Sistemi Operativi

Corso di Laurea in Informatica

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Recap from Last Lecture

- Synchronization **primitives**:
 - Locks
 - Semaphores
 - Monitors

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 - Locks
 - Semaphores
 - Monitors
- 2 fundamental synchronization problems:
 - Producers-Consumers
 - Readers-Writers

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- 5 philosophers sitting at a round table

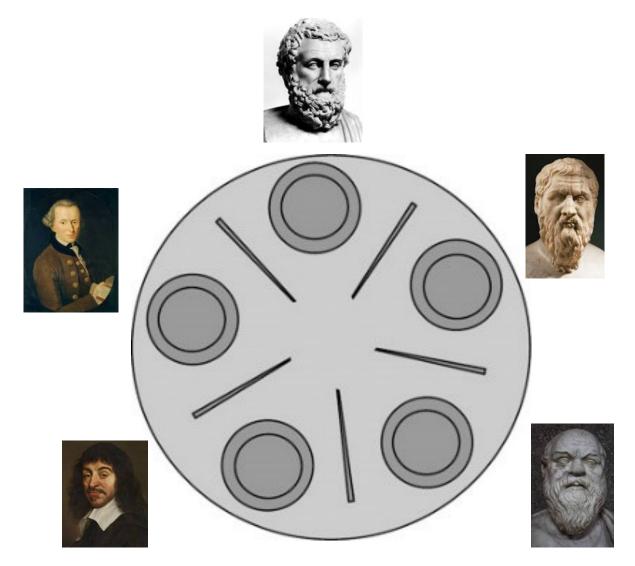
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- 5 philosophers sitting at a round table
- Each philosopher has one chopstick on her/his left and one on her/his right (i.e., 5 chopsticks in total)

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- 2 things philosophers are good at ©:
 - Eating
 - Thinking

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 - Try to pick up the two closest chopsticks (the left and the right ones)
 - Block if a neighbour has already picked up a chopstick
- After eating, put down both chopsticks and go back thinking!





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We still want some concurrency here ©

The Dining Philosophers: Solution 1

```
Semaphore chopsticks[5];
while (True) {
    chopsticks[i].wait(); // wait on the left chopstick
    chopsticks [(i-1)\%5]. wait(); // wait on the right chopstick
    eat();
    chopsticks[i].signal(); // signal on the left chopstick
    chopsticks[(i-1)%5].signal(); // signal on the right chopstick
    think();
```

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Is this solution correct?

No! Possible deadlock if all philosophers take the left chopstick

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Idea: Before picking one chopstick be sure also the second one is available, otherwise wait for the neighbour to finish

Testing if either one of the two neighbours of a given philosopher is currently eating (condition variables)

Never gonna pick a single chopstick!

```
class Philosopher {
    enum Status {
        THINKING,
        HUNGRY,
        EATING
    }
    Status state;

    public Philosopher() {
        this.state = THINKING;
    }
}
```

```
void canEat(int i) {
   State state = this.philosophers[i].state;
   State left = this.philosophers[[(i-1)%5].state;
   State right = this.philosophers[[(i+1)%5].state;
   if(left != EATING && right != EATING && state == HUNGRY) {
        state = EATING;
        this.philosophers[i].notify();
   }
}
```

```
class DiningPhilosophers {
    Philosopher[5] philosophers;

public DiningPhilosopers() {
    for(int i=0; i < 5; ++i) {
        this.philosophers[i] = new Philosopher();
    }
}
// continue implementation ----->
```

```
void synchronized pickup(int i) {
    this.philosophers[i].state = HUNGRY;
    canEat(i);
    if(this.philosophers[i].state != EATING) {
        this.philosophers[i].wait();
    }
}
```

```
void synchronized putdown(int i) {
    this.philosophers[i].state = THINKING;
    canEat((i - 1) % 5); // left neighbour
    canEat((i + 1) % 5); // right neighbour
}
```

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 - Banking system: read vs. update account balances

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 - Producer-Consumer
 - Audio/Video player embedded in a web browser: shared data buffer + network and render threads
 - Reader-Writer
 - Banking system: read vs. update account balances
 - Dining Philosophers
 - Lock on multiple resources: e.g., travel reservation (hotel, airline, car rental databases)

Our Journey

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Thread A printer.wait(); disk.wait(); // copy from disk to printer printer.signal(); disk.signal();

```
Thread B

disk.wait();
printer.wait();

// copy from disk to printer

printer.signal();
disk.signal();
```

Intuitively, a condition where two or more threads are waiting for an event that can only be generated by the very same threads

```
Thread A

printer.wait();
disk.wait();

// copy from disk to printer

printer.signal();
disk.signal();
```

```
Thread B

disk.wait();
printer.wait();

// copy from disk to printer

printer.signal();
disk.signal();
```

Intuitively, a condition where two or more threads are waiting for an event that can only be generated by the very same threads

Thread A printer.wait(); Acquires printer and context switch disk.wait(); // copy from disk to printer printer.signal(); disk.signal();

```
Thread B

disk.wait();
printer.wait();

// copy from disk to printer

printer.signal();
disk.signal();
```

Intuitively, a condition where two or more threads are waiting for an event that can only be generated by the very same threads

```
Thread A

printer.wait();
disk.wait();

// copy from disk to printer

printer.signal();
disk.signal();
```

```
Thread B

B takes over

disk.wait();

printer.wait();

// copy from disk to printer

printer.signal();

disk.signal();
```

Intuitively, a condition where two or more threads are waiting for an event that can only be generated by the very same threads

```
Thread A

printer.wait();
disk.wait();

// copy from disk to printer

printer.signal();
disk.signal();
```

Intuitively, a condition where two or more threads are waiting for an event that can only be generated by the very same threads

Thread A printer.wait(); A executes again and blocks disk.wait(); // copy from disk to printer printer.signal(); disk.signal();

```
Thread B

disk.wait();
printer.wait();

// copy from disk to printer

printer.signal();
disk.signal();
```

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```
Thread A

printer.wait();
disk.wait();

// copy from disk to printer

printer.signal();
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Thread A

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A waits B to release the disk

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printer.signal();
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Thread B

disk.wait();
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printer.signal();
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```

B waits A to release the printer

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- Deadlock prevention (offline): imposes restrictions/rules on how to write deadlock-free programs
- **Deadlock avoidance (online):** runtime support checks resource requests made by threads to avoid deadlocks

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- Related terms but each one refers to a specific situation
- Starvation occurs when a thread waits indefinitely for some resource but other threads are actually making progress using that resource
- The main difference with deadlock is that the system is not completely stuck!

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 - Circular Wait \rightarrow a set of waiting threads $t_1, ..., t_n$ where t_i is waiting on $t_{(i+1)\%n}$

