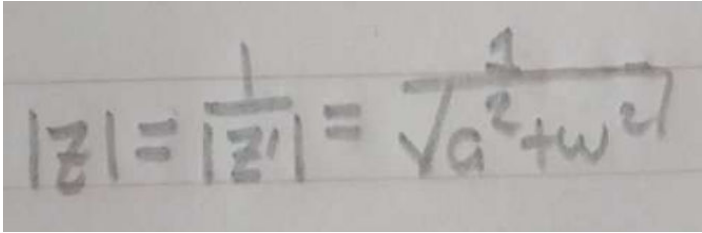
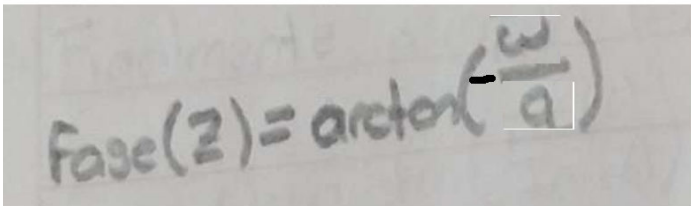


Transformada de fourier

Ploteo del ejercicio a mano

syms omega


$$|Z| = \frac{1}{|Z'|} = \frac{1}{\sqrt{a^2 + \omega^2}}$$


$$\text{Phase}(Z) = \arctan\left(-\frac{\omega}{a}\right)$$

Propiedad de Adrian

```
a=2;  
x_mag=1/(a^2+omega^2)
```

x_mag =

$$\frac{1}{\omega^2 + 4}$$

```
x_ph=atan(-omega/a)
```

x_ph =

$$-\arctan\left(\frac{\omega}{2}\right)$$

```
figure  
yyaxis left  
fplot(x_mag)  
ylabel(" |X(\omega)| ")  
yyaxis right  
fplot(x_ph)  
ylabel("\angle X(\omega) ")
```

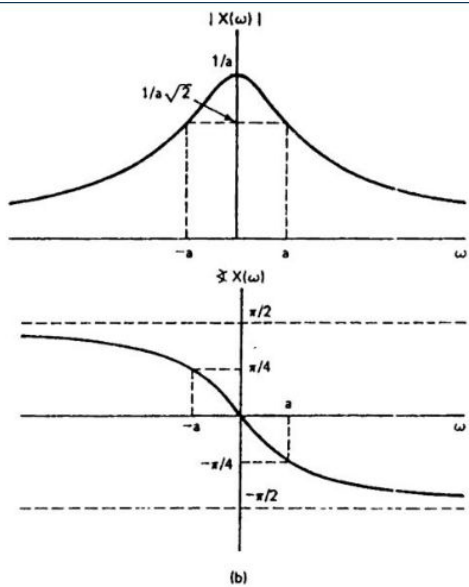
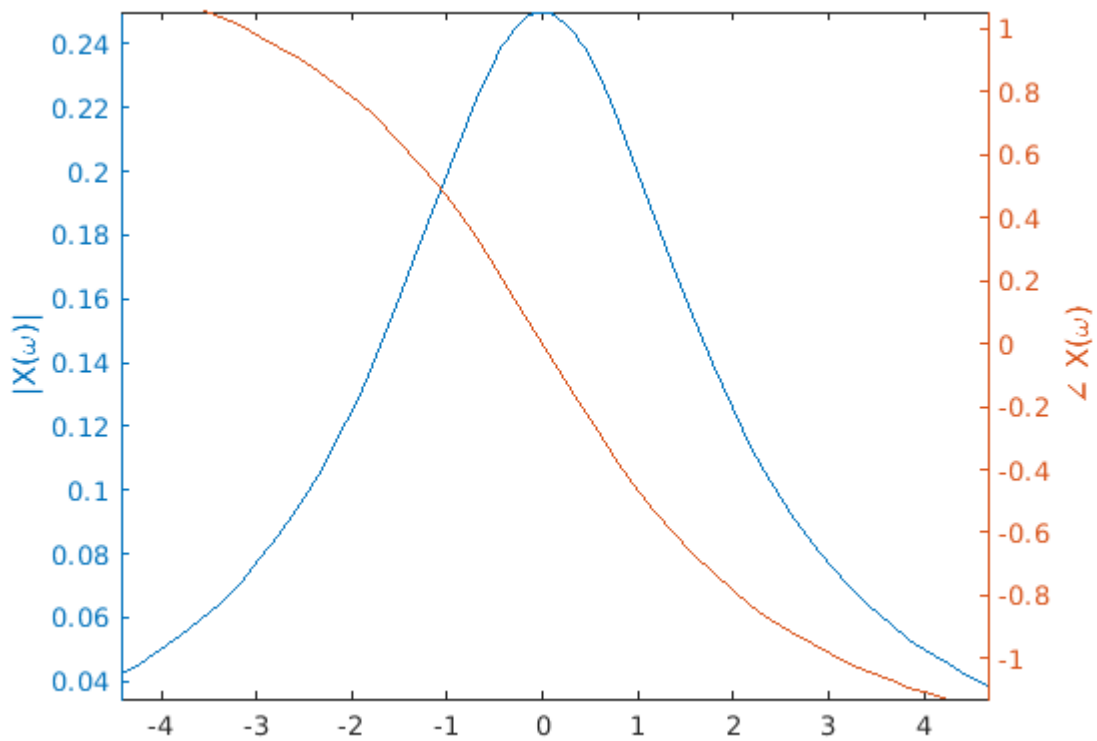
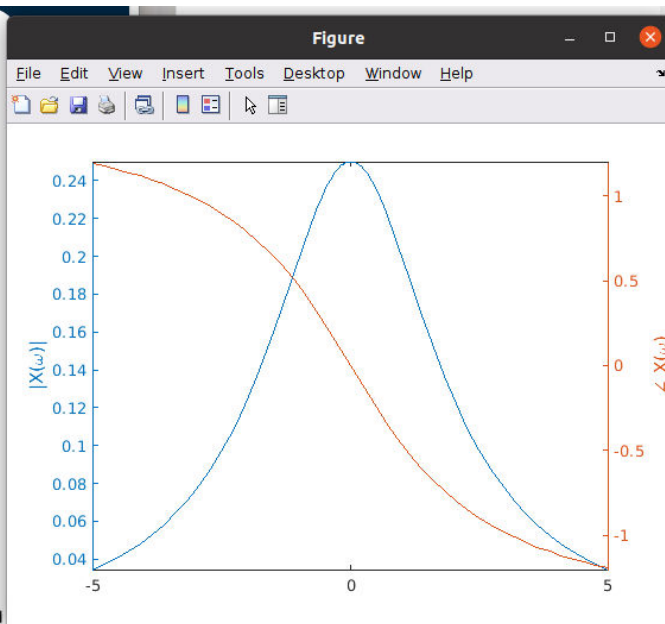


