



# AES\_Project\_2021\_2022

Politecnico di Milano

Automation and Control Engineering

## Group's Members:

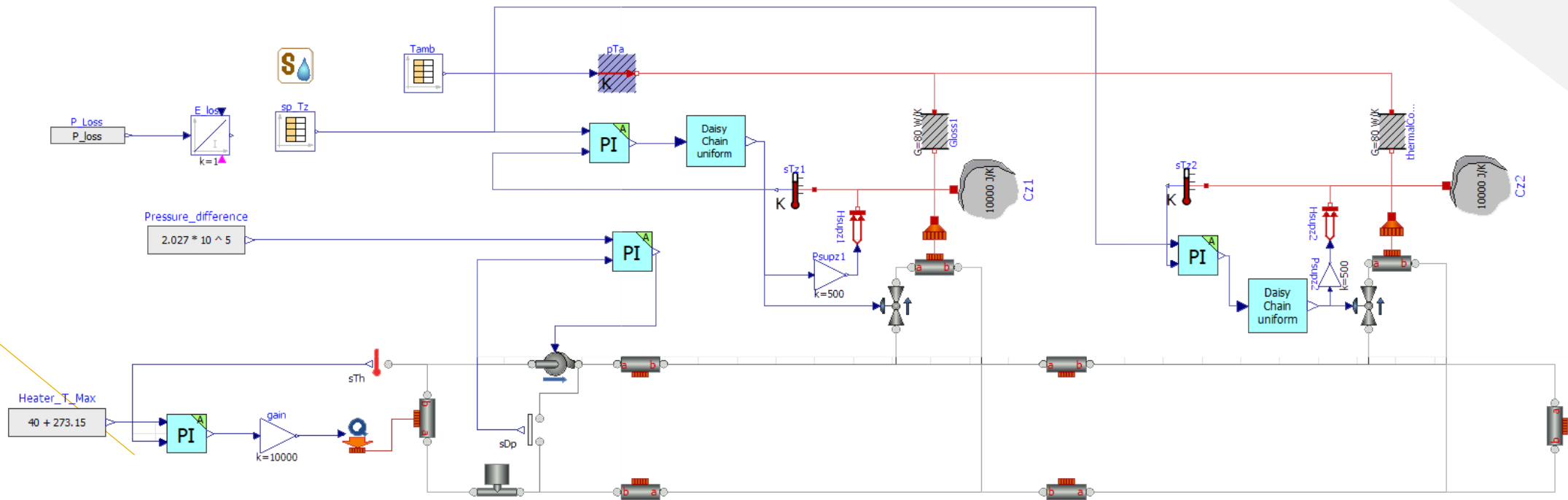
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Riva Alessandro

