



Session 35

Unsupervised Learning



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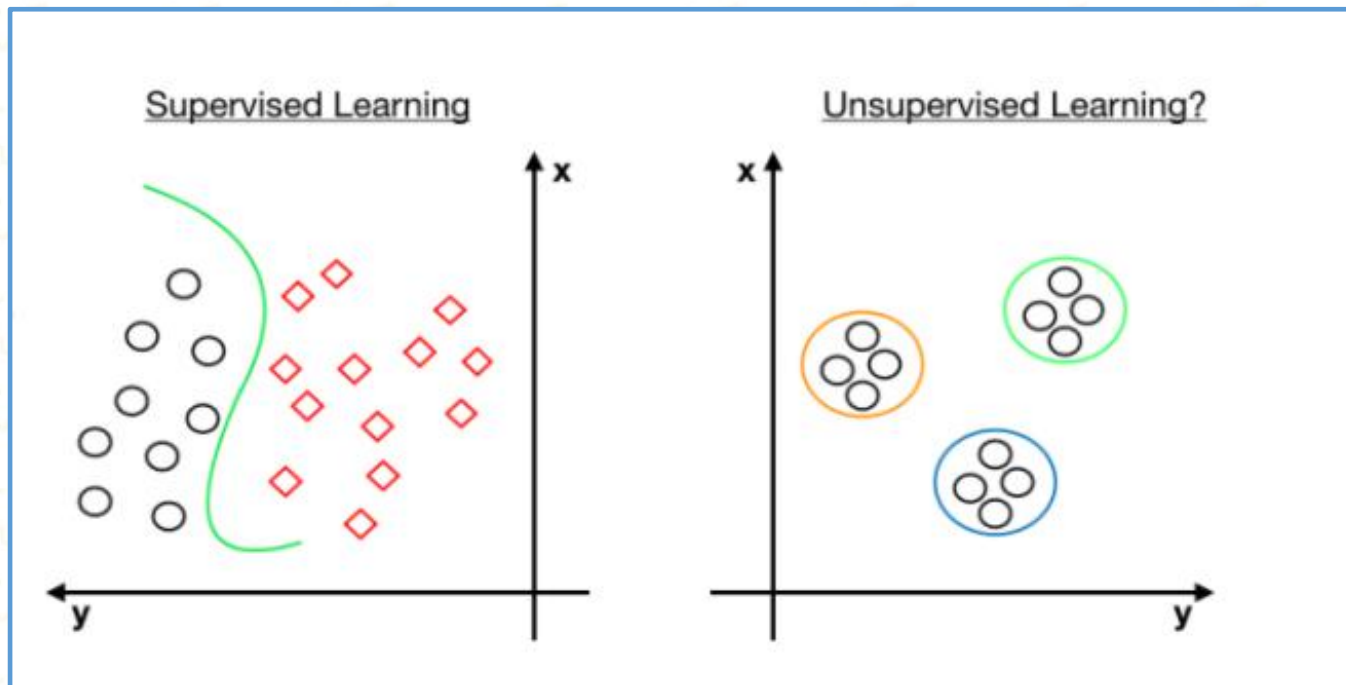
Unsupervised Learning