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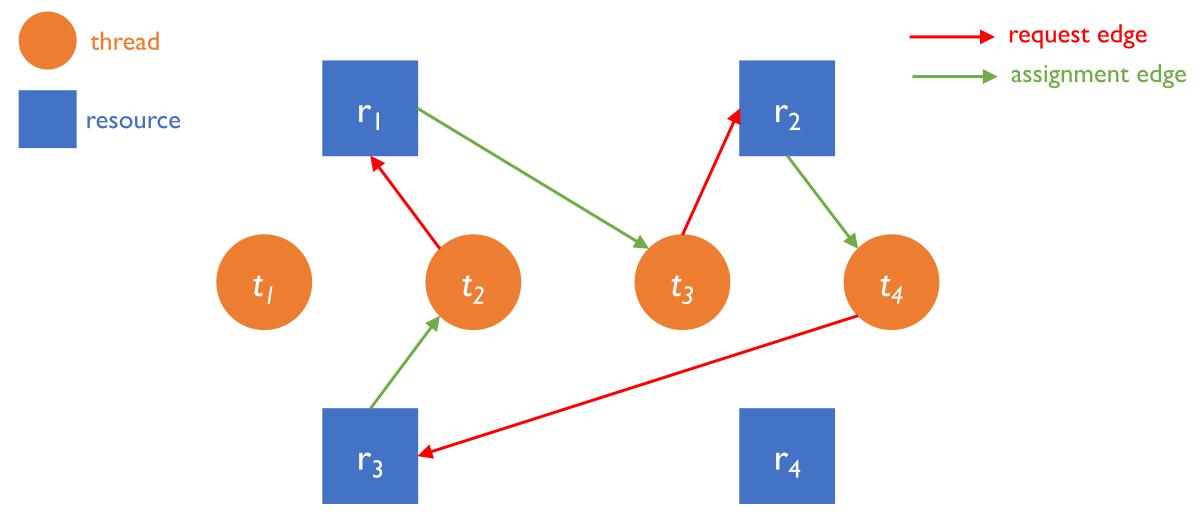
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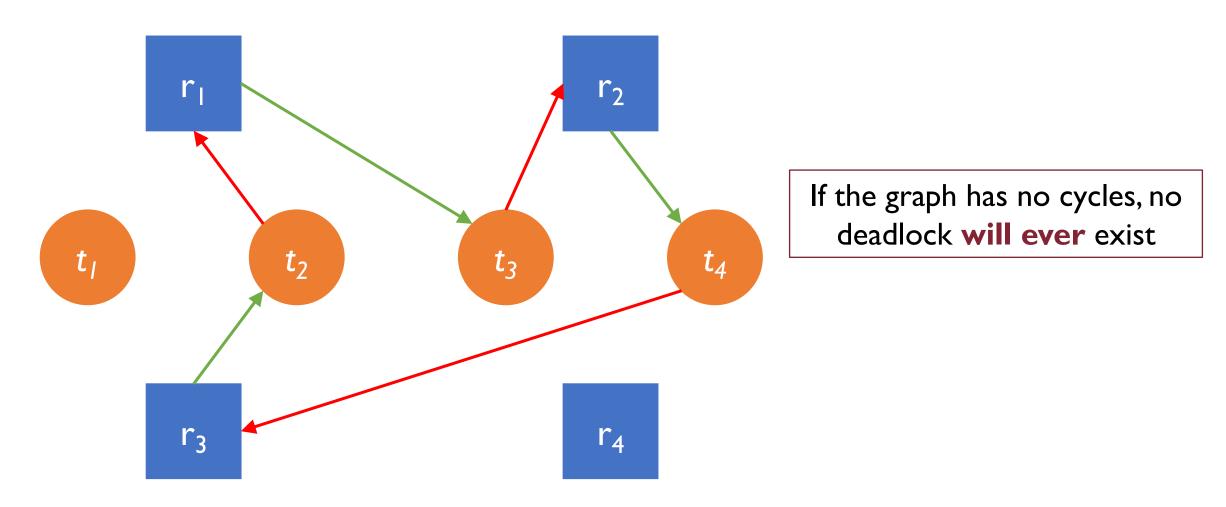
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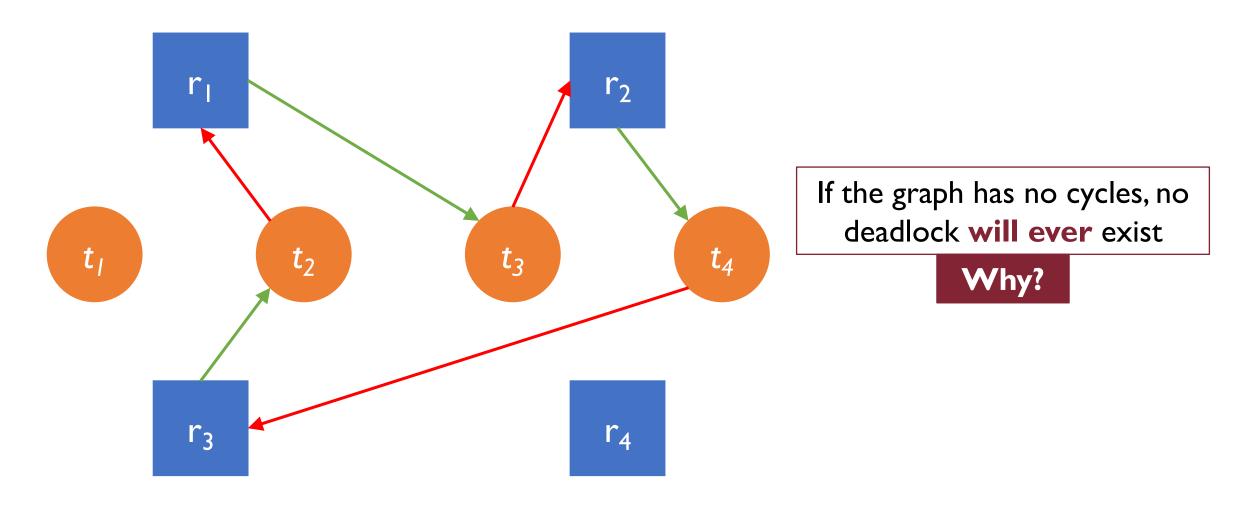
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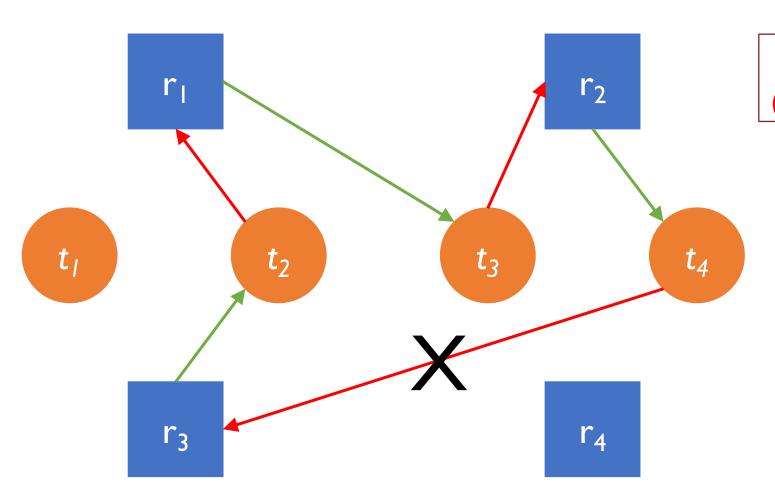
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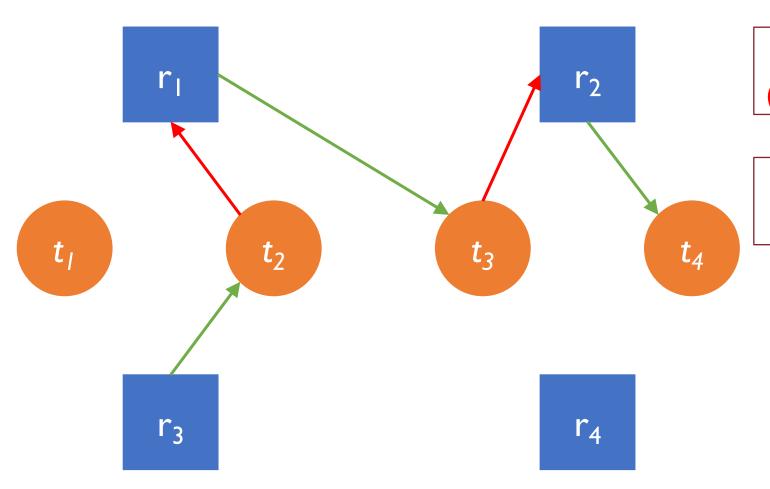






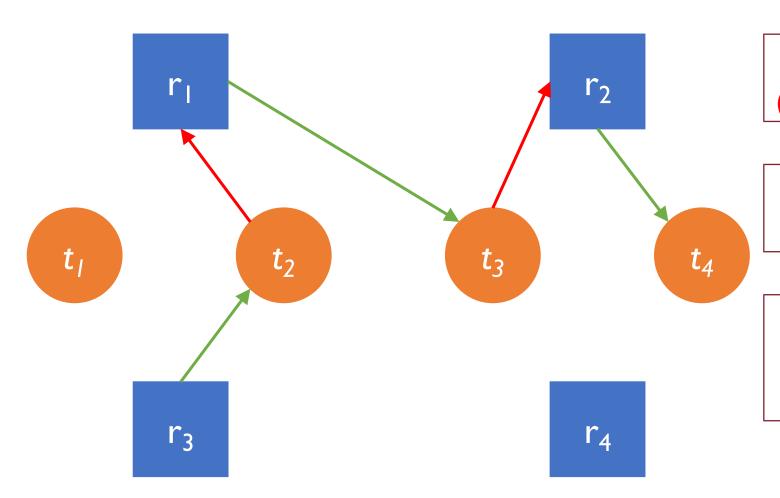


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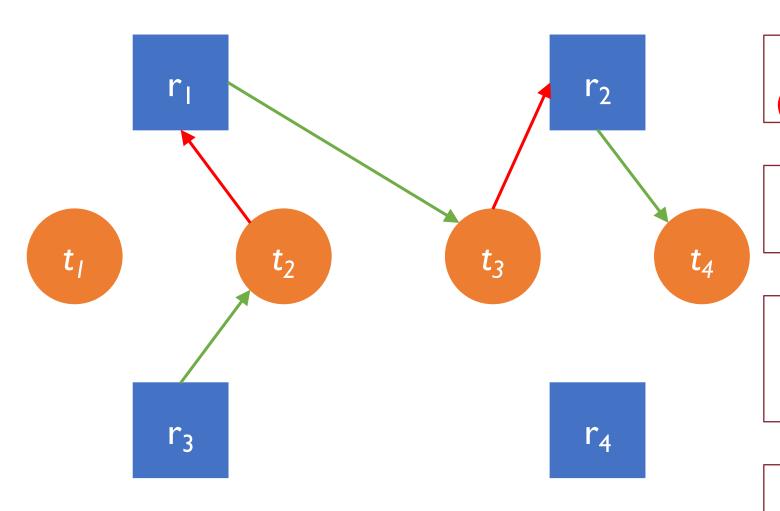
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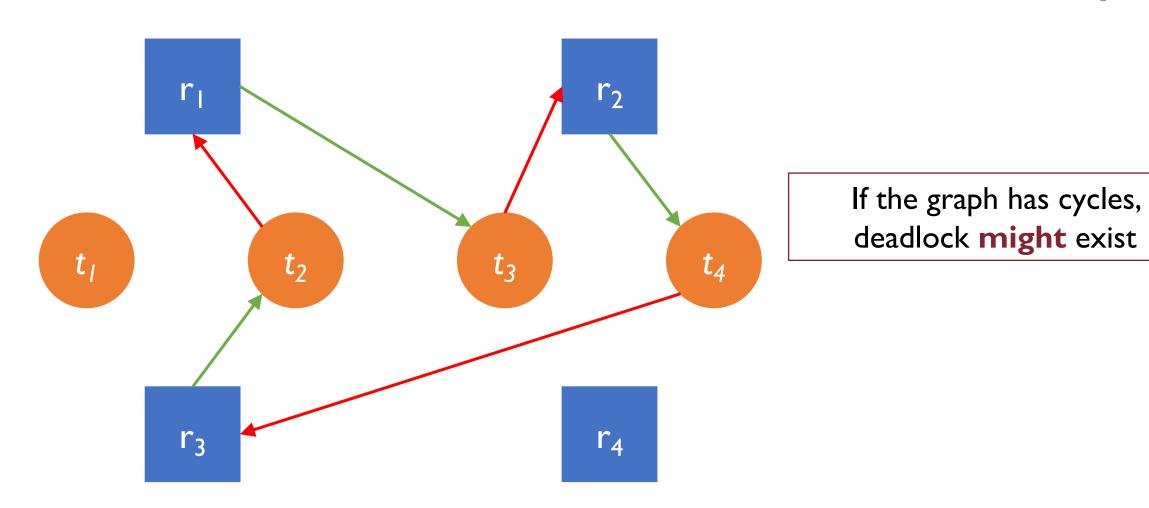


