





观数以形

艾新波 / 2018·北京



课程体系









第3章 格言联璧话学习

🗐 第4章 源于数学、归于工程

中部: 执具

第5章 工欲善其事必先利其器

第6章 基础编程

第7章 数据对象









- 🗐 第11章 相随相伴、谓之关联

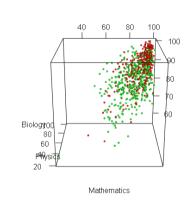
第12章 既是世间法、自当有分别

■ 第13章 方以类聚、物以群分

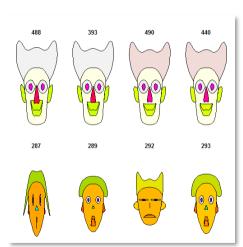
9 第14章 庐山烟雨浙江潮

高维数据空间形态

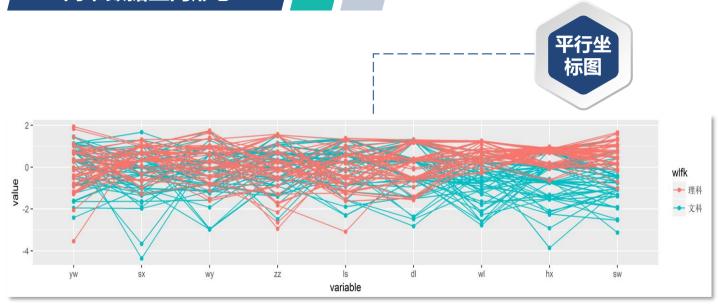








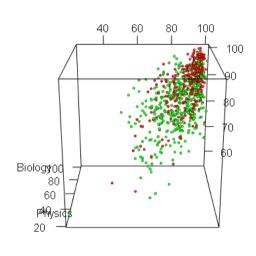
高维数据空间形态



三维散点图

```
#绘制三维散点图
library(rgl)
plot3d(
  x = cjb$sx,
  y = cjb$wl,
  z = cjb$sw,
  xlab = "Mathematics",
  ylab = "Physics",
  zlab = "Biology",
  type = "s",
  size = 0.6,
```

col = c("red", "green")[cjb\$wlfk])



Mathematics

脸谱图

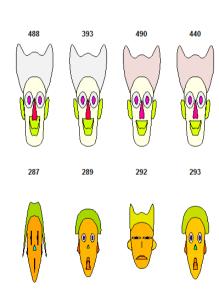
#绘制脸谱图

```
library(aplpack)
selected cols <- c("wl", "hx", "sw")</pre>
selected rows <-
  c(488, 393, 490, 440,
    287, 289, 292, 293)
faces(cjb[selected rows,
          selected cols],
      ncol.plot = 4,
      nrow.plot = 2,
      face.type = 1)
```



脸谱图

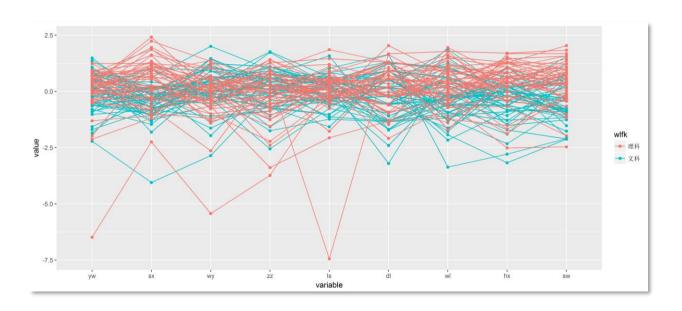
```
#> effect of variables:
#>
    modified item
                       Var
#> "height of face
                     " "w1"
#> "width of face
                     " "hx"
#> "structure of face" "sw"
                     " "w1"
#> "height of mouth
#> "width of mouth
                     " "hx"
#> "smiling
                     " "sw"
                     " "w1"
#> "height of eyes
                     " "hx"
#> "width of eyes
#> "height of hair
                   " "SW"
#> "width of hair
                    " "w1"
#> "style of hair
                    " "hx"
#> "height of nose
                      "sw"
#> "width of nose
                      "w1"
#> "width of ear
                      "hx"
#> "height of ear
                      "SW"
```