Supervised vs Unsupervised

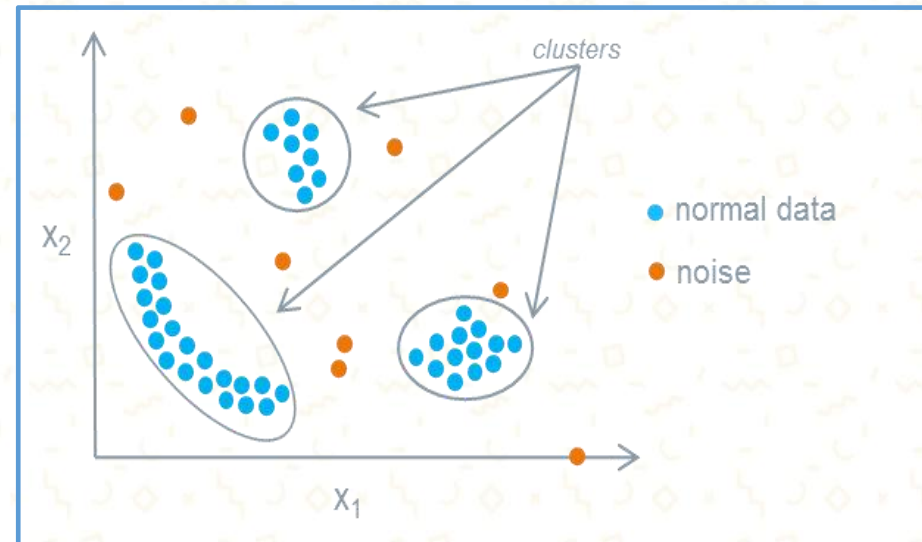
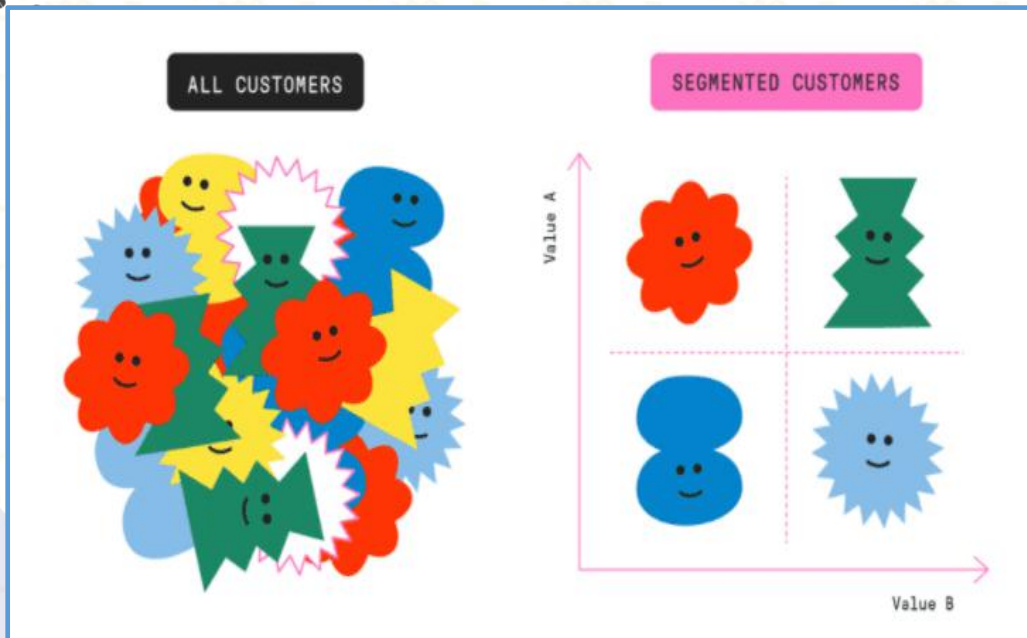
- **Supervised** = Learn to predict the outcome.
 - We know the target label, so we make the model that try to predict the label.
- **Unsupervised** = Finding pattern/ characteristic from data.
 - We do not know our target label, so we make model that try to group the data.





Application of Unsupervised Learning

- Customer segmentation.
 - Understanding different customer groups around which to build marketing or other business strategies.
- Anomaly detection.
- Recommender systems, which involve grouping together users with similar viewing patterns in order to recommend similar content.





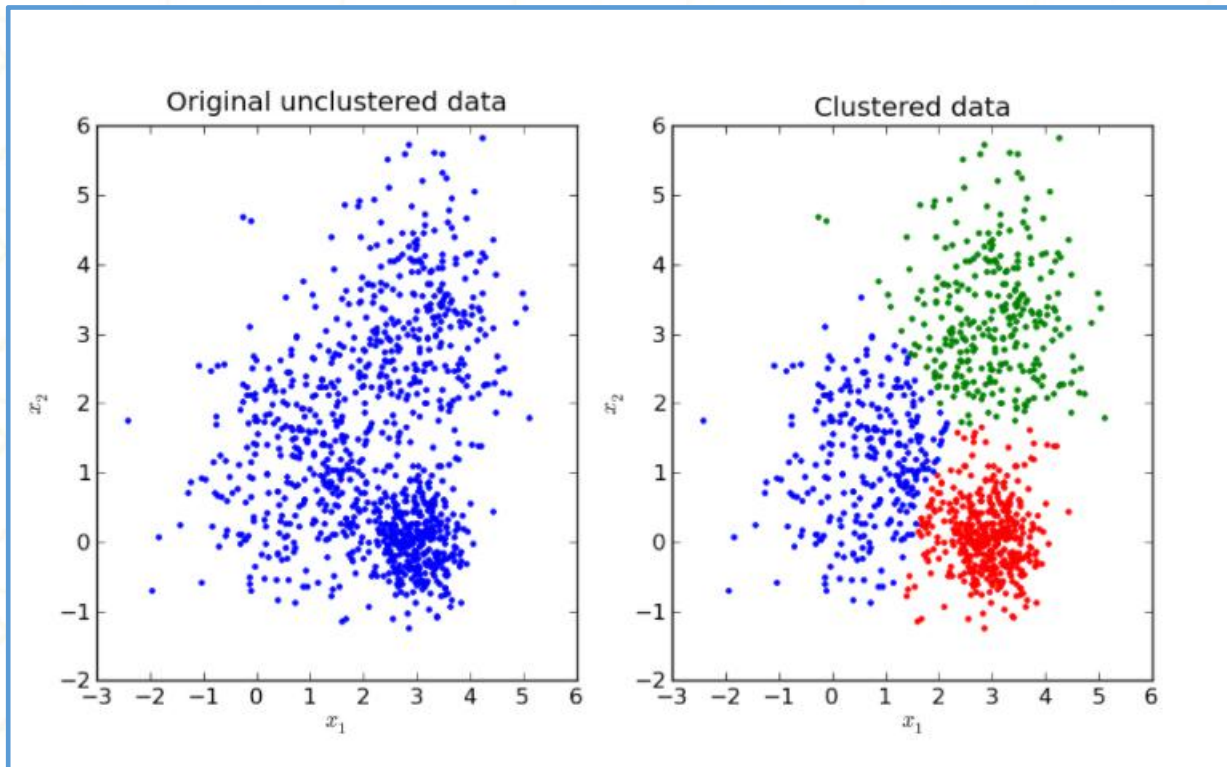
K-Means





K-Means

- K-means clustering algorithm tries to group similar items in the form of clusters.
- The number of groups is represented by K .