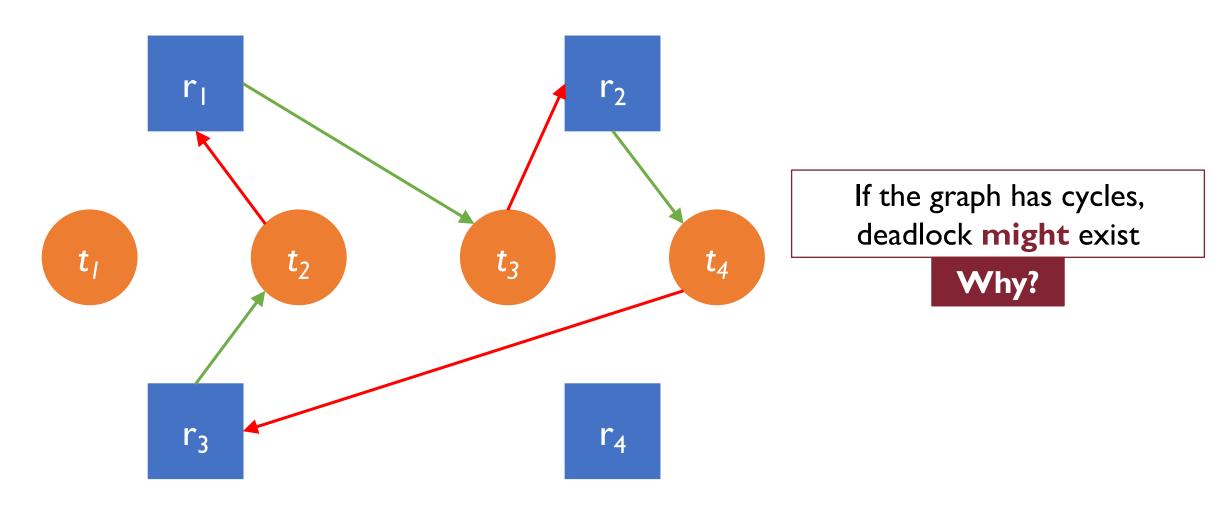
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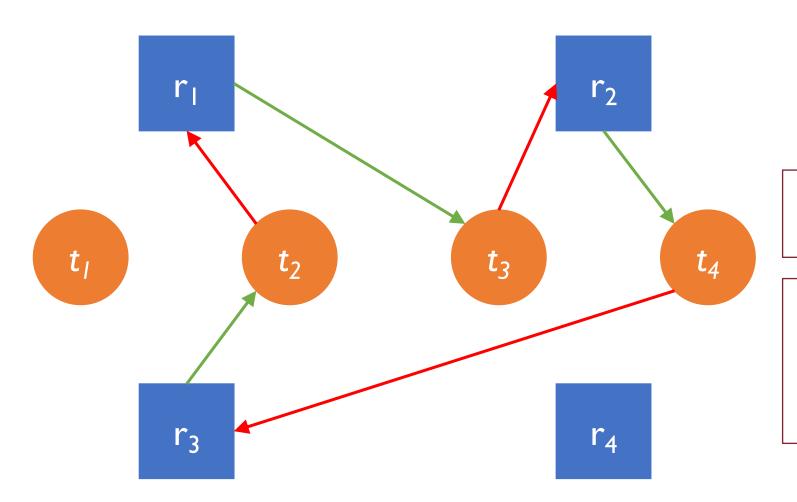
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And so on and so forth...

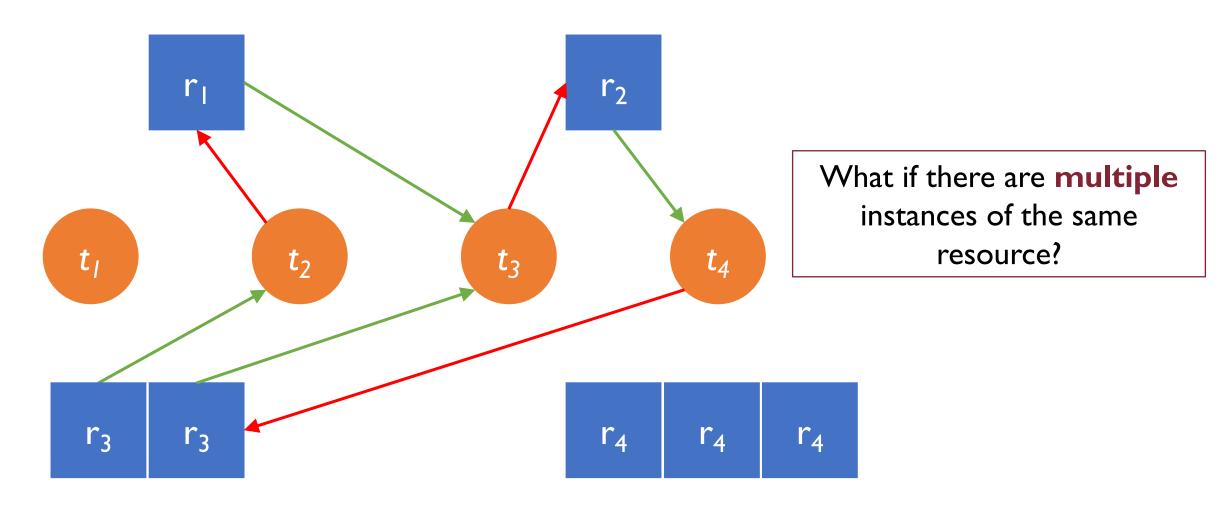




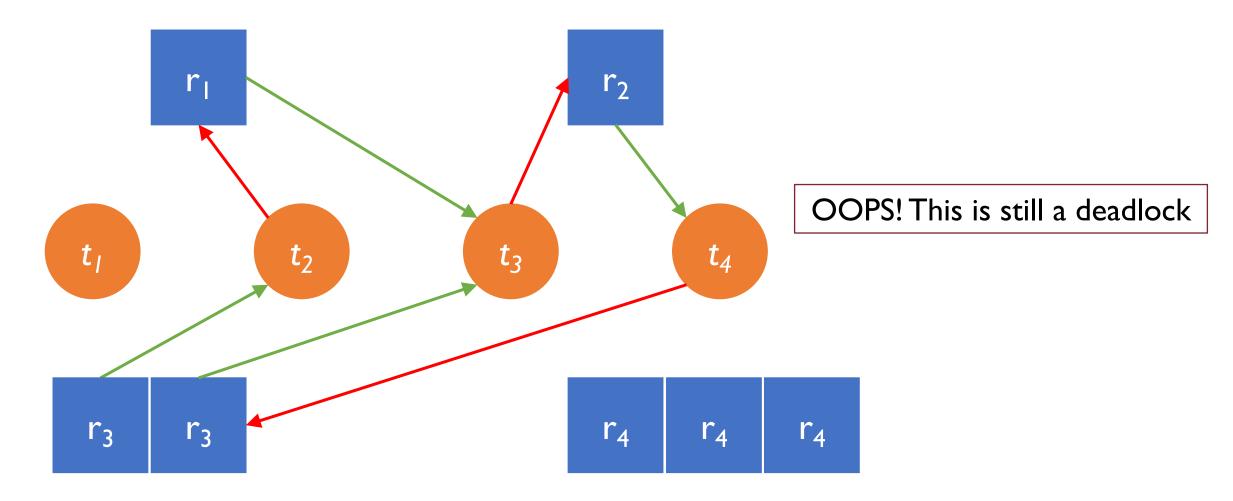


If the graph has cycles, deadlock **might** exist

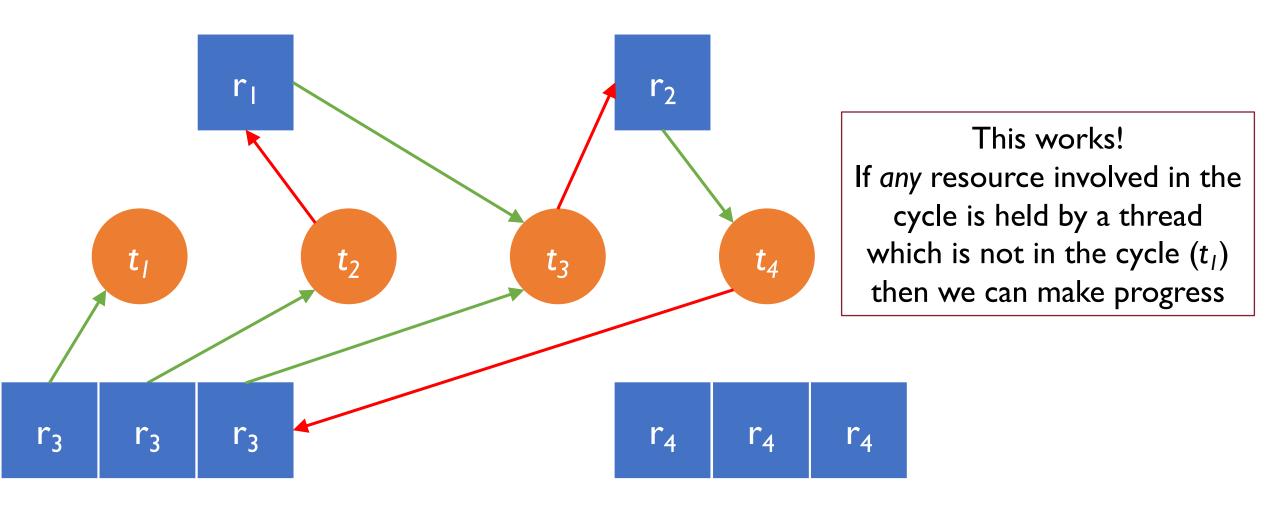
We are implicitly assuming the **multiplicity** of each resource is I (i.e., we have one r_1 , one r_2 , etc.)



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- How? Several ways of doing it:
 - Kill all the threads in the cycle (quite harsh, ugh?)
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- We would like to be more precise than that...

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- When to run such a detection algorithm?
 - Before granting a resource \rightarrow each granted request will take $O(|V|^2)$
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 - On a regular schedule or when the CPU is under-utilized
- What do modern OSs do? Nothing! They leave it to the programmer!

