

Hanna Frances Bobis	hanna.bobis@torontomu.ca	501021980
Ivan Chan	ivan.chan@torontomu.ca	501033549
Alden Shin-Culhane	alden.shinculhane@torontomu.ca	501036054

a. $[W, X, Y \mid Z]$ and $[1, 2, 3, 4, 5 \mid [6, 7, X]]$

Matches if

$W = 1$

$X = 2$

$Y = 3$

$Z = [4, 5 \mid [6, 7, 2]]$

List 1 = $[W, X, Y \mid Z]$

Substitute values:

$\Rightarrow [1, 2, 3 \mid [4, 5 \mid [6, 7, 2]]]$

Rearranging list:

$\Rightarrow [1, 2, 3, 4, 5 \mid [6, 7, 2]]$

$\Rightarrow [1, 2, 3, 4, 5, 6, 7, 2]$

List 2 = $[1, 2, 3, 4, 5 \mid [6, 7, X]]$

Substitute values:

$\Rightarrow [1, 2, 3, 4, 5 \mid [6, 7, 2]]$

Simplify:

$\Rightarrow [1, 2, 3, 4, 5, 6, 7, 2]$

$[1, 2, 3, 4, 5, 6, 7, 2] = [1, 2, 3, 4, 5, 6, 7, 2]$

Therefore List1 = List2 when $W = 1, X = 2, Y = 3, Z = [4, 5 \mid [6, 7, 2]]$

b. $[p \mid [q \mid [r \mid [s \mid [t \mid [V]]]]]]$ and $[X, Y \mid Z]$

Matches if

$X = p$

$Y = q$

$Z = [r, s, t, V]$

$List1 = [p \mid [q \mid [r \mid [s \mid [t \mid [V]]]]]]$

Rearranging list:

$\Rightarrow [p, q, r, s, t, V]$

$List2 = [X, Y \mid Z]$

Substitute values:

$\Rightarrow [p, q \mid [r, s, t, V]]$

Simplify list:

$\Rightarrow [p, q, r, s, t, V]$

$[p, q, r, s, t, V] = [p, q, r, s, t, V]$

Therefore, $List1 = List2$ when $X = p, Y = q, Z = [r, s, t, V]$

c. $[[Z \mid [x, y]], e, f, g]$ and $[[a, [x, y]] \mid V]$

$List1 = [[Z \mid [x, y]], e, f, g]$

Rearranging:

$\Rightarrow [[Z \mid [x, y]] \mid [e, f, g]]$

$\Rightarrow [[Z, x, y] \mid e, f, g]$

$List2 = [[a, [x, y]] \mid V]$

These lists do not match. In list 1, $[Z \mid [x, y]] = [Z, x, y]$ which has 3 elements, whereas in list 2, $[a, [x, y]]$ only has two elements. Also, the values x, y are separate elements in list1, while they are a sub-list $[x, y]$ in list2.

d. $[[a], B, C \mid D]$ and $[[a \mid [B]] \mid [C \mid D]]$

List1 = $[[a], B, C \mid D]$

List2 = $[[a \mid [B]] \mid [C \mid D]]$

Rearranging:

$\Rightarrow [[a, B] \mid [C \mid D]]$

$[a], B \neq [a, B]$ therefore List1 and List2 do not match. In List1, the elements $[a]$, and B are two separate members of the parent list. However in List2, $[a, B]$ are grouped together as a sub-list as one member of the parent list.

e. $[\text{minus} \mid [Y, X \mid [\text{minus}, Y \mid [X]]]]$ and $[X, \text{plus}, \text{minus} \mid [X, Y, \text{minus}]]$

List1 = $[\text{minus} \mid [Y, X \mid [\text{minus}, Y \mid [X]]]]$

Simplifying:

$\Rightarrow [\text{minus} \mid [Y, X \mid [\text{minus}, Y, X]]]$

$\Rightarrow [\text{minus} \mid [Y, X, \text{minus}, Y, X]]$

$\Rightarrow [\text{minus}, Y, X, \text{minus}, Y, X]$

List2 = $[X, \text{plus}, \text{minus} \mid [X, Y, \text{minus}]]$

Simplifying:

$\Rightarrow [X, \text{plus}, \text{minus}, X, Y, \text{minus}]$

Matches if

$X = \text{minus}$

Y = plus

Substituting values in List1:

[minus, plus, minus, minus, plus, minus]

Substituting values in List2:

[minus, plus, minus, minus, plus, minus]

[minus, plus, minus, minus, plus, minus] = [minus, plus, minus, minus, plus, minus]

Therefore, List1 = List2 when X = minus, and Y = plus.

f. [bike | A] and [C | [C | [C | [C | [C]]]]]

List1 = [bike | A]

List2 = [C | [C | [C | [C | [C]]]]]

Simplifying

= [C | [C | [C | [C, C]]]]

= [C | [C | [C, C, C]]]

= [C | [C, C, C, C]]

Matches if

C = bike

A = [bike, bike, bike, bike]

Substituting values in List1:

[bike | [bike, bike, bike, bike]]

Substituting values in List2:

[bike | [bike, bike, bike, bike]]

[bike | [bike, bike, bike, bike]] = [bike | [bike, bike, bike, bike]]

Therefore, List1 = List2 when C = bike and A = [bike, bike, bike, bike]

g. [a, b | [C | [D, E | C]]] and [F | [G, H, [], [[D]]]]

List1 = [a, b | [C | [D, E | C]]]

Simplifying:

⇒ [a, b, | [C, D, E | C]]

⇒ [a, b, C, D, E | C]

List2 = [F | [G, H, [], [[D]]]]

Rearranging:

⇒ [F, G, H, [], [[D]]]

Matches if

F = a

G = b

H = []

C = []

D = []

E = [[]]

Substituting values in List1:

[a, b, [], [], [[]]] | []

Simplifying:

⇒ [a, b, [], [], [[]]]

Substituting values in List2:

[a, b, [], [], [[]]]

`[a, b, [], [], [[]]] = [a, b, [], [], [[]]]`

Therefore `List1 = List2` when `F = a`, `G = b`, `H = []`, `C = []`, `D = []`,
`E = [[]]`.

h. `[Fox, [[in], socks], [on], box, on | [[knox]]]` and `[[The, cat],
[[in], The], Hat | [Comes | Back]]`

`List1 = [Fox, [[in], socks], [on], box, on | [[knox]]]`

Simplifying:

\Rightarrow `[Fox, [[in], socks], [on], box, on, [knox]]`

`List2 = [[The, cat], [[in], The], Hat | [Comes | Back]]`

Simplifying:

\Rightarrow `[[The, cat], [[in], The], Hat, Comes | Back]`

Matches if

`Fox = [socks, cat]`

`The = socks`

`Hat = [on]`

`Comes = box`

`Back = [on, [knox]]`

Substituting values into `List1`:

`[[socks, cat], [[in], socks], [on], box, on, [knox]]`

Substituting values into `List2`:

`[[socks, cat], [[in], socks], [on], box | [on, [knox]]]`

Simplifying:

⇒ [[socks, cat], [[in], socks], [on], box on, [knox]]

[[socks, cat], [[in], socks], [on], box on, [knox]] = [[socks, cat], [[in], socks], [on], box on, [knox]].

Therefore List1 = List2 when Fox = [socks, cat], The = socks, Hat = [on], Comes = box, Back = [on, [knox]].