How K-Means works?

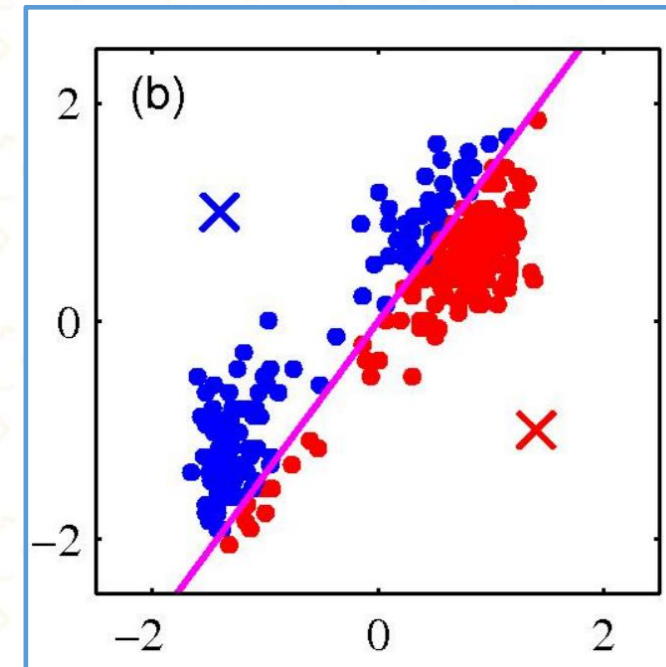
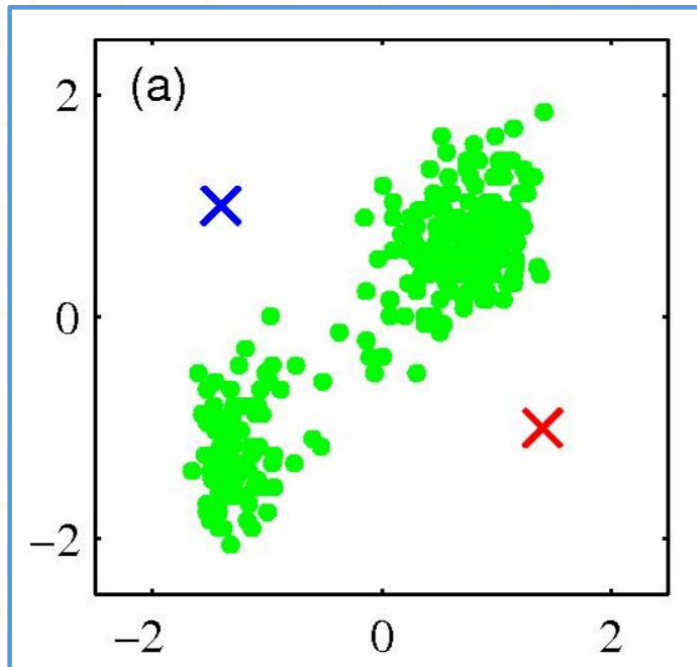
1. **Choose k objects** as initial cluster centers
2. **Assign each object** to the cluster with the nearest center
3. **Update cluster centers** as the mean point of the cluster
4. Go back to Step 2, stop when there is no change





How K-Means works?