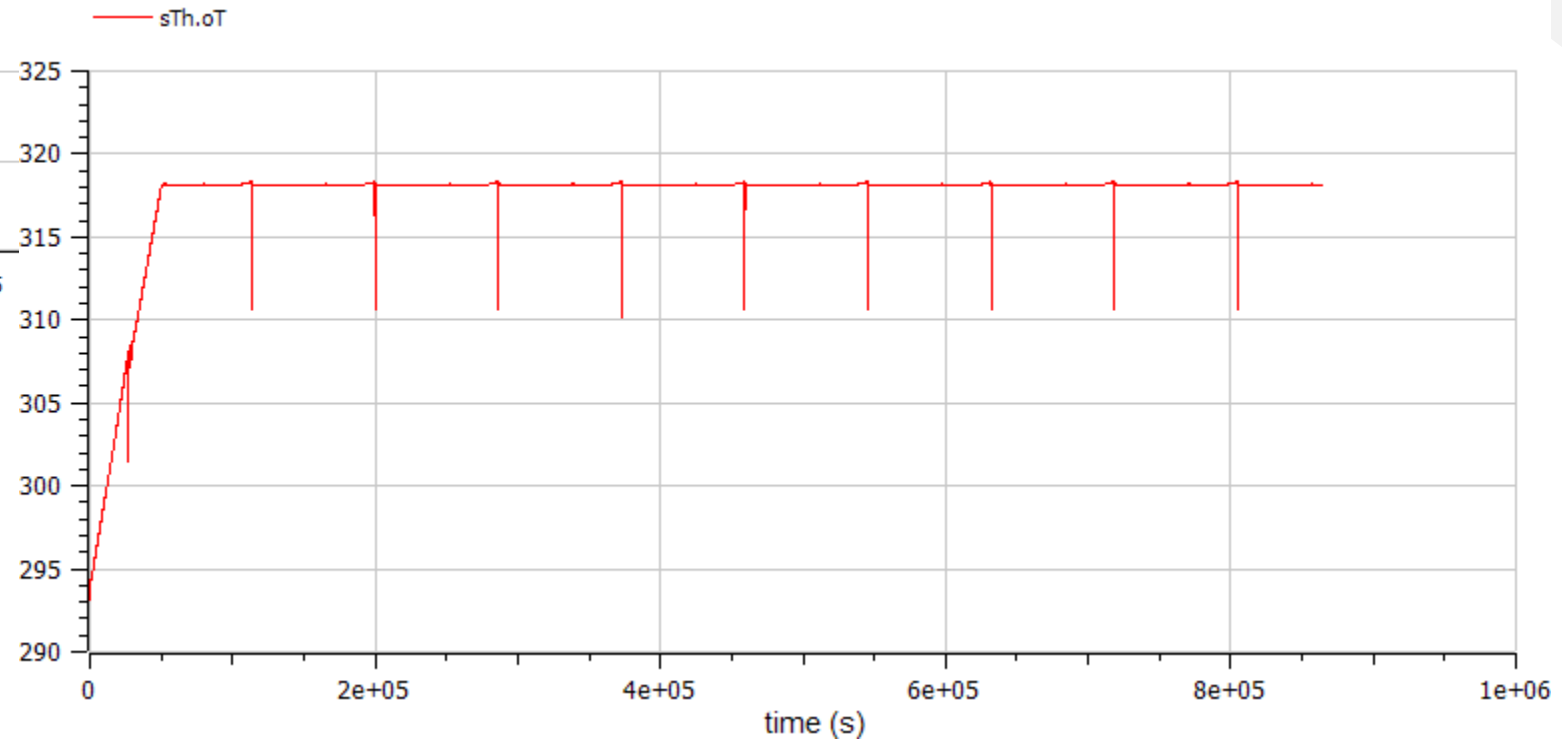
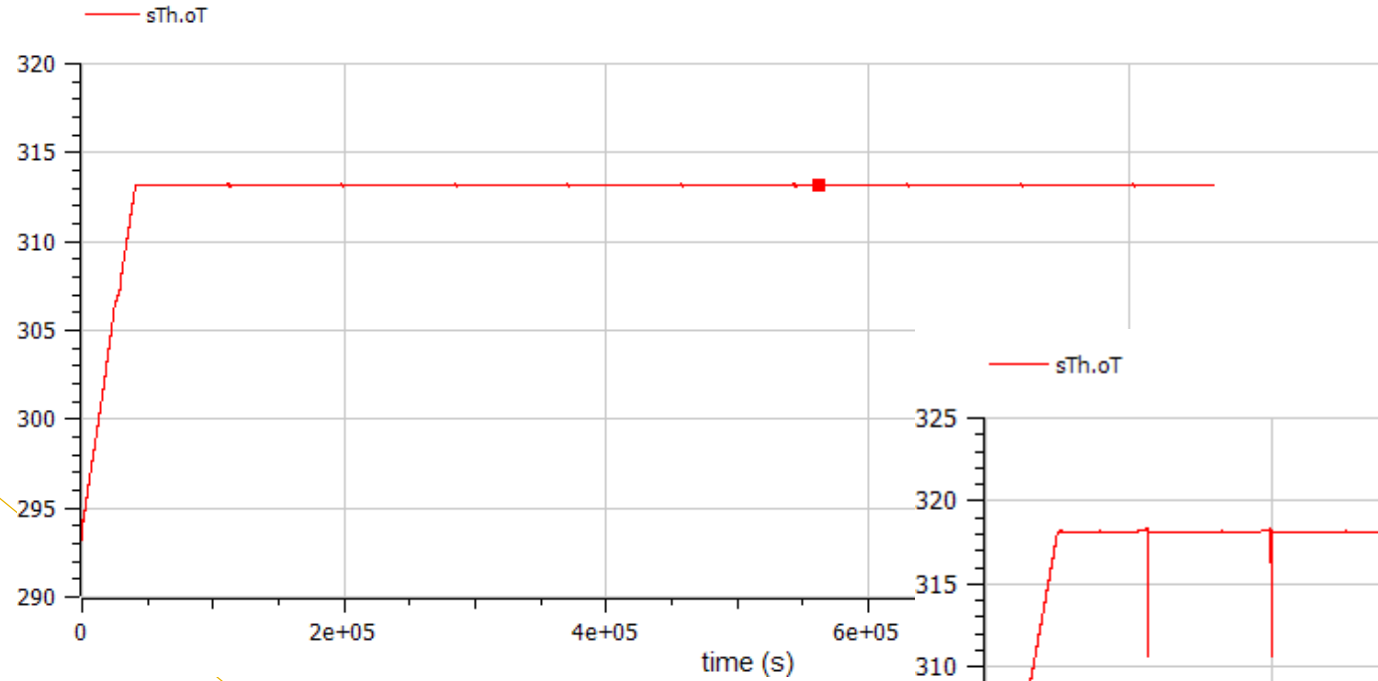
# Controlled system



# Heater model and tracking

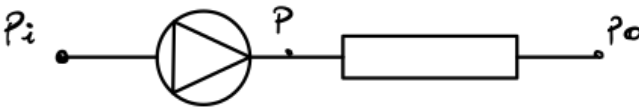
- Energy balance  $c\rho V\dot{T}_h = K_h u + wc(T_c - T_h) \rightarrow T_h(s) = \frac{K_h/cw}{1+s\frac{\rho V}{w}} \cdot u + \frac{T_c}{1+s\frac{\rho V}{w}}$
- V: total volume of water in the network,  $w_n = 0.5 \frac{kg}{s}$  nominal flow rate
- Select experimentally a  $wc \rightarrow wc = 0,008 \text{ rad/s}$  (good tradeoff)
- $Ti = 4,7517 \cdot 10^3$
- $K = 8,287$

