Tree-like subgraph $\mathcal{T}^*$.