- Pick K random points as cluster centers (means)
 - Shown here for $K=2$

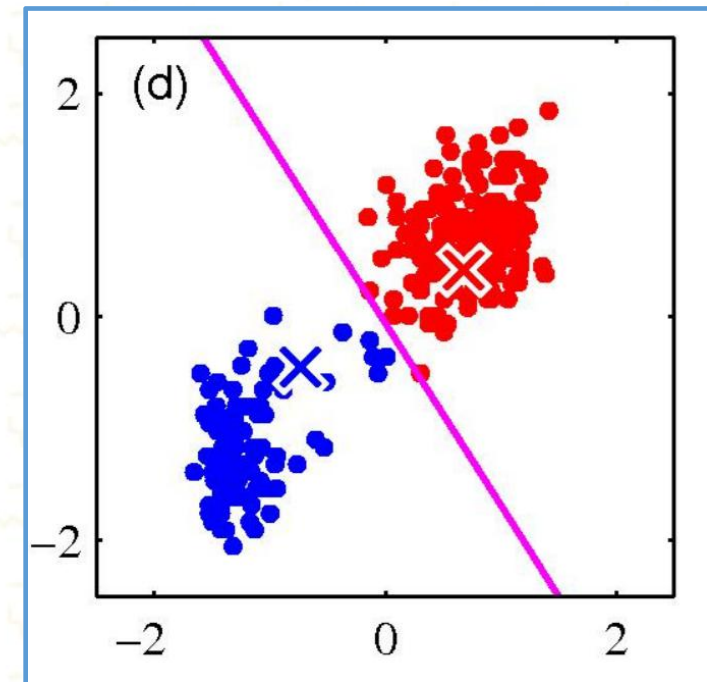
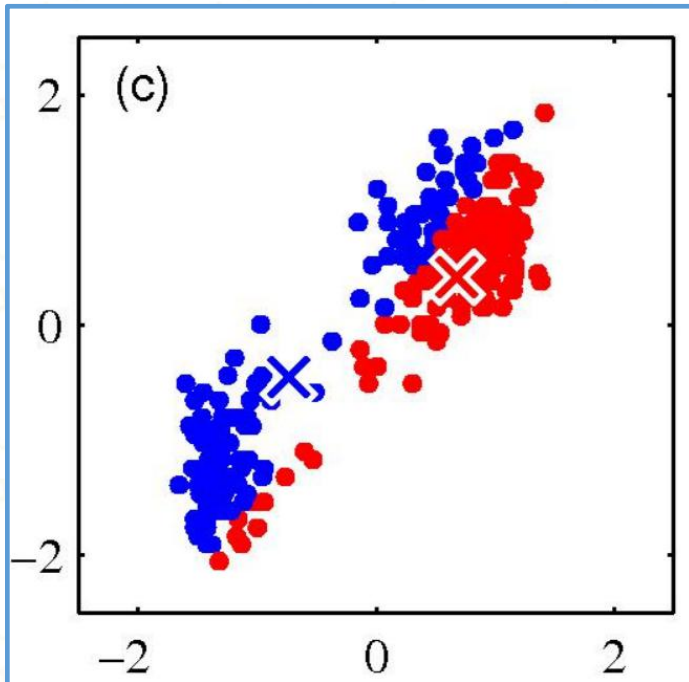


- Iterative Step 1
 - • Assign data points to closest cluster center



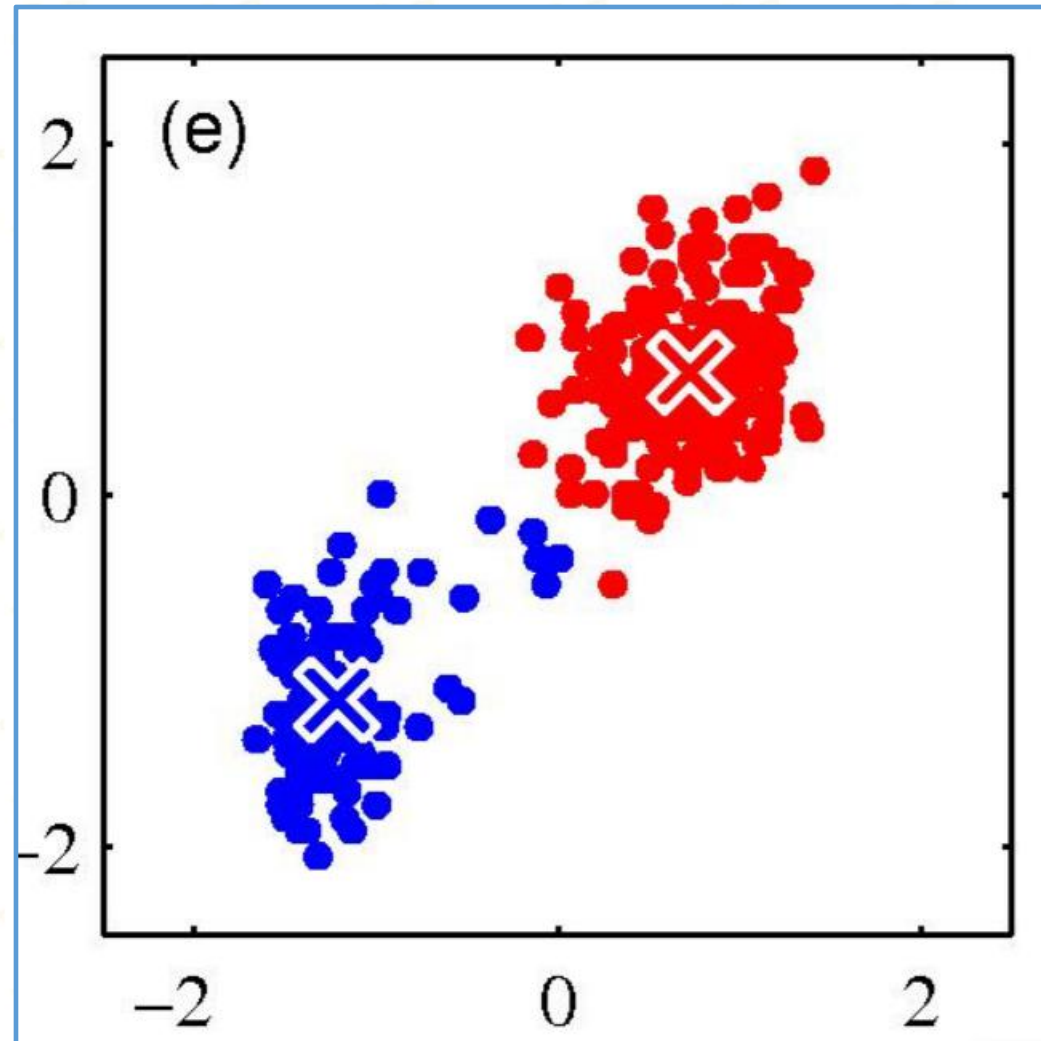
How K-Means works?