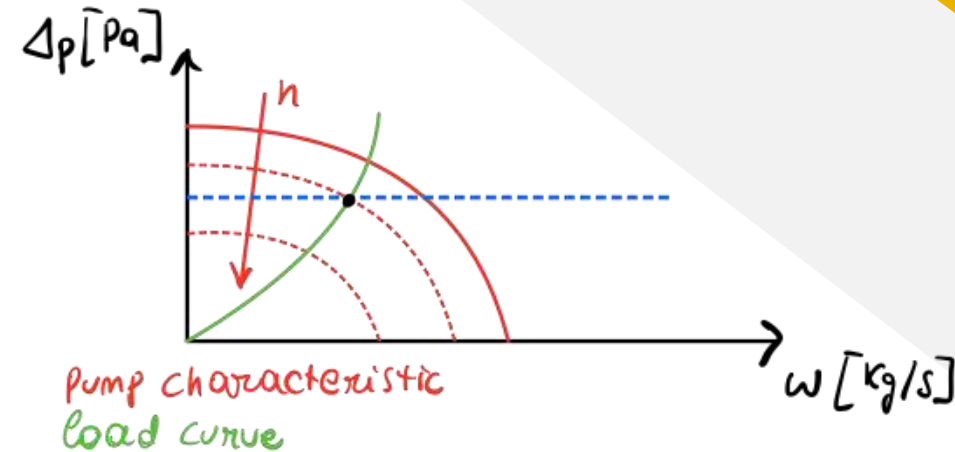
# Heater Temperature



# Pump model

- Pump:  $\Delta p = H_0(n) - H_1(n)w^2 \rightarrow \Delta p = 6 \cdot 10^3 n - 666,7nw^2$
- Pipe Network :  $\Delta p = K_L \rho w^2 \rightarrow \Delta p = 4 \cdot 10^7 w^2$
- Flow rate assumed equal in the whole network  $\rightarrow$  **Assumption**

$$\begin{cases} p - p_i = 6 \cdot 10^5 n - 666,7 \cdot n w^2 \\ p - p_o = 4 \cdot 10^7 w^2 \end{cases}$$




- **EQUILIBRIUM**
  - Compute the equilibrium point for  $n$ , by imposing  $\Delta p = 2,027 \cdot 10^5 \text{ Pa} \rightarrow \bar{n} = 0.338$

# Pump Model

- Linearization

$$\Delta p = \frac{6 \cdot 10^5 n}{1 + \frac{666,7 n}{4 \cdot 10^7}} = \frac{24 \cdot 10^{12} n}{4 \cdot 10^7 + 666,7 n} = \frac{a n}{b + c n} \quad \begin{array}{l} a = 24 \cdot 10^{12} \\ b = 4 \cdot 10^7 \\ c = 666,7 \end{array}$$

$$\delta p = \left. \frac{a(b + cn) - a n c}{(b + cn)^2} \right|_{\bar{n}} \delta n = \frac{a(b + c\bar{n}) - a\bar{n}c}{(b + c\bar{n})^2} \delta n \Rightarrow \delta p \approx 6e5 \delta n$$

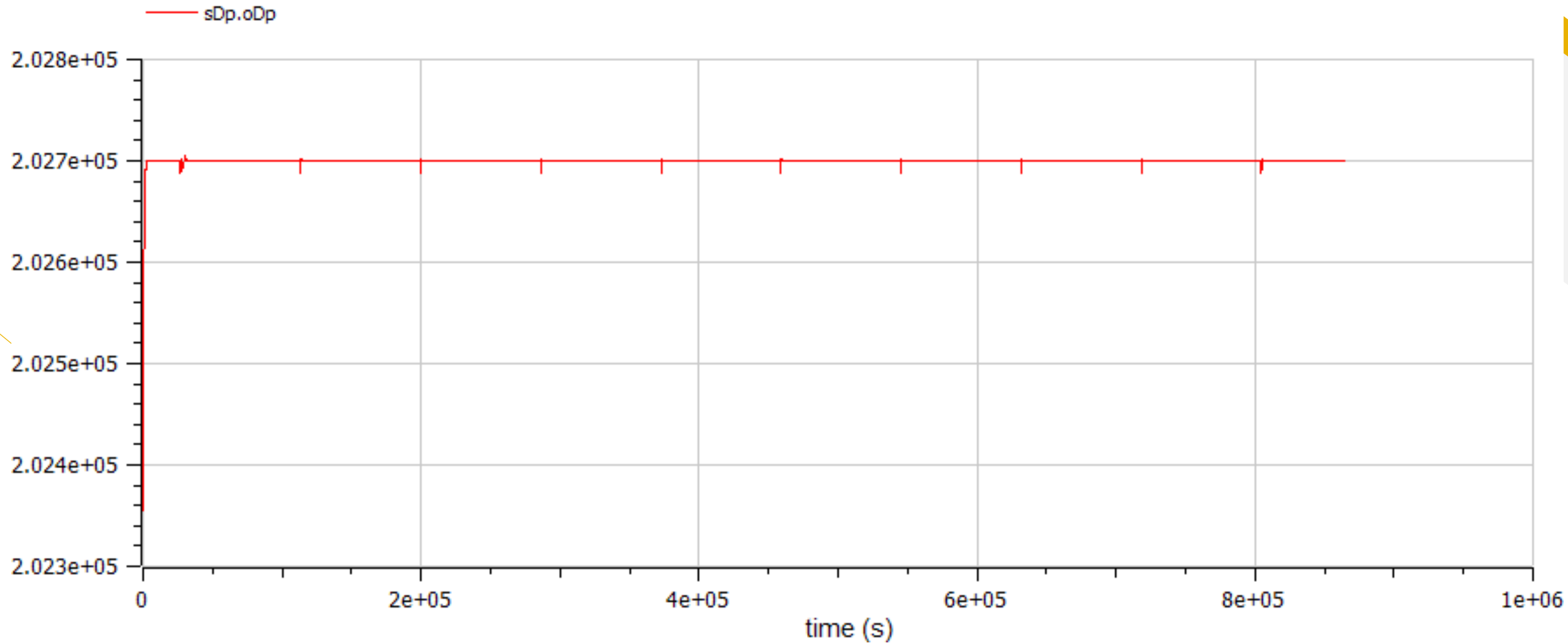
«Algebraic model» → Hydraulics dynamics much faster than temperature, can be neglected  
(in reality:  $G(s) = \frac{\mu}{1+s\tau}$  with  $\tau$  very small)