平行坐标图

```
cjb top w <- cjb %>%
  filter(wlfk == "文科") %>%
  arrange(zcj) %>%
  select(4:13) %>%
  mutate at(vars(yw:sw), jitter) %>%
  head(n = 50)
# (采用同样的方法得到理科cjb top 1, 此处略)
cjb top <- rbind(cjb top w, cjb top 1)</pre>
Ggally::ggparcoord(cjb top,
           columns = 1:9,
           groupColumn = 10) +
  geom point()
```

平行坐标图

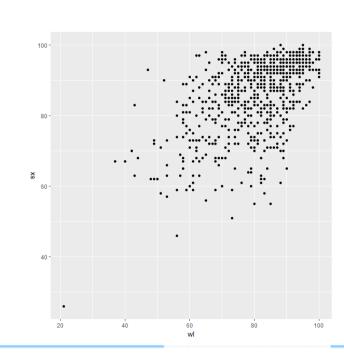


数据空间的其它形态: 密度

- □ 密度是数据空间的形态之一
- □ 物理上的密度是指物质每单位体积内的

质量:
$$\rho = \frac{m}{V}$$

- 数据空间当然没有质量,密度只能是指密集程度而已
- 一个简单的计算方法是:单位面积/体积内数据点的个数
- 换言之,这里的密度,指的是单位体积 内的数量,而非质量



数据空间的其它形态: 密度

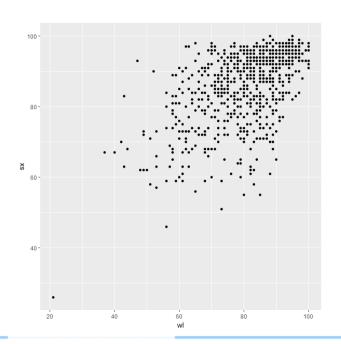
```
#汇总统计
                                              # A tibble: 1,331 x 3
breaks <-c(0, seq(50, 100, len=11))
                                              # Groups: wl [11]
wl sx freq <- cjb %>%
                                                wl sx frea
                                                <fct> <fct> <dbl>
  select(wl, sx) %>%
                                              1 (0,50] (0,50]
  mutate at (
                                              2 (0,50] (50,55]
                                              3 (0,50] (55,60]
    vars(wl, sx),
                                              4 (0,50] (60,65]
    function(x) {
                                              5 (0,501 (65,701
                                              6 (0,50] (70,75]
      cut(x, breaks = breaks)
                                              7 (0,50] (75,80]
    }) %>%
                                               8 (0,50] (80,85]
                                               9 (0,50] (85,90]
  group by (wl, sx) %>%
                                              10 (0,50] (90,95]
  summarise(freq = n()) %>%
                                              # ... with 1,321 more rows
```

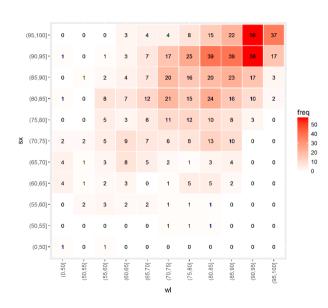
complete(wl, sx, fill = list(freq = 0))

数据空间的其它形态: 密度

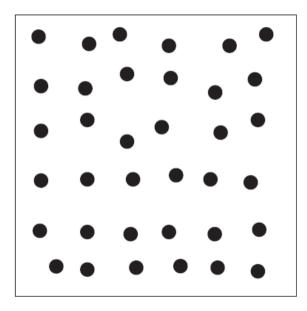
```
qqplot(wl sx freq, aes(x = wl, y = sx, fill = freq)) +
  geom tile(colour="white", size = 0.5) +
  geom text(aes(label = freq), size = 3) +
  scale fill gradient(
    low = "white",
    high = "red") +
  theme (axis.text.x =
          element text(
            angle = 90,
            hiust = 1,
            viust = (0.5) +
  coord fixed()
```