- Iterative Step 2
 - Update cluster center
 - Change the cluster center to the average of the assigned points
- Repeat until convergence





How K-Means works?





Evaluating clustering performance

1. Inertia

- Sum of squared distance from each point (x_i) to its cluster (C_k).
- If the inertia is small, it means that the points are close each other.

$$\sum_{i=1}^n (x_i - C_k)^2$$

2. Silhouette score

- a : mean distance to all other points in its cluster.
- b : mean distance to all other points in the next nearest cluster.
- The score range between -1 to 1. It is better when the score is near to 1.

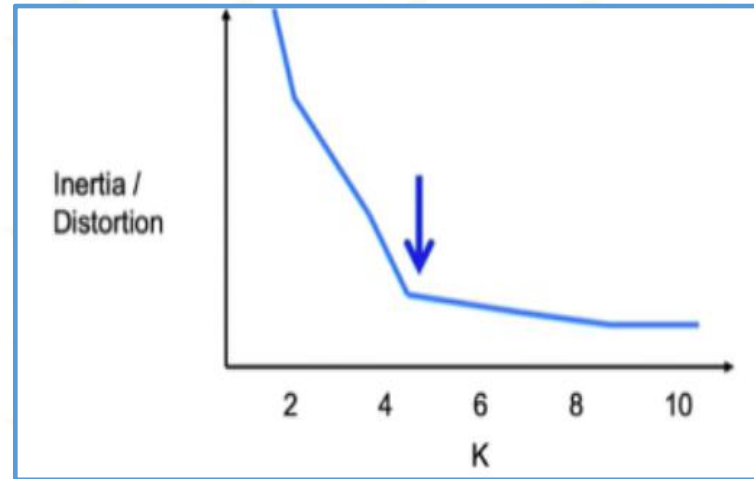
$$SC = \frac{b-a}{\max(a,b)}$$





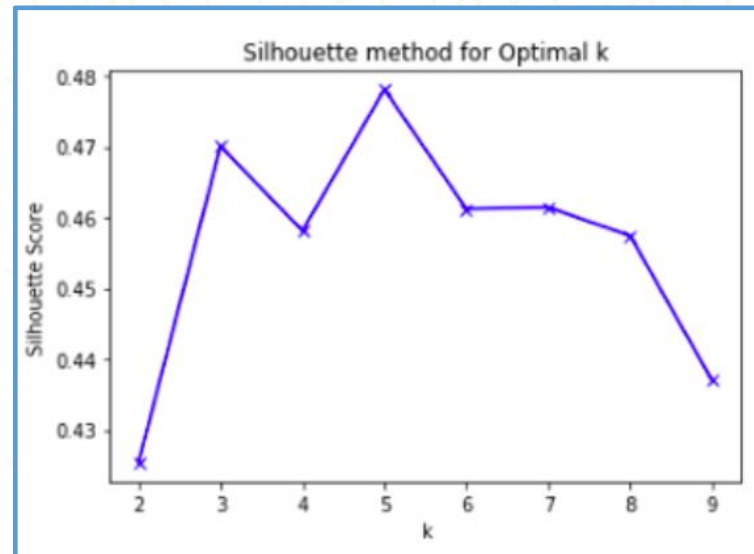
How to choose the K?

1. Elbow method



2. Silhouette score

- High score is better





Discussion on the K-means

▣ Advantages of K-means

- It is very simple to implement.
- It is scalable to a huge data set and also faster to large datasets.
- It adapts the new examples very frequently.
- Generalization of clusters for different shapes and sizes.