Use a PI =  $\frac{K(1+sTi)}{sTi}$  →  $L(s) = \frac{k_L*(1+sTi)}{s(1+s\tau)}$  → dominant closed loop pole at  $1/Ti$

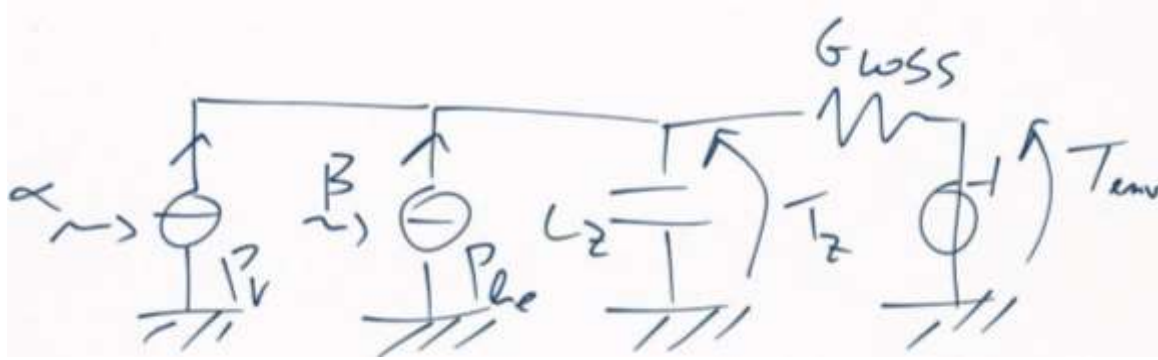
Design choices:  $Ta = 2500s$  →  $Ti = 500s$  (system settles quickly)

$K = 0,001$  (to reduce oscillations)

# Pump Control



# Zones model



$$\begin{cases} \alpha \in [0, 1] \\ \beta \in [0, 1] \end{cases}$$

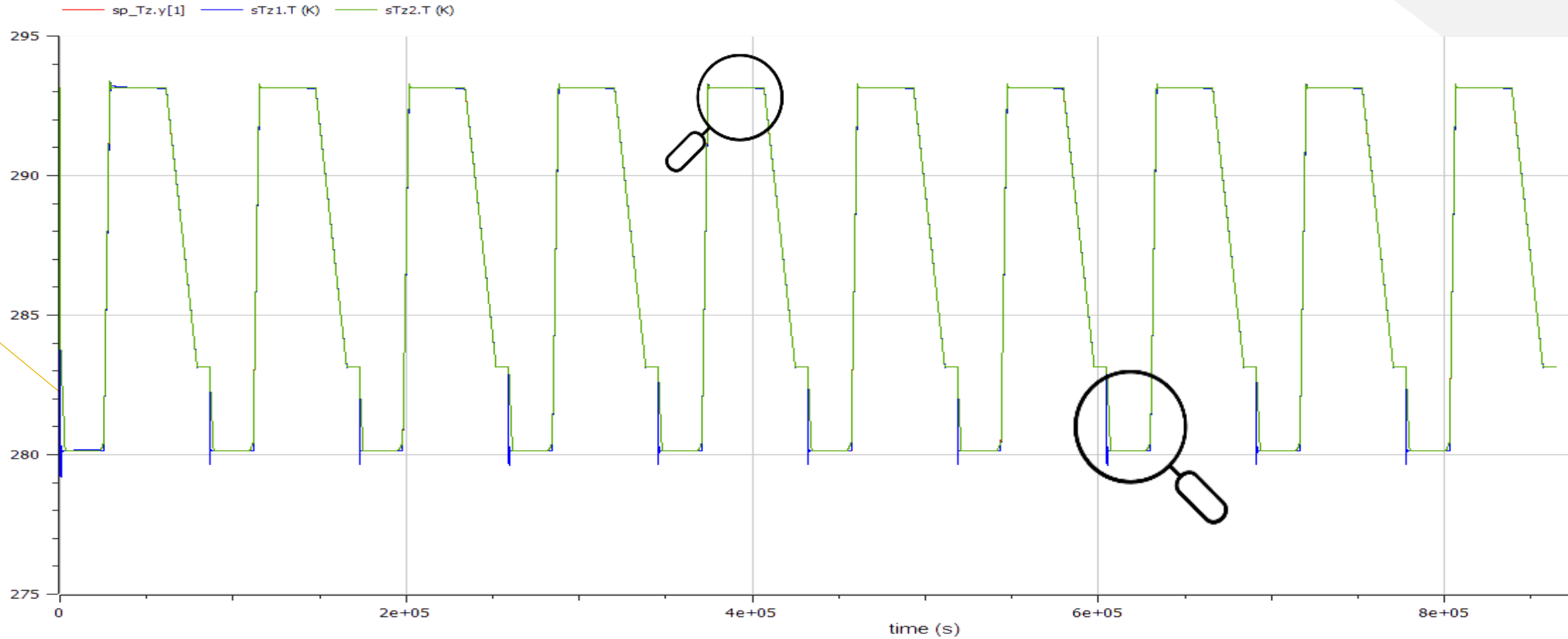
$$c_z \dot{T}_z = \beta K_{he} + \alpha G (T_{Grid} - T_z) - G_{Loss} (T_z - T_{env})$$