数据空间的其它形态:密度





数据空间的其它形态: 均匀程度



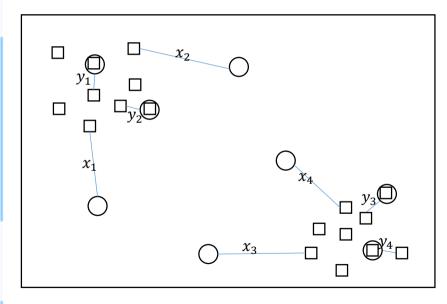
A data set that is uniformly distributed in the data space

数据空间的其它形态:均匀程度

Hopkins统计量告诉我们所拿到的数据多大程度上接近于均匀散布的形态对于给定数据集 D:

- (1) 均匀地从D的空间中抽取 n 个点 $p_1, p_2, ..., p_{n_i}$ 对于每个点 p_i 令 x_i 为 p_i 与它在D 中的最近邻的距离: $x_i = \min_{v \in D} \{dist(p_i, v)\}$
- (2) 从D中抽取 n 个点 $q_1, q_2, ..., q_n$,对于每个点 q_i ,令 y_i 为 q_i 与它在D-{ q_i }中最近 邻之间的距离: $y_i = \min_{v \in D \{a_i\}} \{dist(q_i, v)\}$
- (3) 计算霍普金斯统计量: $H = \frac{\sum_{i=1}^{n} y_i}{\sum_{i=1}^{n} x_i + \sum_{i=1}^{n} y_i}$

数据空间的其它形态:均匀程度



霍普金斯统计量:

$$H = \frac{\sum_{i=1}^{n} y_i}{\sum_{i=1}^{n} x_i + \sum_{i=1}^{n} y_i}$$

若D分布均匀,则H接近于0.5 若D是高度倾斜的,则H接近于0

一般而言,n ≪ |D|

推荐的做法:

$$n=0.05 \times |D|$$
或是 $n=0.1 \times |D|$

数据空间的其它形态: 均匀程度

```
library(clustertend)
set.seed(2012)
scores <- cjb %>%
  select(yw:sw)
n \leftarrow floor(nrow(cjb) * 0.05)
hopkins stat <- unlist(replicate(100, hopkins(scores, n)))
mean (hopkins stat)
#> [1] 0.1577968
```

内容小结

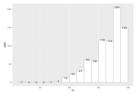


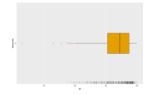
+ 利用少量数字来描述图形

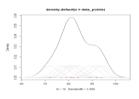
内容小结

The decimal point is at the

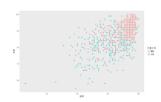
- 89 | 0 90 | 0 91 | 00 92 | 0000 93 | 0000 94 | 00 95 | 000000
- 96 | 000000 97 | 000000000
- 97 | 000000000 98 | 000
- 99 | 0

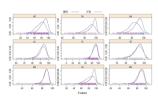


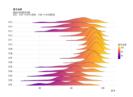


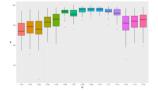


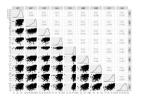


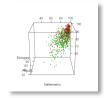












通过几何图形 来展示数据

内容小结

- 1. 集中的趋势:均值、中位数、众数、.....
- 2. 分散的程度: 标准差、方差、极差、.....
- 3. 峰度、偏度
- 4. 均匀程度
- 5. 密度
- 6. 相关系数

来描述图形

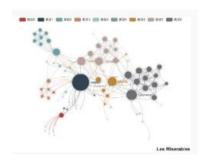
利用少量数字

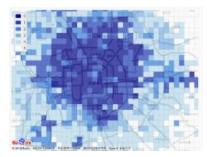
7.

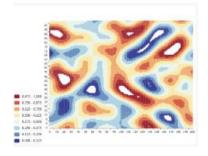
更多内容......

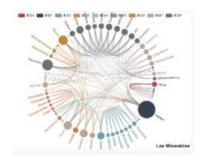












謝謝聆听 Thank you

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课程 网址: https://github.com/byaxb/RDataAnalytics