▣ Disadvantages of K-means

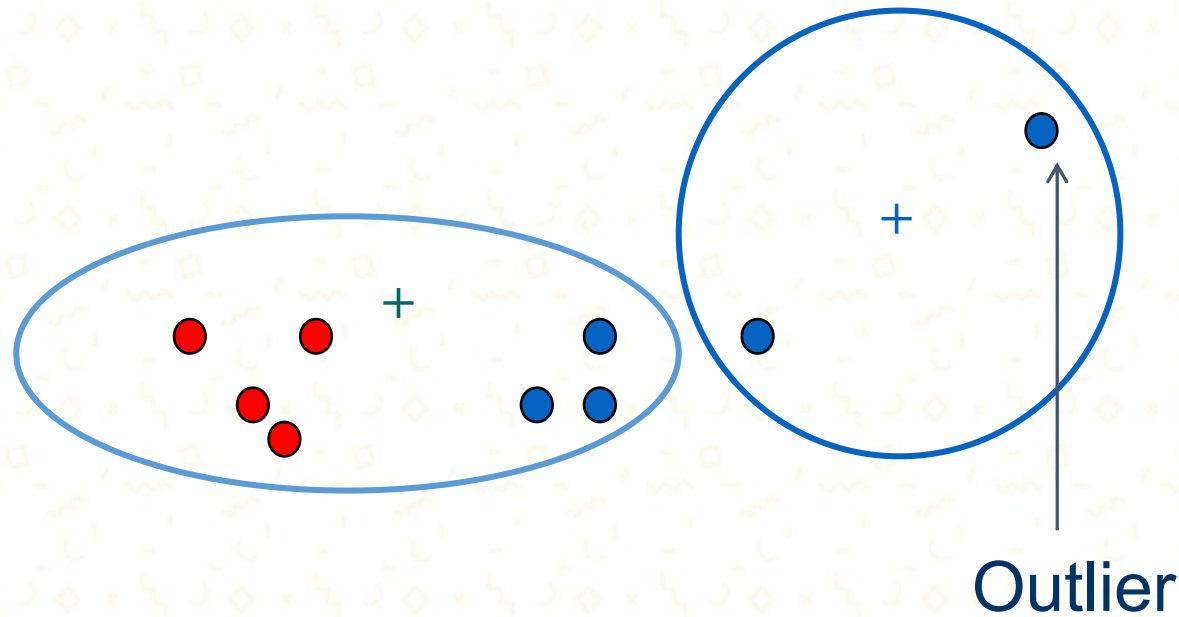
- It is sensitive to the outliers.
- Choosing the k values manually is a tough job.
- As the number of dimensions increases its scalability decreases.





A Problem of K-Means

- Sensitive to outliers
- Outlier: objects with extremely large (or small) values





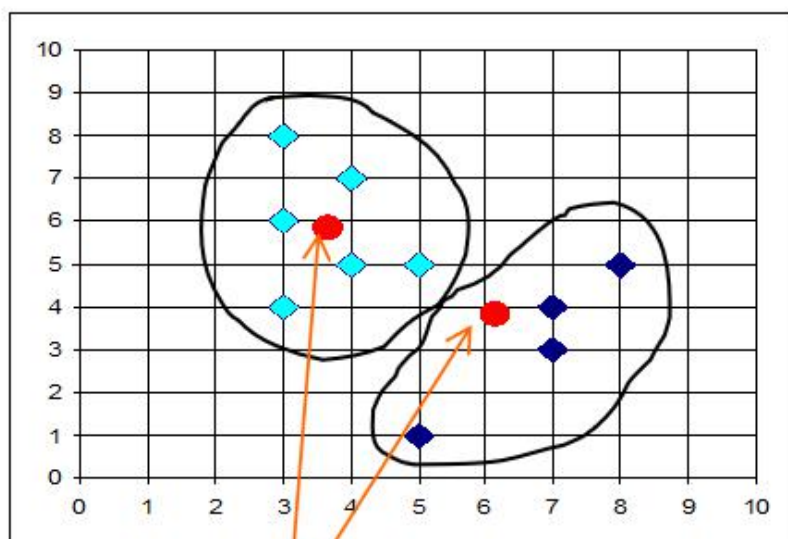
K-Medoids



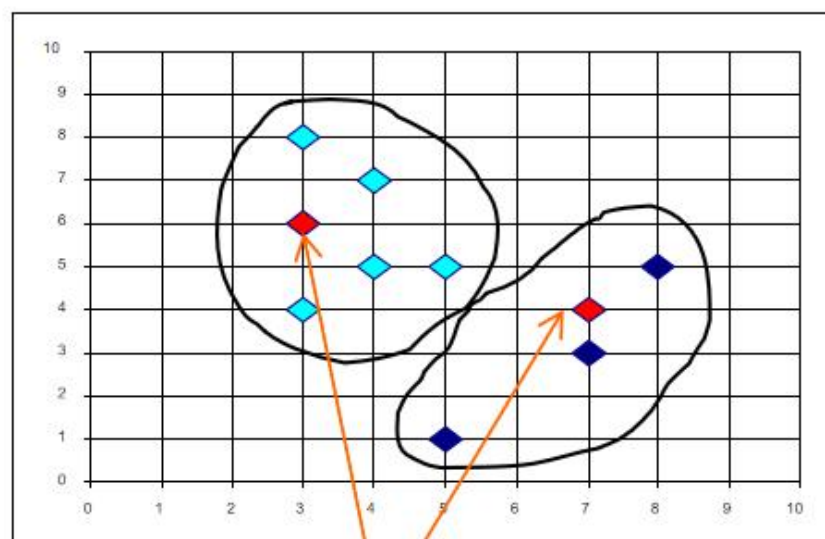


K-Medoids

- K-medoids: Find k representative objects, called medoids.
 - While K-Means tries to minimize the within cluster sum-of-squares,
 - K-Medoids tries to minimize the sum of distances between each point and the medoid of its cluster.



k-means



k-medoids



How K-Medoids (PAM) works?