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 it, the OS preempts (releases) all the resources that the thread is already holding
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 - Circular Wait → impose an ordering (i.e., numbering) on resources and enforce to request them in such order

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Deadlock Avoidance: Resource Reservation

Each thread provides information about the maximum number of resources it might need during execution

> $m_i = maximum$ number of resources that thread i might request $c_i = current$ number of resources that thread i is holding $C = \sum_{i=1}^{\infty} c_i = total$ number of resources currently allocated R = maximum number of resources overall available

Any thread sequence is **safe** if for each thread it holds that:

$$\underbrace{m_i - c_i}_{\text{resources } t_i \text{ might still request}} \leq \underbrace{R - C}_{\text{resources currently available}} + \underbrace{\sum_{j=1}^{i-1} c_j}_{\text{resources currently allocated up to } t_j, j < i}$$

Deadlock Avoidance: Safe State

- A state in which there is a safe sequence for the threads
- An unsafe state does not necessarily mean deadlock (i.e., some threads may not request the maximum number of resources as declared)
- Grant a resource to a thread if the new state is safe, otherwise make it wait even if the resource is available
- This policy ensures no circular-wait condition exists

- 3 threads: t_1 , t_2 , and t_3 are compating for 12 tape drives (resources)
- Currently, II drives are allocated to the threads, leaving I available

| Thread | m _i | c _i | m _i – c _i |
|----------------|----------------|----------------|---------------------------------|
| t _i | 4 | 3 | I |
| t_2 | 8 | 4 | 4 |
| t ₃ | 12 | 4 | 8 |

Is the current state safe?

| Thread | m _i | c _i | m _i – c _i |
|----------------|----------------|----------------|---------------------------------|
| t _l | 4 | 3 | I |
| t ₂ | 8 | 4 | 4 |
| t ₃ | 12 | 4 | 8 |

The current state is safe in that there exists a sequence of threads (t_1, t_2, t_3) where each one will get the maximum number of resources without waiting

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 t_2 can use the current allocation, plus t_1 's resources and I drive left (4 drives)

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 t_3 can use the current allocation, plus t_1 's & t_2 's resources and I drive left (8 drives)

| Thread | m _i | c _i | m _i – c _i |
|----------------|----------------|----------------|---------------------------------|
| t _i | 4 | 3 | I |
| t ₂ | 8 | 4 | 4 |
| t ₃ | 12 | 5 | 7 |

Suppose t₃ requests one more drive, then now there are no more available drives

Theoretically, everything might still work (e.g., t₁ may never request another drive)

However, t₃ must wait because allocating that extra drive would lead to an unsafe state, which in turn might lead to deadlock

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- Edges can now be of 3 types:
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 - Claim (dotted) Edge \rightarrow a directed edge (t_i, r_j) indicates that t_i might request r_j in the future
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 - Assignment Edge \rightarrow a directed edge (r_j, t_i) indicates that the OS has allocated r_j to t_i
- Satisfying a request means converting a claim into an assignment edge

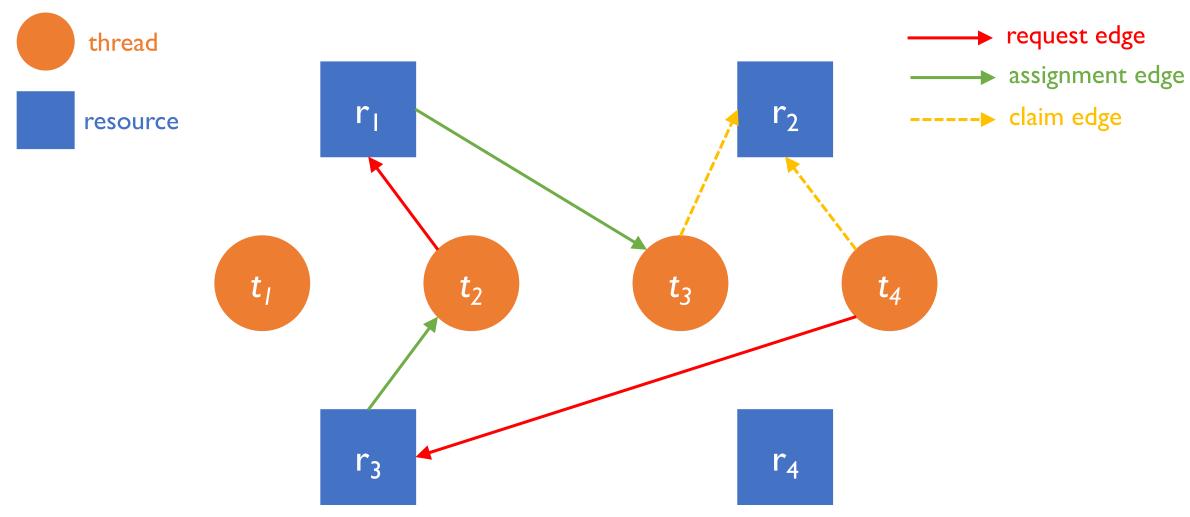
99

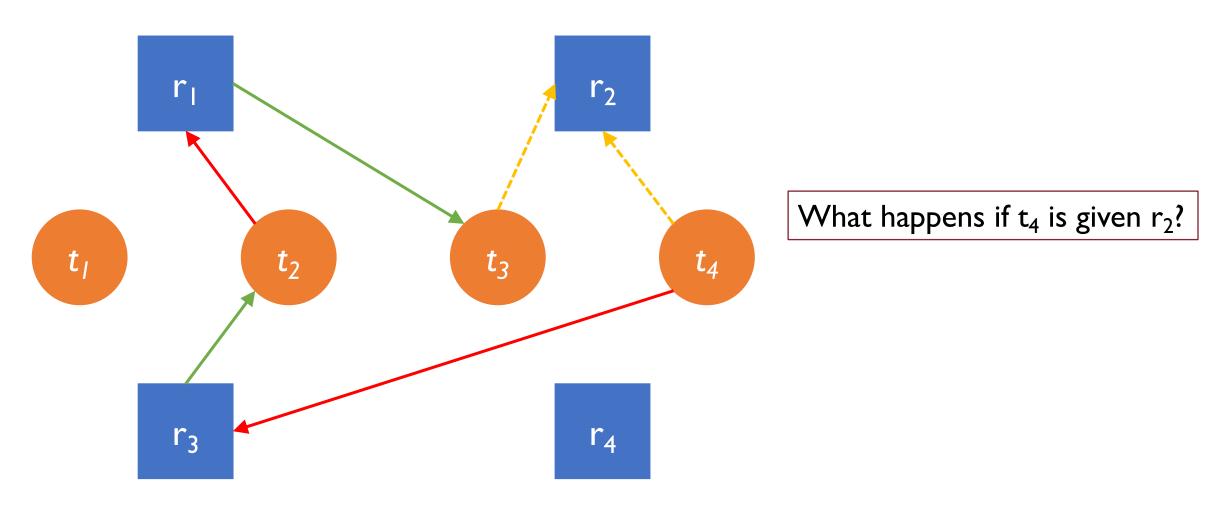
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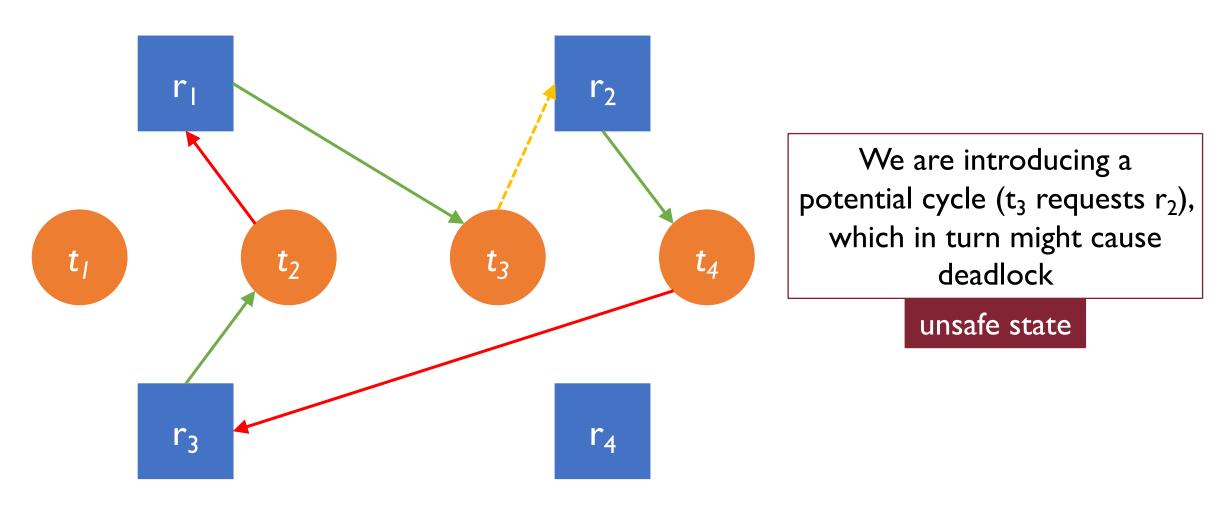
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- In other words, the claim edge is converted into a request edge and the thread will wait