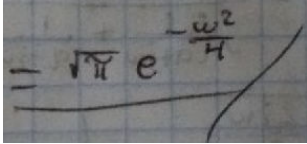
Figure 4.14 Fourier transform of the signal $x(t) = e^{-at}u(t)$, $a > 0$, considered



Segundo ejercicio

$$x(t) = e^{-t^2}.$$

$X(\omega)$



Propiedad de Erik

- Plotear
- Usar la función fourier y comparar resultados

```
syms t omega
x=exp(-t^2)
```

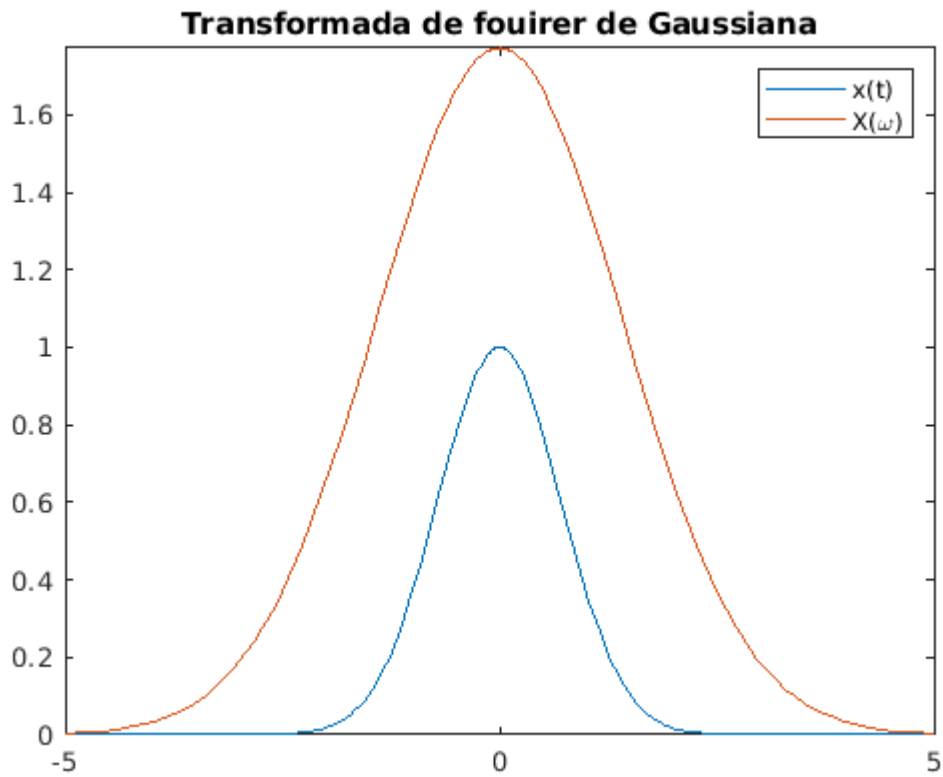
$$x = e^{-t^2}$$

```
X=sqrt(pi)*exp(-omega^2/4)
```