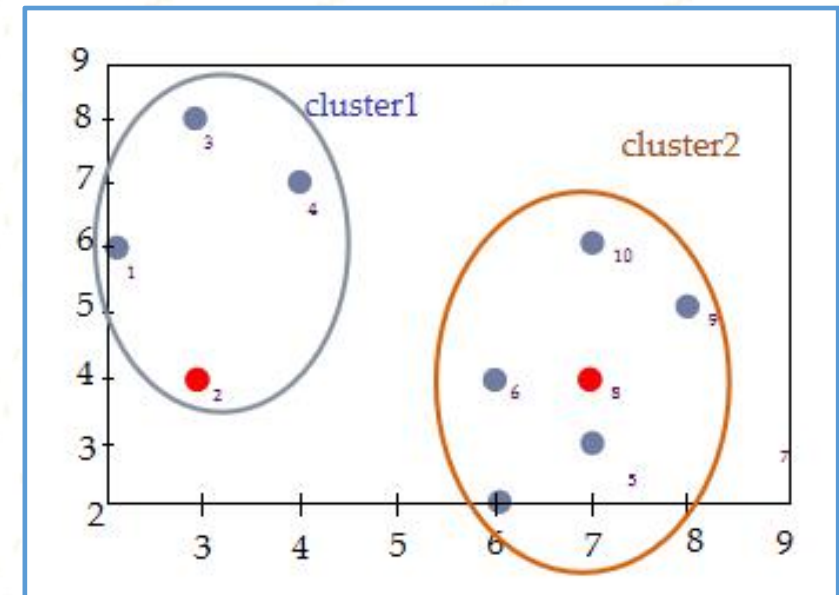
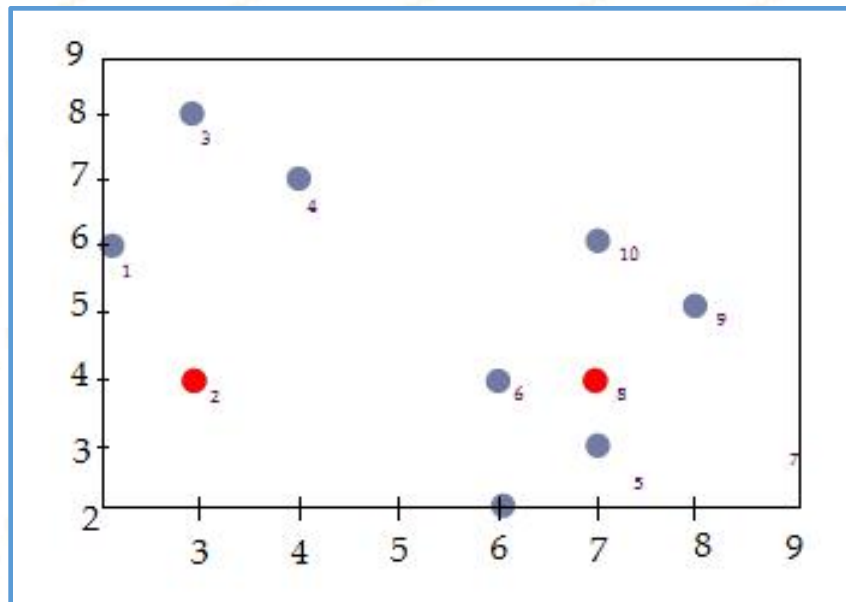
- Partitioning Around Medoids (PAM)
 - 1. Initialize: select k random points out of the n data points as the medoids.
 - 2. Repeat:
 - Assign each point to the cluster with the closest medoid m .
 - Randomly select a non-representative object oi
 - Compute the total cost of swapping S , the medoid m with oi
 - If $S < 0$:
 - Swap m with oi to form new set of medoids.
 - Stop when convergence criteria is meet.





How K-Medoids works?

- Pick K random medoids
- Shown here for K=2
- Assign data points to closest cluster center

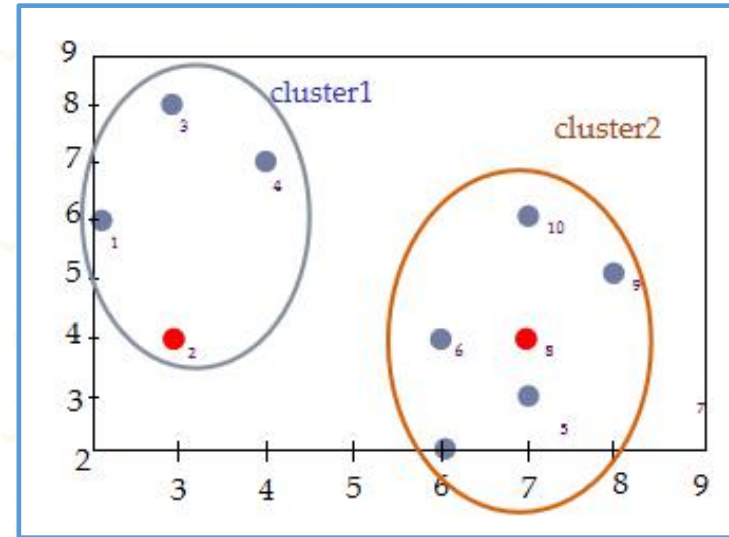




How K-Medoids works?