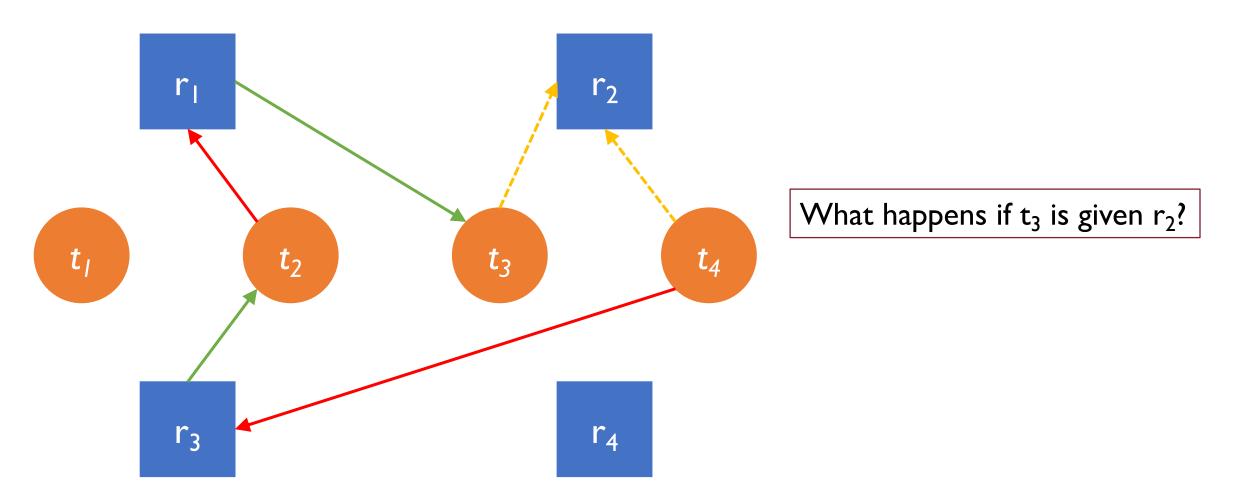
- A cycle in this extended RAG indicates an unsafe state
- If the allocation results in an unsafe state, this will be denied even if the resource is actually available
- In other words, the claim edge is converted into a request edge and the thread will wait
- NOTE: This solution does not work when there are multiple instances of the same resource

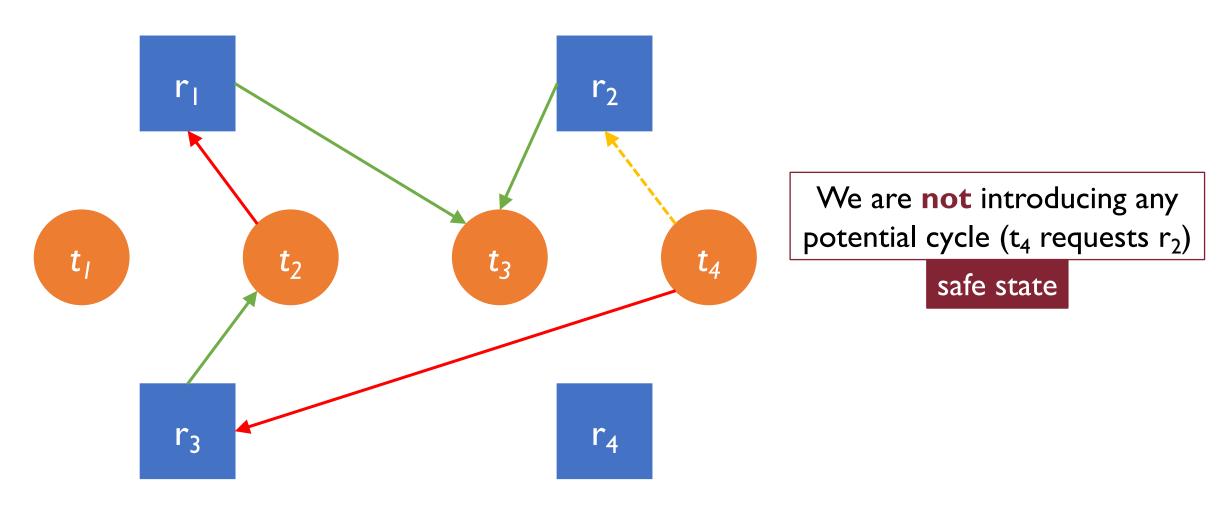




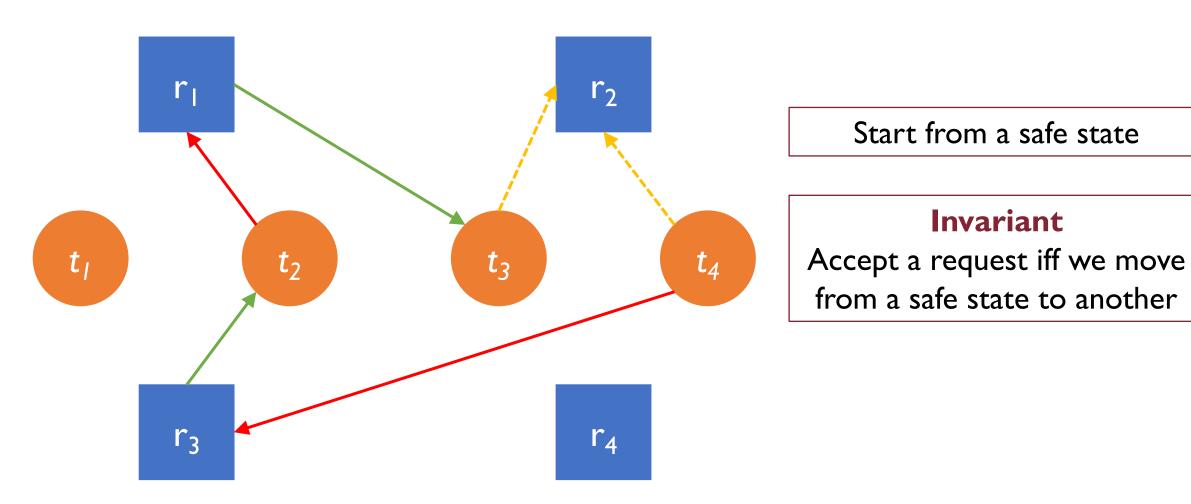
105







Deadlock Avoidance: Resource Allocation Graph



Banker's Algorithm

- Handles multiple instances of the same resource
- Forces threads to provide information on what resource they might need, in advance
- The resources requested must not exceed the total available in the system
- The algorithm allocates resources to a requesting thread if the allocation leaves the system in a safe state, otherwise the thread waits

Banker's Algorithm: Data Structures

- n = number of threads; m = number of resource types
- available [1..m]:m-dimensional vector
 - available[j] = k means there are k resources of type j available
- max[1..n, 1..m]:n x m matrix
 - max[i, j] = k means thread i may require at most k resources of type j
- allocation[1..n, 1..m]:n x m matrix
 - allocation[i, j] = k means thread i has allocated k resources of type j
- need[1..n, 1..m]:n x m matrix
 - need[i, j] = max[i, j] allocation[i, j] = k means thread i may need k
 more resources of type j to complete its task

Banker's Algorithm: Idea

- The algorithm is divided in 2 tasks:
 - isSafeState \rightarrow given the current status of allocation of resources, test if this is a safe state
 - resourceRequest -> given a thread and its resource request decides if such a request can be satisfied

Banker's Algorithm: Idea

- The algorithm is divided in 2 tasks:
 - isSafeState -> given the current status of allocation of resources, test if this is a safe state
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Banker's Algorithm: Idea

- The algorithm is divided in 2 tasks:
 - isSafeState -> given the current status of allocation of resources, test if this is a safe state
 - resourceRequest -> given a thread and its resource request decides if such a request can be satisfied
- A request can be satisfied iff this leads to a safe state!
- In other words, the second tasks uses the output of the first one in order to make a decision

Banker's Algorithm: isSafeState

I. Let work and finish be vectors of length m and n, respectively

```
Initialize: work = available; finish[i] = false; for all i
```

2. Find and i such that:

```
finish[i] = false && need[i] ≤ work

If no such i exists, go to step 4.
```

3. Assume thread i executes:

```
work = work + allocation[i]; finish[i] = true; go to step 2.
```

4. If finish[i] == true for all i, the system is in a safe state

Banker's Algorithm: requestResource

Input: i (thread) and request an m-dimensional vector of requests

- I. If request > need[i] raise an error as thread i is attempting to request more resources that it claimed, otherwise go to step 2.
- 2. If request > available thread i must wait since resources are not available, otherwise go to step 3.
- 3. Even if resources are available, test if this allocation will lead to a safe state by simulating it

```
available -= request; allocation[i] += request; need[i] -= request;
isSafeState() ? OK : rollback() and wait()
```

A snapshot of the current state of the system

| | | | | | RES | OUR | CES | | | |
|--------|----------------|-----|-----|-----|-----|------|-----|----|-------|-----|
| | | | MAX | | ALL | OCAT | ION | AV | AILAE | BLE |
| | | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | - 1 | 0 | 0 | -1 | | | |
| R | T ₁ | - 1 | 7 | 5 | I | 0 | 0 | | | |
| E A | T ₂ | 2 | 3 | 5 | I | 3 | 5 | | | |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | |
| | Total | | | | 2 | 9 | 9 | -1 | 5 | 2 |

QI: How many resources of type A, B, and C are there overall?

| | | | | | RES | OUR | CES | | | |
|--------|-----------------------|---|-----|---|-----|------|-----|----|-------|-----|
| | | | MAX | | ALL | OCAT | ION | AV | AILAE | BLE |
| | | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | I | 0 | 0 | -1 | | | |
| R | T ₁ | I | 7 | 5 | I | 0 | 0 | | | |
| E A | T ₂ | 2 | 3 | 5 | I | 3 | 5 | | | |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | |
| | Total | | | | 2 | 9 | 9 | -1 | 5 | 2 |

QI: How many resources of type A, B, and C are there overall?

| | | | | | RES | OUR | CES | | | |
|--------|----------------|---|-----|---|-----|------|-----|----|-------|-----|
| | | | MAX | | ALL | OCAT | ION | AV | AILAE | BLE |
| | | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | I | 0 | 0 | - 1 | | | |
| R | T ₁ | 1 | 7 | 5 | -1 | 0 | 0 | | | |
| E A | T ₂ | 2 | 3 | 5 | - 1 | 3 | 5 | | | |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | |
| | Total | | | | 2 | 9 | 9 | I | 5 | 2 |

$$A = 2 + 1 = 3$$
 $B = 9 + 5 = 14$
 $C = 9 + 2 = 11$

Q2: What is the content of the NEED matrix?

| | | | | | RES | OUR | CES | | | | | | |
|--------|----------------|-----|-----|---|-----|------|-----|----|--------|-----|---|------|---|
| | | | MAX | | ALL | OCAT | ION | AV | /AILAE | BLE | | NEED | |
| | | A | В | С | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | I | 0 | 0 | I | | | | | | |
| R | T ₁ | - 1 | 7 | 5 | - 1 | 0 | 0 | | | | | | |
| E A | T ₂ | 2 | 3 | 5 | I | 3 | 5 | | | | | | |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | | | | |
| | Total | | | | 2 | 9 | 9 | I | 5 | 2 | | | |

Q2: What is the content of the NEED matrix?