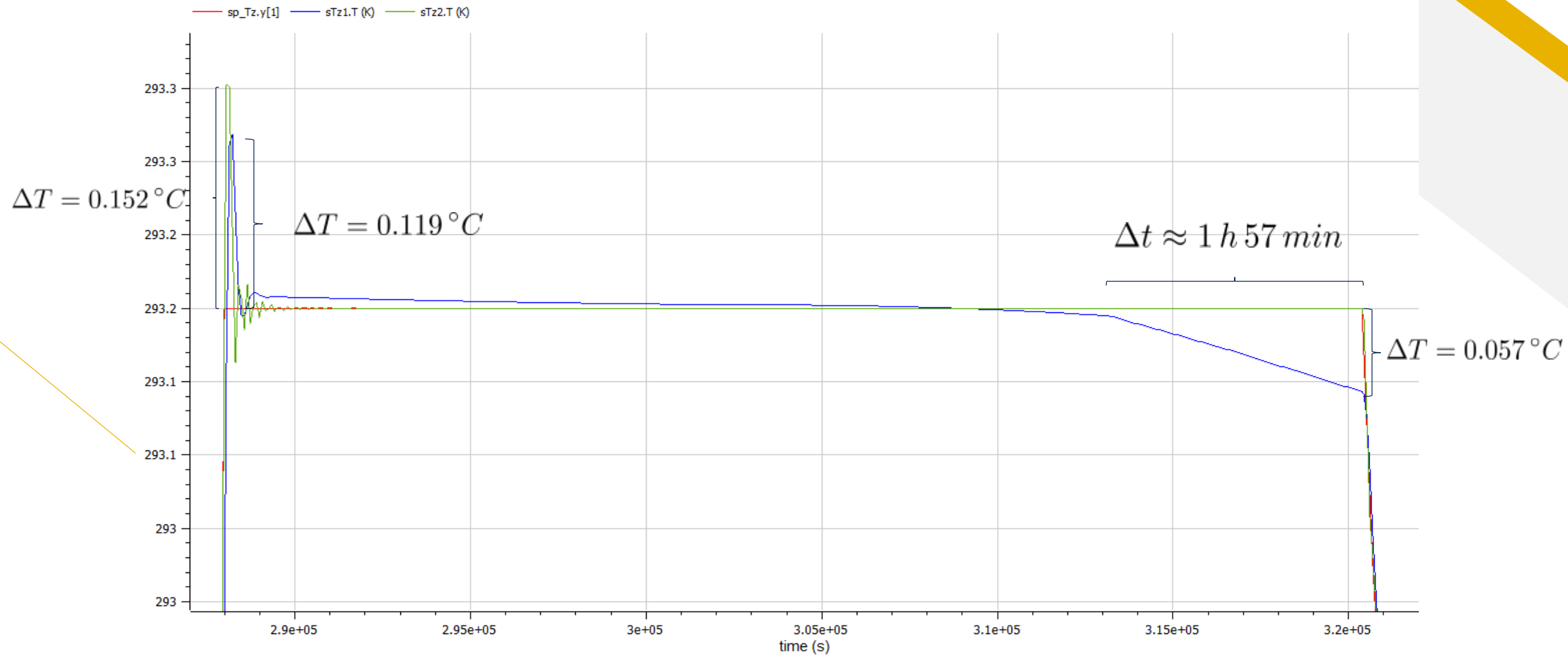
$$\begin{cases} \bar{\alpha} = 0.5 \\ \bar{\beta} = 0 \\ \bar{T}_z = \frac{\bar{\beta} K_{he} + \bar{\alpha} G T_{Grid} + G_{Loss} T_{env}}{\bar{\alpha} G + G_{loss}} \end{cases}$$

