0302 1.0200 1.1220 0.1300 1.0300 1.0712 0.0520 0.0650 0.1030
## [10] 1.1220 0.0065 0.0515 0.0515 1.2854 1.2854 1.8749
```

#### 3.7 Order effects

As explained in the introduction (section 1), by order effects we mean a phenomenon such as the one shown empirically by Ortmann et al. (2015): the fitness of a double mutant "A", "B" is different depending on whether "A" was acquired before "B" or "B" before "A". This, of course, can be generalized to more than two genes.

Note that these order effects are different from the order restrictions discussed in section 3.5. In there we might say that acquiring "B" depends or is facilitated by having "A" mutated (and, unless we allowed for multiple mutations, having "A" mutated means having "A" mutated before "B"). However, once you have the genotype "A, B", its fitness does not depend on the order in which "A" and "B" appeared.

#### 3.7.1 Order effects: three-gene orders

Consider this case, where three specific three-gene orders and two two-gene orders (one of them a subset of one of the three) lead to different fitness compared to the wild-type. We add also modules, to show its usage (but just limit ourselves to using one gene per module here).

Order effects are specified using a x > y, that means that that order effect is satisfied when module x is mutated before module y.

```
o3 <- allFitnessEffects(orderEffects = c(
                              "F > D > M" = -0.3,
                              "D > F > M" = 0.4,
                              "D > M > F" = 0.2,
                              "D > M"
                                           = 0.1,
                              "M > D"
                                          = 0.5),
                         geneToModule =
                              c("M" = "m",
                                "F" = "f",
                                "D" = "d")
(ag <- evalAllGenotypes(o3, addwt = TRUE, order = TRUE))
##
       Genotype Fitness
## 1
             WT
                    1.00
## 2
                    1.00
              d
              f
## 3
                    1.00
## 4
                    1.00
              m
## 5
          d > f
                    1.00
## 6
          d > m
                    1.10
                    1.00
## 7
          f > d
## 8
          f > m
                    1.00
## 9
          m > d
                    1.50
          m > f
## 10
                    1.00
## 11 d > f > m
                    1.54
## 12 d > m > f
                    1.32
## 13 f > d > m
                    0.77
## 14 f > m > d
                    1.50
## 15 m > d > f
                    1.50
## 16 m > f > d
                    1.50
```

(The meaning of the notation in the output table is as follows: "WT" denotes the wild-type, or non-mutated clone. The notation x > y means that a mutation in "x" happened before a mutation in "y". A genotype  $x > y \_ z$  means that a mutation in "x" happened before a mutation in "y"; there is also a mutation in "z", but that is a gene for which order does not matter).

The values for the first nine genotypes come directly from the fitness specifications. The 10th genotype matches D > F > M (= (1 + 0.4)) but also D > M ((1 + 0.1)). The 11th matches D > M > F and D > M. The 12th matches F > D > M but also D > M. Etc.

#### 3.7.2 Order effects and modules with multiple genes

Consider the following case:

There are four genes, d1, d2, f1, f2, where each d belongs to module D and each f belongs to module F.

What to expect for cases such as d1 > f1 or f1 > d1 is clear, as shown in

```
ag[5:16,]
##
      Genotype Fitness
       d1 > d2
## 5
## 6
       d1 > f1
                    1.4
## 7
       d1 > f2
                    1.4
## 8
       d2 > d1
                    1.0
## 9
       d2 > f1
                    1.4
## 10
       d2 > f2
                    1.4
## 11
       f1 > d1
                    0.7
## 12
       f1 > d2
                    0.7
## 13
       f1 > f2
                    1.0
                    0.7
## 14
       f2 > d1
## 15
       f2 > d2
                    0.7
## 16
      f2 > f1
                    1.0
```

Likewise, cases such as d1 > d2 > f1 or f2 > f1 > d1 are clear, because in terms of modules they map to \$D > F\$ or F > D: the observed order of mutation d1 > d2 > f1 means that module D was mutated first and module F was mutated second. Similar for d1 > f2 or f1 > d1 > d2: those map to D > F and F > D. We can see the fitness of those four case in:

and they correspond to the values of those order effects, where F > D = (1 - 0.3) and D > F = (1 + 0.4):

```
ag[c(17, 39, 19, 29), "Fitness"] == c(1.4, 0.7, 1.4, 0.7)
## [1] TRUE TRUE TRUE
```

What if we match several patterns? For example, d1 > f1 > d2 > f2 and d1 > f1 > f2 > d2? The first maps to D > F > D > F and the second to D > F > D. But since we are concerned with which one happened first and which happened second we should expect those two to correspond to the same fitness, that of pattern D > F, as is the case:

More generally, that applies to all the patterns that start with one of the "d" genes:

```
all(ag[41:52, "Fitness"] == 1.4)
## [1] TRUE
```

Similar arguments apply to the opposite pattern, F > D, which apply to all the possible gene mutation orders that start with one of the "f" genes. For example:

```
all(ag[53:64, "Fitness"] == 0.7)
## [1] TRUE
```

#### 3.7.3 Order and modules with 325 genotypes

We can of course have more than two genes per module. This just repeats the above, with five genes (there are 325 genotypes, and that is why we pass the "max" argument to evalAllGenotypes, to allow for more than the default 256).

We can verify that any combination that starts with a "d" gene and then contains at least one "f" gene will have a fitness of 1 + 0.4. And any combination that starts with an "f" gene and contains at least one "d" genes will have a fitness of 1 - 0.3. All other genotypes have a fitness of 1:

```
all(ag2[grep("^d.*f.*", ag2[, 1]), "Fitness"] == 1.4)
## [1] TRUE
all(ag2[grep("^f.*d.*", ag2[, 1]), "Fitness"] == 0.7)
```

```
## [1] TRUE
oe <- c(grep("^f.*d.*", ag2[, 1]), grep("^d.*f.*", ag2[, 1]))
all(ag2[-oe, "Fitness"] == 1)
## [1] TRUE</pre>
```

#### 3.7.4 Order effects and genes without interactions

We will now look at both order effects and interactions. To make things more interesting, we name genes so that the ordered names do split nicely between those with and those without order effects (this, thus, also serves as a test of messy orders of names).

```
foi1 <- allFitnessEffects(
    orderEffects = c("D>B" = -0.2, "B > D" = 0.3),
    noIntGenes = c("A" = 0.05, "C" = -.2, "E" = .1))
```

You can get a verbose view of what the gene names and modules are (and their automatically created numeric codes) by:

```
foi1[c("geneModule", "long.geneNoInt")]
## $geneModule
     Gene Module GeneNumID ModuleNumID
## 1 Root
            Root
## 2
        В
                В
                          1
                                       1
## 3
        D
                D
                          2
                                       2
##
## $long.geneNoInt
     Gene GeneNumID
##
## A
        Α
                   3
                     0.05
## C
        С
                   4 - 0.20
## E
                   5 0.10
```

We can get the fitness of all genotypes (we set max = 325 because that is the number of possible genotypes):

```
agoi1 <- evalAllGenotypes(foi1, max = 325, order = TRUE)
head(agoi1)
##
     Genotype Fitness
## 1
            В
                  1.00
## 2
            D
                  1.00
## 3
            Α
                  1.05
## 4
            C
                  0.80
## 5
            Ε
                  1.10
## 6
        B > D
                  1.30
```

Now:

```
rn <- 1:nrow(agoi1)
names(rn) <- agoi1[, 1]

agoi1[rn[LETTERS[1:5]], "Fitness"] == c(1.05, 1, 0.8, 1, 1.1)
## [1] TRUE TRUE TRUE TRUE</pre>
```

According to the fitness effects we have specified, we also know that any genotype with only two mutations, one of which is either "A", "C" "E" and the other is "B" or "D" will have the fitness corresponding to "A", "C" or "E", respectively:

```
agoi1[grep("^A > [BD]$", names(rn)), "Fitness"] == 1.05
## [1] TRUE TRUE
agoi1[grep("^C > [BD]$", names(rn)), "Fitness"] == 0.8
## [1] TRUE TRUE
agoi1[grep("^E > [BD]$", names(rn)), "Fitness"] == 1.1
## [1] TRUE TRUE
agoi1[grep("^[BD] > A$", names(rn)), "Fitness"] == 1.05
## [1] TRUE TRUE
agoi1[grep("^[BD] > C$", names(rn)), "Fitness"] == 0.8
## [1] TRUE TRUE
agoi1[grep("^[BD] > E$", names(rn)), "Fitness"] == 1.1
## [1] TRUE TRUE
```

We will not be playing many additional games with regular expressions, but let us check those that start with "D" and have all the other mutations, which occupy rows 230 to 253; fitness should be equal (within numerical error, because of floating point arithmetic) to the order effect of "D" before "B" times the other effects (1-0.3)\*1.05\*0.8\*1.1 = 0.7392

and that will also be the value of any genotype with the five mutations where "D" comes before "B" such as those in rows 260 to 265, 277, or 322 and 323, but it will be equal to (1+0.3)\*1.05\*0.8\*1.1 = 1.2012 in those where "B" comes before "D". Analogous arguments apply to four, three, and two mutation genotypes.

## 3.8 Synthetic viability

Synthetic viability and synthetic lethality (e.g., Ashworth, Lord, and Reis-Filho 2011; Hartman, Garvik, and Hartwell 2001) are just special cases of epistasis (section 3.10) but we deal with them here separately.

#### 3.8.1 A simple synthetic viability example

A simple and extreme example of synthetic viability is shown in the following table, where the joint mutant has fitness larger than the wild type, but each single mutant is lethal.

A	В	Fitness
wt	wt	1
wt	$\mathbf{M}$	0
Μ	wt	0
Μ	Μ	(1 + s)

where "wt" denotes wild type and "M" denotes mutant.

We can specify this (setting s = 0.2) as (I play around with spaces, to show there is a certain flexibility with them):

Now, let's look at all the genotypes (we use "addwt" to also get the wt, which by decree has fitness of 1), and disregard order:

```
(asv <- evalAllGenotypes(sv, order = FALSE, addwt = TRUE))
## Genotype Fitness
## 1  WT   1.0
## 2   A   0.0
## 3   B   0.0
## 4   A, B   1.2</pre>
```

Asking the program to consider the order of mutations of course makes no difference:

```
evalAllGenotypes(sv, order = TRUE, addwt = TRUE)
##
     Genotype Fitness
## 1
           WT
                   1.0
## 2
             Α
                   0.0
             В
                   0.0
## 3
## 4
        A > B
                   1.2
        B > A
                   1.2
```

Another example of synthetic viability is shown in section 5.2.2.

Of course, if multiple simultaneous mutations are not possible in the simulations, it is not possible to go from the wildtype to the double mutant in this model where the single mutants are not viable.

#### 3.8.2 Synthetic viability using Bozic model

If we were to use the above specification with Bozic's models, we might not get what we think we should get:

```
evalAllGenotypes(sv, order = FALSE, addwt = TRUE, model = "Bozic")
## Genotype Death_rate
## 1 WT 1.0
## 2 A 2.0
## 3 B 2.0
## 4 A, B 0.8
```

What gives here? The simulation code would alert you of this (see section 3.4) in this particular case because there are "-1", which might indicate that this is not what you want. The problem is that you probably want the Death rate to be infinity (the birth rate was 0, so no clone viability, when we used birth rates —section 3.2.2).

Let us say so explicitly:

```
s < -0.2
svB <- allFitnessEffects(epistasis = c("-A : B" = -Inf,</pre>
                                         "A : -B" = -Inf.
                                         "A:B" = s)
evalAllGenotypes(svB, order = FALSE, addwt = TRUE, model = "Bozic")
##
     Genotype Death rate
           WT
## 1
                      1.0
## 2
             Α
                      Inf
             В
                      Inf
## 3
## 4
         A, B
                      0.8
```

Likewise, values of s larger than one have no effect beyond setting s = 1 (a single term of (1-1) will drive the product to 0, and as we cannot allow negative death rates negative values are set to 0):

```
s <- 1
svB1 <- allFitnessEffects(epistasis = c("-A : B" = -Inf,</pre>
                                          "A : -B" = -Inf,
                                          "A:B" = s)
evalAllGenotypes(svB1, order = FALSE, addwt = TRUE, model = "Bozic")
##
     Genotype Death_rate
## 1
            WT
                         1
## 2
             Α
                       Tnf
## 3
             В
                       Inf
## 4
         A, B
                         0
s <- 3
```

```
svB3 <- allFitnessEffects(epistasis = c("-A : B" = -Inf,</pre>
                                          "A : -B" = -Inf,
                                          "A:B" = s)
evalAllGenotypes(svB3, order = FALSE, addwt = TRUE, model = "Bozic")
     Genotype Death rate
## 1
           WT
## 2
             Α
                      Inf
## 3
             В
                      Inf
## 4
         A, B
                        0
```

Of course, death rates of 0.0 are likely to lead to trouble down the road, when we actually conduct simulations (see section 3.4).

#### 3.8.3 Synthetic viability, non-zero fitness, and modules

This is a slightly more elaborate case, where there is one module and the single mutants have different fitness between themselves, which is non-zero. Without the modules, this is the same as in Misra et al. Misra, Szczurek, and Vingron (2014), Figure 1b, which we go over in section 5.2.

A	В	Fitness
wt	wt	1
wt	M	$1+s_b$
Μ	wt	$1+s_a$
Μ	M	$1 + s_{ab}$

where  $s_a, s_b < 0$  but  $s_{ab} > 0$ .

```
sa < -0.1
sb < -0.2
sab < -0.25
sv2 <- allFitnessEffects(epistasis = c("-A : B" = sb,</pre>
                               "A : -B" = sa,
                               "A:B" = sab),
                           geneToModule = c(
                               "A" = "a1, a2",
                               "B" = "b"))
evalAllGenotypes(sv2, order = FALSE, addwt = TRUE)
##
      Genotype Fitness
## 1
             WT
                   1.00
## 2
             a1
                   0.90
## 3
             a2
                   0.90
## 4
              b
                   0.80
                   0.90
## 5
        a1, a2
```

```
## 6 a1, b 1.25
## 7 a2, b 1.25
## 8 a1, a2, b 1.25
```

And if we look at order, of course it makes no difference:

```
evalAllGenotypes(sv2, order = TRUE, addwt = TRUE)
##
         Genotype Fitness
## 1
                WT
                      1.00
## 2
                      0.90
                a1
## 3
                a2
                      0.90
## 4
                 b
                      0.80
## 5
                      0.90
          a1 > a2
           a1 > b
## 6
                      1.25
## 7
          a2 > a1
                      0.90
                      1.25
## 8
           a2 > b
## 9
           b > a1
                      1.25
## 10
           b > a2
                      1.25
## 11 a1 > a2 > b
                      1.25
## 12 a1 > b > a2
                      1.25
## 13 a2 > a1 > b
                      1.25
## 14 a2 > b > a1
                      1.25
## 15 b > a1 > a2
                      1.25
## 16 b > a2 > a1
                      1.25
```

## 3.9 Synthetic mortality or synthetic lethality

In contrast to section 3.8, here the joint mutant has decreased viability:

A	В	Fitness
wt	wt	1
wt	${ m M}$	$1+s_b$
M	wt	$1+s_a$
M	M	$1 + s_{ab}$

where  $s_a, s_b > 0$  but  $s_{ab} < 0$ .

```
## 1 WT 1.0
## 2 A 1.1
## 3 B 1.2
## 4 A, B 0.2
```

And if we look at order, of course it makes no difference:

```
evalAllGenotypes(sm1, order = TRUE, addwt = TRUE)
##
     Genotype Fitness
## 1
           WT
## 2
            Α
                   1.1
## 3
            В
                   1.2
## 4
        A > B
                   0.2
## 5
        B > A
                   0.2
```

## 3.10 Epistasis

#### 3.10.1 Epistasis: two alternative specifications

We want the following mapping of genotypes to fitness:

A	В	Fitness
wt	wt	1
wt	M	$1+s_b$
Μ	$\mathbf{wt}$	$1+s_a$
M	M	$1 + s_{ab}$

Suppose that the actual numerical values are  $s_a = 0.2, s_b = 0.3, s_{ab} = 0.7$ .

We specify the above as follows:

```
sa <- 0.2
sb <- 0.3
sab <- 0.7
e2 <- allFitnessEffects(epistasis =</pre>
                              c("A: -B" = sa,
                                "-A:B" = sb,
                                "A : B" = sab)
evalAllGenotypes(e2, order = FALSE, addwt = TRUE)
##
     Genotype Fitness
           WT
## 1
                   1.0
## 2
             Α
                   1.2
## 3
             В
                   1.3
## 4
                   1.7
         A, B
```

That uses the "-" specification, so we explicitly exclude some patterns: with "A:-B" we say "A when there is no B".

But we can also use a specification where we do not use the "-". That requires a different numerical value of the interaction, because now, as we are rewriting the interaction term as genotype "A is mutant, B is mutant" the double mutant will incorporate the effects of "A mutant", "B mutant" and "both A and B mutants". We can define a new  $s_2$  that satisfies  $(1 + s_{ab}) = (1 + s_a)(1 + s_b)(1 + s_2)$  so  $(1 + s_2) = (1 + s_{ab})/((1 + s_a)(1 + s_b))$  and therefore specify as:

```
s2 \leftarrow ((1 + sab)/((1 + sa) * (1 + sb))) - 1
e3 <- allFitnessEffects(epistasis =
                              c("A" = sa,
                                 "B" = sb,
                                "A : B" = s2))
evalAllGenotypes(e3, order = FALSE, addwt = TRUE)
     Genotype Fitness
## 1
            WT
                   1.0
## 2
             Α
                   1.2
## 3
             В
                   1.3
                   1.7
## 4
         A, B
```

Note that this is the way you would specify effects with FFPopsim (Zanini and Neher 2012). Whether this specification or the previous one with "-" is simpler will depend on the model. For synthetic mortality and viability, I think the one using "-" is simpler to map genotype tables to fitness effects. See also section 3.10.2 and 3.10.3 and the example in section 5.4.2.

Finally, note that we can also specify some of these effects by combining the graph and the epistasis, as shown in section 5.2.1 or 5.4.2.

#### 3.10.2 Epistasis with three genes and two alternative specifications

Suppose we have

A	В	С	Fitness
$\overline{\mathrm{M}}$	wt	wt	$1+s_a$
wt	M	wt	$1+s_b$
wt	wt	M	$1+s_c$
Μ	M	wt	$1+s_{ab}$
wt	M	M	$1+s_{bc}$
Μ	wt	M	$(1+s_a)(1+s_c)$
Μ	Μ	Μ	$1 + s_{abc}$

where missing rows have a fitness of 1 (they have been deleted for conciseness). Note

that the mutant for exactly A and C has a fitness that is the product of the individual terms (so there is no epistasis in that case).

```
sa <- 0.1
sb <- 0.15
sc <- 0.2
sab <- 0.3
sbc < -0.25
sabc <- 0.4
sac \leftarrow (1 + sa) * (1 + sc) - 1
E3A <- allFitnessEffects(epistasis =
                              c("A:-B:-C" = sa,
                                "-A:B:-C" = sb,
                                "-A:-B:C" = sc,
                                "A:B:-C" = sab,
                                "-A:B:C" = sbc,
                                "A:-B:C" = sac,
                                "A : B : C" = sabc)
evalAllGenotypes(E3A, order = FALSE, addwt = FALSE)
##
     Genotype Fitness
## 1
            Α
                  1.10
## 2
            В
                  1.15
            С
## 3
                  1.20
## 4
         A, B
                  1.30
         A, C
                  1.32
## 5
## 6
         B, C
                  0.75
## 7
     A, B, C
                  1.40
```

We needed to pass the  $s_{ac}$  coefficient explicitly, even if it that term was just the product. We can try to avoid using the "-", however (but we will need to do other calculations). For simplicity, I use capital "S" in what follows where the letters differ from the previous specification:

```
E3B <- allFitnessEffects(epistasis =
                               c("A" = sa,
                                 "B" = sb.
                                 "C" = sc,
                                 "A:B" = Sab,
                                 "B:C" = Sbc,
                                 ## "A:C" = sac, ## not needed now
                                 "A : B : C" = Sabc)
evalAllGenotypes(E3B, order = FALSE, addwt = FALSE)
##
     Genotype Fitness
## 1
            Α
                  1.10
## 2
            В
                  1.15
## 3
            C
                  1.20
## 4
         A, B
                  1.30
## 5
                  1.32
         A, C
## 6
         B, C
                  0.75
                  1.40
## 7
      A, B, C
```

The above two are, of course, identical:

```
all(evalAllGenotypes(E3A, order = FALSE, addwt = FALSE) ==
    evalAllGenotypes(E3B, order = FALSE, addwt = FALSE))
## [1] TRUE
```

We avoid specifying the "A:C", as it just follows from the individual "A" and "C" terms, but given a specified genotype table, we need to do a little bit of addition and multiplication to get the coefficients.

#### 3.10.3 Why can we specify some effects with a "-"?

Let's suppose we want to specify the synthetic viability example seen before:

A	В	Fitness
wt	wt	1
wt	$\mathbf{M}$	0
M	wt	0
Μ	Μ	(1 + s)

where "wt" denotes wild type and "M" denotes mutant.

If you want to directly map the above table to the fitness table for the program, to specify the genotype "A is wt, B is a mutant" you can specify it as "-A,B", not just as "B". Why? Because just the presence of a "B" is also compatible with genotype "A is mutant and B is mutant". If you use "-" you are explicitly saying what should not be there so that "-A,B" is NOT compatible with "A, B". Otherwise, you need

to carefully add coefficients. Depending on what you are trying to model, different specifications might be simpler. See the examples in section 3.10.1 and 3.10.2. You have both options.

#### 3.10.4 Epistasis: modules

There is nothing conceptually new, but we will show an example here:

```
sa < -0.2
sb <- 0.3
sab <- 0.7
em <- allFitnessEffects(epistasis =</pre>
                              c("A: -B" = sa,
                                "-A:B" = sb,
                                "A : B" = sab),
                          geneToModule = c("A" = "a1, a2",
                                            "B" = "b1, b2")
evalAllGenotypes(em, order = FALSE, addwt = TRUE)
##
             Genotype Fitness
## 1
                   WT
                           1.0
## 2
                           1.2
                   a1
## 3
                   a2
                           1.2
                           1.3
## 4
                   b1
## 5
                   b2
                           1.3
                           1.2
## 6
               a1, a2
               a1, b1
                           1.7
## 7
## 8
               a1, b2
                           1.7
## 9
               a2, b1
                           1.7
## 10
               a2, b2
                           1.7
## 11
               b1, b2
                           1.3
## 12
          a1, a2, b1
                           1.7
## 13
          a1, a2, b2
                           1.7
          a1, b1, b2
                           1.7
## 14
## 15
          a2, b1, b2
                           1.7
## 16 a1, a2, b1, b2
                           1.7
```

Of course, we can do the same thing without using the "-", as in section 3.10.1:

```
"B" = "b1, b2")
evalAllGenotypes(em2, order = FALSE, addwt = TRUE)
##
             Genotype Fitness
## 1
                    WT
                           1.0
## 2
                    a1
                           1.2
## 3
                           1.2
                    a2
## 4
                    b1
                           1.3
## 5
                   b2
                           1.3
## 6
               a1, a2
                           1.2
## 7
               a1, b1
                           1.7
                           1.7
## 8
               a1, b2
## 9
               a2, b1
                           1.7
                           1.7
## 10
               a2, b2
## 11
               b1, b2
                           1.3
                           1.7
## 12
           a1, a2, b1
## 13
           a1, a2, b2
                           1.7
## 14
           a1, b1, b2
                           1.7
           a2, b1, b2
                           1.7
## 15
## 16 a1, a2, b1, b2
                           1.7
```

#### 3.11 I do not want epistasis, but I want modules!

Sometimes you might want something like having several modules, say "A" and "B", each with a number of genes, but with "A" and "B" showing no interaction.

It is a terminological issue whether we should allow noIntGenes (no interaction genes), as explained in section 3.3 to actually be modules. The reasoning for not allowing them is that the situation depicted above (several genes in module A, for example) actually is one of interaction: the members of "A" are combined using an "OR" operator (i.e., the fitness consequences of having one or more genes of A mutated are the same), not just simply multiplying their fitness; similarly for "B". This is why no interaction genes also mean no modules allowed.

So how do you get what you want in this case? Enter the names of the modules in the epistasis component but have no term for ":" (the colon). Let's see an example:

```
## 2
                        a1
                               1.10
## 3
                        a2
                               1.10
## 4
                        b1
                               1.20
## 5
                        b2
                               1.20
## 6
                        b3
                               1.20
## 7
                    a1, a2
                               1.10
## 8
                    a1, b1
                               1.32
## 9
                    a1, b2
                               1.32
## 10
                    a1, b3
                               1.32
## 11
                    a2, b1
                               1.32
## 12
                    a2, b2
                               1.32
## 13
                   a2, b3
                               1.32
## 14
                   b1, b2
                               1.20
## 15
                   b1, b3
                               1.20
## 16
                   b2, b3
                               1.20
## 17
               a1, a2, b1
                               1.32
## 18
               a1, a2, b2
                               1.32
## 19
               a1, a2, b3
                               1.32
## 20
               a1, b1, b2
                               1.32
## 21
               a1, b1, b3
                               1.32
## 22
               a1, b2, b3
                               1.32
## 23
               a2, b1, b2
                               1.32
## 24
               a2, b1, b3
                               1.32
## 25
               a2, b2, b3
                               1.32
               b1, b2, b3
## 26
                               1.20
## 27
           a1, a2, b1, b2
                               1.32
## 28
           a1, a2, b1, b3
                               1.32
## 29
           a1, a2, b2, b3
                               1.32
## 30
           a1, b1, b2, b3
                               1.32
## 31
           a2, b1, b2, b3
                               1.32
## 32 a1, a2, b1, b2, b3
                               1.32
```

In previous versions these was possible using the longer, still accepted way of specifying a : with a value of 0, but this is no longer needed:

```
fnme <- allFitnessEffects(epistasis = c("A" = 0.1,</pre>
                                           "B" = 0.2,
                                           "A : B" = 0.0),
                            geneToModule = c("A" = "a1, a2",
                                              "B" = "b1, b2, b3"))
evalAllGenotypes(fnme, order = FALSE, addwt = TRUE)
##
                 Genotype Fitness
## 1
                       WT
                              1.00
## 2
                       a1
                              1.10
## 3
                       a2
                              1.10
```

```
## 4
                        b1
                               1.20
## 5
                        b2
                               1.20
## 6
                        b3
                               1.20
## 7
                    a1, a2
                               1.10
## 8
                    a1, b1
                               1.32
## 9
                    a1, b2
                               1.32
                    a1, b3
                               1.32
## 10
## 11
                    a2, b1
                               1.32
## 12
                    a2, b2
                               1.32
## 13
                    a2, b3
                               1.32
## 14
                    b1, b2
                               1.20
                    b1, b3
## 15
                               1.20
## 16
                    b2, b3
                               1.20
               a1, a2, b1
                               1.32
## 17
## 18
               a1, a2, b2
                               1.32
## 19
               a1, a2, b3
                               1.32
## 20
               a1, b1, b2
                               1.32
## 21
               a1, b1, b3
                               1.32
## 22
               a1, b2, b3
                               1.32
## 23
               a2, b1, b2
                               1.32
## 24
               a2, b1, b3
                               1.32
## 25
               a2, b2, b3
                               1.32
                               1.20
## 26
               b1, b2, b3
## 27
           a1, a2, b1, b2
                               1.32
## 28
           a1, a2, b1, b3
                               1.32
           a1, a2, b2, b3
## 29
                               1.32
## 30
           a1, b1, b2, b3
                               1.32
           a2, b1, b2, b3
## 31
                               1.32
## 32 a1, a2, b1, b2, b3
                               1.32
```

This can, of course, be extended to more modules.

# 3.12 A longer example: Poset, epistasis, synthetic mortality and viability, order effects and genes without interactions, with some modules

We will now put together a complex example. We will use the poset from section 3.6.3 but will also add:

- Order effects that involve genes in the poset. In this case, if C happens before F, fitness decreases by 1-0.1. If it happens the other way around, there is no effect on fitness beyond their individual contributions.
- Order effects that involve two new modules, "H" and "I" (with genes "h1, h2" and "i1", respectively), so that if H happens before I fitness increases by 1+0.12.

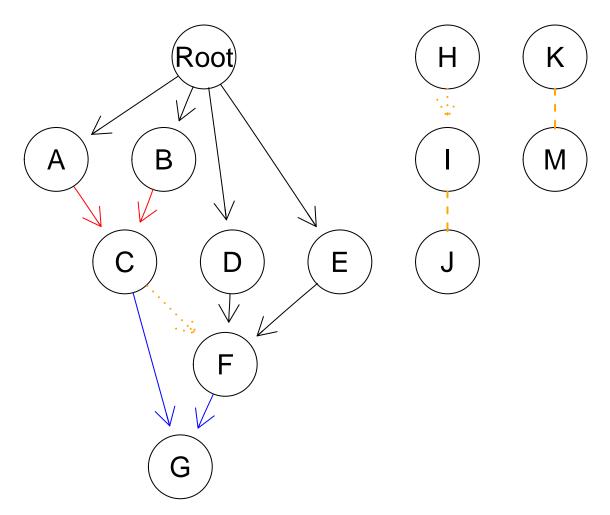
- Synthetic mortality between modules "I" (already present in the epistatic interaction) and "J" (with genes "j1" and "j2"): the joint presence of these modules leads to cell death (fitness of 0).
- Synthetic viability between modules "K" and "M" (with genes "k1", "k2" and "m1", respectively), so that their joint presence is viable but adds nothing to fitness (i.e., mutation of both has fitness 1), whereas each single mutant has a fitness of 1-0.5.
- A set of 5 driver genes  $(n1, \ldots, n5)$  with fitness that comes from an exponential distribution with rate of 10.

As we are specifying many different things, we will start by writing each set of effects separately:

```
p4 <- data.frame(
    parent = c(rep("Root", 4), "A", "B", "D", "E", "C", "F"),
    child = c("A", "B", "D", "E", "C", "C", "F", "F", "G", "G"),
    s = c(0.01, 0.02, 0.03, 0.04, 0.1, 0.1, 0.2, 0.2, 0.3, 0.3),
    sh = c(rep(0, 4), c(-.9, -.9), c(-.95, -.95), c(-.99, -.99)),
    typeDep = c(rep("--", 4),
                 "XMPN", "XMPN", "MN", "MN", "SM", "SM"))
oe \leftarrow c("C > F" = -0.1, "H > I" = 0.12)
sm <- c("I:J" = -1)
sv \leftarrow c("-K:M" = -.5, "K:-M" = -.5)
epist <- c(sm, sv)
modules <- c("Root" = "Root", "A" = "a1",
              "B" = "b1, b2", "C" = "c1",
              "D" = "d1, d2", "E" = "e1",
              "F" = "f1, f2", "G" = "g1",
              "H" = "h1, h2", "I" = "i1",
              "J" = "j1, j2", "K" = "k1, k2", "M" = "m1")
set.seed(1) ## for reproducibility
noint \leftarrow \text{rexp}(5, 10)
names(noint) <- paste0("n", 1:5)</pre>
fea <- allFitnessEffects(rT = p4, epistasis = epist,</pre>
                          orderEffects = oe,
                          noIntGenes = noint,
                          geneToModule = modules)
```

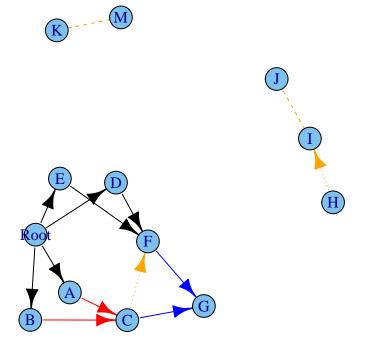
How does it look?

```
plot(fea)
```



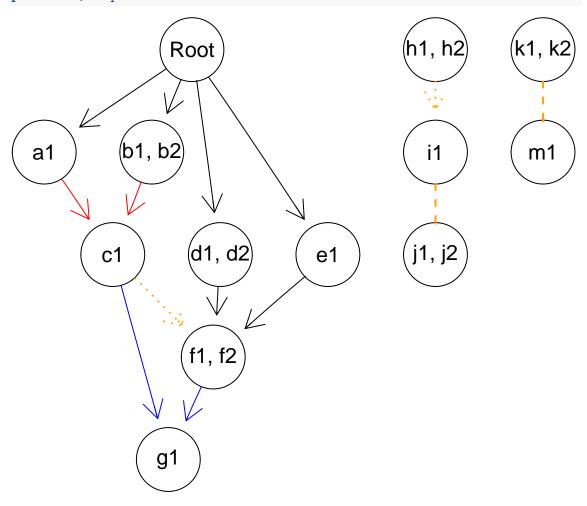
or

# plot(fea, "igraph")



We can, if we want, expand the modules using a "graphNEL" graph

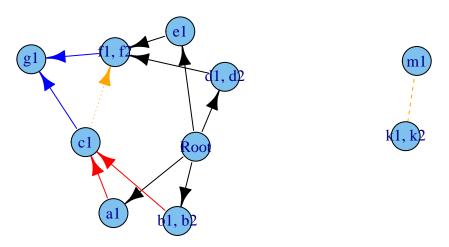
## plot(fea, expandModules = TRUE)



or an "igraph" one

plot(fea, "igraph", expandModules = TRUE)





We will not evaluate the fitness of all genotypes, since the number of all ordered genotypes is  $> 7 * 10^{22}$ . We will look at some specific genotypes:

```
evalGenotype("k1 > i1 > h2", fea) ## 0.5
## [1] 0.5
evalGenotype("k1 > h1 > i1", fea) ## 0.5 * 1.12
## [1] 0.56

evalGenotype("k2 > m1 > h1 > i1", fea) ## 1.12
## [1] 1.12

evalGenotype("k2 > m1 > h1 > i1 > c1 > n3 > f2", fea)
## [1] 0.005113
## 1.12 * 0.1 * (1 + noint[3]) * 0.05 * 0.9
```

Finally, let's generate some ordered genotypes randomly:

```
set.seed(2) ## for reproducibility
evalGenotype(randomGenotype(fea), fea, echo = TRUE, verbose = TRUE)
## Genotype: k2 > i1 > c1 > n1 > m1
   Individual s terms are: 0.0755182 -0.9
## Fitness: 0.1076
## [1] 0.1076
## Genotype: k2 > i1 > c1 > n1 > m1
## Individual s terms are : 0.0755182 -0.9
## Fitness: 0.107552
evalGenotype(randomGenotype(fea), fea, echo = TRUE, verbose = TRUE)
## Genotype: n2 > h1 > h2
  Individual s terms are: 0.118164
## Fitness: 1.118
## [1] 1.118
## Genotype: n2 > h1 > h2
## Individual s terms are: 0.118164
## Fitness: 1.11816
evalGenotype(randomGenotype(fea), fea, echo = TRUE, verbose = TRUE)
## Genotype: d2 > k2 > c1 > f2 > n4 > m1 > n3 > f1 > b1 > g1 > n5 > h1 > j2
   Individual s terms are : 0.0145707 0.0139795 0.0436069 0.02 0.1 0.03 -0.95 0.3
## Fitness: 0.07258
## [1] 0.07258
## Genotype: d2 > k2 > c1 > f2 > n4 > m1 > n3 > f1 > b1 > g1 > n5 > h1 > j2
## Individual s terms are : 0.0145707 0.0139795 0.0436069 0.02 0.1 0.03 -0.95 0.3
## Fitness: 0.0725829
evalGenotype(randomGenotype(fea), fea, echo = TRUE, verbose = TRUE)
## Genotype: h2 > c1 > f1 > n2 > b2 > a1 > n1 > i1
   Individual s terms are : 0.0755182 0.118164 0.01 0.02 -0.9 -0.95 -0.1 0.12
## Fitness: 0.006244
## [1] 0.006244
## Genotype: h2 > c1 > f1 > n2 > b2 > a1 > n1 > i1
   Individual s terms are: 0.0755182 0.118164 0.01 0.02 -0.9 -0.95 -0.1 0.12
## Fitness: 0.00624418
evalGenotype(randomGenotype(fea), fea, echo = TRUE, verbose = TRUE)
## Genotype: h2 > j1 > m1 > d2 > i1 > b2 > k2 > d1 > b1 > n3 > n1 > g1 > h1 > c1 >
## Individual s terms are: 0.0755182 0.0145707 0.0436069 0.01 0.02 -0.9 0.03 0.04
## Fitness: 0
## [1] 0
## Genotype: h2 > j1 > m1 > d2 > i1 > b2 > k2 > d1 > b1 > n3 > n1 > g1 > h1 > c1 >
   Individual s terms are: 0.0755182 0.0145707 0.0436069 0.01 0.02 -0.9 0.03 0.04
## Fitness:
evalGenotype(randomGenotype(fea), fea, echo = TRUE, verbose = TRUE)
## Genotype: n1 > m1 > n3 > i1 > j1 > n5 > k1
   Individual s terms are : 0.0755182 0.0145707 0.0436069 -1
## Fitness: 0
```

```
## [1] 0
## Genotype: n1 > m1 > n3 > i1 > j1 > n5 > k1
   Individual s terms are : 0.0755182 0.0145707 0.0436069 -1
   Fitness: 0
evalGenotype(randomGenotype(fea), fea, echo = TRUE, verbose = TRUE)
## Genotype: d2 > n1 > g1 > f1 > f2 > c1 > b1 > d1 > k1 > a1 > b2 > i1 > n4 > h2 >
   Individual s terms are: 0.0755182 0.118164 0.0139795 0.01 0.02 -0.9 0.03 -0.95
##
## Fitness: 0.004205
## [1] 0.004205
## Genotype: d2 > n1 > g1 > f1 > f2 > c1 > b1 > d1 > k1 > a1 > b2 > i1 > n4 > h2 >
   Individual s terms are: 0.0755182 0.118164 0.0139795 0.01 0.02 -0.9 0.03 -0.95
   Fitness: 0.00420528
evalGenotype(randomGenotype(fea), fea, echo = TRUE, verbose = TRUE)
## Genotype: j1 > f1 > j2 > a1 > n4 > c1 > n3 > k1 > d1 > h1
   Individual s terms are : 0.0145707 0.0139795 0.01 0.1 0.03 -0.95 -0.5
## Fitness: 0.02943
## [1] 0.02943
## Genotype: j1 > f1 > j2 > a1 > n4 > c1 > n3 > k1 > d1 > h1
   Individual s terms are: 0.0145707 0.0139795 0.01 0.1 0.03 -0.95 -0.5
## Fitness: 0.0294308
evalGenotype(randomGenotype(fea), fea, echo = TRUE, verbose = TRUE)
## Genotype: n5 > f2 > f1 > h2 > n4 > c1 > n3 > b1
   Individual s terms are: 0.0145707 0.0139795 0.0436069 0.02 0.1 -0.95
## Fitness: 0.06023
## [1] 0.06023
## Genotype: n5 > f2 > f1 > h2 > n4 > c1 > n3 > b1
   Individual s terms are: 0.0145707 0.0139795 0.0436069 0.02 0.1 -0.95
## Fitness: 0.0602298
evalGenotype(randomGenotype(fea), fea, echo = TRUE, verbose = TRUE)
## Genotype: h1 > d1 > f2
##
   Individual s terms are: 0.03 -0.95
## Fitness: 0.0515
## [1] 0.0515
## Genotype: h1 > d1 > f2
## Individual s terms are : 0.03 -0.95
## Fitness: 0.0515
```

# 3.13 Homozygosity, heterozygosity, oncogenes, tumor suppressors

We are using what is conceptually a single linear chromosome. However, you can use it to model scenarios where the numbers of copies affected matter, by properly duplicating the genes.

Suppose we have a tumor suppressor gene, G, with two copies, one from Mom and

one from Dad. We can have a table like:

$\overline{O_M}$	$O_D$	Fitness
wt	wt	1
wt	${ m M}$	1
M	wt	1
M	M	(1+s)

where s > 0, meaning that you need two hits, one in each copy, to trigger the clonal expansion.

What about oncogenes? A simple model is that one single hit leads to clonal expansion and additional hits lead to no additional changes, as in this table for gene O, where again the M or D subscript denotes the copy from Mom or from Dad:

$\overline{O_M}$	$O_D$	Fitness
wt	wt	1
wt	${ m M}$	(1+s)
${\bf M}$	wt	(1+s)
M	M	(1+s)

If you have multiple copies you can proceed similarly. As you can see, these are nothing but special cases of synthetic mortality (3.9), synthetic viability (3.8) and epistasis (3.10).

### 3.14 Gene-specific mutation rates

You can specify gene-specific mutation rates. Instead of passing a scalar value for mu, you pass a named vector. (This does not work with the old v. 1 format, though; yet another reason to stop using that format). This is a simple example (many more are available in the tests, see file ./tests/testthat/test.per-gene-mutation-rates.R).

#### 3.15 Mutator genes

You can specify mutator/antimutator genes (e.g. Gerrish et al. 2007; Tomlinson, Novelli, and Bodmer 1996). These are genes that, when mutated, lead to an increase/decrease in the mutation rate all over the genome (similar to what happens with, say, mutations in mismatch-repair genes or microsatellite instability in cancer).

The specification is very similar to that for fitness effects, except we do not (at least for now) the use of DAGs for poset-like structures nor allow for order effects (we have seen no reference in the literature to suggest any of these would be relevant). You can, however, specify epistasis and use modules. Note that the mutator genes must be a subset of the genes in the fitness effects; if you want to have mutator genes that have no direct fitness effects, give them a fitness effect of 0.

This first is a very simple example with simple fitness effects and modules for mutators. We will specify the fitness and mutator effects and evaluate the fitness and mutator effects:

```
fe2 <- allFitnessEffects(noIntGenes =</pre>
                          c(a1 = 0.1, a2 = 0.2,
                            b1 = 0.01, b2 = 0.3, b3 = 0.2,
                            c1 = 0.3, c2 = -0.2)
fm2 <- allMutatorEffects(epistasis = c("A" = 5,</pre>
                                        "B" = 10.
                                        "C" = 3),
                         geneToModule = c("A" = "a1, a2",
                                           "B" = "b1, b2, b3",
                                           "C" = "c1, c2")
## Show the fitness effect of a specific genotype
evalGenotype("a1, c2", fe2, verbose = TRUE)
##
##
   Individual s terms are: 0.1 -0.2
## [1] 0.88
## Show the mutator effect of a specific genotype
evalGenotypeMut("a1, c2", fm2, verbose = TRUE)
##
   Individual mutator product terms are: 5 3
## [1] 15
## Fitness and mutator of a specific genotype
evalGenotypeFitAndMut("a1, c2", fe2, fm2, verbose = TRUE)
##
##
    Individual s terms are: 0.1 -0.2
##
##
    Individual mutator product terms are : 5 3
```

```
## [1] 0.88 15.00
```

You can also use the evalAll functions. We do not show the output here to avoid cluttering the vignette:

```
## Show only all the fitness effects
evalAllGenotypes(fe2, order = FALSE)

## Show only all mutator effects
evalAllGenotypesMut(fm2)

## Show all fitness and mutator
evalAllGenotypesFitAndMut(fe2, fm2, order = FALSE)
```

Building upon the above, the next is an example where we have a bunch of no interaction genes that affect fitness, and a small set of genes that affect the mutation rate (but have no fitness effects).

Let us check what the effects are of a few genotypes:

```
## These only affect mutation, not fitness
evalGenotypeFitAndMut("a1, a2", fe3, fm3, verbose = TRUE)
##
##
   Individual s terms are: 0 0
##
##
   Individual mutator product terms are : 5
## [1] 1 5
evalGenotypeFitAndMut("a1, b3", fe3, fm3, verbose = TRUE)
##
##
   Individual s terms are: 0 0
##
##
    Individual mutator product terms are: 5 10
```

```
## [1]
       1 50
## These only affect fitness: the mutator multiplier is 1
evalGenotypeFitAndMut("g1", fe3, fm3, verbose = TRUE)
##
##
   Individual s terms are: 0.019206
## [1] 1.019 1.000
evalGenotypeFitAndMut("g3, g9", fe3, fm3, verbose = TRUE)
##
##
   Individual s terms are : 0.0530139 0.0592025
## [1] 1.115 1.000
## These affect both
evalGenotypeFitAndMut("g3, g9, a2, b3", fe3, fm3, verbose = TRUE)
##
##
    Individual s terms are : 0 0 0.0530139 0.0592025
##
##
   Individual mutator product terms are: 5 10
       1.115 50.000
## [1]
```

Finally, we will do a simulation with those data

```
## We do not show this in the vignette to avoid cluttering it
## with output
mue1
```

Of course, it is up to you to keep things reasonable: mutator effects are multiplicative, so if you specify, say, 20 genes (without modules), or 20 modules, each with a mutator effect of 50, the overall mutation rate can be increased by a factor of  $50^{20}$  and that is unlikely to be what you really want.

You can play with the following case (an extension of the example above), where a clone with a mutator phenotype and some fitness enhancing mutations starts giving rise to many other clones, some with additional mutator effects, and thus leading to the number of clones blowing up (as some also accumulate additional fitness-enhancing mutations). Things start getting out of hand shortly after time 250. The code below takes a few minutes and is commented, but you can run it to get an idea of the increase in the number of clones and their relationships (the usage of plotClonePhylog is explained in section 8).

