

$$= \pi/2 + 2/2$$

$$= \pi/2 + 1$$

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Therefore, the value of the definite integral of  $(1 + \sin(2x))$  with respect to  $x$  from 0 to  $\pi/2$  is  $\pi/2 + 1$ .

### **B. Solve the differential equation**

$$(2x - y + 1)dx + (2y - x - 1)dy = 0$$

To solve the given differential equation:  $(2x - y + 1)dx + (2y - x - 1)dy = 0$ , we can follow these steps:

If we calculate the partial derivatives of  $(2x - y + 1)$  with respect to  $x$  and  $(2y - x - 1)$  with respect to  $y$ :

$$\partial(2x - y + 1)/\partial x = 2$$

$$\partial(2y - x - 1)/\partial y = 2$$

Since these partial derivatives are not equal, the equation is not exact.

To make the equation exact, we need an integrating factor. We can calculate it using the formula:

$$\text{Integrating factor (IF)} = e^{\int P(x)dx + \int Q(y)dy}$$

Where  $P(x)$  and  $Q(y)$  are the coefficients of  $dx$  and  $dy$ , respectively. In this case,  $P(x) = 2x - y + 1$  and  $Q(y) = 2y - x - 1$ .

$$\int P(x)dx = \int (2x - y + 1)dx = x^2 - xy + x + C_1(y)$$

$$\int Q(y)dy = \int (2y - x - 1)dy = y^2 - xy - y + C_2(x)$$

Here,  $C_1(y)$  and  $C_2(x)$  represent constants of integration that depend on  $y$  and  $x$ , respectively.