NEED[i, j] = MAX[i, j] - ALLOCATION[i, j]

| | | | | | RES | OUR | CES | | | | | | |
|--------|----------------|---|-----|---|-----|------|-----|-----|-------|-----|---|------|---|
| | | | MAX | | ALL | OCAT | ION | AV | AILAE | BLE | | NEED | |
| | | A | В | С | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | I | 0 | 0 | I | | | | | | |
| R | T ₁ | 1 | 7 | 5 | - 1 | 0 | 0 | | | | | | |
| E A | T ₂ | 2 | 3 | 5 | I | 3 | 5 | | | | | | |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | | | | |
| | Total | | | | 2 | 9 | 9 | - 1 | 5 | 2 | | | |

Q2: What is the content of the NEED matrix?

NEED[i, j] = MAX[i, j] - ALLOCATION[i, j]

| | | | | | RES | OUR | CES | | | | | | |
|--------|-----------------------|---|-----|---|-----|------|-----|----|-------|-----------|-----------------|------|---|
| | | | MAX | | ALL | OCAT | ION | AV | AILAB | LE | | NEED | |
| | | A | В | С | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | I | 0 | 0 | - 1 | | | | 0 -0 = 0 | | |
| R | T_1 | ı | 7 | 5 | I | 0 | 0 | | | | | | |
| E A | T ₂ | 2 | 3 | 5 | ı | 3 | 5 | | | | | | |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | | | | |
| | Total | | | | 2 | 9 | 9 | 1 | 5 | 2 | | | |

Q2: What is the content of the NEED matrix?

NEED[i, j] = MAX[i, j] - ALLOCATION[i, j]

| | | | | | RES | OUR | CES | | | | | | |
|--------|-----------------------|---|-----|---|-----|------|-----|----|-------|-----|---|-----------------------|---|
| | | | MAX | | ALL | OCAT | ION | AV | AILAB | BLE | | NEED | |
| | | A | В | С | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | T | 0 | 0 | -1 | | | | 0 | 0-0 = 0 | |
| R | T ₁ | 1 | 7 | 5 | I | 0 | 0 | | | | | | |
| E A | T ₂ | 2 | 3 | 5 | - 1 | 3 | 5 | | | | | | |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | | | | |
| | Total | | | | 2 | 9 | 9 | -1 | 5 | 2 | | | |

Q2: What is the content of the NEED matrix?

NEED[i, j] = MAX[i, j] - ALLOCATION[i, j]

| | | | | | RES | OUR | CES | | | | | | |
|--------|-----------------------|---|-----|---|-----|------|-----|----|-------|-----|---|------|---------|
| | | | MAX | | ALL | OCAT | ION | AV | AILAE | BLE | | NEED | |
| | | A | В | С | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | 1 | 0 | 0 | 1 | | | | 0 | 0 | I-I = 0 |
| R | T ₁ | 1 | 7 | 5 | - I | 0 | 0 | | | | | | |
| E A | T ₂ | 2 | 3 | 5 | I | 3 | 5 | | | | | | |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | | | | |
| | Total | | | | 2 | 9 | 9 | -1 | 5 | 2 | | | |

Q2: What is the content of the NEED matrix?

NEED[i, j] = MAX[i, j] - ALLOCATION[i, j]

| | | | | | RES | OUR | CES | | | | | | |
|--------|-----------------------|---|-----|---|-----|------|-----|----|-------|----|---|------|---|
| | | | MAX | | ALL | OCAT | ION | AV | AILAB | LE | | NEED | |
| | | A | В | С | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | I | 0 | 0 | I | | | | 0 | 0 | 0 |
| R | T ₁ | 1 | 7 | 5 | I | 0 | 0 | | | | 0 | 7 | 5 |
| E A | T ₂ | 2 | 3 | 5 | I | 3 | 5 | | | | I | 0 | 0 |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | | 0 | 0 | 2 |
| | Total | | | | 2 | 9 | 9 | 1 | 5 | 2 | | | |

Q3: Is the system in a safe state? Why?

| | | | | | RES | OUR | CES | | | | | | |
|--------|-----------------------|---|-----|-----|-----|------|-----|----|-------|-----|---|------|---|
| | | | MAX | | ALL | OCAT | ION | AV | AILAE | BLE | | NEED | |
| | | A | В | С | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | - 1 | 0 | 0 | -1 | | | | 0 | 0 | 0 |
| R | T ₁ | 1 | 7 | 5 | ı | 0 | 0 | | | | 0 | 7 | 5 |
| E A | T ₂ | 2 | 3 | 5 | ı | 3 | 5 | | | | 1 | 0 | 0 |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | | 0 | 0 | 2 |
| | Total | | | | 2 | 9 | 9 | -1 | 5 | 2 | | | |

Let's start with T₀

| | | | | | RES | OUR | CES | | | | | | |
|--------|-----------------------|---|-----|---|-----|------|-----|----|-------|-----|---|------|---|
| | | | MAX | | ALL | OCAT | ION | AV | AILAE | BLE | | NEED | |
| | | A | В | С | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | I | 0 | 0 | I | | | | 0 | 0 | 0 |
| R | T ₁ | ı | 7 | 5 | I | 0 | 0 | | | | 0 | 7 | 5 |
| E A | T ₂ | 2 | 3 | 5 | - 1 | 3 | 5 | | | | I | 0 | 0 |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | | 0 | 0 | 2 |
| | Total | | | | 2 | 9 | 9 | I | 5 | 2 | | | |

Eventually, T_0 finishes and releases all its resources

| | | | | | RES | OUR | CES | | | | | | |
|--------|-----------------------|-----|-----|---|-----|------|-----|----|-------|-----|---|------|---|
| | | | MAX | | ALL | OCAT | ION | AV | AILAE | BLE | | NEED | |
| | | A | В | С | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | T | - | - | - | | | | - | - | - |
| R | T ₁ | - 1 | 7 | 5 | I | 0 | 0 | | | | 0 | 7 | 5 |
| E A | T ₂ | 2 | 3 | 5 | - 1 | 3 | 5 | | | | I | 0 | 0 |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | | 0 | 0 | 2 |
| | Total | | | | 2 | 9 | 8 | I | 5 | 3 | | | |

 T_1 can't execute as it still might NEED (0, 7, 5) and AVAILABLE = (1, 5, 3)

| | | | | | RES | OUR | CES | | | | | | |
|--------|-----------------------|---|-----|---|-----|------|-----|----|-------|----|---|------|---|
| | | | MAX | | ALL | OCAT | ION | AV | AILAB | LE | | NEED | |
| | | A | В | С | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | I | - | - | - | | | | - | - | - |
| R | T ₁ | I | 7 | 5 | I | 0 | 0 | | | | 0 | 7 | 5 |
| E A | T ₂ | 2 | 3 | 5 | - 1 | 3 | 5 | | | | ı | 0 | 0 |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | | 0 | 0 | 2 |
| | Total | | | | 2 | 9 | 8 | 1 | 5 | 3 | | | |

 T_2 can execute as it still might NEED (1, 0, 0) and AVAILABLE = (1, 5, 3)

| | | | | | RES | OUR | CES | | | | | | |
|--------|-----------------------|---|-----|---|-----|------|-----|----|-------|-----|---|------|---|
| | | | MAX | | ALL | OCAT | ION | AV | AILAB | BLE | | NEED | |
| | | A | В | С | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | ı | - | - | - | | | | - | - | - |
| R | T_1 | 1 | 7 | 5 | I | 0 | 0 | | | | 0 | 7 | 5 |
| E A | T ₂ | 2 | 3 | 5 | I | 3 | 5 | | | | I | 0 | 0 |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | | 0 | 0 | 2 |
| | Total | | | | 2 | 9 | 8 | 1 | 5 | 3 | | | |

 T_2 can execute as it still might NEED (1, 0, 0) and AVAILABLE = (1, 5, 3)

| | | | | | RES | OUR | CES | | | | | | |
|--------|-----------------------|---|-----|---|-----|------|-----|----|-------|-----|---|------|---|
| | | | MAX | | ALL | OCAT | ION | AV | AILAB | BLE | | NEED | |
| | | A | В | С | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | I | - | - | - | | | | - | - | - |
| R | T_1 | 1 | 7 | 5 | - 1 | 0 | 0 | | | | 0 | 7 | 5 |
| E A | T ₂ | 2 | 3 | 5 | 2 | 3 | 5 | | | | 0 | 0 | 0 |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | | 0 | 0 | 2 |
| | Total | | | | 3 | 9 | 8 | 0 | 5 | 3 | | | |

T₂ eventually finishes and releases all its resources

| | | | | | RES | OUR | CES | | | | | | |
|--------|-----------------------|----|-----|----|-----|------|-----|----|-------|-----|---|------|---|
| | | | MAX | | ALL | OCAT | ION | AV | AILAE | BLE | | NEED | |
| | | A | В | С | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | -1 | - | - | - | | | | - | - | - |
| R | T ₁ | -1 | 7 | 5 | - 1 | 0 | 0 | | | | 0 | 7 | 5 |
| E A | T ₂ | 2 | 3 | 5 | - | - | - | | | | - | - | - |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | | 0 | 0 | 2 |
| | Total | | | | T | 6 | 3 | 2 | 8 | 8 | | | |

 T_3 can execute as it still might NEED (0, 0, 2) and AVAILABLE = (2, 8, 8)

| | | | | | RES | OUR | CES | | | | | | |
|--------|-----------------------|----|-----|-----|-----|------|-----|----|-------|-----|---|------|---|
| | | | MAX | | ALL | OCAT | ION | AV | AILAE | BLE | | NEED | |
| | | A | В | С | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | - 1 | - | - | - | | | | - | - | - |
| R | T ₁ | -1 | 7 | 5 | - 1 | 0 | 0 | | | | 0 | 7 | 5 |
| E A | T ₂ | 2 | 3 | 5 | - | - | - | | | | - | - | - |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | | 0 | 0 | 2 |
| | Total | | | | - 1 | 6 | 3 | 2 | 8 | 8 | | | |