$x =$

$$\frac{3991211251234741 e^{-\frac{\omega^2}{4}}}{2251799813685248}$$

```
figure
fplot(x)
hold on
fplot(X)
hold off
legend("x(t)", "X(\omega)")
title("Transformada de Fourier de Gaussiana")
```



```
% Usando la función fourier
X_sym=fourier(x)
```

X_sym =

$$\sqrt{\pi} e^{-\frac{\omega^2}{4}}$$

Inversa

$$x(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} X(\omega) e^{j\omega t} d\omega, \quad X(\omega) = \frac{1}{(1+j\omega)^2}$$

$$\Rightarrow x(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} \frac{e^{j\omega t}}{(1+j\omega)^2} d\omega = t e^{-t} u(t)$$

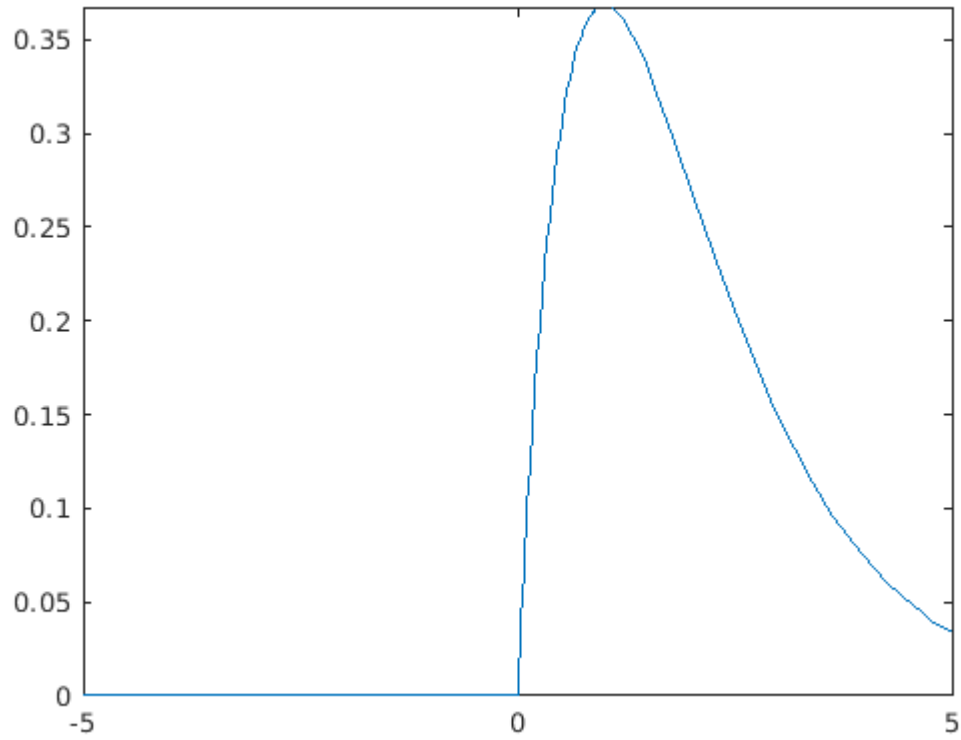
Propiedad de Erik

```
%Plotear resultado
x=t*exp(-t)*heaviside(t)
```

$$x = t e^{-t} \text{heaviside}(t)$$

```
figure
```

```
fplot(x)
```



```
%Usar función ifourier  
x_sym=ifourier(1/(1+1j*omega)^2,omega)
```

```
x_sym =
```

$$\frac{\pi \omega e^{-\omega} + \pi \omega e^{-\omega} \text{sign}(\omega)}{2 \pi}$$

```
figure  
fplot(x_sym)
```

