

Therefore, the number of people who speak only English and not Hindi is 25, and the total number of people who speak English is 50.

2. **Simplify  $z = \frac{(\cos \theta + i \sin \theta)^5}{(\cos \theta - i \sin \theta)^4}$  into  $x + iy$  form and find its modulus and the amplitude.**

Rewriting the denominator using the conjugate property:

$$(\cos \theta - i \sin \theta) = (\cos \theta + i \sin \theta)^*$$

Using the De Moivre's theorem, we can simplify the numerator and denominator:

$$(\cos \theta + i \sin \theta)^5 = \cos(5\theta) + i \sin(5\theta)$$

Now using the formula,

$$(\cos \theta + i \sin \theta)^* = \cos(-\theta) + i \sin(-\theta) = \cos \theta - i \sin \theta$$

Substituting these simplified expressions back into the original equation:

$$z = (\cos(5\theta) + i \sin(5\theta)) / (\cos \theta - i \sin \theta)$$

Rationalising the denominator we get,

$$z = [(\cos(5\theta) + i \sin(5\theta)) * (\cos \theta + i \sin \theta)] / [(\cos \theta - i \sin \theta) * (\cos \theta + i \sin \theta)]$$

Expanding the numerator and denominator:

$$z = [\cos(5\theta)\cos\theta + i \sin(5\theta)\cos\theta + i \cos(5\theta)\sin\theta - \sin(5\theta)\sin\theta] / [\cos^2(\theta) + \sin^2(\theta)]$$

Simplifying:

$$z = [(\cos(5\theta)\cos\theta - \sin(5\theta)\sin\theta) + i (\sin(5\theta)\cos\theta + \cos(5\theta)\sin\theta)] / 1$$

Using the trigonometric identities:

$$z = [\cos(6\theta) + i \sin(6\theta)] / 1$$

Therefore, z simplifies to:

$$z = \cos(6\theta) + i \sin(6\theta)$$