 T_3 can execute as it still might NEED (0, 0, 2) and AVAILABLE = (2, 3, 6)

| | | | | | RES | SOUR | CES | | | | | | |
|--------|----------------|---|-----|----|-----|------|-----|----|-------|-----|---|------|---|
| | | | MAX | | ALL | OCAT | ION | AV | AILAE | BLE | | NEED | |
| | | A | В | С | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | -1 | - | - | - | | | | - | - | - |
| R | T ₁ | I | 7 | 5 | - 1 | 0 | 0 | | | | 0 | 7 | 5 |
| E A | T ₂ | 2 | 3 | 5 | - | - | - | | | | - | - | - |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 5 | | | | 0 | 0 | 0 |
| | Total | | | | 1 | 6 | 5 | 2 | 8 | 6 | | | |

T₃ eventually finishes and releases all its resources

| | | | | | RES | OUR | CES | | | | | | |
|--------|-----------------------|---|-----|---|-----|------|-----|----|-------|-----|---|------|---|
| | | | MAX | | ALL | OCAT | ION | AV | AILAE | BLE | | NEED | |
| | | A | В | С | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | I | - | - | - | | | | - | - | - |
| R | T ₁ | 1 | 7 | 5 | -1 | 0 | 0 | | | | 0 | 7 | 5 |
| E A | T ₂ | 2 | 3 | 5 | - | - | - | | | | - | - | - |
| D S | T ₃ | 0 | 6 | 5 | - | - | - | | | | - | - | - |
| | Total | | | | ı | 0 | 0 | 2 | 14 | -11 | | | |

 T_1 can now execute since NEED (0, 7, 5) and AVAILABLE = (2, 14, 11)

| | | | | | RES | OUR | CES | | | | | | |
|--------|-----------------------|---|-----|---|-----|------|-----|----|-------|-----|---|------|---|
| | | | MAX | | ALL | OCAT | ION | AV | AILAE | BLE | | NEED | |
| | | A | В | С | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | 1 | - | - | - | | | | - | - | - |
| R | T ₁ | I | 7 | 5 | I | 7 | 5 | | | | 0 | 0 | 0 |
| E A | T ₂ | 2 | 3 | 5 | - | - | - | | | | - | - | - |
| D S | T ₃ | 0 | 6 | 5 | - | - | - | | | | - | - | - |
| | Total | | | | - 1 | 7 | 5 | 2 | 7 | 6 | | | |

We have found a sequence of execution T_0, T_2, T_3, T_1 which leads to safe state!

| | | | | | RES | OUR | CES | | | | | | |
|--------|-----------------------|---|-----|---|-----|------|-----|----|-------|-----|---|------|---|
| | | | MAX | | ALL | OCAT | ION | AV | AILAE | BLE | | NEED | |
| | | A | В | С | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | I | - | - | - | | | | - | - | - |
| R | T_1 | I | 7 | 5 | - | - | - | | | | - | - | - |
| E A | T ₂ | 2 | 3 | 5 | - | - | - | | | | - | - | - |
| D S | T ₃ | 0 | 6 | 5 | - | - | - | | | | - | - | - |
| | Total | | | | - | - | - | 3 | 14 | 11 | | | |

Q4: If T_1 issues a REQUEST (0, 5, 2), can this be granted immediately?

| | | | | | RES | OUR | CES | | | | | | |
|--------|-----------------------|---|-----|---|-----|------|-----|----|-------|-----------|---|------|---|
| | | | MAX | | ALL | OCAT | ION | AV | AILAE | LE | | NEED | |
| | | A | В | С | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | I | 0 | 0 | - 1 | | | | 0 | 0 | 0 |
| R | T ₁ | 1 | 7 | 5 | -1 | 0 | 0 | | | | 0 | 7 | 5 |
| E A | T ₂ | 2 | 3 | 5 | -1 | 3 | 5 | | | | 1 | 0 | 0 |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | | 0 | 0 | 2 |
| | Total | | | | 2 | 9 | 9 | 1 | 5 | 2 | | | |

We have to ask ourselves: I. if the request can be satisfied; 2. if it will lead to a safe state

| | | | | | RES | OUR | CES | | | | | | |
|--------|-----------------------|---|-----|---|-----|------|-----|----|-------|-----------|---|------|---|
| | | | MAX | | ALL | OCAT | ION | AV | AILAE | LE | | NEED | |
| | | A | В | С | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | I | 0 | 0 | - 1 | | | | 0 | 0 | 0 |
| R | T ₁ | 1 | 7 | 5 | -1 | 0 | 0 | | | | 0 | 7 | 5 |
| E A | T ₂ | 2 | 3 | 5 | -1 | 3 | 5 | | | | 1 | 0 | 0 |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | | 0 | 0 | 2 |
| | Total | | | | 2 | 9 | 9 | 1 | 5 | 2 | | | |

To answer I. check if: a. REQUEST <= NEED and b. REQUEST <= AVAILABLE

| | | | | | RES | OUR | CES | | | | | | |
|--------|-----------------------|-----|-----|----|-----|------|-----|----|-------|-----|---|------|---|
| | | | MAX | | ALL | OCAT | ION | AV | AILAE | BLE | | NEED | |
| | | A | В | С | A | В | С | A | В | C | A | В | С |
| T H | T ₀ | 0 | 0 | -1 | 0 | 0 | -1 | | | | 0 | 0 | 0 |
| R | T_1 | - 1 | 7 | 5 | -1 | 0 | 0 | | | | 0 | 7 | 5 |
| E A | T ₂ | 2 | 3 | 5 | - 1 | 3 | 5 | | | | 1 | 0 | 0 |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | | 0 | 0 | 2 |
| | Total | | | | 2 | 9 | 9 | I | 5 | 2 | | | |

I.a. REQUEST <= NEED?

| | | RESOURCES | | | | | | | | | | | |
|-----------|-----------------------|-----------|---|-----|------------|---|----|-----------|---|---|------|---|---|
| | | MAX | | | ALLOCATION | | | AVAILABLE | | | NEED | | |
| | | A B C | | | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | - 1 | 0 | 0 | -1 | | | | 0 | 0 | 0 |
| R T_1 | T ₁ | 1 | 7 | 5 | -1 | 0 | 0 | | | | 0 | 7 | 5 |
| E A | T ₂ | 2 | 3 | 5 | -1 | 3 | 5 | | | | 1 | 0 | 0 |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | | 0 | 0 | 2 |
| | Total | | | | 2 | 9 | 9 | -1 | 5 | 2 | | | |

I.a. REQUEST <= NEED?

YES! $(0, 5, 2) \le (0, 7, 5)$

| | | RESOURCES | | | | | | | | | | | |
|--------|-----------------------|-----------|---|---|------------|---|---|-----------|---|---|------|---|---|
| | | MAX | | | ALLOCATION | | | AVAILABLE | | | NEED | | |
| | | A B C | | A | В | С | A | В | С | A | В | С | |
| T H | T ₀ | 0 | 0 | I | 0 | 0 | I | | | | 0 | 0 | 0 |
| R | T ₁ | 1 | 7 | 5 | I | 0 | 0 | | | | 0 | 7 | 5 |
| E A | T ₂ | 2 | 3 | 5 | ı | 3 | 5 | | | | I | 0 | 0 |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | | 0 | 0 | 2 |
| | Total | | | | 2 | 9 | 9 | I | 5 | 2 | | | |

I.b. REQUEST <= AVAILABLE?

| | | RESOURCES | | | | | | | | | | | |
|--|-----------------------|-----------|---|---|------------|---|---|-----------|---|---|------|---|---|
| | | MAX | | | ALLOCATION | | | AVAILABLE | | | NEED | | |
| | | A B C | | | A | В | С | A | В | С | A | В | С |
| $\begin{array}{ccc} T & & T_0 \\ H & & \\ R & & T_1 \end{array}$ | T ₀ | 0 | 0 | I | 0 | 0 | I | | | | 0 | 0 | 0 |
| | T ₁ | 1 | 7 | 5 | -1 | 0 | 0 | | | | 0 | 7 | 5 |
| E A | T ₂ | 2 | 3 | 5 | -1 | 3 | 5 | | | | I | 0 | 0 |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | | 0 | 0 | 2 |
| | Total | | | | 2 | 9 | 9 | -1 | 5 | 2 | | | |

I.b. REQUEST <= AVAILABLE? YES! (0, 5, 2) <= (1, 5, 2)

| | | RESOURCES | | | | | | | | | | | |
|-----------|-----------------------|-----------|---|-----|------------|---|----|-----------|---|---|------|---|---|
| | | MAX | | | ALLOCATION | | | AVAILABLE | | | NEED | | |
| | | A B C | | | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | - 1 | 0 | 0 | -1 | | | | 0 | 0 | 0 |
| R T_1 | T ₁ | 1 | 7 | 5 | -1 | 0 | 0 | | | | 0 | 7 | 5 |
| E A | T ₂ | 2 | 3 | 5 | -1 | 3 | 5 | | | | 1 | 0 | 0 |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | | 0 | 0 | 2 |
| | Total | | | | 2 | 9 | 9 | -1 | 5 | 2 | | | |

To answer 2. we simulate the request is granted and see if we are still in a safe state

| | | | | | RES | OUR | CES | | | | | | |
|--------|-----------------------|---|-----|-----|-----|------|-----|----|-------|-----|---|------|---|
| | | | MAX | | ALL | OCAT | ION | AV | AILAE | BLE | | NEED | |
| | | A | В | С | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | - 1 | 0 | 0 | -1 | | | | 0 | 0 | 0 |
| R | T ₁ | 1 | 7 | 5 | ı | 0 | 0 | | | | 0 | 7 | 5 |
| E A | T ₂ | 2 | 3 | 5 | ı | 3 | 5 | | | | 1 | 0 | 0 |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | | 0 | 0 | 2 |
| | Total | | | | 2 | 9 | 9 | -1 | 5 | 2 | | | |