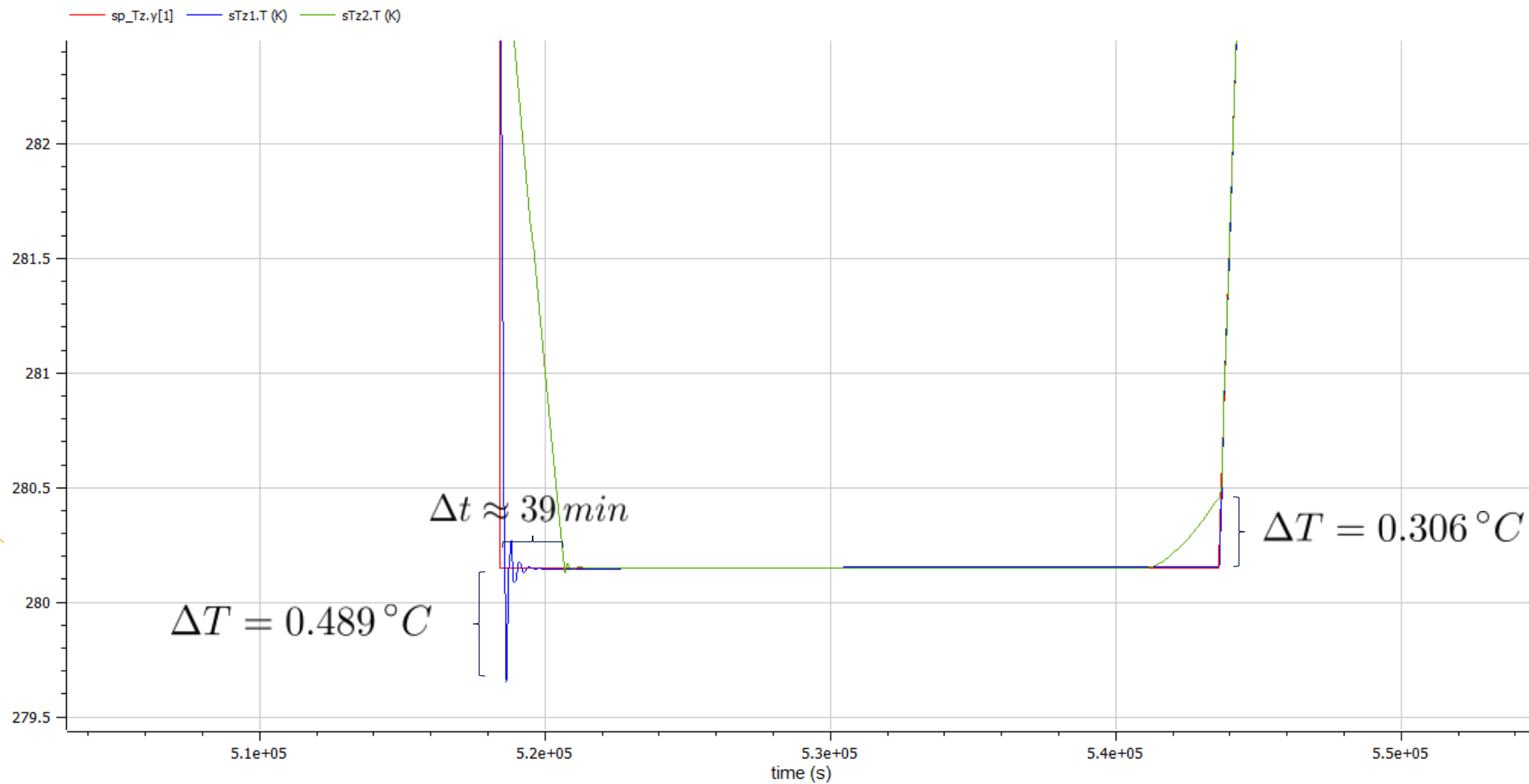
$$\delta \bar{T}_z = \left[ -\frac{\bar{\alpha} G}{c_z} - \frac{G_{Loss}}{c_z} \right] \delta T_s + \left[ \frac{G}{c_z} (T_{Grid} - \bar{T}_z) \frac{K_{he}}{c_z} \right] \begin{bmatrix} \delta \alpha \\ \delta \beta \end{bmatrix}$$