Data Objects

	A_1	A_2
O_1	2	6
O_2	3	4
O_3	3	8
O_4	4	7
O_5	6	2
O_6	6	4
O_7	7	3
O_8	7	4
O_9	8	5
O_{10}	7	6



Compute the absolute error criterion [for the set of Medoids (O_2, O_8)]

$$E = \sum_{i=1}^k \sum_{p \in C_i} |p - o_i| = (|O_1 - O_2| + |O_3 - O_2| + |O_4 - O_2|) + (|O_5 - O_8| + |O_6 - O_8| + |O_7 - O_8| + |O_9 - O_8| + |O_{10} - O_8|)$$

The absolute error criterion [for the set of Medoids (O_2, O_8)]

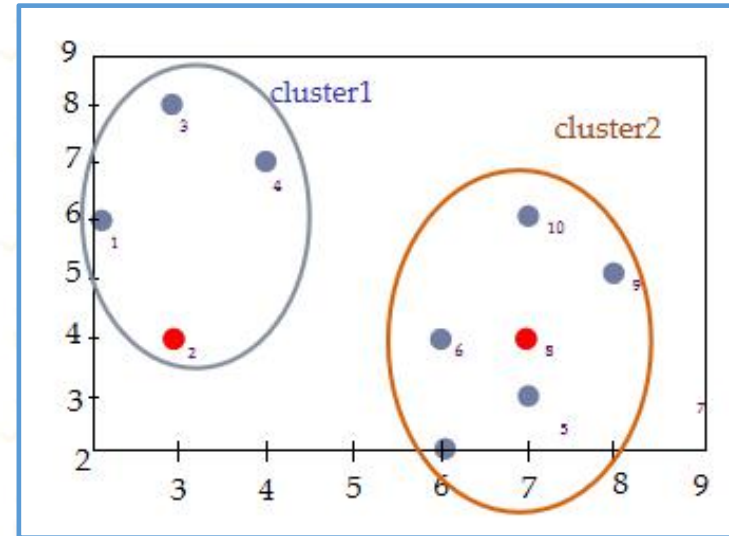
$$E = (3+4+4)+(3+1+1+2+2) = 20$$



How K-Medoids works?

Data Objects

	A ₁	A ₂
O ₁	2	6
O ₂	3	4
O ₃	3	8
O ₄	4	7
O ₅	6	2
O ₆	6	4
O ₇	7	3
O ₈	7	4
O ₉	8	5
O ₁₀	7	6



- Choose a random object O₇
- Swap O₈ and O₇
- Compute the absolute error criterion [for the set of Medoids (O₂, O₇)]

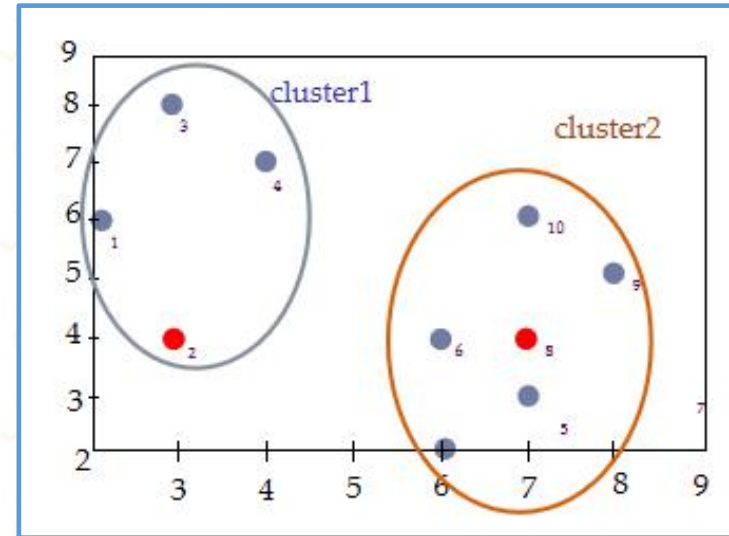
$$E = (3+4+4)+(2+2+1+3+3) = 22$$



How K-Medoids works?

Data Objects

	A_1	A_2
O_1	2	6
O_2	3	4
O_3	3	8
O_4	4	7
O_5	6	2
O_6	6	4
O_7	7	3
O_8	7	4
O_9	8	5
O_{10}	7	6



→ Compute the cost function

Absolute error [O_2, O_7] - Absolute error [for O_2, O_8]

$$S = 22 - 20$$

$S > 0 \Rightarrow$ It is a bad idea to replace O_8 by O_7





Discussion on the K-medoids

Advantages:

- It is simple to understand and easy to implement.
- K-Medoid Algorithm is fast and converges in a fixed number of steps.
- PAM is less sensitive to outliers than other partitioning algorithms.

Disadvantages:

- It may obtain different results for different runs on the same dataset because the first k medoids are chosen randomly.
- PAM algorithm for K-medoid clustering works well for dataset but cannot scale well for large data set due to high computational overhead.





Lets Practice!

Thank
YOU