```
set.seed(1) ## for reproducibility
## 17 genes, 7 with no direct fitness effects
ni \leftarrow c(rep(0, 7), runif(10, min = -0.01, max = 0.1))
names(ni) <- c("a1", "a2", "b1", "b2", "b3", "c1", "c2",</pre>
               paste0("g", 1:10))
## Next is for nicer figure labeling.
## consider drivers those with s >0
gp <- which(ni > 0)
fe3 <- allFitnessEffects(noIntGenes = ni,</pre>
                          drvNames = names(ni)[gp])
set.seed(12)
mue1 <- oncoSimulIndiv(fe3, muEF = fm3,</pre>
                        mu = 1e-6,
                        initSize = 1e5,
                        model = "McFL",
                        detectionSize = 5e6,
                        finalTime = 270,
                        keepPhylog = TRUE,
                        onlyCancer = FALSE)
mue1
## If you decrease N even further it gets even more cluttered
op <- par(ask = TRUE)
plotClonePhylog(mue1, N = 10, timeEvents = TRUE)
plot(mue1, plotDrivers = TRUE, addtot = TRUE,
     plotDiversity = TRUE)
## The stacked plot is slow; be patient
## Most clones have tiny population sizes, and their lines
## are piled on top of each other
plot(mue1, addtot = TRUE,
     plotDiversity = TRUE, type = "stacked")
par(op)
```

# 4 Plotting fitness landscapes

The evalAllGenotypes and related functions allow you to obtain tables of the genotype to fitness mappings. It might be more convenient to actually plot that, allowing us to quickly identify local minima and maxima and get an idea of how the fitness landscape looks.

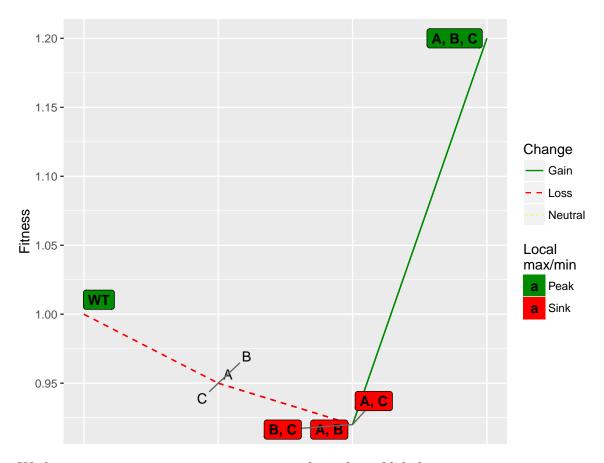
In plotFitnessLandscape I have blatantly and shamelessly copied most of the looks of the plots of MAGELLAN (Brouillet et al. 2015) (see also http://wwwabi.snv.jussieu.fr/public/Magellan/), a very nice web-based tool for fitness landscape plotting and analysis (MAGELLAN provides some other extra functionality and epistasis statistics not provided here).

As an example, let us show the previous example of Weissman et al. we saw in 5.4:

```
d1 <- -0.05 ## single mutant fitness 0.95
d2 <- -0.08 ## double mutant fitness 0.92
d3 <- 0.2 ## triple mutant fitness 1.2
s2 <- ((1 + d2)/(1 + d1)^2) - 1
s3 <- ( (1 + d3)/((1 + d1)^3 * (1 + s2)^3) ) - 1

wb <- allFitnessEffects(
    epistasis = c(
        "A" = d1,
        "B" = d1,
        "C" = d1,
        "A:B" = s2,
        "A:C" = s2,
        "B:C" = s2,
        "A:B:C" = s3))</pre>
```

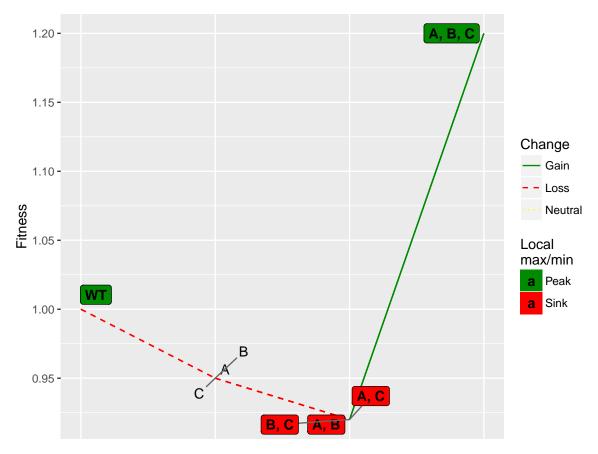
plotFitnessLandscape(wb, use\_ggrepel = TRUE)



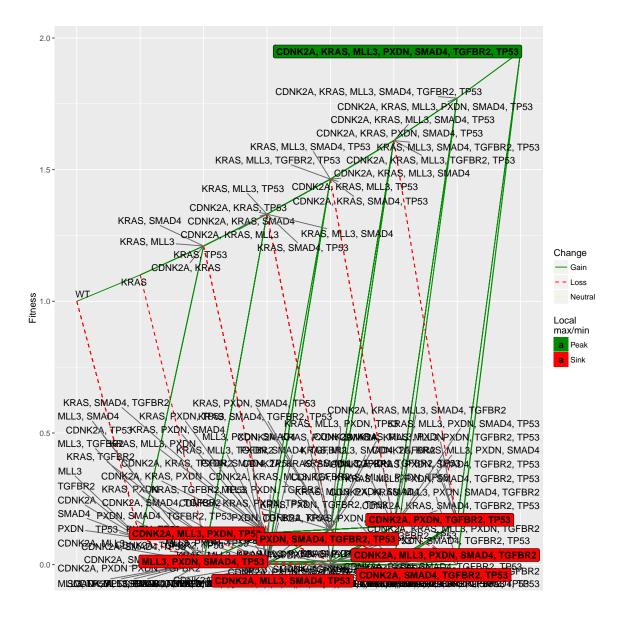
We have set  ${\tt use\_ggrepel}$  = TRUE to avoid overlap of labels.

For some types of objects, directly invoking plot will give you the fitness plot

```
(ewb <- evalAllGenotypes(wb, order = FALSE))</pre>
##
     Genotype Fitness
## 1
                  0.95
             Α
## 2
             В
                  0.95
## 3
             С
                  0.95
## 4
         A, B
                  0.92
## 5
         A, C
                  0.92
## 6
         B, C
                  0.92
## 7
      A, B, C
                  1.20
plot(ewb, use_ggrepel = TRUE)
```



This is another example we saw before (5.5), that will give a very busy plot:



# 5 Specifying fitness effects: some examples from the literature

#### 5.1 Bauer et al., 2014

In the model of Bauer and collaborators (Bauer, Siebert, and Traulsen 2014, 54) we have "For cells without the primary driver mutation, each secondary driver mutation leads to a change in the cell's fitness by  $s_P$ . For cells with the primary driver mutation, the fitness advantage obtained with each secondary driver mutation is  $s_{DP}$ ."

The proliferation probability is given as:

- $\frac{1}{2}(1+s_p)^k$  when there are k secondary drivers mutated and no primary diver;
- $\frac{1}{2} \frac{1+S_D^+}{1+S_D^-} (1+S_{DP})^k$  when the primary driver is mutated;

apoptosis is one minus the proliferation rate.

#### 5.1.1 Using a DAG

We cannot find a simple mapping from their expressions to our fitness parameterization, but we can get fairly close by using a DAG; in this one, note the unusual feature of having one of the "s" terms (that for the driver dependency on root) be negative. Using the parameters given in the legend of their Figure 3 for  $s_p, S_D^+, S_D^-, S_{DP}$  and obtaining that negative value for the dependency of the driver on root we can do:

```
K <- 4
sp <- 1e-5
sdp <- 0.015
sdplus <- 0.05
sdminus <- 0.1
cnt \langle -(1 + sdplus)/(1 + sdminus)
prod cnt <- cnt - 1
bauer <- data.frame(parent = c("Root", rep("D", K)),</pre>
                     child = c("D", paste0("s", 1:K)),
                     s = c(prod_cnt, rep(sdp, K)),
                     sh = c(0, rep(sp, K)),
                     typeDep = "MN")
fbauer <- allFitnessEffects(bauer)</pre>
(b1 <- evalAllGenotypes(fbauer, order = FALSE, addwt = TRUE))
##
                Genotype Fitness
## 1
                      WT
                          1.0000
                          0.9545
## 2
                       D
## 3
                      s1
                          1.0000
## 4
                       s2
                          1.0000
## 5
                       s3
                          1.0000
```

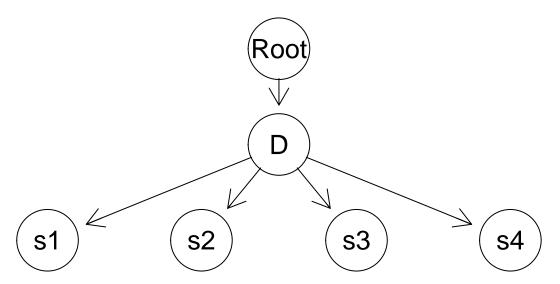
```
## 6
                           1.0000
                      s4
## 7
                   D, s1
                           0.9689
## 8
                   D, s2
                           0.9689
## 9
                   D, s3
                           0.9689
                           0.9689
## 10
                   D, s4
## 11
                  s1, s2
                           1.0000
## 12
                  s1, s3
                           1.0000
## 13
                           1.0000
                  s1, s4
## 14
                  s2, s3
                           1.0000
## 15
                  s2, s4
                           1.0000
## 16
                  s3, s4
                           1.0000
## 17
               D, s1, s2
                           0.9834
## 18
               D, s1, s3
                           0.9834
               D, s1, s4
## 19
                           0.9834
## 20
               D, s2, s3
                           0.9834
## 21
               D, s2, s4
                           0.9834
## 22
               D, s3, s4
                           0.9834
## 23
              s1, s2, s3
                           1.0000
## 24
              s1, s2, s4
                           1.0000
## 25
              s1, s3, s4
                           1.0000
              s2, s3, s4
## 26
                           1.0000
## 27
          D, s1, s2, s3
                           0.9981
## 28
          D, s1, s2, s4
                           0.9981
## 29
          D, s1, s3, s4
                           0.9981
## 30
          D, s2, s3, s4
                           0.9981
## 31
         s1, s2, s3, s4
                           1.0000
## 32 D, s1, s2, s3, s4
                           1.0131
```

(We use "D" for "driver" or "primary driver", as is it is called in the original paper, and "s" for secondary drivers, somewhat similar to passengers).

Note that what we specify as "typeDep" is irrelevant (MN, SMN, or XMPN make no difference).

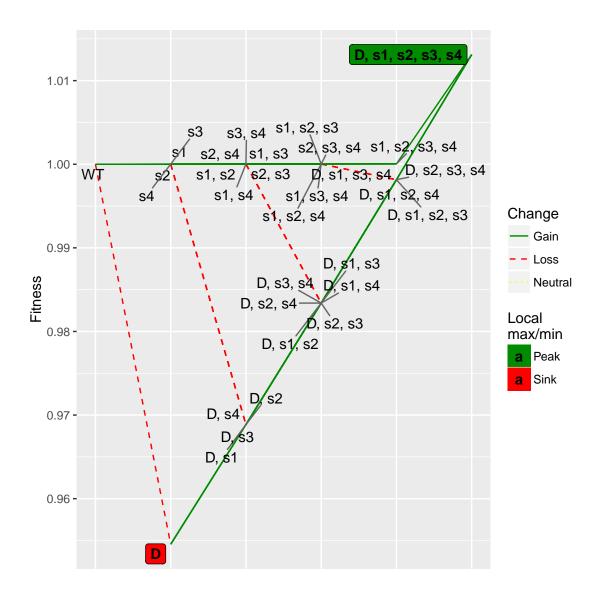
This is the DAG:

```
plot(fbauer)
```



And if you compare the tabular output of evalAllGenotypes you can see that the values of fitness reproduces the fitness landscape that they show in their Figure 1. We can also use our plot for fitness landscapes:

plot(b1, use\_ggrepel = TRUE)



#### 5.1.2 Specifying fitness of genotypes directly

An alternative approach to specify the fitness, if the number of genotypes is reasonably small, is to directly evaluate fitness as given by their expressions. Then, use the genotFitness argument to allFitnessEffects.

We will create all possible genotypes; then we will write a function that gives the fitness of each genotype according to their expression; finally, we will call this function on the data frame of genotypes, and pass this data frame to allFitnessEffects.

Now, show the fitness of all genotypes:

```
evalAllGenotypes(bauer2, order = FALSE, addwt = TRUE)
##
                Genotype Fitness
## 1
                      WT
                          1.0000
## 2
                       D
                          0.9545
## 3
                      s1
                          1.0000
## 4
                      s2
                          1.0000
## 5
                      s3
                          1.0000
## 6
                      s4
                          1.0000
## 7
                   D, s1
                          0.9689
                   D, s2
## 8
                          0.9689
## 9
                   D, s3
                          0.9689
## 10
                   D, s4
                          0.9689
## 11
                  s1, s2
                          1.0000
## 12
                  s1, s3
                          1.0000
## 13
                  s1, s4
                          1.0000
## 14
                  s2, s3
                          1.0000
                  s2, s4
## 15
                          1.0000
## 16
                  s3, s4
                          1.0000
## 17
               D, s1, s2
                          0.9834
## 18
               D, s1, s3
                          0.9834
                          0.9834
## 19
              D, s1, s4
## 20
              D, s2, s3
                          0.9834
## 21
              D, s2, s4
                          0.9834
## 22
              D, s3, s4
                          0.9834
## 23
              s1, s2, s3
                          1.0000
              s1, s2, s4
## 24
                          1.0000
## 25
              s1, s3, s4
                          1.0000
```

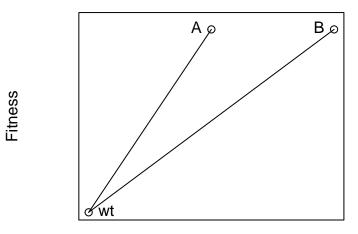
```
## 26
             s2, s3, s4
                          1.0000
## 27
          D, s1, s2, s3
                          0.9981
## 28
          D, s1, s2, s4
                          0.9981
          D, s1, s3, s4
## 29
                          0.9981
## 30
          D, s2, s3, s4
                          0.9981
## 31
         s1, s2, s3, s4
                          1.0000
## 32 D, s1, s2, s3, s4
                          1.0131
```

Can we use modules in this example, if we use the "lego system"? Sure, as in any other case.

#### 5.2 Misra et al., 2014

Figure 1 of Misra, Szczurek, and Vingron (2014) presents three scenarios which are different types of epistasis.

#### **5.2.1** Example 1.a



In that figure it is evident that the fitness effect of "A" and "B" are the same. There are two different models depending on whether "AB" is just the product of both, or there is epistasis. In the first case probably the simplest is:

```
## 3 B 1.10
## 4 A, B 1.21
```

If the double mutant shows epistasis, as we saw before (section 3.10.1) we have a range of options. For example:

```
s < -0.1
sab <- 0.3
m1a2 <- allFitnessEffects(epistasis = c("A:-B" = s,</pre>
                                           "-A:B" = s.
                                           "A:B" = sab)
evalAllGenotypes(m1a2, order = FALSE, addwt = TRUE)
     Genotype Fitness
## 1
            WT
                   1.0
## 2
             Α
                   1.1
             В
                   1.1
## 3
## 4
         A, B
                   1.3
```

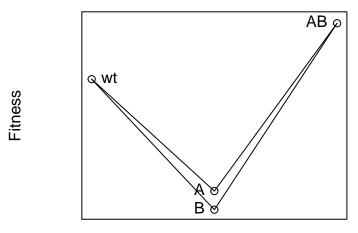
But we could also modify the graph dependency structure, and we have to change the value of the coefficient, since that is what multiplies each of the terms for "A" and "B":  $(1 + s_{AB}) = (1 + s)^2(1 + s_{AB})$ 

```
sab3 \leftarrow ((1 + sab)/((1 + s)^2)) - 1
m1a3 <- allFitnessEffects(data.frame(parent = c("Root", "Root"),</pre>
                                         child = c("A", "B"),
                                         s = s,
                                         sh = 0,
                                         typeDep = "MN"),
                            epistasis = c("A:B" = sab3))
evalAllGenotypes(m1a3, order = FALSE, addwt = TRUE)
##
     Genotype Fitness
## 1
            WT
                    1.0
## 2
             Α
                    1.1
## 3
             В
                    1.1
## 4
         A, B
                    1.3
```

And, obviously

#### **5.2.2** Example 1.b

This is a specific case of synthetic viability (see also section 3.8):



Here,  $S_A, S_B < 0$ ,  $S_B < 0$ ,  $S_{AB} > 0$  and  $(1 + S_{AB})(1 + S_A)(1 + S_B) > 1$ .

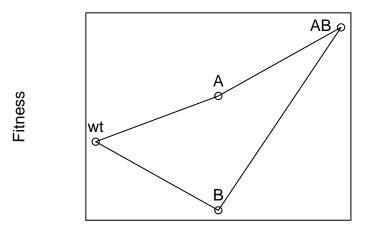
As before, we can specify this in several different ways. The simplest is to specify all genotypes:

```
sa < -0.6
sb < -0.7
sab <- 0.3
m1b1 <- allFitnessEffects(epistasis = c("A:-B" = sa,
                                          "-A:B" = sb,
                                          "A:B" = sab))
evalAllGenotypes(m1b1, order = FALSE, addwt = TRUE)
##
     Genotype Fitness
## 1
           WT
                   1.0
## 2
            Α
                   0.4
## 3
            В
                   0.3
                   1.3
## 4
         A, B
```

We could also use a tree and modify the "sab" for the epistasis, as before (5.2.1).

#### 5.2.3 Example 1.c

The final case, in figure 1.c of Misra et al., is just epistasis, where a mutation in one of the genes is deleterious (possibly only mildly), in the other is beneficial, and the double mutation has fitness larger than any of the other two.



Here we have that  $s_A > 0$ ,  $s_B < 0$ ,  $(1 + s_{AB})(1 + s_A)(1 + s_B) > (1 + s_{AB})$  so  $s_{AB} > \frac{-s_B}{1+s_B}$ 

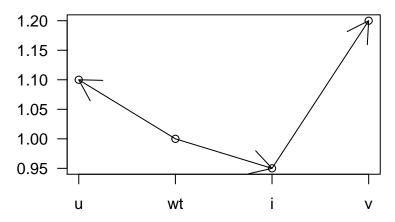
As before, we can specify this in several different ways. The simplest is to specify all genotypes:

```
sa <- 0.2
sb < -0.3
sab <- 0.5
m1c1 <- allFitnessEffects(epistasis = c("A:-B" = sa,</pre>
                                           "-A:B" = sb,
                                           "A:B" = sab))
evalAllGenotypes(m1c1, order = FALSE, addwt = TRUE)
##
     Genotype Fitness
## 1
            WT
                   1.0
## 2
                   1.2
             Α
## 3
             В
                   0.7
         A, B
                   1.5
```

We could also use a tree and modify the "sab" for the epistasis, as before (5.2.1).

### 5.3 Ochs and Desai, 2015

In Ochs and Desai (2015) the authors present a model shown graphically as (the actual numerical values are arbitrarily set by me):

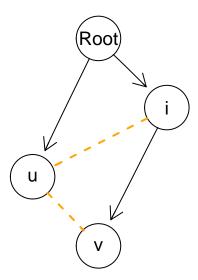


In their model,  $s_u > 0$ ,  $s_v > s_u$ ,  $s_i < 0$ , we can only arrive at v from i, and the mutants "ui" and "uv" can never appear as their fitness is 0, or  $-\infty$ , so  $s_{ui} = s_{uv} = -1$  (or  $-\infty$ ).

We can specify this combining a graph and epistasis specifications:

A figure showing that model is

```
plot(od)
```



And the fitness of all genotype is

```
evalAllGenotypes(od, order = FALSE, addwt = TRUE)
##
     Genotype Fitness
           WT
## 1
                  1.00
## 2
             i
                  0.95
## 3
            u
                  1.10
## 4
                  0.00
             v
## 5
                  0.00
         i, u
                  1.20
## 6
         i, v
## 7
                  0.00
         u, v
                  0.00
     i, u, v
```

We could alternatively have specified fitness either directly specifying the fitness of each genotype or specifying epistatic effects. Let us use the second approach:

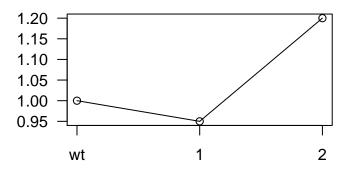
```
u \leftarrow 0.2; i \leftarrow -0.02; vi \leftarrow 0.6; ui \leftarrow uv \leftarrow -Inf
od2 <- allFitnessEffects(</pre>
    epistasis = c("u" = u,
                                 "u:i" = ui,
                      "u:v" = uv, "i" = i,
                      "v:-i" = -Inf, "v:i" = vi))
evalAllGenotypes(od, addwt = TRUE)
##
      Genotype Fitness
             WT
## 1
                    1.00
## 2
                    0.95
              i
## 3
                    1.10
              u
## 4
                    0.00
              v
                    0.00
## 5
          i, u
## 6
                    1.20
           i, v
## 7
                    0.00
          u, v
## 8
       i, u, v
                    0.00
```

We will return to this model when we explain the usage of fixation for stopping the simulations (see @{fixation}).

#### 5.4 Weissman et al., 2009

In their figure 1a, Weissman et al. (2009) present this model (actual numeric values are set arbitrarily)

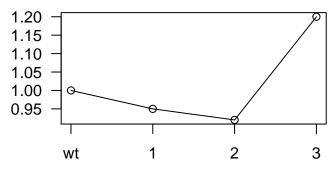
#### 5.4.1 Figure 1.a}



where the 1" and2" refer to the total number of mutations in two different loci. This is, therefore, very similar to the example in section 5.2.2. Here we have, in their notation,  $\delta_1 < 0$ , fitness of single "A" or single "B" =  $1 + \delta_1$ ,  $S_{AB} > 0$ ,  $(1 + S_{AB})(1 + \delta_1)^2 > 1$ .

#### 5.4.2 Figure 1.b

In their figure 1b they show



Where, as before, 1, 2, 3, denote the total number of mutations over three different loci and  $\delta_1 < 0$ ,  $\delta_2 < 0$ , fitness of single mutant is  $(1 + \delta_1)$ , of double mutant is  $(1 + \delta_2)$  so that  $(1 + \delta_2) = (1 + \delta_1)^2(1 + s_2)$  and of triple mutant is  $(1 + \delta_3)$ , so that  $(1 + \delta_3) = (1 + \delta_1)^3(1 + s_2)^3(1 + s_3)$ .

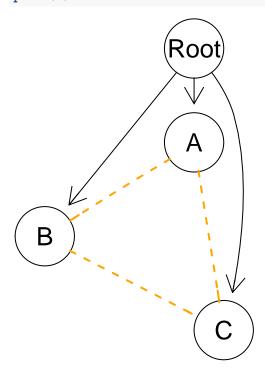
We can specify this combining a graph with epistasis:

```
d1 <- -0.05 ## single mutant fitness 0.95
d2 <- -0.08 ## double mutant fitness 0.92
d3 <- 0.2 ## triple mutant fitness 1.2

s2 <- ((1 + d2)/(1 + d1)^2) - 1
s3 <- ( (1 + d3)/((1 + d1)^3 * (1 + s2)^3) ) - 1</pre>
```

The model can be shown graphically as:

#### plot(w)



And fitness of all genotypes is:

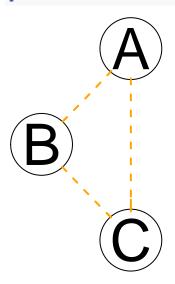
```
evalAllGenotypes(w, order = FALSE, addwt = TRUE)
##
     Genotype Fitness
## 1
                 1.00
           WT
## 2
                 0.95
            Α
## 3
            В
                 0.95
## 4
            С
                 0.95
## 5
         A, B
                 0.92
## 6
         A, C
                 0.92
## 7
         B, C
                 0.92
## 8 A, B, C
                 1.20
```

Alternatively, we can directly specify what each genotype adds to the fitness, given the included genotype. This is basically replacing the graph by giving each of "A", "B", and "C" directly:

```
wb <- allFitnessEffects(</pre>
    epistasis = c(
         "A" = d1,
         "B" = d1,
         "C" = d1,
         "A:B" = s2,
         "A:C" = s2,
         "B:C" = s2,
         "A:B:C" = s3)
evalAllGenotypes(wb, order = FALSE, addwt = TRUE)
##
     Genotype Fitness
## 1
            WT
                  1.00
## 2
             Α
                  0.95
## 3
             В
                  0.95
             C
                  0.95
## 4
                  0.92
## 5
         A, B
## 6
         A, C
                  0.92
         B, C
                  0.92
## 7
## 8 A, B, C
                  1.20
```

The plot, of course, is not very revealing and we cannot show that there is a three-way interaction (only all three two-way interactions):

#### plot(wb)

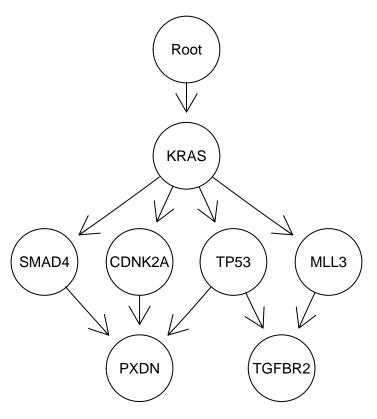


As we have seen several times already (sections 3.10.1, 3.10.2, 3.10.3) we can also give the genotypes directly and, consequently, the fitness of each genotype (not the added contribution):

```
wc <- allFitnessEffects(</pre>
    epistasis = c(
        "A:-B:-C" = d1,
        "B:-C:-A" = d1,
        "C:-A:-B" = d1,
        "A:B:-C" = d2,
        "A:C:-B" = d2,
        "B:C:-A" = d2,
        "A:B:C" = d3))
evalAllGenotypes(wc, order = FALSE, addwt = TRUE)
##
     Genotype Fitness
## 1
           WT
                  1.00
## 2
                  0.95
            Α
## 3
            В
                  0.95
## 4
            С
                  0.95
## 5
         A, B
                  0.92
         A, C
## 6
                  0.92
## 7
         B, C
                  0.92
## 8 A, B, C
                  1.20
```

#### 5.5 Gerstung et al., 2011, pancreatic cancer poset

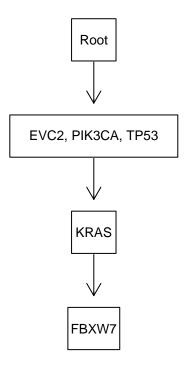
Similar to what we did in v.1 (see section 12.1) we can specify the pancreatic cancer poset in Gerstung et al. (2011) (their figure 2B, left). We use directly the names of the genes, since that is immediately supported by the new version.



Of course the "s" and "sh" are set arbitrarily here.

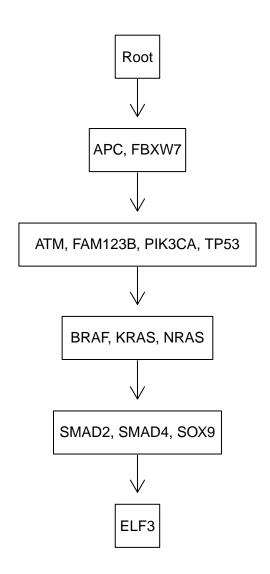
### 5.6 Raphael and Vandin's 2014 modules

In Raphael and Vandin (2015), the authors show several progression models in terms of modules. We can code the extended poset for the colorectal cancer model in their Figure 4.a is (s and sh are arbitrary):



We have used the (experimental) autofit option to fit the labels to the edges. Note how we can use the same name for genes and modules, but we need to specify all the modules.

Their Figure 5b is



# 6 Running and plotting the simulations: starting, ending, and examples

### 6.1 Starting and ending

After you have decided the specifics of the fitness effects and the model, you need to decide:

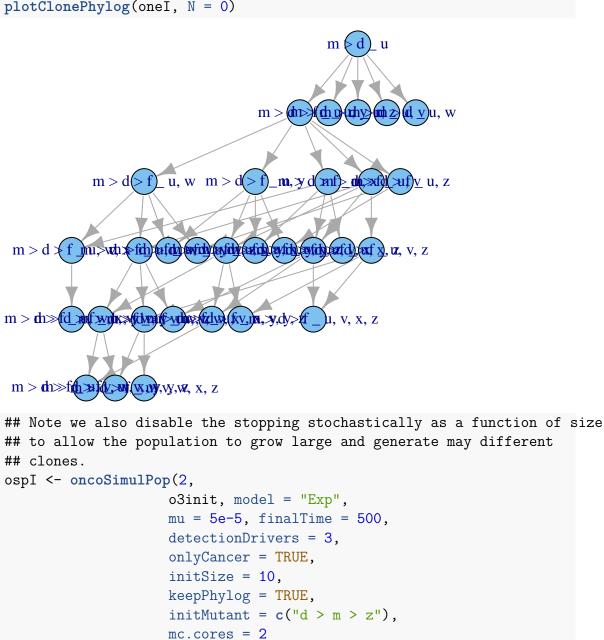
- Where will you start your simulation from. This involves deciding the initial population size (argument initSize) and, possibly, the genotype of the initial population; the later is covered in section 6.2.
- When will you stop it: how long to run it, and whether or not to require simulations to reach cancer (under some definition of what it means to reach cancer). This is covered in 6.3.

### 6.2 Can I start the simulation from a specific mutant?

You bet. In version 2 you can specify the genotype for the initial mutant with the same flexibility as in evalGenotype. Here we show a couple of examples (we use the representation of the parent-child relationships —discussed in section 8— of the clones so that you can see which clones appear, and from which, and check that we are not making mistakes).

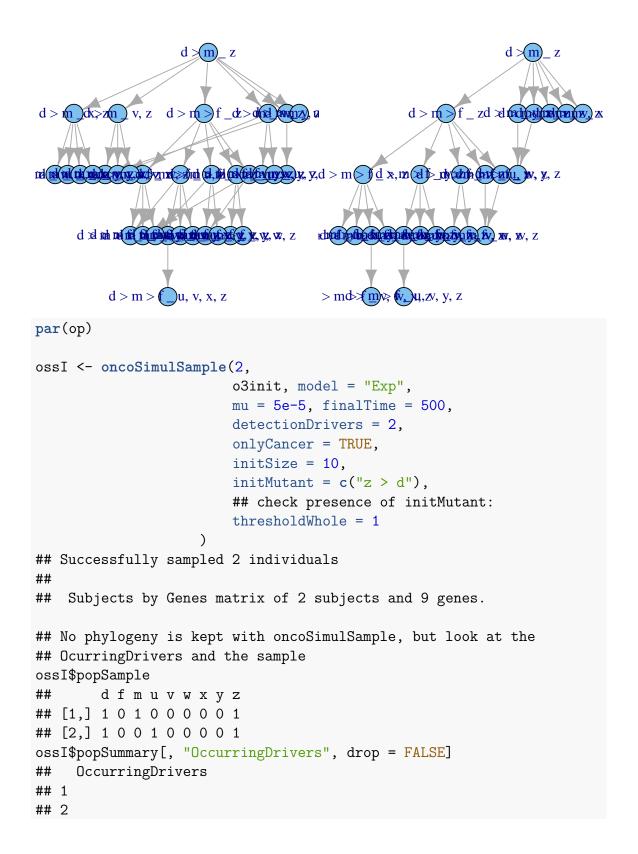
```
o3init <- allFitnessEffects(orderEffects = c(
                             "M > D > F" = 0.99
                             "D > M > F" = 0.2,
                             "D > M"
                                         = 0.1,
                             "M > D"
                                         = 0.9),
                        noIntGenes = c("u" = 0.01,
                                        "v" = 0.01,
                                        w'' = 0.001.
                                        "x" = 0.0001.
                                        "v" = -0.0001,
                                        z'' = -0.001,
                        geneToModule =
                             c("M" = "m",
                               "F" = "f",
                               "D" = "d")
oneI <- oncoSimulIndiv(o3init, model = "McFL",</pre>
                       mu = 5e-5, finalTime = 500,
                       detectionDrivers = 3,
                       onlyCancer = FALSE,
                       initSize = 1000,
```

```
keepPhylog = TRUE,
    initMutant = c("m > u > d")
    )
plotClonePhylog(oneI, N = 0)
```



op  $\leftarrow$  par(mar = rep(0, 4), mfrow = c(1, 2))

plotClonePhylog(ospI[[1]])
plotClonePhylog(ospI[[2]])



## 6.3 Ending the simulations

OncoSimulR provides very flexible ways to decide when to stop a simulation. Here we focus on a single simulation; see further options with multiple simulations in 7.

- onlyCancer = TRUE. A simulation will be repeated until any one of the "reach cancer" conditions is met, if this happens before the simulation reaches finalTime<sup>9</sup>. These conditions are:
  - Total population size becomes larger than detectionSize.
  - The number of drivers in any one genotype or clone becomes equal to, or larger than, detectionDrivers; note that this allows you to stop the simulation as soon as a **specific genotype** is found, by using exactly and only the genes that make that genotype as the drivers.
  - The tumor is detected according to a stochastic detection mechanism, where the probability of "detecting the tumor" increases with population size; this is explained below (6.3.1) and is controlled by argument detectionProb.
  - A gene or gene combination among those listed in fixation becomes fixed in the population (i.e., has a frequency is 1) (see details in (6.4).

As we exit as soon as any of the exiting conditions is reached, if you only care about one condition, set the other to NA (see also section 6.3.1.1).

• onlyCancer = FALSE. A simulation will run only once, and will exit as soon as any of the above conditions are met or as soon as the total population size becomes zero or we reach finalTime.

As an example of onlyCancer = TRUE, focusing on the first two mechanisms, suppose you give detectionSize = 1e4 and detectionDrivers =3 (and you have detectionProb = NA). A simulation will exit as soon as it reaches a total population size of 1e4 or any clone has four drivers, whichever comes first (if any of these happen before finalTime).

In the onlyCancer = TRUE case, what happens if we reach finalTime (or the population size becomes zero) before any of the "reach cancer" conditions have been fulfilled? The simulation will be repeated again, within the following limits:

- max.wall.time: the total wall time we allow an individual simulation to run;
- max.num.tries: the maximum number of times we allow a simulation to be repeated to reach cancer;
- max.wall.time.total and max.num.tries.total, similar to the above but over a set of simulations in function oncoSimulSample.

Incidentally, we keep track of the number of attempts used (the component other\$attemptsUsed\$) before we reach cancer, so you can estimate (as from a negative binomial sampling) the probability of reaching your desired end point under different scenarios.

The onlyCancer = FALSE case might be what you want to do when you examine general population genetics scenarios without focusing on possible sampling issues. To do this, set finalTime to the value you want and set onlyCancer = FALSE; in addition, set detectionProb to "NA" and detectionDrivers and detectionSize

 $<sup>^9{</sup>m Of}$  course, the "reach cancer" idea and the <code>onlyCancer</code> argument are generic names; this could have been labeled "reach whatever interests me".

to "NA" or to huge numbers<sup>10</sup>. In this scenario you simply collect the simulation output at the end of the run, regardless of what happened with the population (it became extinct, it did not reach a large size, it did not accumulate drivers, etc).

#### 6.3.1 Stochastic detection mechanism: "detectionProb"

This is the process that is controlled by the argument detectionProb. Here the probability of tumor detection increases with the total population size. This is biologically a reasonable assumption: the larger the tumor, the more likely it is it will be detected.

At regularly spaced times during the simulation, we compute the probability of detection as a function of size and determine (by comparing against a random uniform number) if the simulation should finish. For simplicity, and to make sure the probability is bounded between 0 and 1, we use the function

$$P(N) = \begin{cases} 1 - e^{-cPDetect(N - PDBaseline)} & \text{if } N > PDBaseline \\ 0 & \text{if } N \le PDBaseline \end{cases}$$
 (1)

where P(N) is the probability that a tumor with a population size N will be detected, and cPDetect controls the increase in P(N) with population size; with PDBaseline we both control the minimal population size at which this mechanism stats operating (because we will rarely want detection unless there is some meaningful increase of population size over initSize) and we model the increase in P(N) as a function of differences with respect to PDBaseline.

The P(N) refers to the probability of detection at each one of the occasions when we assess the probability of exiting. When, or how often, do we do that? When we assess probability of exiting is controlled by checkSizePEvery, which will often be much larger than sampleEvery<sup>11</sup>. Biologically, a way to think of checkSizePEvery is "time between doctor appointments".

An important **warning**, though: for populations that are growing very, very fast or where some genes might have very large effects on fitness even a moderate **checkSizePEvery** of, say, 10, might be inappropriate, since populations could have increased by several orders of magnitude between successive checks. This issue is also discussed in section 2.1.1 and 2.2.

Finally, you can specify cPDetect directly (you will need to set n2 and p2 to NA). However, it might be more intuitive to specify the pair n2, p2, such that P(n2) = p2

<sup>&</sup>lt;sup>10</sup>Setting detectionDrivers and detectionSize to "NA" is in fact equivalent to setting them to the largest possible numbers for these variables:  $2^{32} - 1$  and  $\infty$ , respectively.

<sup>&</sup>lt;sup>11</sup>We assess probability of exiting at every sampling time, as given by sampleEvery, that is the smallest possible sampling time that is separated from the previous time of assessment by at least checkSizePEvery. In other words, the interval between successive assessments will be the smallest multiple integer of sampleEvery that is larger than checkSizePEvery. For example, suppose sampleEvery = 2 and checkSizePEvery = 3: we will assess exiting at times 4, 8, 12, 16, .... If sampleEvery = 3 and checkSizePEvery = 3: we will assess exiting at times 6, 12, 18, ....

(and from that pair we solve for the value of carpetbagged).

You can get a feeling for the effects of these arguments by playing with the following code, that we do not execute here for the sake of speed. Here no mutation has any effect, but there is a non-zero probability of exiting as soon as the total population size becomes larger than the initial population size. So, eventually, all simulations will exit and, as we are using the McFarland model, population size will vary slightly around the initial population size.

```
gi2 \leftarrow rep(0, 5)
names(gi2) <- letters[1:5]</pre>
oi2 <- allFitnessEffects(noIntGenes = gi2)
s5 <- oncoSimulPop(200,
                    oi2,
                    model = "McFL",
                    initSize = 1000,
                    detectionProb = c(p2 = 0.1,
                                       n2 = 2000,
                                       PDBaseline = 1000,
                                        checkSizePEvery = 2),
                    detectionSize = NA,
                    finalTime = NA,
                    keepEvery = NA,
                    detectionDrivers = NA)
hist(unlist(lapply(s5, function(x) x$FinalTime)))
```

As you decrease checkSizePEvery the distribution of "FinalTime" will resemble more and more an exponential distribution.

In this vignette, there are some further examples of using this mechanism in 6.6.5 and 6.6.2, with the default arguments.

#### 6.3.1.1 Stochastic detection mechanism and minimum number of drivers

We said above that we exit as soon as any of the conditions is reached (i.e., we use an OR operation over the exit conditions). There is a special exception to this procedure: if you set AND\_DrvProbExit = TRUE, both the number of drivers and the detectionProb mechanism condition must fulfilled. This means that the detectionProb mechanism not assessed unless the detectionDrivers condition is. Using AND\_DrvProbExit = TRUE allows to run simulations and ensure that all of the returned simulations will have at least some cells with the number of drivers as specified by detectionDrivers. Note, though, that this does not guarantee that when you sample the population, all those drivers will be detected (as this depends on the actual proportion of cells with the drivers and the settings of samplePop).

## 6.4 Fixation of genes/gene combinations with Ochs and Desai example

In some cases we might be interested in running simulations until a particular set of genes, or gene combinations, reaches fixation. This exit condition might be more relevant than some of the above in many non-cancer-related evolutionary genetics scenarios.

Simulations will stop as soon as any of the genes or gene combinations in the vector (or list) fixation reaches a frequency of 1. These gene combinations might have non-zero intersection (i.e., they might share genes), and those genes need not be drivers. If we want simulations to only stop when fixation of those genes/gene combinations is reached, we will set all other stopping conditions to NA. It is, of course, up to you to ensure that those stopping conditions are reasonable (that they can be reached) and to use, or not, finalTime; otherwise, simulations will eventually abort (e.g., when max.wall.time or max.num.tries are reached). Since we are asking for fixation, the Exp or Bozic models will often not be appropriate here; instead, models with competition and limited population size such as McFL are more appropriate.

We return here to the example from section @(ochsdesai).

Ochs and Desai explain that "Each simulated population was evolved until either the uphill genotype or valley-crossing genotype fixed." (see Ochs and Desai (2015), p.2, section "Simulations"). We will do the same here. We specify that we want to end the simulation when either the "u" or the "v, i" genotypes have reached fixation, by passing those genotype combinations as the fixation argument (in this example using fixation = c("u", "v") would have been equivalent, since the "v" genotype has fitness of 0).

We want to be explicit that fixation will be the one and only condition for ending the simulations, and thus we set arguments detectionDrivers, finalTime, detectionSize and detectionProb explicitly to NA. (We set the number of repetitions only to 50 for the sake of speed when creating the vignette).

```
finalTime = NA,
detectionSize = NA,
detectionProb = NA,
onlyCancer = TRUE,
initSize = initS,
mc.cores = 2)
```

What is the frequency of each genotype among the simulations? (or, what is the frequency of fixation of each genotype?)

```
sampledGenotypes(samplePop(od100))
##
## Subjects by Genes matrix of 10 subjects and 3 genes.
## Genotype Freq
## 1 i, v 2
## 2 u 8
##
## Shannon's diversity (entropy) of sampled genotypes: 0.5004
```

Note the very large variability in reaching fixation

```
head(summary(od100)[, c(1:3, 8:9)])
     NumClones TotalPopSize LargestClone FinalTime NumIter
## 1
              3
                           10
                                          10
                                                  985.8
                                                          39440
              3
## 2
                           34
                                          34
                                                  517.1
                                                          20689
              3
## 3
                           29
                                          29
                                                 1569.7
                                                          62804
## 4
              3
                           33
                                                 2051.7
                                          33
                                                          82077
              4
                           47
                                          47
                                                1249.2
## 5
                                                          49979
              3
## 6
                           31
                                          31
                                                 3291.8 131690
```

## 6.5 Plotting genotype/driver abundance over time; plotting the simulated trajectories

We have seen many of these plots already, starting with 2 and 3 and we will see many more below, in the examples, starting with section 6.6.1 such as in figures 4 and 5. In a nutshell, what we are plotting is the information contained in the pops.by.time matrix, the matrix that contains the abundances of all the clones (or genotypes) at each of the sampling periods.

The functions that do the work are called plot and these are actually methods for objects of class "oncosimul" and "oncosimulpop". You can access the help by doing <code>?plot.oncosimul</code>, for example.

What entities are shown in the plot? You can show the trajectories of:

- numbers of drivers (e.g., 4);
- genotypes or clones (e.g., 5).

(Of course, showing "drivers" requires that you have specified certain genes as drivers.

What types of plots are available?

- line plots;
- stacked plots;
- stream plots.

All those three are shown in both of 4 and 5.

If you run multiple simulations using oncoSimulPop you can plot the trajectories of all of the simulations.

## 6.6 Several examples of simulations and plotting simulation trajectories

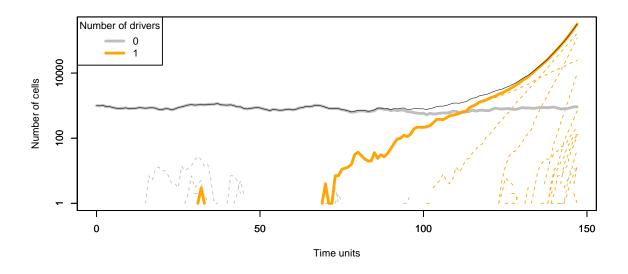
### 6.6.1 Bauer's example again

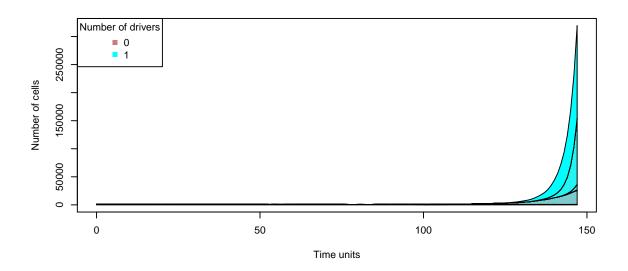
We will use the model of Bauer, Siebert, and Traulsen (2014) that we saw in section 5.1.