To answer 2. we simulate the request is granted and see if we are still in a safe state

| | | | | | RES | OUR | CES | | | | | | |
|--------|-----------------------|-----|-----|----|-----|------|-----|----|-------|-----|---|------|---|
| | | | MAX | | ALL | OCAT | ION | AV | AILAE | BLE | | NEED | |
| | | A | В | С | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | -1 | 0 | 0 | -1 | | | | 0 | 0 | 0 |
| R | T ₁ | - 1 | 7 | 5 | 1 | 5 | 2 | | | | 0 | 2 | 3 |
| E A | T ₂ | 2 | 3 | 5 | I | 3 | 5 | | | | I | 0 | 0 |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | | 0 | 0 | 2 |
| | Total | | | | 2 | 14 | -11 | T | 0 | 0 | | | |

Let's start with T₀

| | | | | | RES | OUR | CES | | | | | | |
|--------|-----------------------|-----|-----|---|-----|------|-----|----|-------|-----|---|------|---|
| | | | MAX | | ALL | OCAT | ION | AV | AILAE | BLE | | NEED | |
| | | A | В | С | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | I | 0 | 0 | I | | | | 0 | 0 | 0 |
| R | T ₁ | - 1 | 7 | 5 | I | 5 | 2 | | | | 0 | 2 | 3 |
| E A | T ₂ | 2 | 3 | 5 | - 1 | 3 | 5 | | | | I | 0 | 0 |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | | 0 | 0 | 2 |
| | Total | | | | 2 | 14 | 11 | 1 | 0 | 0 | | | |

Eventually, T_0 finishes and releases all its resources

| | | | | | RES | OUR | CES | | | | | | |
|--------|-----------------------|-----|-----|---|-----|------|-----|----|-------|-----|---|------|---|
| | | | MAX | | ALL | OCAT | ION | AV | AILAE | BLE | | NEED | |
| | | A | В | С | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | I | - | - | - | | | | - | - | - |
| R | T ₁ | - 1 | 7 | 5 | I | 5 | 2 | | | | 0 | 2 | 3 |
| E A | T ₂ | 2 | 3 | 5 | - 1 | 3 | 5 | | | | I | 0 | 0 |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | | 0 | 0 | 2 |
| | Total | | | | 2 | 14 | 10 | T | 0 | 1 | | | |

 T_1 can't execute as it still might NEED (0, 2, 3) and AVAILABLE = (1, 0, 1)

| | | | | | RES | OUR | CES | | | | | | |
|--------|-----------------------|---|-----|-----|-----|------|-----|----|-------|-----|---|------|---|
| | | | MAX | | ALL | OCAT | ION | AV | AILAE | BLE | | NEED | |
| | | A | В | С | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | - 1 | - | - | - | | | | - | - | - |
| R | T ₁ | I | 7 | 5 | I | 5 | 2 | | | | 0 | 2 | 3 |
| E A | T ₂ | 2 | 3 | 5 | - 1 | 3 | 5 | | | | I | 0 | 0 |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | | 0 | 0 | 2 |
| | Total | | | | 2 | 14 | 10 | -1 | 0 | 1 | | | |

 T_2 can execute as it still might NEED (1, 0, 0) and AVAILABLE = (1, 0, 1)

| | | | | | RES | OUR | CES | | | | | | |
|--------|-----------------------|----|-----|---|-----|------|-----|----|--------|-----|---|------|---|
| | | | MAX | | ALL | OCAT | ION | AV | /AILAB | BLE | | NEED | |
| | | A | В | С | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | I | - | - | - | | | | - | - | - |
| R | T_1 | 1_ | 7 | 5 | - 1 | 5 | 2 | | | | 0 | 2 | 3 |
| E A | T ₂ | 2 | 3 | 5 | I | 3 | 5 | | | | I | 0 | 0 |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | | 0 | 0 | 2 |
| | Total | | | | 2 | 14 | 10 | I | 0 | 1 | | | |

 T_2 can execute as it still might NEED (1, 0, 0) and AVAILABLE = (1, 0, 1)

| | | | | | RES | OUR | CES | | | | | | |
|--------|-----------------------|---|-----|---|-----|------|-----|----|-------|-----|---|------|---|
| | | | MAX | | ALL | OCAT | ION | AV | AILAE | BLE | | NEED | |
| | | A | В | С | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | 1 | - | - | - | | | | - | - | - |
| R | T ₁ | I | 7 | 5 | I | 5 | 2 | | | | 0 | 2 | 3 |
| E A | T ₂ | 2 | 3 | 5 | 2 | 3 | 5 | | | | 0 | 0 | 0 |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | | 0 | 0 | 2 |
| | Total | | | | 3 | 14 | 10 | 0 | 0 | 1 | | | |

T₂ eventually finishes and releases all its resources

| | | | | | RES | OUR | CES | | | | | | |
|--------|-----------------------|-----|-----|----|-----|------|-----|----|-------|-----|---|------|---|
| | | | MAX | | ALL | OCAT | ION | AV | AILAE | BLE | | NEED | |
| | | A | В | С | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | -1 | - | - | - | | | | - | - | - |
| R | T_1 | - 1 | 7 | 5 | - 1 | 5 | 2 | | | | 0 | 2 | 3 |
| E A | T ₂ | 2 | 3 | 5 | - | - | - | | | | - | - | - |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | | 0 | 0 | 2 |
| | Total | | | | 1 | -11 | 5 | 2 | 3 | 6 | | | |

 T_3 can execute as it still might NEED (0, 0, 2) and AVAILABLE = (2, 3, 6)

| | | | | | RES | OUR | CES | | | | | | |
|--------|-----------------------|---|-----|----|-----|------|-----|----|-------|-----|---|------|---|
| | | | MAX | | ALL | OCAT | ION | AV | AILAE | BLE | | NEED | |
| | | A | В | С | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | -1 | - | - | - | | | | - | - | - |
| R | T ₁ | I | 7 | 5 | - 1 | 5 | 2 | | | | 0 | 2 | 3 |
| E A | T ₂ | 2 | 3 | 5 | - | - | - | | | | - | - | - |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 3 | | | | 0 | 0 | 2 |
| | Total | | | | - 1 | 11 | 5 | 2 | 3 | 6 | | | |

 T_3 can execute as it still might NEED (0, 0, 2) and AVAILABLE = (2, 3, 6)

| | | | | | RES | OUR | CES | | | | | | |
|--------|-----------------------|---|-----------|---|-----|------|-----|----|-------|-----|---|------|---|
| | | | MAX | | ALL | OCAT | ION | AV | AILAE | BLE | | NEED | |
| | | A | A B C 0 1 | | | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | I | - | - | - | | | | - | - | - |
| R | T_1 | 1 | 7 | 5 | T | 5 | 2 | | | | 0 | 2 | 3 |
| E A | T ₂ | 2 | 3 | 5 | - | - | - | | | | - | - | - |
| D S | T ₃ | 0 | 6 | 5 | 0 | 6 | 5 | | | | 0 | 0 | 0 |
| | Total | | | | - 1 | 11 | 7 | 2 | 3 | 4 | | | |

T₃ eventually finishes and releases all its resources

| | | | | | RES | OUR | CES | | | | | | |
|--------|----------------|----|-----|----|-----|------|-----|----|-------|-----|---|------|---|
| | | | MAX | | ALL | OCAT | ION | AV | AILAE | BLE | | NEED | |
| | | A | В | C | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | -1 | - | - | - | | | | - | - | - |
| R | T ₁ | -1 | 7 | 5 | - 1 | 5 | 2 | | | | 0 | 2 | 3 |
| E A | T ₂ | 2 | 3 | 5 | - | - | - | | | | - | - | - |
| D S | T ₃ | 0 | 6 | 5 | - | - | - | | | | - | - | - |
| | Total | | | | 1 | 5 | 2 | 2 | 9 | 9 | | | |

 T_1 can now execute since NEED (0, 2, 3) and AVAILABLE = (2, 9, 9)

| | | | | | RES | OUR | CES | | | | | | |
|--------|----------------|---|-----|---|-----|------|-----|----|-------|-----|---|------|---|
| | | | MAX | | ALL | OCAT | ION | AV | AILAE | BLE | | NEED | |
| | | A | В | С | A | В | С | A | В | С | A | В | С |
| T H | T ₀ | 0 | 0 | I | - | - | - | | | | - | - | - |
| R | T ₁ | ı | 7 | 5 | - 1 | 7 | 5 | | | | 0 | 0 | 0 |
| E A | T ₂ | 2 | 3 | 5 | - | - | - | | | | - | - | - |
| D S | T ₃ | 0 | 6 | 5 | - | - | - | | | | - | - | - |
| | Total | | | | I | 7 | 5 | 2 | 7 | 6 | | | |

We have found a sequence of execution T_0, T_2, T_3, T_1 which leads to safe state!

| | | | RESOURCES | | | | | | | | | | |
|----------------------------|-----------------------|-----|-----------|---|------------|---|---|-----------|----|----|------|---|---|
| | | MAX | | | ALLOCATION | | | AVAILABLE | | | NEED | | |
| | | A | В | С | A | В | С | A | В | С | A | В | С |
| T H R E A D | T ₀ | 0 | 0 | I | - | - | - | | | | - | - | - |
| | T_1 | I | 7 | 5 | - | - | - | | | | - | - | - |
| | T ₂ | 2 | 3 | 5 | - | - | - | | | | - | - | - |
| | T ₃ | 0 | 6 | 5 | - | - | - | | | | - | - | - |
| | Total | | | | - | - | - | 3 | 14 | 11 | | | |

 Deadlock → a situation in which a set of threads/processes cannot proceed because each one requires resources held by another

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- Detection and Recovery → recognize deadlock after it has occurred and break it
- Prevention → design resource allocation strategies which guarantee at least one of the 4 necessary deadlock conditions never holds
- Avoidance -> runtime checks to avoid deadlock online
- In practice, most OSs don't do anything and leave it all to applications