# Zones set point tracking

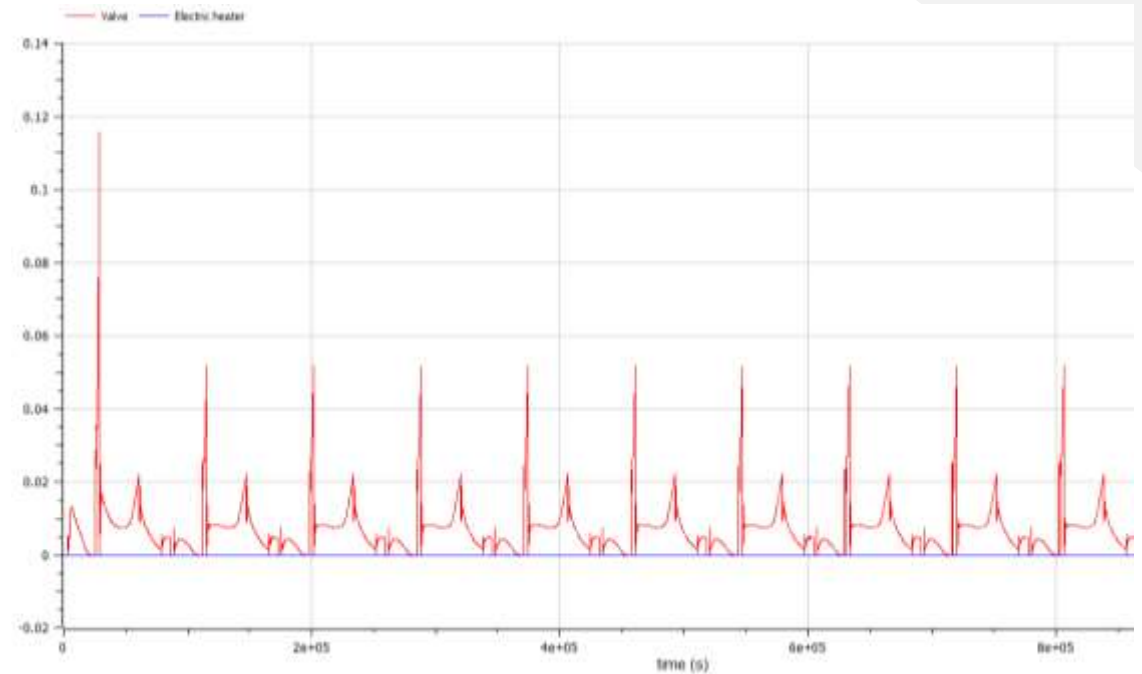
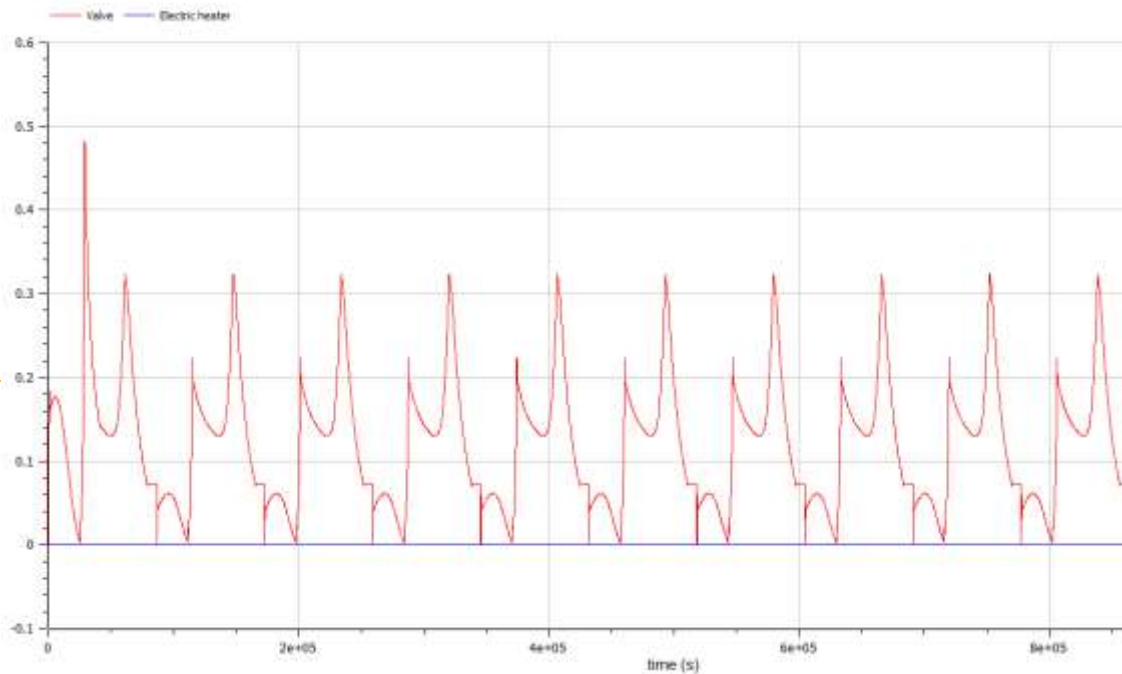