```
K <- 5
sd <- 0.1
sdp < -0.15
sp < -0.05
bauer <- data.frame(parent = c("Root", rep("p", K)),</pre>
                     child = c("p", paste0("s", 1:K)),
                     s = c(sd, rep(sdp, K)),
                     sh = c(0, rep(sp, K)),
                     typeDep = "MN")
fbauer <- allFitnessEffects(bauer, drvNames = "p")</pre>
set.seed(1)
## Use fairly large mutation rate
b1 <- oncoSimulIndiv(fbauer, mu = 5e-5, initSize = 1000,
                      finalTime = NA,
                      onlyCancer = TRUE,
                      detectionProb = "default")
```

We will now use a variety of plots

```
par(mfrow = c(3, 1))
## First, drivers
plot(b1, type = "line", addtot = TRUE)
plot(b1, type = "stacked")
plot(b1, type = "stream")
```





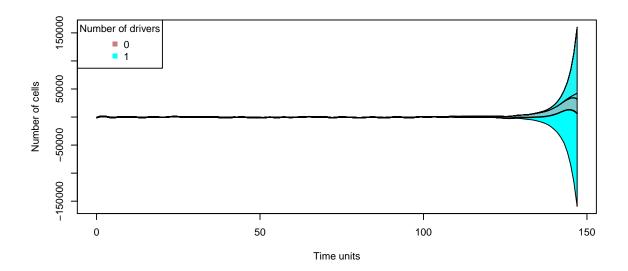


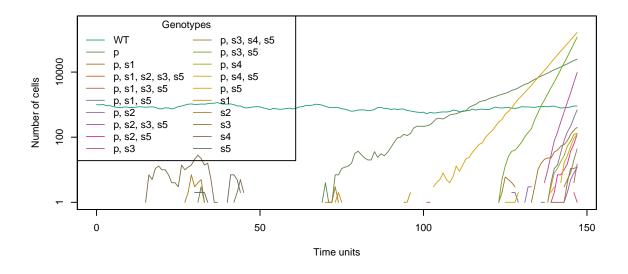
Figure 4: Three drivers' plots of a simulation of Bauer's model

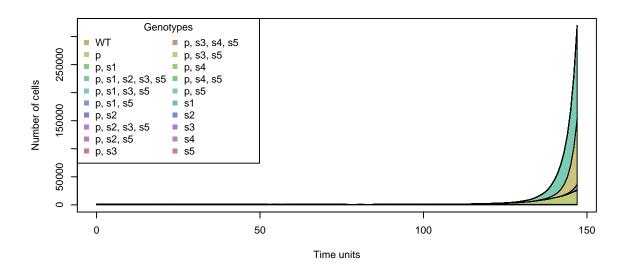
```
par(mfrow = c(3, 1))
## Next, genotypes
plot(b1, show = "genotypes", type = "line")
plot(b1, show = "genotypes", type = "stacked")
plot(b1, show = "genotypes", type = "stream")
```

In this case, probably the stream plots are most helpful. Note, however, that (in contrast to some figures in the literature showing models of clonal expansion) the stream plot (or the stacked plot) does not try to explicitly show parent-descendant relationships, which would hardly be realistically possible in these plots (although the plots of phylogenies in section 8 could be of help).

### 6.6.2 McFarland model with 5000 passengers and 70 drivers

```
set.seed(678)
nd <- 70
np <- 5000
s < -0.1
sp <- 1e-3
spp <- -sp/(1 + sp)
mcf1 <- allFitnessEffects(noIntGenes = c(rep(s, nd), rep(spp, np)),</pre>
                           drvNames = seq.int(nd))
mcf1s <- oncoSimulIndiv(mcf1,</pre>
                          model = "McFL",
                          mu = 1e-7,
                          detectionProb = "default",
                          detectionSize = NA,
                          detectionDrivers = NA,
                          sampleEvery = 0.025,
                          keepEvery = 8,
                          initSize = 2000,
                          finalTime = 4000,
                          onlyCancer = FALSE)
summary(mcf1s)
##
     NumClones TotalPopSize LargestClone MaxNumDrivers MaxDriversLast
## 1
##
     NumDriversLargestPop TotalPresentDrivers FinalTime NumIter
## 1
                                              5
                                                     1961
                                                            81003
##
     HittedWallTime HittedMaxTries errorMF minDMratio minBMratio
## 1
              FALSE
                              FALSE 0.0129
                                                   1585
                                                               1972
      OccurringDrivers
##
## 1 5, 24, 30, 57, 67
par(mfrow = c(2, 1))
## I use thinData to make figures smaller and faster
```





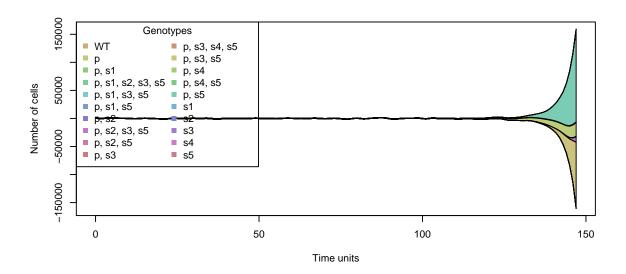
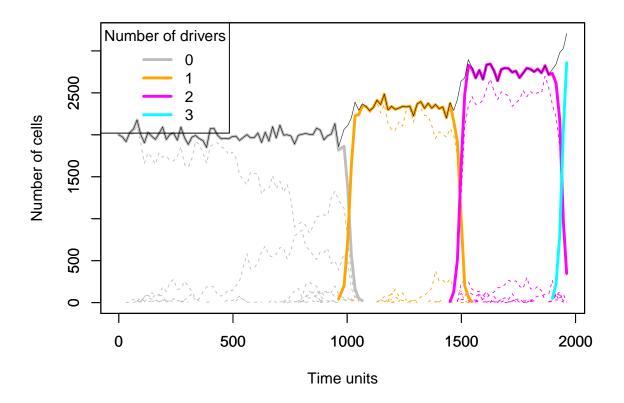
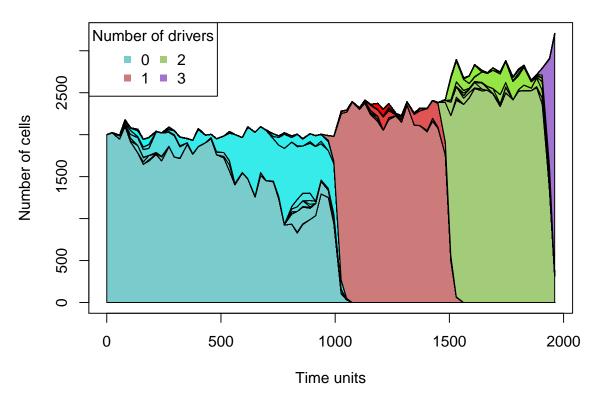


Figure 5: Three genotypes' plots of a simulation of Bauer's model





With the above output (where we see there are over 500 different genotypes) trying to represent the genotypes makes no sense.

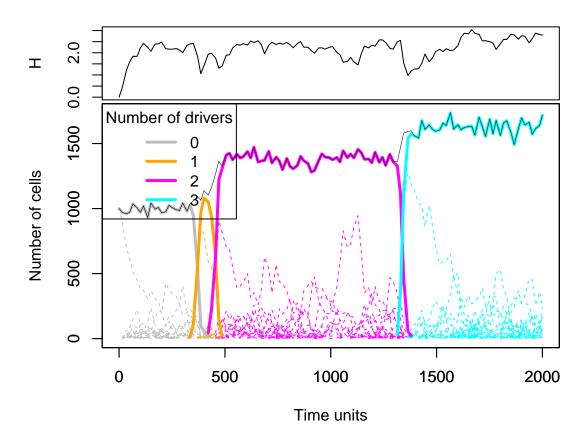
## 6.6.3 McFarland model with 50,000 passengers and 70 drivers: clonal competition

The next is too slow (takes a couple of minutes in an i5 laptop) and too big to run in a vignette, because we keep track of over 4000 different clones (which leads to a result object of over 800 MB):

```
set.seed(123)
nd <- 70
np <- 50000
s <- 0.1
sp <- 1e-4 ## as we have many more passengers
spp \leftarrow -sp/(1 + sp)
mcfL <- allFitnessEffects(noIntGenes = c(rep(s, nd), rep(spp, np)),</pre>
                            drvNames = seq.int(nd))
mcfLs <- oncoSimulIndiv(mcfL,</pre>
                           model = "McFL",
                           mu = 1e-7,
                           detectionSize = 1e8,
                           detectionDrivers = 100,
                           sampleEvery = 0.02,
                           keepEvery = 2,
                           initSize = 1000,
                           finalTime = 2000,
                           onlyCancer = FALSE)
```

But you can access the pre-stored results and plot them (beware: this object has been trimmed by removing empty passenger rows in the Genotype matrix)

```
data(mcfLs)
plot(mcfLs, addtot = TRUE, lwdClone = 0.9, log = "",
    thinData = TRUE, thinData.keep = 0.3,
    plotDiversity = TRUE)
```

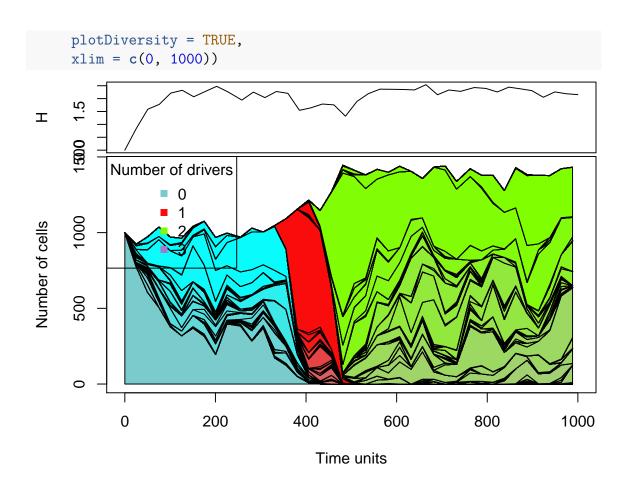


The argument plotDiversity = TRUE asks to show a small plot on top with Shannon's diversity index.

```
summary(mcfLs)
##
     NumClones TotalPopSize LargestClone MaxNumDrivers MaxDriversLast
## 1
                        1718
                                       253
##
     NumDriversLargestPop TotalPresentDrivers FinalTime NumIter
## 1
                                             70
                                                     2000
                                                            113759
##
     HittedWallTime HittedMaxTries errorMF minDMratio minBMratio
## 1
              FALSE
                              FALSE 0.01922
                                                  184.1
                                                              199.6
     OccurringDrivers
##
## 1
       13, 38, 40, 69
## number of passengers per clone
summary(colSums(mcfLs$Genotypes[-(1:70), ]))
##
      Min. 1st Qu.
                    Median
                               Mean 3rd Qu.
                                                Max.
##
      0.00
              4.00
                                        7.75
                       6.00
                               5.67
                                               13.00
```

Note that we see clonal competition between clones with the same number of drivers (and with different drivers, of course). We will return to this (section 6.6.6).

A stacked plot might be better to show the extent of clonal competition (plotting takes some time —a stream plot reveals similar patterns and is also slower than the line plot). I will aggressively thin the data for this plot so it is faster and smaller (but we miss some of the fine grain, of course):



### 6.6.4 Loading fitnessEffects data for simulation examples

We will use several of the previous examples. Most of them are in file examplesFitnessEffects, where they are stored inside a list, with named components (names the same as in the examples above):

```
data(examplesFitnessEffects)
names(examplesFitnessEffects)
    [1] "cbn1"
                  "cbn2"
                            "smn1"
                                               "fp3"
                                                         "fp4m"
                                                                   "o3"
##
                                     "xor1"
    [8] "ofe1"
                  "ofe2"
                                     "sv"
                                               "svB"
                                                         "svB1"
##
                            "foi1"
                                                                   "sv2"
                                                                  "w"
## [15] "sm1"
                  "e2"
                            "E3A"
                                     "em"
                                               "fea"
                                                         "fbauer"
## [22] "pancr"
```

### 6.6.5 Simulation with a conjunction example

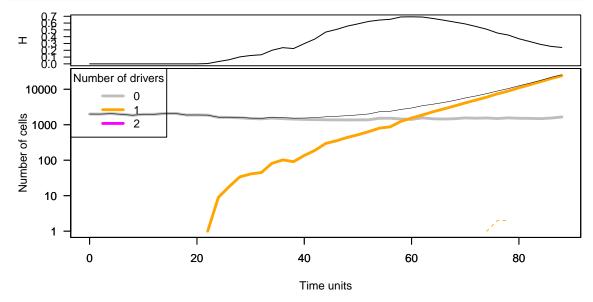
We will simulate using the simple CBN-like restrictions of section 3.5.4 with two different models.

```
data(examplesFitnessEffects)
evalAllGenotypes(examplesFitnessEffects$cbn1, order = FALSE)[1:10, ]
## Genotype Fitness
```

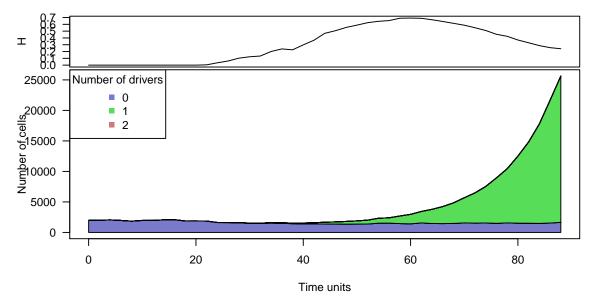
```
## 1
                  1.10
## 2
             b
                  1.10
## 3
                  0.10
             С
## 4
             d
                  1.10
## 5
                  1.10
             е
## 6
                  0.10
             g
## 7
                  1.21
          a, b
## 8
          a, c
                  0.11
## 9
          a, d
                  1.21
## 10
          a, e
                  1.21
sm <-
       oncoSimulIndiv(examplesFitnessEffects$cbn1,
                      model = "McFL",
                       mu = 5e-7,
                       detectionSize = 1e8,
                       detectionDrivers = 2,
                       detectionProb = "default",
                       sampleEvery = 0.025,
                       keepEvery = 5,
                       initSize = 2000,
                       onlyCancer = TRUE)
summary(sm)
     {\tt NumClones\ TotalPopSize\ LargestClone\ MaxNumDrivers\ MaxDriversLast}
## 1
             6
                        2721
                                     2005
##
     NumDriversLargestPop TotalPresentDrivers FinalTime NumIter
## 1
                                              4
                                                     2257
                                                             90282
##
     HittedWallTime HittedMaxTries errorMF minDMratio minBMratio
                              FALSE 0.01502
## 1
              FALSE
                                                 309424
                                                            333333
##
     OccurringDrivers
           a, b, c, e
set.seed(1234)
evalAllGenotypes(examplesFitnessEffects$cbn1, order = FALSE,
                 model = "Bozic")[1:10, ]
##
      Genotype Death_rate
## 1
                     0.90
             a
## 2
             b
                     0.90
## 3
                     1.90
             С
## 4
             d
                     0.90
## 5
                     0.90
             е
                     1.90
## 6
             g
## 7
          a, b
                     0.81
                     1.71
## 8
          a, c
## 9
          a, d
                     0.81
                     0.81
## 10
          a, e
       oncoSimulIndiv(examplesFitnessEffects$cbn1,
sb <-
                        model = "Bozic",
```

```
mu = 5e-6,
                       detectionProb = "default",
                       detectionSize = 1e8,
                       detectionDrivers = 4,
                        sampleEvery = 2,
                        initSize = 2000,
                        onlyCancer = TRUE)
summary(sb)
     NumClones TotalPopSize LargestClone MaxNumDrivers MaxDriversLast
## 1
             7
                       25636
                                    23975
     NumDriversLargestPop TotalPresentDrivers FinalTime NumIter
##
## 1
                        1
                                             5
##
     HittedWallTime HittedMaxTries errorMF minDMratio minBMratio
## 1
              FALSE
                              FALSE
                                         NA
                                                  33333
                                                             33333
     OccurringDrivers
## 1
        a, b, c, e, g
```

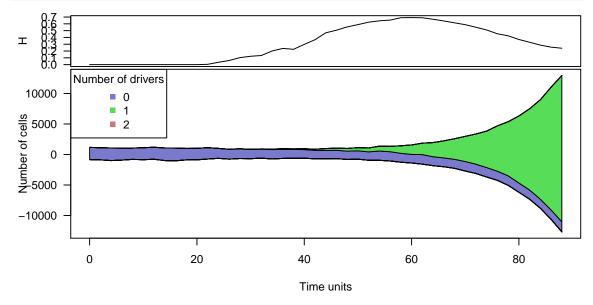
As usual, we will use several plots here.



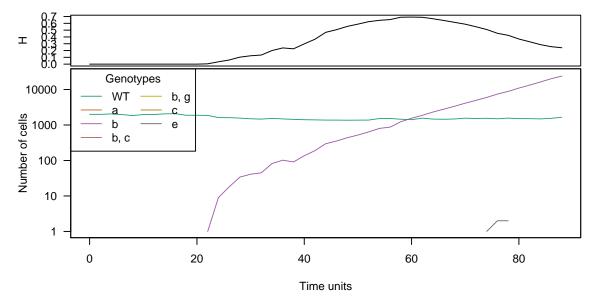
```
## Drivers, stacked
par(cex = 0.75, las = 1)
plot(sb,show = "drivers", type = "stacked", plotDiversity = TRUE)
```



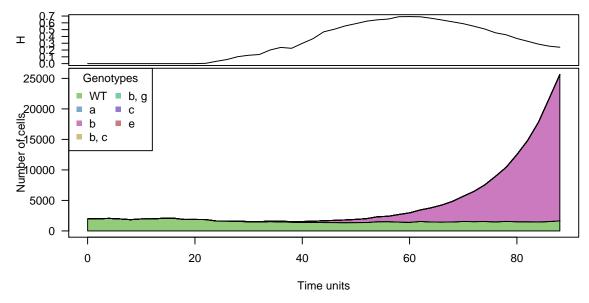
```
## Drivers, stream
par(cex = 0.75, las = 1)
plot(sb,show = "drivers", type = "stream", plotDiversity = TRUE)
```



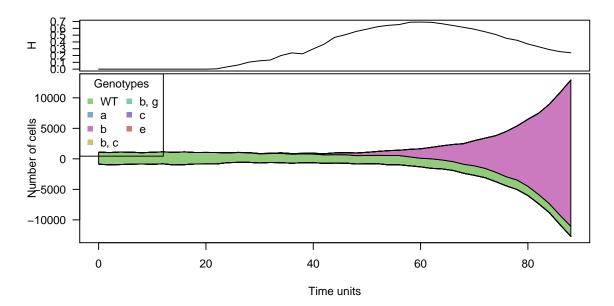
```
## Genotypes, line plot
par(cex = 0.75, las = 1)
plot(sb,show = "genotypes", type = "line", plotDiversity = TRUE)
```



```
## Genotypes, stacked
par(cex = 0.75, las = 1)
plot(sb,show = "genotypes", type = "stacked", plotDiversity = TRUE)
```



```
## Genotypes, stream
par(cex = 0.75, las = 1)
plot(sb,show = "genotypes", type = "stream", plotDiversity = TRUE)
```

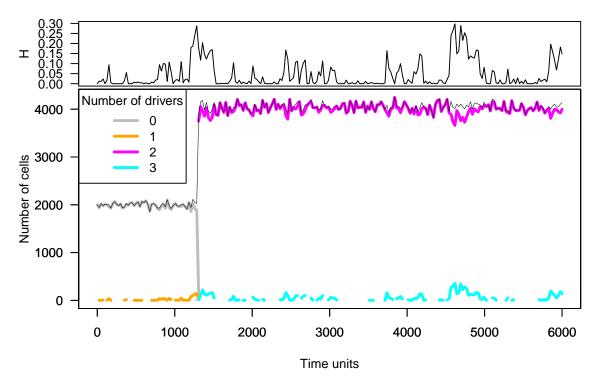


The above illustrates again that different types of plots can be useful to reveal different patterns in the data. For instance, here, because of the huge relative frequency of one of the clones/genotypes, the stacked and stream plots do not reveal the other clones/genotypes as we cannot use a log-transformed y-axis, even if there are other clones/genotypes present.

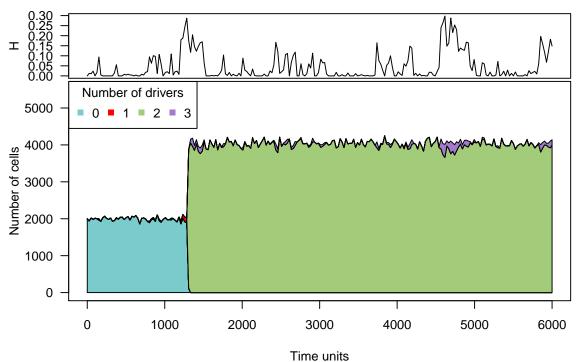
### 6.6.6 Simulation with order effects and McFL model

(We use a somewhat large mutation rate than usual, so that the simulation runs quickly.)

We show a stacked and a line plot of the drivers:



```
par(las = 1, cex = 0.85)
plot(tmp, type = "stacked", plotDiversity = TRUE,
    ylim = c(0, 5500), legend.ncols = 4,
    thinData = TRUE, thinData.keep = 0.2)
```

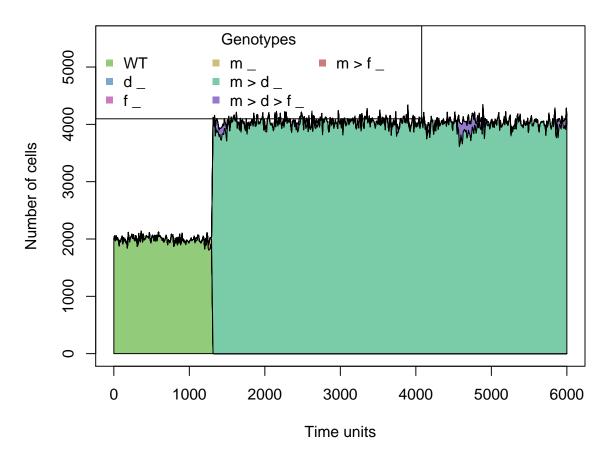


In this example (and at least under Linux, with both GCC and clang), we can see that the mutants with three drivers do not get established when we stop the simulation at time 6000. This is one case where the summary statistics about number

of drivers says little of value, as fitness is very different for genotypes with the same number of mutations, and does not increase in a simple way with drivers:

```
evalAllGenotypes(examplesFitnessEffects[["o3"]], addwt = TRUE,
                  order = TRUE)
##
       Genotype Fitness
## 1
                    1.00
             WT
## 2
              d
                    1.00
## 3
              f
                    1.00
## 4
              m
                    1.00
## 5
          d > f
                    1.00
          d > m
## 6
                    1.10
## 7
          f > d
                    1.00
## 8
          f > m
                    1.00
## 9
          m > d
                    1.50
## 10
          m > f
                    1.00
## 11 d > f > m
                    1.54
## 12 d > m > f
                    1.32
## 13 f > d > m
                    0.77
## 14 f > m > d
                    1.50
## 15 m > d > f
                    1.50
## 16 m > f > d
                    1.50
```

A few figures could help:

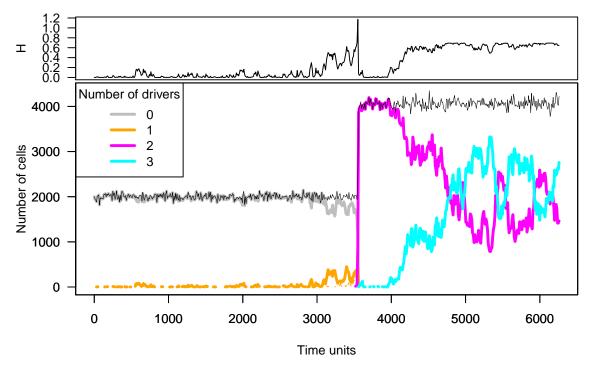


(When reading the figure legends, recall that genotype  $x > y \_ z$  is one where a mutation in "x" happened before a mutation in "y", and there is also a mutation in "z" for which order does not matter. Here, there are no genes for which order does not matter and thus there is nothing after the " $\_$ ").

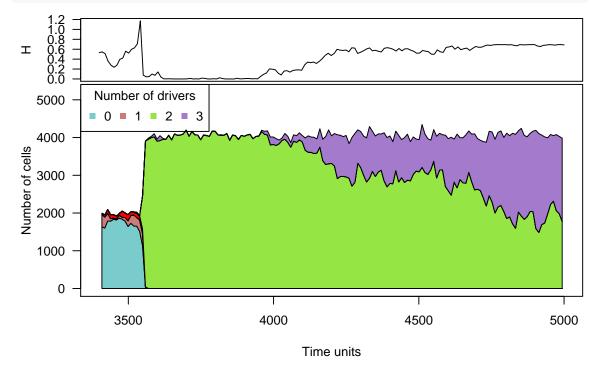
In this case, the clones with three drivers end up displacing those with two by the time we stop; moreover, notice how those with one driver never really grow to a large population size, so we basically go from a population with clones with zero drivers to a population made of clones with two or three drivers:

```
## Individual OncoSimul trajectory with call:
    oncoSimulIndiv(fp = examplesFitnessEffects[["o3"]], model = "McFL",
##
       mu = 5e-05, detectionSize = 1e+08, detectionDrivers = 3,
       sampleEvery = 0.025, initSize = 2000, keepEvery = 5, extraTime = 1500,
##
##
       finalTime = 20000, onlyCancer = FALSE, max.num.tries = 10)
##
##
     NumClones TotalPopSize LargestClone MaxNumDrivers MaxDriversLast
## 1
                       4222
                                    2758
##
     NumDriversLargestPop TotalPresentDrivers FinalTime NumIter
## 1
                                             3
                                                    6259
##
     HittedWallTime HittedMaxTries errorMF minDMratio minBMratio
## 1
              FALSE
                             FALSE 0.01442
                                                  6161
                                                             6667
##
     OccurringDrivers
## 1
              d, f, m
##
## Final population composition:
         Genotype
                     N
## 1
                     0
## 2
                     0
             d
         d > f _
## 3
                     0
## 4
             f
## 5
             m _
         m > d
## 6
                  1464
## 7 m > d > f
                  2758
## 8
         m > f
```

use a drivers plot:

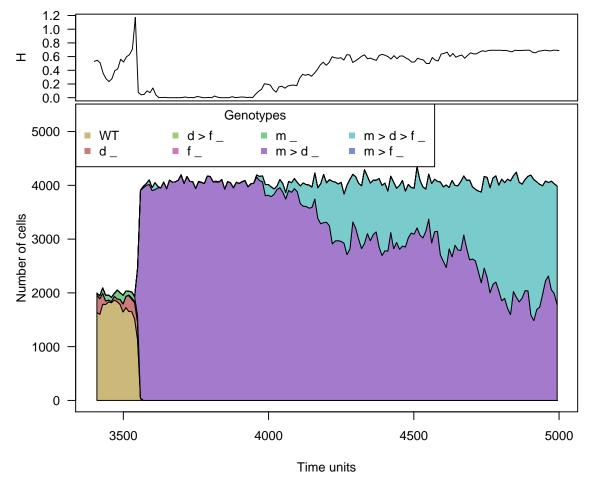


```
par(las = 1, cex = 0.85)
plot(tmp, type = "stacked", plotDiversity = TRUE,
    legend.ncols = 4, ylim = c(0, 5200), xlim = c(3400, 5000),
    thinData = TRUE, thinData.keep = 0.5)
```



Now show the genotypes explicitly:

```
## Improve telling apart the most abundant
## genotypes by sorting colors
## differently via breakSortColors
```



As before, the argument plotDiversity = TRUE asks to show a small plot on top with Shannon's diversity index. Here, as before, the quick clonal expansion of the clone with two drivers leads to a sudden drop in diversity (for a while, the population is made virtually of a single clone). Note, however, that compared to section 6.6.3, we are modeling here a scenario with very few genes, and correspondingly very few possible genotypes, and thus it is not strange that we observe very little diversity.

(We have used extraTime to continue the simulation well past the point of detection, here specified as three drivers. Instead of specifying extraTime we can set the detectionDrivers value to a number larger than the number of existing possible drivers, and the simulation will run until finalTime if onlyCancer = FALSE.)

### 6.7 Interactive graphics

It is possible to create interactive stacked area and stream plots using the *streamgraph* package, available from https://github.com/hrbrmstr/streamgraph. However, that package is not available as a CRAN or BioConductor package, and thus we cannot depend on it for this vignette (or this package). You can, however, paste the code below and make it run locally.

Before calling the streamgraph function, though, we need to convert the data from the original format in which it is stored into "long format". A simple convenience function is provided as OncoSimulWide2Long in *OncoSimulR*.

As an example, we will use the data we generated above for section 6.6.1.

## 7 Sampling multiple simulations

Often, you will want to simulate multiple runs of the same scenario, and then obtain the matrix of runs by mutations (a matrix of individuals/samples by genes or, equivalently, a vector of "genotypes"), and do something with them. OncoSimulR offers several ways of doing this.

The key function here is samplePop, either called explicitly after oncoSimulPop (or oncoSimulIndiv), or implicitly as part of a call to oncoSimulSample. With samplePop you can use single cell or whole tumor sampling (for details see the help of samplePop). Depending on how the simulations were conducted, you might also sample at different times, or as a function of population sizes. A major difference between procedures has to do with whether or not you want to keep the complete history of the simulations.

You want to keep the complete history of simulations. You will simulate using:

- oncoSimulIndiv repeatedly (maybe within mclapply, to parallelize the run).
- oncoSimulPop. oncoSimulPop is basically a thin wrapper around oncoSimulIndiv that uses mclapply.

In both cases, you specify the conditions for ending the simulations (as explained in 6.3). Then, you use function samplePop to obtain the matrix of samples by mutations.

You do not want to keep the complete history of the simulations. You will simulate using:

- oncoSimulIndiv repeatedly, with argument keepEvery = NA.
- oncoSimulPop, with argument keepEvery = NA.
  - In both cases you specify the conditions for ending the simulations (as explained in 6.3). Then, you use function samplePop.
- oncoSimulSample, specifying the conditions for ending the simulations (as explained in 6.3). In this case, you will not use samplePop, as that is implicitly called by oncoSimulSample. The output is directly the matrix (and a little bit of summary from each run), and during the simulation it only stores one time point.

Why the difference between the above cases? If you keep the complete history, you can take samples at any of the times between the beginning and the end of the simulations. If you do not keep the history, you can only sample at the time the simulation exited. Why would you want to use the second route? If we are only interested in the final matrix of individuals by mutations, keeping the complete history above is wasteful because we store fully all of the simulations (for example in the call to oncoSimulPop) and then sample (in the call to samplePop). Further criteria to use when choosing between sampling procedures is whether you need

detectionSize and detectionDrivers do differ between simulations: if you use oncoSimulPop the arguments for detectionSize and detectionDrivers must be the same for all simulations but this is not the case for oncoSimulSample. See further comments in 7.2. Finally, parallelized execution is available for oncoSimulPop but, by design, not for oncoSimulSample.

The following are a few examples. First we run oncoSimulPop to obtain 4 simulations and in the last line we sample from them:

```
pancrPop <- oncoSimulPop(4, pancr,</pre>
                           detectionSize = 1e7,
                           keepEvery = 10,
                           mc.cores = 2)
summary(pancrPop)
##
     NumClones TotalPopSize LargestClone MaxNumDrivers MaxDriversLast
## 1
              8
                     10946839
                                    10871880
## 2
             12
                                                           0
                                                                            0
                     11014517
                                    10305505
                                                           0
## 3
             15
                     10855196
                                     8836921
                                                                            0
## 4
                     10487828
                                                           0
                                                                            0
             11
                                    10387174
##
     NumDriversLargestPop TotalPresentDrivers FinalTime NumIter
## 1
                          0
                                                 0
                                                          950
                                                                  1685
                          0
## 2
                                                 0
                                                          220
                                                                   928
                          0
## 3
                                                 0
                                                         1632
                                                                  2067
                          0
                                                 0
                                                         1227
## 4
                                                                  1911
##
     HittedWallTime HittedMaxTries errorMF minDMratio minBMratio
## 1
                                            NA
                                                    142857
               FALSE
                                FALSE
                                                                 142857
## 2
                                FALSE
                                            NA
               FALSE
                                                    142857
                                                                 142857
## 3
               FALSE
                                            NA
                                FALSE
                                                    142857
                                                                 142857
## 4
               FALSE
                                FALSE
                                            NA
                                                    142857
                                                                 142857
##
     OccurringDrivers
## 1
## 2
## 3
## 4
samplePop(pancrPop)
##
    Subjects by Genes matrix of 4 subjects and 7 genes.
##
         CDNK2A KRAS MLL3 PXDN SMAD4 TGFBR2 TP53
##
## [1,]
                         0
                               0
                                      0
                                                   0
              0
                    1
                                              0
## [2,]
              0
                    1
                         0
                               0
                                      0
                                              0
                                                   0
                    1
                         1
                               0
                                              0
                                                   0
## [3,]
              0
                                      0
## [4,]
                    1
                         0
                               0
                                      0
                                                   0
```

Now a simple multiple call to oncoSimulIndiv wrapped inside mclapply; this is basically the same we just did above. We set the class of the object to allow direct usage of samplePop. (Note: in Windows mc.cores > 1 is not supported, so for the

vignette to run in Windows, Linux, and Mac we explicitly set it here in the call to mclapply. For regular usage, you will not need to do this; just use whatever is appropriate for your operating system and number of cores. As well, we do not need any of this with oncoSimulPop because the code inside oncoSimulPop already takes care of setting mc.cores to 1 in Windows).

```
library(parallel)
if(.Platform$OS.type == "windows") {
    mc.cores <- 1
} else {
    mc.cores <- 2
}
p2 <- mclapply(1:4, function(x) oncoSimulIndiv(pancr,
                                                   detectionSize = 1e7,
                                                   keepEvery = 10),
                                                   mc.cores = mc.cores)
class(p2) <- "oncosimulpop"</pre>
samplePop(p2)
##
##
    Subjects by Genes matrix of 4 subjects and 7 genes.
        CDNK2A KRAS MLL3 PXDN SMAD4 TGFBR2 TP53
##
## [1,]
              0
                   1
                              0
                         0
                                     0
                                                  0
## [2,]
              0
                   1
                         0
                              0
                                     0
                                            0
                                                  0
                                            0
                                                  0
## [3,]
              0
                   1
                         0
                              0
                                     0
              0
                   1
                         0
                              0
                                     0
                                            0
                                                  0
## [4,]
```

Above, we have kept the complete history of the simulations as you can check by doing, for instance

```
tail(pancrPop[[1]]$pops.by.time)
##
          [,1] [,2] [,3]
                               [,4] [,5] [,6]
                                                [,7] [,8]
                                                            [,9]
## [91,]
          900 2822
                             74715
                                       0
                                             0
                                                   0
                                                               0
                        0
                                                         0
## [92,]
          910 3077
                        5
                            200221
                                       4
                                             1
                                                   9
                                                               4
                                                         0
## [93,]
          920 3189
                        3
                            543301
                                      12
                                             0
                                                  36
                                                         1
                                                              46
## [94,]
          930 3151
                                      79
                                             1
                                                 602
                                                         2
                                                             327
                      26
                           1472375
## [95,]
                     162
          940 3339
                           4010774
                                     530
                                             5
                                                4985
                                                         5
                                                            2896
## [96,]
          950 3202 1728 10871880 4546
                                             7 41214
                                                        13 24249
```

If we were not interested in the complete history of simulations we could have done instead (note the argument keepEvery = NA)

```
summary(pancrPopNH)
     NumClones TotalPopSize LargestClone MaxNumDrivers MaxDriversLast
##
## 1
             10
                     10486872
                                    9758231
                                                          0
## 2
             12
                                                          0
                                                                           0
                     10035970
                                    9365305
## 3
              9
                                                          0
                                                                           0
                     10964671
                                   10849615
## 4
             13
                     10699972
                                    9938986
                                                          0
                                                                           0
##
     NumDriversLargestPop TotalPresentDrivers FinalTime NumIter
## 1
                          0
                                                0
                                                        1687
                                                                 2371
## 2
                          0
                                                0
                                                        1247
                                                                 1896
## 3
                          0
                                                0
                                                        2129
                                                                 2861
                          0
                                                         441
## 4
                                                0
                                                                 1100
     HittedWallTime HittedMaxTries errorMF minDMratio minBMratio
##
## 1
               FALSE
                               FALSE
                                            NA
                                                    142857
                                                                142857
## 2
               FALSE
                               FALSE
                                            NA
                                                   142857
                                                                142857
## 3
                               FALSE
                                            NA
               FALSE
                                                   142857
                                                                142857
## 4
               FALSE
                               FALSE
                                            NA
                                                   142857
                                                                142857
##
     OccurringDrivers
## 1
## 2
## 3
## 4
samplePop(pancrPopNH)
##
##
    Subjects by Genes matrix of 4 subjects and 7 genes.
##
        CDNK2A KRAS MLL3 PXDN SMAD4 TGFBR2 TP53
## [1,]
              0
                   1
                         0
                              0
## [2,]
                                                  0
              0
                   1
                         0
                               0
                                     0
                                             0
## [3,]
              0
                   1
                         0
                               0
                                     0
                                             0
                                                  0
## [4,]
              0
                   1
                         0
                               0
                                     0
                                                  0
                                             0
```

which only keeps the very last sample:

```
pancrPopNH[[1]]$pops.by.time
## [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [,10] [,11]
## [1,] 1687 8445 20135 6 9758231 689061 30 9 5887 4 5064
```

Or we could have used oncoSimulSample:

```
pancrSamp <- oncoSimulSample(4, pancr)</pre>
## Successfully sampled 4 individuals
##
    Subjects by Genes matrix of 4 subjects and 7 genes.
pancrSamp$popSamp
        CDNK2A KRAS MLL3 PXDN SMAD4 TGFBR2 TP53
## [1,]
              0
                    1
                         0
                               0
                                     0
                                             0
                                                  0
## [2,]
              0
                    1
                         0
                               0
                                     0
                                             0
                                                  0
                                                  0
## [3,]
              0
                    1
                         0
                               0
                                     0
                                             0
```

## [4,] 0 1 0 0 0 0

Again, why the above differences? If we are only interested in the final matrix of populations by mutations, keeping the complete history the above is wasteful, because we store fully all of the simulations (in the call to oncoSimulPop) and then sample (in the call to samplePop).

# 7.1 Whole-tumor and single-cell sampling, and do we always want to sample?

samplePop is designed to emulate the process of obtaining a sample from a (set of) "patient(s)". But there is no need to sample. The history of the population, with a granularity that is controlled by argument keepEvery, is kept in the matrix pops.by.time which contains the number of cells of every clone at every sampling point (see further details in 11.1). This is the information used in the plots that show the trajectory of a simulation, the plots that show the change in genotype or driver abundance over time (see section 6.5 and examples mentioned there).

Regardless of whether and how you plot the information in pops.by.time, you can also sample one or multiple simulations using samplePop. In whole-tumor sampling the resolution is the whole tumor (or the whole population). Thus, a key argument is thresholdWhole, the threshold for detecting a mutation: a gene is considered mutated if it is altered in at least "thresholdWhole" proportion of the cells in that simulation (at a particular time point). This of course means that your "sampled genotype" might not correspond to any existing genotype because we are summing over all cells in the population; for instance, suppose that at the time we take the sample there are only two clones in the population, one clone with a frequency of 0.4 that has gene A mutated, and a second clone one with a frequency of 0.6 that has gene B mutated. If you set thresholdWhole to values  $\leq 0.4$  the sampled genotype will show both A and B mutated. Single-cell sampling is provided as an option in contrast to whole-tumor sampling. Here any sampled genotype will correspond to an existing genotype as you are sampling with single-cell resolution.

When samplePop is run on a set of simulated data of, say, 100 simulated trajectories (100 "subjects"), it will produce a matrix with 100 rows (100 "subjects"). But if it makes sense in the context of your problem (e.g., multiple samples per patient?) you can of course run samplePop repeatedly.

# 7.2 Differences between "samplePop" and "oncoSimulSample"

samplePop provides two sampling times: "last" and "uniform". It also allows you to sample at the first sample time(s) at which the population(s) reaches a given size, which can be either the same or different for each simulation (with argument popSizeSample). "last" means to sample each individual in the very last time period

of the simulation. "uniform" means sampling each individual at a time chosen uniformly from all the times recorded in the simulation between the time when the first driver appeared and the final time period. "unif" means that it is almost sure that different individuals will be sampled at different times. "last" does not guarantee that different individuals will be sampled at the same time unit, only that all will be sampled in the last time unit of their simulation.

With oncoSimulSample we obtain samples that correspond to timeSample = "last" in samplePop by specifying a unique value for detectionSize and detectionDrivers. The data from each simulation will correspond to the time point at which those are reached (analogous to timeSample = "last"). How about uniform sampling? We pass a vector of detectionSize and detectionDrivers, where each value of the vector comes from a uniform distribution. This is not identical to the "uniform" sampling of oncoSimulSample, as we are not sampling uniformly over all time periods, but are stopping at uniformly distributed values over the stopping conditions. Arguably, however, the procedure in samplePop might be closer to what we mean with "uniformly sampled over the course of the disease" if that course is measured in terms of drivers or size of tumor.

An advantage of oncoSimulSample is that we can specify arbitrary sampling schemes, just by passing the appropriate vector detectionSize and detectionDrivers. A disadvantage is that if we change the stopping conditions we can not just resample the data, but we need to run it again.

There is no difference between oncoSimulSample and oncoSimulPop + samplePop in terms of the typeSample argument (whole tumor or single cell).

Finally, there are some additional differences between the two functions. oncoSimulPop can run parallelized (it uses mclapply). This is not done with oncoSimulSample because this function is designed for simulation experiments where you want to examine many different scenarios simultaneously. Thus, we provide additional stopping criteria (max.wall.time.total and max.num.tries.total) to determine whether to continue running the simulations, that bounds the total running time of all the simulations in a call to oncoSimulSample. And, if you are running multiple different scenarios, you might want to make multiple, separate, independent calls (e.g., from different R processes) to oncoSimulSample, instead of relying in mclapply, since this is likely to lead to better usage of multiple cores/CPUs if you are examining a large number of different scenarios.

### 8 Showing the genealogical relationships of clones

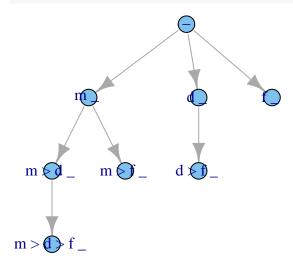
If you run simulations with keepPhylog = TRUE, the simulations keep track of when every clone is generated, and that will allow us to see the parent-child relationships between clones. (This is disabled by default: the code runs a little bit slower and the result is larger.)

Let us re-run a previous example:

```
set.seed(15)
tmp <- oncoSimulIndiv(examplesFitnessEffects[["o3"]],</pre>
                        model = "McFL",
                        mu = 5e-5,
                        detectionSize = 1e8,
                        detectionDrivers = 3,
                        sampleEvery = 0.025,
                        max.num.tries = 10,
                        keepEvery = 5,
                        initSize = 2000,
                        finalTime = 20000,
                        onlyCancer = FALSE,
                        extraTime = 1500,
                        keepPhylog = TRUE
tmp
##
  Individual OncoSimul trajectory with call:
##
    oncoSimulIndiv(fp = examplesFitnessEffects[["o3"]], model = "McFL",
       mu = 5e-05, detectionSize = 1e+08, detectionDrivers = 3,
##
##
       sampleEvery = 0.025, initSize = 2000, keepEvery = 5, extraTime = 1500,
       finalTime = 20000, onlyCancer = FALSE, keepPhylog = TRUE,
##
##
       max.num.tries = 10)
##
##
     NumClones TotalPopSize LargestClone MaxNumDrivers MaxDriversLast
             8
## 1
                        4222
                                     2758
                                                        3
                                                                       3
##
     NumDriversLargestPop TotalPresentDrivers FinalTime NumIter
## 1
                         3
                                              3
                                                     6259
##
     HittedWallTime HittedMaxTries errorMF minDMratio minBMratio
                              FALSE 0.01442
                                                               6667
## 1
              FALSE
                                                   6161
##
     OccurringDrivers
## 1
              d, f, m
##
## Final population composition:
##
         Genotype
                      N
## 1
                      0
## 2
             d
                      0
## 3
         d > f
```

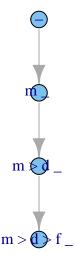
We can plot the parent-child relationships<sup>12</sup> of every clone ever created (with fitness larger than 0—clones without viability are never shown):

#### plotClonePhylog(tmp, N = 0)



However, we often only want to show clones that exist (have number of cells > 0) at a certain time (while of course showing all of their ancestors, even if those are now extinct —i.e., regardless of their current numbers).

#### plotClonePhylog(tmp, N = 1)

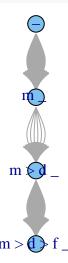


If we set keepEvents = TRUE the arrows show how many times each clone appeared:

<sup>&</sup>lt;sup>12</sup>There are several packages in R devoted to phylogenetic inference and related issues. For instance, *ape*. I have not used that infrastructure because of our very specific needs and circumstances; for instance, internal nodes are observed, we can have networks instead of trees, and we have no uncertainty about when events occurred.

(The next can take a while)

```
plotClonePhylog(tmp, N = 1, keepEvents = TRUE)
```



And we can show the plot so that the vertical axis is proportional to time (though you might see overlap of nodes if a child node appeared shortly after the parent):

```
plotClonePhylog(tmp, N = 1, timeEvents = TRUE)
```



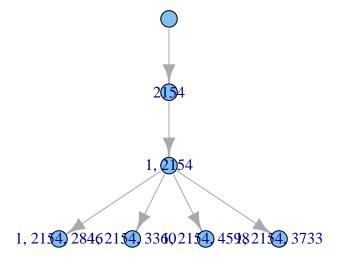
We can obtain the adjacency matrix doing

We can see another example here:

```
set.seed(456)
```

Showing only clones that exist at the end of the simulation (and all their parents):

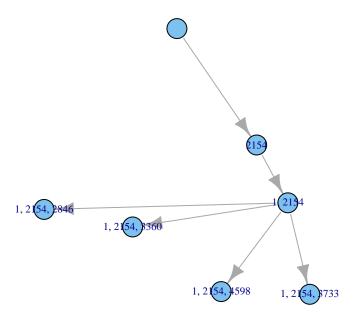
#### plotClonePhylog(mcf1s, N = 1)



Notice that the labels here do not have a "\_", since there were no order effects in fitness. However, the labels show the genes that are mutated, just as before.

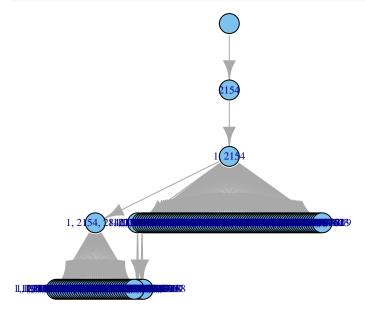
Similar, but with vertical axis proportional to time:

```
par(cex = 0.7)
plotClonePhylog(mcf1s, N = 1, timeEvents = TRUE)
```



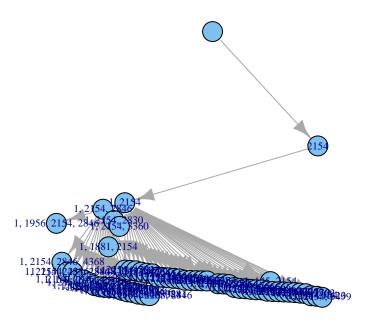
What about those that existed in the last 200 time units?

```
par(cex = 0.7)
plotClonePhylog(mcf1s, N = 1, t = c(800, 1000))
```



And try now to show also when the clones appeared (we restrict the time to between 900 and 1000, to avoid too much clutter):

```
par(cex = 0.7)
plotClonePhylog(mcf1s, N = 1, t = c(900, 1000), timeEvents = TRUE)
```

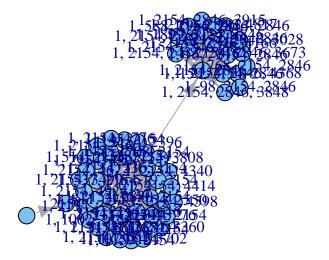


(By playing with t, it should be possible to obtain animations of the phylogeny. We will not pursue it here.)

If the previous graph seems cluttered, we can represent it in a different way by calling *igraph* directly after storing the graph and using the default layout:

```
g1 <- plotClonePhylog(mcf1s, N = 1, t = c(900, 1000),
returnGraph = TRUE)
```

#### plot(g1)



which might be easier to show complex relationships or identify central or key clones.

It is of course quite possible that, especially if we consider few genes, the parent-child relationships will form a network, not a tree, as the same child node can have multiple parents. You can play with this example, modified from one we saw before (section 3.5.6):

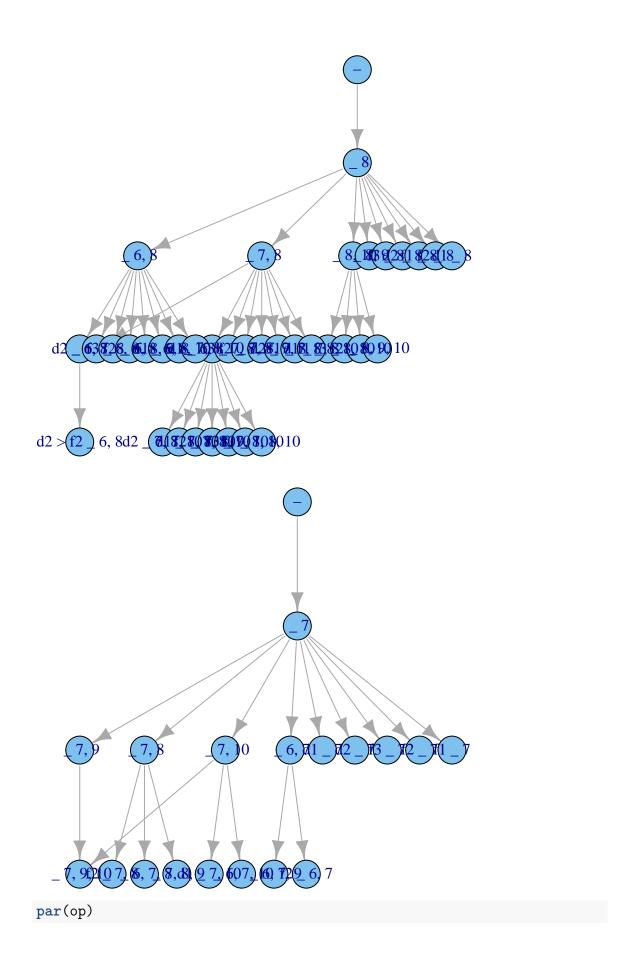
```
op <- par(ask = TRUE)
while(TRUE) {</pre>
```

### 8.1 Parent-child relationships from multiple runs

If you use oncoSimulPop you can store and plot the "phylogenies" of the different runs:

We will plot the first two:

```
op <- par(mar = rep(0, 4), mfrow = c(2, 1))
plotClonePhylog(oiP1[[1]])
plotClonePhylog(oiP1[[2]])</pre>
```



This is so far disabled in function <code>oncoSimulSample</code>, since that function is optimized for other uses. This might change in the future.

### 9 Generating random fitness landscapes

In most of the examples seen above, we have fully specified the fitness of the different genotypes (either by providing directly the full mapping genotypes to fitness, or by providing that mapping by specifying the effects of the different gene combinations). In some cases, however, we might want to specify a particular model that generates the fitness landscape, and then have fitnesses be random variables obtained under this model. In other words, in this random fitness landscape the fitness of the genotypes is a random variable generated under some specific model. Random fitness landscapes are used extensively, for instance, to understand the evolutionary consequences of different types of epistatic interactions (e.g., Szendro, Schenk, et al. (2013), Franke et al. (2011)) and there are especially developed tools for plotting and analyzing random fitness landscapes (e.g., Brouillet et al. (2015)).

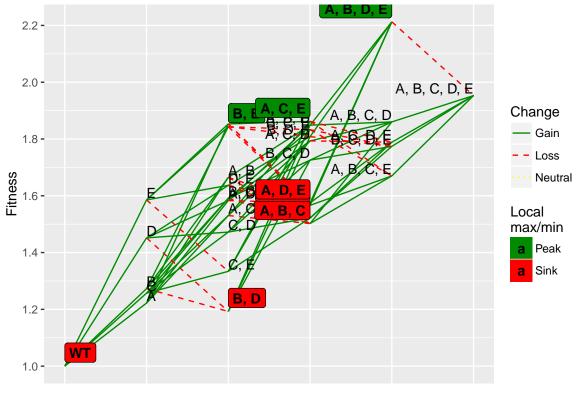
With OncoSimulR it is possible to generate mappings of genotype to fitness using the function rfitness that allows you to use from a pure House of Cards model to a purely additive model. I have followed Szendro, Schenk, et al. (2013) and Franke et al. (2011) and model fitness as

$$f_i = -c \ d(i, reference) + x_i \tag{2}$$

where d(i, j) is the Hamming distance between genotypes i and j (the number of positions that differ), c is the decrease in fitness of a genotype per each unit increase in Hamming distance from the reference genotype, and  $x_i$  is a random variable (in this case, a normal deviate of mean 0 and standard deviation sd). You can change the reference genotype to any of the genotypes: for the deterministic part, you make the fittest genotype be the one with all positions mutated by setting reference = "max", or use the wildtype by using a string of 0s, or randomly select a genotype as a reference by using reference = "random" or reference = "random2".

And by changing c and sd you can flexibly modify the relative weight of the purely House of Cards vs. additive component. The expression used above is also very similar to the one on Greene and Crona (2014) if you use rfitness with the argument reference = "max".

What can you do with these genotype to fitness mappings? You could plot them, you could use them as input for oncoSimulIndiv and related functions, or you could export them (to\_Magellan) and plot them externally (e.g., in MAGELLAN: http://wwwabi.snv.jussieu.fr/public/Magellan/, Brouillet et al. (2015)).



```
oncoSimulIndiv(allFitnessEffects(genotFitness = r1))
##
## Individual OncoSimul trajectory with call:
    oncoSimulIndiv(fp = allFitnessEffects(genotFitness = r1))
##
##
     NumClones TotalPopSize LargestClone MaxNumDrivers MaxDriversLast
##
## 1
             6
                  156344752
                                156304634
     NumDriversLargestPop TotalPresentDrivers FinalTime NumIter
##
## 1
                                                             2521
     HittedWallTime HittedMaxTries errorMF minDMratio minBMratio
##
## 1
              FALSE
                             FALSE
                                         NA
                                                157684
                                                             2e+05
##
     OccurringDrivers
```

```
## 1
## Final population composition:
    Genotype
                     N
##
## 1
                  2412
        A, E
## 2
                  8620
        B, E
## 3
                 25790
        C, E
## 4
                   867
## 5
        D, E
                  2429
## 6 E 156304634
```

# 10 Measures of evolutionary predictability and genotype diversity

Several measures of evolutionary predictability have been proposed in the literature (see, e.g., Szendro, Franke, et al. (2013) and references therein). We provide two, Lines of Descent (LOD) and Paths to the Maximum (POM), following Szendro, Franke, et al. (2013); we also provide a simple measure of diversity of the actual genotypes sampled.

In Szendro, Franke, et al. (2013) "(...) paths defined as the time ordered sets of genotypes that at some time contain the largest subpopulation" are called "path of the maximum" (POM) (see their p. 572). In our case, POM are obtained from the pops.by.time return object (i.e., from the genotypes at each of the sampling times) and, thus, the POMs will be affected by how often we sample and keep samples (arguments sampleEvery and keepEvery), since we are running a continuous time process.

Szendro, Franke, et al. (2013) also define Lines of descent (LODs) which "(...) represent the lineages that arrive at the most populated genotype at the final time". In that same page (572) they provide the details on how the LODs are obtained. My implementation is not exactly identical to the definition given in p. 572 of Szendro et al. First, in case this might be useful, for each simulation I keep all the paths that "(...) arrive at the most populated genotype at the final time" (first paragraph in p. 572 of Szendro et al.), whereas they only keep one (see second column of p. 572). However, I do provide a single LOD for each run, too. This is the first path to arrive at the genotype that eventually becomes the most populated genotype at the final time (and, in this sense, agrees with the LOD of Szendro et al.). However, in contrast to what is apparently done in Szendro ("A given genotype may undergo several episodes of colonization and extinction that are stored by the algorithm, and the last episode before the colonization of the final state is used to construct the step."), I do not check that this genotype (which is the one that will become the most populated at final time) does not become extinct before the final colonization. So there could be other paths (all in all paths) that are actually the one(s) that are colonizers of the most populated genotype (with no extinction before the final colonization).

To briefly show some output, we will use again the 5.5 example:

```
mc.cores = 2)
## Look a the first POM
str(POM(pancr16)[1:3])
## List of 3
## $ : chr [1:2] "" "KRAS"
## $ : chr [1:2] "" "KRAS"
## $ : chr [1:2] "" "KRAS, TP53"
## Note here that for each simulation there is a "all paths" and
## a "lod_single", as explained above
LOD(pancr16)[1:2]
## [[1]]
## [[1]]$all_paths
## [[1]]$all paths[[1]]
## + 2/? vertices, named:
## [1]
            KRAS
##
##
## [[1]]$lod_single
## + 2/? vertices, named:
## [1]
            KRAS
##
##
## [[2]]
## [[2]]$all_paths
## [[2]]$all_paths[[1]]
## + 2/? vertices, named:
## [1]
            KRAS
##
##
## [[2]]$lod_single
## + 2/? vertices, named:
## [1]
            KRAS
## The diversity of LOD (lod_single) and POM might or might not
## be identical
diversityPOM(POM(pancr16))
## [1] 1.363
diversityLOD(LOD(pancr16))
## [1] 0.918
## Show the genotypes and their diversity (which might, or might
## not, differ from the diversity of LOD and POM)
sampledGenotypes(samplePop(pancr16))
##
```

### 11 FAQ, odds and ends

# 11.0.1 What we mean by "clone"; and "I want clones disregarding passengers"

In this vignette we often use "clone" or "genotype" interchangeably. A clone denotes a set of cells that have identical genotypes. So if you are using a fitness specification with four genes (i.e., your genome has only four loci), there can be up to  $16 = 2^4$  different genotypes or clones. Any two entities that differ in the genotype are different clones. And this applies regardless of whether or not you declare that some genes (loci) are drivers or not. So if you have four genes, it does not matter whether only the first or all four are regarded as drivers; you will always have at most 16 different clones or 16 different genotypes. Of course you can arrive at the same clone/genotype by different routes. Just think about loci A and B in our four-loci genome, and how you can end up with a cell with both A and B mutated.

Analogously, if you have 100 genes, 10 drivers and 90 passengers, you can have up to 2<sup>100</sup> different clones or genotypes. Sure, one cell might have driver A mutated and passenger B mutated, and another cell might have driver A mutated and passenger C mutated. So if you only look at drivers you might be tempted to say that they are "the same clone for all practical purposes"; but they really are not the same clone as they differ in their genotype and this makes a lot of difference computationally.

If you want summaries of simulations that collapse over some genes (say, some "passengers", the 90 passengers we just mentioned) look at the help for samplePop, argument geneNames. This would allow you, for instance, to look at the diversity of clones/genotypes, considering as identical those genotypes that only differ in genes you deem relevant; something similar to defining a "drivers' clone" as the set formed from the union of all sets of cells that have identical genotype with respect to only the drivers (so that in the example just mentioned both cells would be considered "the same clone" as they only differ with respect to passengers). However, this "disregard some genes" only applies to summaries of simulations once we are done simulating data. OncoSimulR will always track clones, as defined above, regardless of whether many of those clones have the same genotype if you were to only focus on driver genes; see also section 11.1.

Labeling something as a "driver", therefore, does not affect what we mean by clone. Yes, labeling something as a driver can affect when you stop simulations if you use detectionDrivers as a stopping mechanism (see section 6.3). But, again, this has nothing to do with the definition of "clone".

If this is all obvious to you, ignore it. I am adding it here because I've seen strange misunderstandings that eventually could be traced to the apparently multiple meanings of clone. (And to make the story complete, Mather, Hasty, and Tsimring (2012) use the expression "class"—e.g., Algorithm 4 in the paper, Algorithm 5 in the supplementary material).

# 11.1 Does OncoSimulR keep track of individuals or of clones? And how can it keep track of such large populations?

OncoSimulR keeps track of clones, where a clone is a set of cells that are genetically identical (note that this means completely identical over the whole set of genes/markers you are using; see section 11.0.1).

We do not need to keep track of individual cells because, for all purposes, and since we do not consider spatial structure, two or more cells that are genetically identical are interchangeable. This means, for instance, that the computational cost of keeping a population of a single clone with 1 individual or with  $10^9$  individuals is exactly the same: we just keep track of the genotype and the number of cells. (Sure, it is much more likely we will see a mutation soon in a clone with  $10^9$  cells than in a clone with 1, but that is a different issue.)

#### 11.1.1 sampleEvery, keepPhylog, and pruning

At each sampling time (where sampleEvery determines the time units between sampling times) the abundance of all the clones with number of cells > 0 is recorded. This is the structure that at the end of the run is converted into the pops.by.time matrix.

Now, some clones might arise from mutation between successive population samples but these might be extinct at the time we take a population sample. These clones do not appear in the pops.by.time matrix because, as we just said, they have 0 cells at the time of sampling. Of course, some of these clones might appear again later and reach a size larger than 0 at some posterior sampling time; it is at this time when this/these clone(s) will appear in the pops.by.time matrix. This pruning of clones with 0 cells can allow considerable savings in computing time (OncoSimulR needs to keep track the genotype of clones, their population sizes, their birth, death, and mutation rates, their next mutation time and the last time they were updated and thus it is important that we only loop over structures with information that is really needed).

However, as explained in section @{moretimings}, we still need to track clones as clones, not simply as classes such as "number of mutated genes". Therefore, very large genomes can represent a problem if they lead to the creation and tracking of many different clones (even if they have the same number of mutated genes). In this case, programs that only keep track of numbers of mutated genes or of drivers, not individual clones, can of course achieve better speed.

What about the genealogy? If you ask OncoSimulR to keep track of the complete parent-child relationships (keepPhylog = TRUE), you might see in the genealogy clones that are not present in pops.by.time if these are clones that never had a population size larger than 0 at any sampling time. To give an example, suppose that we will take population samples at times 0, 1, and 2. Clone A, with a population

size larger than 0 at time 1, gives rise at time 1.5 to clone B; clone B then gives rise to clone C at time 1.8. Finally, suppose that at time 2 only clone C is alive (when we carry out the update of the population with Algorithm 5 from Mather, Hasty, and Tsimring (2012), clones A and B have size 0). Now, at time 1 clones B and C did not yet exist, and clone B is never alive at times 1 or 2. Thus, clone B is not present in pops.by.time. But we cannot remove clone B from our genealogy if we want to reflect the complete history of C. Thus, pops.by.time will show only clones A and C (not B) but the complete genealogy will show clones A, B, C (and will show that B appeared from A at time 1.5 and C appeared from B at time 1.8). Since function plotClonePhylog offers a lot of flexibility with respect to what clones to show depending on their population sizes at different times, you can prevent being shown B, but its existence is there should you need it (see also 2.3.6).

#### 11.2Dealing with errors in "oncoSimulPop"

When running OncoSimulR under Windows mclapply does not use multiple cores, and errors from oncoSimulPop are reported directly. For example:

```
## This code will only be evaluated under Windows
if(.Platform$OS.type == "windows")
    try(pancrError <- oncoSimulPop(10, pancr,</pre>
                                initSize = 1e-5,
                                detectionSize = 1e7,
                                keepEvery = 10,
                                mc.cores = 2))
```

Under POSIX operating systems (e.g., GNU/Linux or Mac OSX) oncoSimulPop can ran parallelized by calling mclapply. Now, suppose you did something like

```
## Do not run under Windows
if(.Platform$OS.type != "windows")
    pancrError <- oncoSimulPop(10, pancr,</pre>
                                initSize = 1e-5,
                                detectionSize = 1e7,
                                keepEvery = 10.
                                mc.cores = 2)
## Warning in mclapply(seq.int(Nindiv), function(x) oncoSimulIndiv(fp =
```

## fp, : all scheduled cores encountered errors in user code

The warning you are seeing tells you there was an error in the functions called by mclapply. If you check the help for mclpapply you'll see that it returns a try-error object, so we can inspect it. For instance, we could do:

```
pancrError[[1]]
```

But the output of this call might be easier to read:

#### pancrError[[1]][1]

And from here you could see the error that was returned by oncoSimulIndiv: initSize < 1 (which is indeed true: we pass initSize = 1e-5).

# 11.3 Whole tumor sampling, genotypes, and allele counts: what gives?

You are obtaining genotypes, regardless of order. When we use "whole tumor sampling", it is the frequency of the mutations in each gene that counts, not the order. So, for instance, "c, d" and "c, d" both contribute to the counts of "c" and "d". Similarly, when we use single cell sampling, we obtain a genotype defined in terms of mutations, but there might be multiple orders that give this genotype. For example, d > c and c > d both give you a genotype with "c" and "d" mutated, and thus in the output you can have two columns with both genes mutated.

# 11.4 Doesn't the BNB algorithm require small mutation rates for it to be advantageous?

As discussed in the original paper by Mather, Hasty, and Tsimring (2012) (see also their supplementary material), the BNB algorithm can achieve considerable speed advantages relative to other algorithms especially when mutation events are rare relative to birth and death events; the larger the mutation rate, the smaller the gains compared to other algorithms. As mentioned in their supplementary material (see p.5) "Note that the 'cost' of each step in BNB is somewhat higher than in SSA [SSA is the original Gillespie Stochastic Simulation Algorithm] since it requires generation of several random numbers as compared to only two uniform random numbers for SSA. However this cost increase is small compared with significant benefits of jumping over birth and death reactions for the case of rare mutations."

Since the earliest versions, OncoSimulR has provided information to assess these issues. The output of function oncoSimulIndiv includes a list called "other" that itself includes two lists named "minDMratio" and "minBMratio", the smallest ratio, over all simulations, of death rate to mutation rate or birth rate to mutation rate, respectively. As explained above, the BNB algorithm thrives when those are large. Note, though, we say "it thrives": these ratios being large is not required for the BNB algorithm to be an exact simulation algorithm; these ratios being large make BNB comparatively much faster than other algorithms.

# 11.5 Can we use the BNB algorithm with state-dependent birth or death rates?

As discussed in the original paper by Mather, Hasty, and Tsimring (2012) (see sections 2.6 and 3.2 of the paper and section E of the supplementary material), the BNB algorithm can be used as an approximate stochastic simulation algorithm "(...) with non-constant birth, death, and mutation rates by evolving the system with a BNB step restricted to a short duration t." (p. 9 in supplementary material). The justification is that "(...) the propensities for reactions can be considered approximately constant during some short interval." (p. 1234). This is the reason why, when we use McFarland's model, we set a very short sampleEvery. In addition, the output of the simulation functions contains the simple summary statistic errorMF that can be used to assess the quality of the approximation<sup>13</sup>.

Note that, as the authors point out, approximations are common with stochastic simulation algorithms when there is density dependence, but the advantage of the BNB algorithm compared to, say, most tau-leap methods is that clones of different population sizes are treated uniformly. Mather, Hasty, and Tsimring (2012) further present results from simulations comparing the BNB algorithm with the original direct SSA method and the tau-leaps (see their Fig. 5), which shows that the approximation is very accurate as soon as the interval between samples becomes reasonably short.

# 11.6 Sometimes I get exceptions when running with mutator genes

Yes, sure, the following will cause an exception; this is similar to the example used in @(ex-mut-antimut) but there is one crucial difference:

```
sd <- 0.1 ## fitness effect of drivers
sm <- 0 ## fitness effect of mutator
nd <- 20 ## number of drivers
nm <- 5 ## number of mutators
mut <- 50 ## mutator effect THIS IS THE DIFFERENCE</pre>
```

<sup>&</sup>lt;sup>13</sup>Death rates are affected by density dependence and, thus, it is on the death rates where the approximation that they are constant over a short interval plays a role. Thus, we examine how large the difference between successive death rates is. More precisely, let A and C denote two successive sampling periods, with  $D_A = log(1 + N_A/K)$  and  $D_C = log(1 + N_C/K)$  their death rates. errorMF\_size stores the largest  $abs(D_C - D_A)$  between any two sampling periods ever seen during a simulation. errorMF stores the largest  $abs(D_C - D_A)/D_A$ . Additionally, a simple procedure to use is to run the simulations with different values of sampleEvery, say the default value of 0.025 and values that are 10, 20, and 50 times larger or smaller, and assess their effects on the output of the simulations and the errorMF statistic itself. You can check that using a sampleEvery much smaller than 0.025 rarely makes any difference in errorMF or in the simulation output (though it increases computing time significantly). And, just for the fun of it, you can also check that using huge values for sampleEvery can lead to trouble and will be manifested too in the simulation output with large and unreasonable jumps in total population sizes and sudden extinctions.

Now, simulate using the fitness and mutator specification. We fix the number of drivers to cancer, and we stop when those numbers of drivers are reached. Since we only care about the time it takes to reach cancer, not the actual trajectories, we set keepEvery = NA:

What happened? That you are using five mutator genes, each with an effect of multiplying by 50 the mutation rate. So the genotype with all those five genes mutated will have an increased mutation rate of  $50^5 = 312500000$ . If you set the mutation rate to the default of 1e-6 you have a mutation rate of 312 which makes no sense (and leads to all sorts of numerical issues down the road and an early warning).

Oh, but you want to accumulate mutator effects and have some, or the early ones, have a large effects and the rest progressively smaller effects? You can do that using epistatic effects for mutator effects.

# 11.7 What are good values of sampleEvery?

First, we need to differentiate between the McFarland and the exponential models. If you use the McFarland model, you should read section 11.5 but, briefly, the small default is probably a good choice.

With the exponential model, however, simulations can often be much faster if sampleEvery is large. How large? As large as you can make it. sampleEvery should not be larger than your desired keepEvery, where keepEvery determines the

resolution or granularity of your samples (i.e., how often you take a snapshot of the population). If you only care about the final state, then set keepEvery = NA.

The other factors that affects choosing a reasonable sampleEvery are mutation rate and population size. If population growth is very fast or mutation rate very large, you need to sample frequently to avoid the "Recoverable exception ti set to DBL\_MIN. Rerunning." issue (see discussion in section 2.4).

### 11.8 What can you do with the simulations?

This is up to you. In section 12.2 we show an example where we infer an Oncogenetic tree from simulated data and in section 1.3 we go over a varied set of scientific questions where OncoSimulR could help.

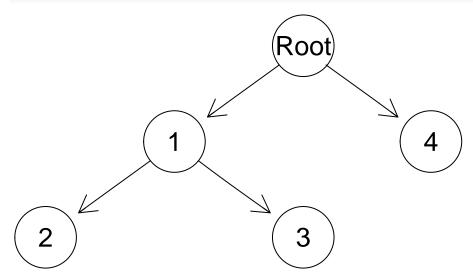
### 12 Using v.1 posets and simulations

It is strongly recommended that you use the new (v.2) procedures for specifying fitness effects. However, the former v.1 procedures are still available, with only very minor changes to function calls. What follows below is the former vignette. You might want to use v.1 because for certain models (e.g., small number of genes, with restrictions as specified by a simple poset) simulations might be faster with v.1 (fitness evaluation is much simpler —we are working on further improving speed).

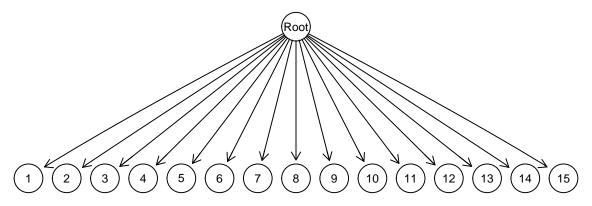
### 12.1 Specifying restrictions: posets

How to specify the restrictions is shown in the help for poset. It is often useful, to make sure you did not make any mistakes, to plot the poset. This is from the examples (we use an "L" after a number so that the numbers are integers, not doubles; we could alternatively have modified storage.mode).

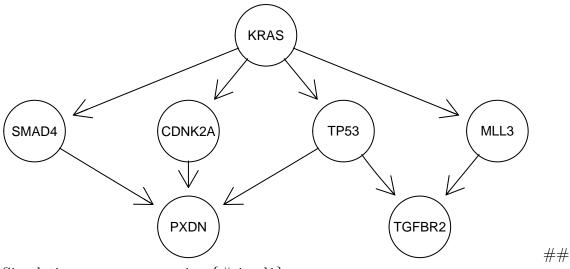
```
## Node 2 and 3 depend on 1, and 4 depends on no one
p1 <- cbind(c(1L, 1L, 0L), c(2L, 3L, 4L))
plotPoset(p1, addroot = TRUE)</pre>
```



```
## A simple way to create a poset where no gene (in a set of 15)
## depends on any other.
p4 <- cbind(OL, 15L)
plotPoset(p4, addroot = TRUE)</pre>
```



Specifying posets is actually straightforward. For instance, we can specify the pancreatic cancer poset in Gerstung et al. (2011) (their figure 2B, left). We specify the poset using numbers, but for nicer plotting we will use names (KRAS is 1, SMAD4 is 2, etc). This example is also in the help for poset:



Simulating cancer progression {#simul1}

We can simulate the progression in a single subject. Using an example very similar to the one in the help:

```
## use poset p1101
data(examplePosets)
p1101 <- examplePosets[["p1101"]]

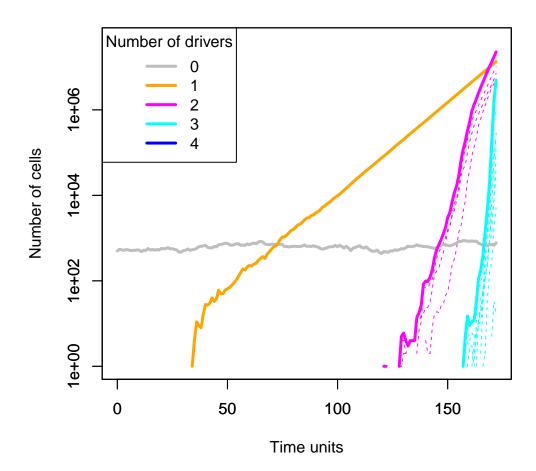
## Bozic Model
b1 <- oncoSimulIndiv(p1101, keepEvery = 15)
summary(b1)</pre>
```

```
##
     NumClones TotalPopSize LargestClone MaxNumDrivers
## 1
                   29971152
                                 11440859
##
     MaxDriversLast NumDriversLargestPop TotalPresentDrivers
## 1
                                        1
##
     FinalTime NumIter HittedWallTime HittedMaxTries errorMF
## 1
          1639
                  3670
                                                 FALSE
                                                            NA
                                 FALSE
##
     minDMratio minBMratio OccurringDrivers
          90909
                     90909 1, 2, 3, 7, 8, 9
## 1
```

The first thing we do is make it simpler (for future examples) to use a set of restrictions. In this case, those encoded in poset p1101. Then, we run the simulations and look at a simple summary and a plot.

If you want to plot the trajectories, it is better to keep more frequent samples, so you can see when clones appear:

```
b2 <- oncoSimulIndiv(p1101, keepEvery = 1)
summary(b2)
     NumClones TotalPopSize LargestClone MaxNumDrivers
##
            20
                                 13518940
## 1
                   41196600
##
     MaxDriversLast NumDriversLargestPop TotalPresentDrivers
## 1
                  4
##
     FinalTime NumIter HittedWallTime HittedMaxTries errorMF
## 1
           172
                  2591
                                 FALSE
                                                FALSE
                                                            NA
##
     minDMratio minBMratio
                                     OccurringDrivers
## 1
          90909
                     90909 1, 2, 3, 4, 5, 6, 7, 8, 9
plot(b2)
```



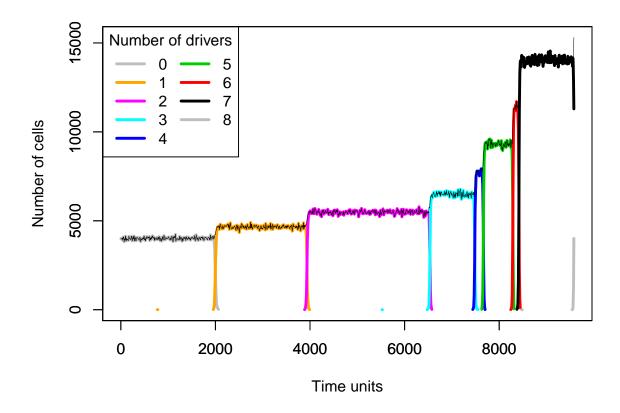
As we have seen before, the stacked plot here is less useful and that is why I do not evaluate that code for this vignette.

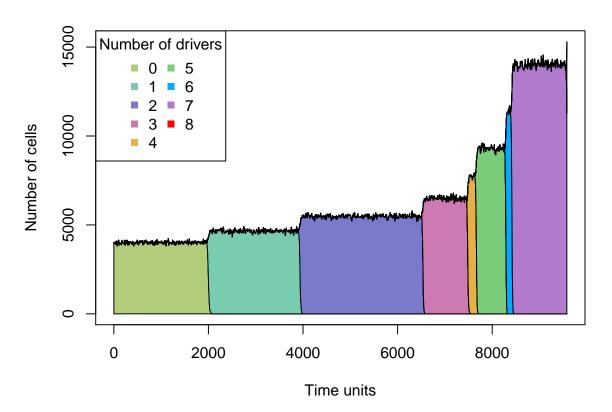
```
plot(b2, type = "stacked")
```

The following is an example where we do not care about passengers, but we want to use a different graph, and we want a few more drivers before considering cancer has been reached. And we allow it to run for longer. Note that in the McFL model detectionSize really plays no role. Note also how we pass the poset: it is the same as before, but now we directly access the poset in the list of posets.

(Very rarely the above run will fail to reach cancer. If that happens, execute it again.)

As usual, we will plot using both a line and a stacked plot:





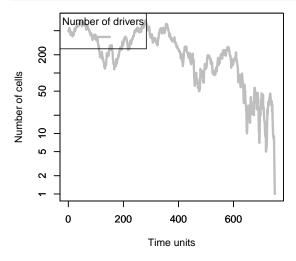
The default is to simulate progression until a simulation reaches cancer (i.e., only simulations that satisfy the detectionDrivers or the detectionSize will be returned).

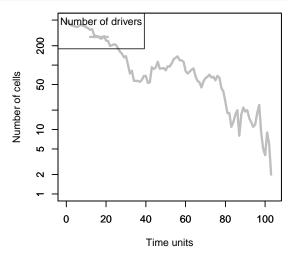
If you use the McFL model with large enough initSize this will often be the case but not if you use very small initSize. Likewise, most of the Bozic runs do not reach cancer. Lets try a few:

```
b3 <- oncoSimulIndiv(p1101, onlyCancer = FALSE)
summary(b3)
     NumClones TotalPopSize LargestClone MaxNumDrivers
##
## 1
##
     MaxDriversLast NumDriversLargestPop TotalPresentDrivers
## 1
##
     FinalTime NumIter HittedWallTime HittedMaxTries errorMF
## 1
           751
                   753
                                 FALSE
                                                FALSE
                                                            NA
     minDMratio minBMratio OccurringDrivers
##
## 1
          90909
                      90909
b4 <- oncoSimulIndiv(p1101, onlyCancer = FALSE)
summary(b4)
##
     NumClones TotalPopSize LargestClone MaxNumDrivers
## 1
             1
                           0
     MaxDriversLast NumDriversLargestPop TotalPresentDrivers
##
## 1
##
     FinalTime NumIter HittedWallTime HittedMaxTries errorMF
## 1
                   104
                                 FALSE
           104
                                                FALSE
                                                            NΑ
##
     minDMratio minBMratio OccurringDrivers
## 1
          90909
                     90909
```

Plot those runs:

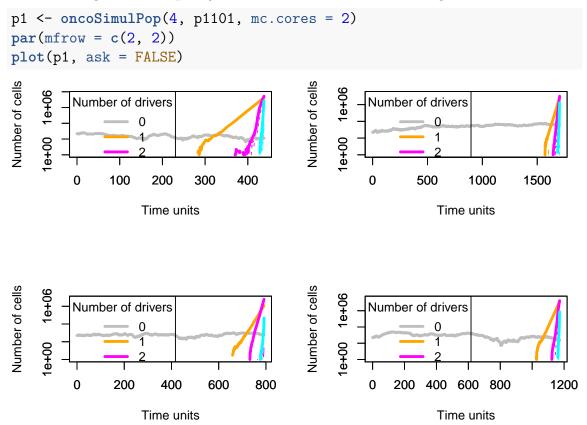
```
par(mfrow = c(1, 2))
par(cex = 0.8) ## smaller font
plot(b3)
plot(b4)
```





#### 12.1.1 Simulating progression in several subjects

To simulate the progression in a bunch of subjects (we will use only four, so as not to fill the vignette with plots) we can do, with the same settings as above:



We can also use stream and stacked plots, though they might not be as useful in this case. For the sake of keeping the vignette small, these are commented out.

```
par(mfrow = c(2, 2))
plot(p1, type = "stream", ask = FALSE)

par(mfrow = c(2, 2))
plot(p1, type = "stacked", ask = FALSE)
```

### 12.2 Sampling from a set of simulated subjects

You will often want to do something with the simulated data. For instance, sample the simulated data. Here we will obtain the trajectories for 100 subjects in a scenario without passengers. Then we will sample with the default options and store that as a vector of genotypes (or a matrix of subjects by genes):

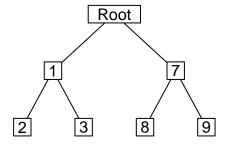
The function samplePop samples that object, and also gives you some information about the output:

```
genotypes <- samplePop(m1)
##
## Subjects by Genes matrix of 100 subjects and 11 genes.</pre>
```

What can you do with it? That is up to you. As an example, let us try to infer an Oncogenetic tree (and plot it) using the *Oncotree* package Szabo and Pappas (2013) after getting a quick look at the marginal frequencies of events:

```
colSums(genotypes)/nrow(genotypes)
## 1 2 3 4 5 6 7 8 9 10 11
## 0.49 0.04 0.02 0.00 0.00 0.04 0.03 0.04 0.00 0.00

require(Oncotree)
ot1 <- oncotree.fit(genotypes)
## The following events had no observed occurances, so they will not be included in
## 4 5 6 10 11
plot(ot1)</pre>
```

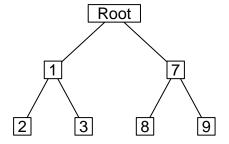


Your run will likely differ from mine, but with the defaults (detection size of  $10^8$ ) it is likely that events down the tree will never appear. You can set detectionSize = 1e9 and you will see that events down the tree are now found in the cross-sectional sample.

Alternatively, you can use single cell sampling and that, sometimes, recovers one or a couple more events.

```
genotypesSC <- samplePop(m1, typeSample = "single")
##
## Subjects by Genes matrix of 100 subjects and 11 genes.
colSums(genotypesSC)/nrow(genotypesSC)
## 1 2 3 4 5 6 7 8 9 10 11
## 0.59 0.06 0.12 0.00 0.00 0.05 0.08 0.14 0.00 0.00

ot2 <- oncotree.fit(genotypesSC)
## The following events had no observed occurances, so they will not be included in
## 4 5 6 10 11
plot(ot2)</pre>
```

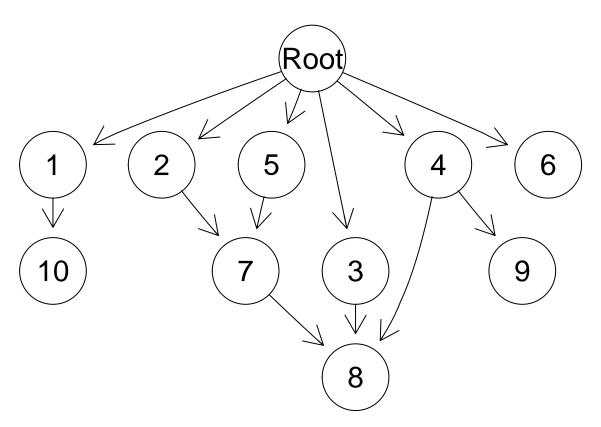


You can of course rename the columns of the output matrix to something else if you want so the names of the nodes will reflect those potentially more meaningful names.

# 13 Generating random DAGs for restrictions

You might want to randomly generate DAGs like those often found in the literature on Oncogenetic trees et al. Function sim0Graph might help here.

```
## No seed fixed, so reruns will give different DAGs.
(a1 <- simOGraph(10))
        Root 1 2 3 4 5 6 7 8 9 10
##
## Root
           0 1 1 1 1 1 1 0 0 0
## 1
           0 0 0 0 0 0 0 0 0
           0 0 0 0 0 0 0 1 0 0
##
           0 0 0 0 0 0 0 0 1 0
## 3
           0 0 0 0 0 0 0 0 1 1
## 4
           0 0 0 0 0 0 0 1 0 0
## 5
                                 0
           0 0 0 0 0 0 0 0 0
## 6
## 7
           0 0 0 0 0 0 0 0 1 0
           0 0 0 0 0 0 0 0 0
## 8
           0 0 0 0 0 0 0 0 0
## 9
           0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0
library(graph) ## for simple plotting
plot(as(a1, "graphNEL"))
```



Once you obtain the adjacency matrices, it is for now up to you to convert them into appropriate posets or fitnessEffects objects.

Why this function? I searched for, and could not find any that did what I wanted, in particular bounding the number of parents, being able to specify the approximate depth<sup>14</sup> of the graph, and optionally being able to have DAGs where no node is connected to another both directly (an edge between the two) and indirectly (there is a path between the two through other nodes). So I wrote my own code. The code is fairly simple to understand (all in file generate-random-trees.R). I would not be surprised if this way of generating random graphs has been proposed and named before; please let me know, best if with a reference.

Should we remove direct connections if there are indirect? Or, should we set removeDirectIndirect = TRUE? Except for Farahani and Lagergren (2013), none of the DAGs I've seen in the context of CBNs, Oncogenetic trees, etc, include both direct and indirect connections between nodes. If these exist, reasoning about the model can be harder. For example, with CBN (AND or CMPN or monotone relationships) adding a direct connection makes no difference iff we assume that the relationships encoded in the DAG are fully respected (e.g., all  $s_h = -\infty$ ). But it can make a difference if we allow for deviations from the monotonicity, specially if we only check for the satisfaction of the presence of the immediate ancestors. And things get even trickier if we combine XOR with AND. The code for computing fitness, however, should deal with all of this just fine.

<sup>&</sup>lt;sup>14</sup>Where depth is defined in the usual way to mean smallest number of nodes —or edges— to traverse to get from the bottom to the top of the DAG.

## 14 Session info and packages used

This is the information about the version of R and packages used:

```
sessionInfo()
## R Under development (unstable) (2016-11-03 r71622)
## Platform: x86 64-pc-linux-gnu (64-bit)
## Running under: Debian GNU/Linux stretch/sid
##
## locale:
                                   LC NUMERIC=C
    [1] LC_CTYPE=en_GB.utf8
##
    [3] LC TIME=en GB.utf8
                                   LC COLLATE=en GB.utf8
##
    [5] LC_MONETARY=en_GB.utf8
                                   LC_MESSAGES=en_GB.utf8
##
    [7] LC PAPER=en GB.utf8
                                   LC NAME=C
                                   LC TELEPHONE=C
    [9] LC ADDRESS=C
## [11] LC_MEASUREMENT=en_GB.utf8 LC_IDENTIFICATION=C
##
## attached base packages:
## [1] parallel methods
                                      graphics grDevices
                            stats
## [6] utils
                           base
                 datasets
##
## other attached packages:
##
    [1] igraph_1.0.1
                             graph_1.53.0
    [3] BiocGenerics_0.21.0 Oncotree_0.3.3
##
##
    [5] boot_1.3-18
                            pander_0.6.0
##
    [7] bookdown 0.1
                            BiocStyle_2.3.3
##
  [9] rmarkdown_1.1
                             testthat_1.0.2
## [11] OncoSimulR_2.5.3
##
## loaded via a namespace (and not attached):
##
    [1] gtools_3.5.0
                            splines_3.4.0
##
    [3] lattice_0.20-34
                            colorspace_1.2-7
##
    [5] miniUI 0.1.1
                           htmltools 0.3.5
##
    [7] stats4 3.4.0
                           yaml 2.1.13
    [9] mgcv_1.8-15
                            chron 2.3-47
## [11] nloptr_1.0.4
                           DBI_0.5-1
## [13] Rgraphviz 2.19.0
                           RColorBrewer 1.1-2
## [15] plyr_1.8.4
                            stringr_1.1.0
## [17] MatrixModels_0.4-1 munsell_0.4.3
## [19] gtable 0.2.0
                            evaluate 0.10
## [21] knitr 1.14
                           SparseM 1.72
## [23] httpuv_1.3.3
                           quantreg_5.29
## [25] pbkrtest_0.4-6
                           Rcpp_0.12.7
## [27] xtable 1.8-2
                            scales 0.4.0
## [29] formatR 1.4
                           mime_0.5
## [31] lme4 1.1-12
                            smatr 3.4-3
```

```
digest_0.6.10
## [33] ggplot2_2.1.0
## [35] stringi_1.1.2
                            dplyr_0.5.0
## [37] ggrepel_0.6.3
                            shiny 0.14.2
## [39] grid 3.4.0
                            tools 3.4.0
## [41] magrittr 1.5
                            lazyeval_0.2.0
## [43] tibble 1.2
                            crayon 1.3.2
## [45] car 2.1-3
                            MASS 7.3-45
## [47] Matrix 1.2-7.1
                            data.table 1.9.6
## [49] assertthat 0.1
                            minga 1.2.4
## [51] R6 2.2.0
                            nnet 7.3-12
## [53] nlme 3.1-128
```

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