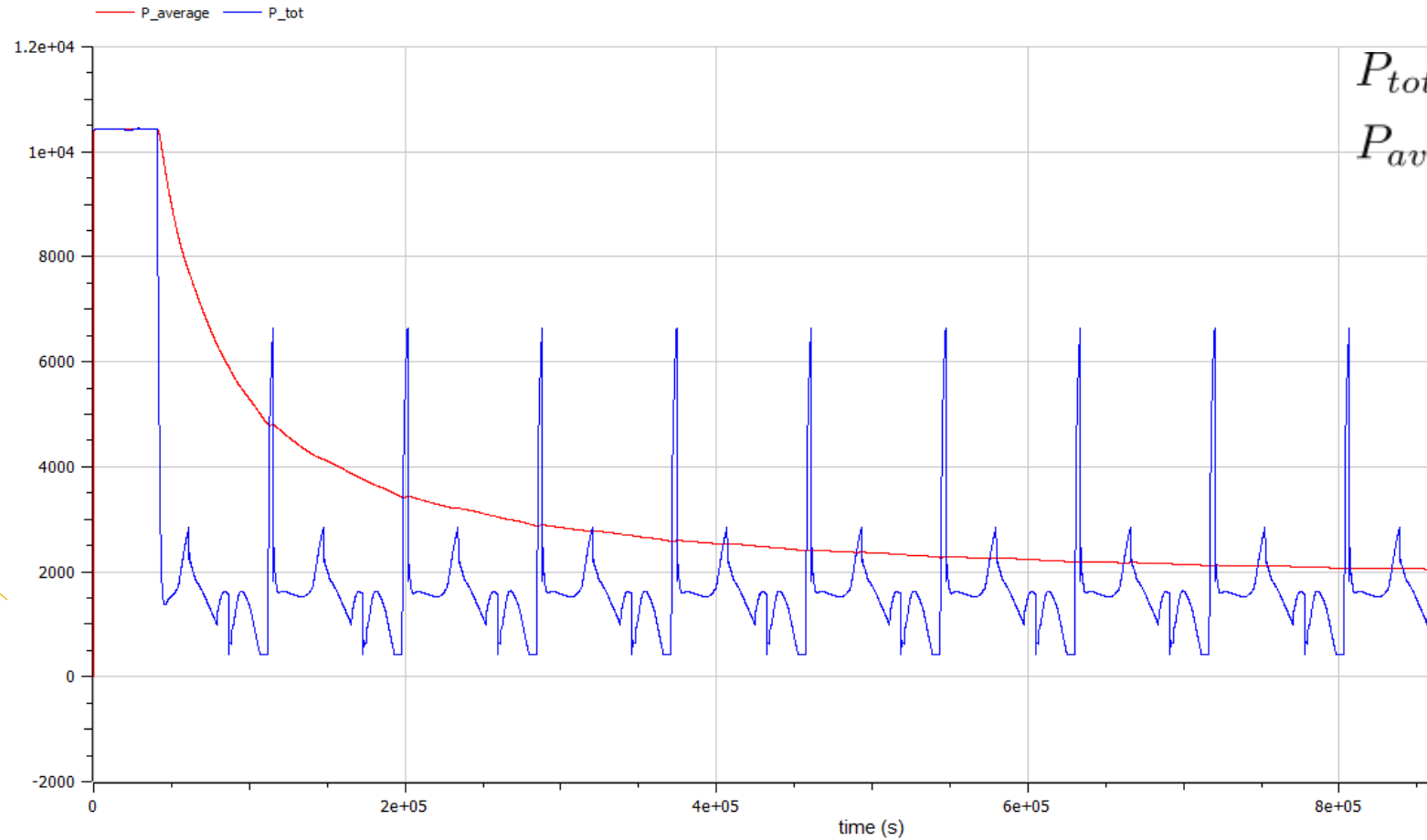


# Control signals of each actuator

$$\begin{cases} \alpha \in [0, 1] \\ \beta \in [0, 1] \end{cases}$$

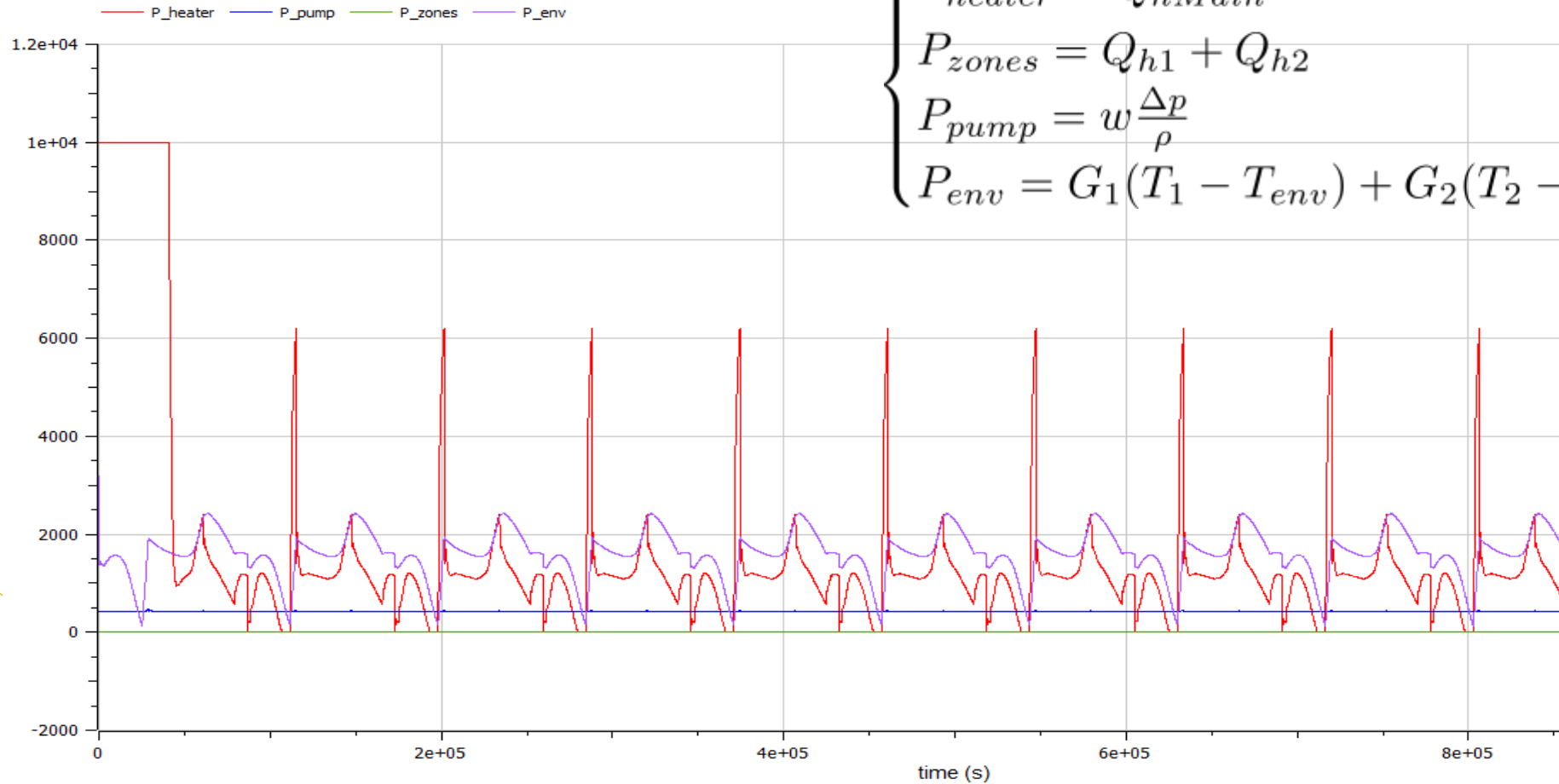


# Power consumption



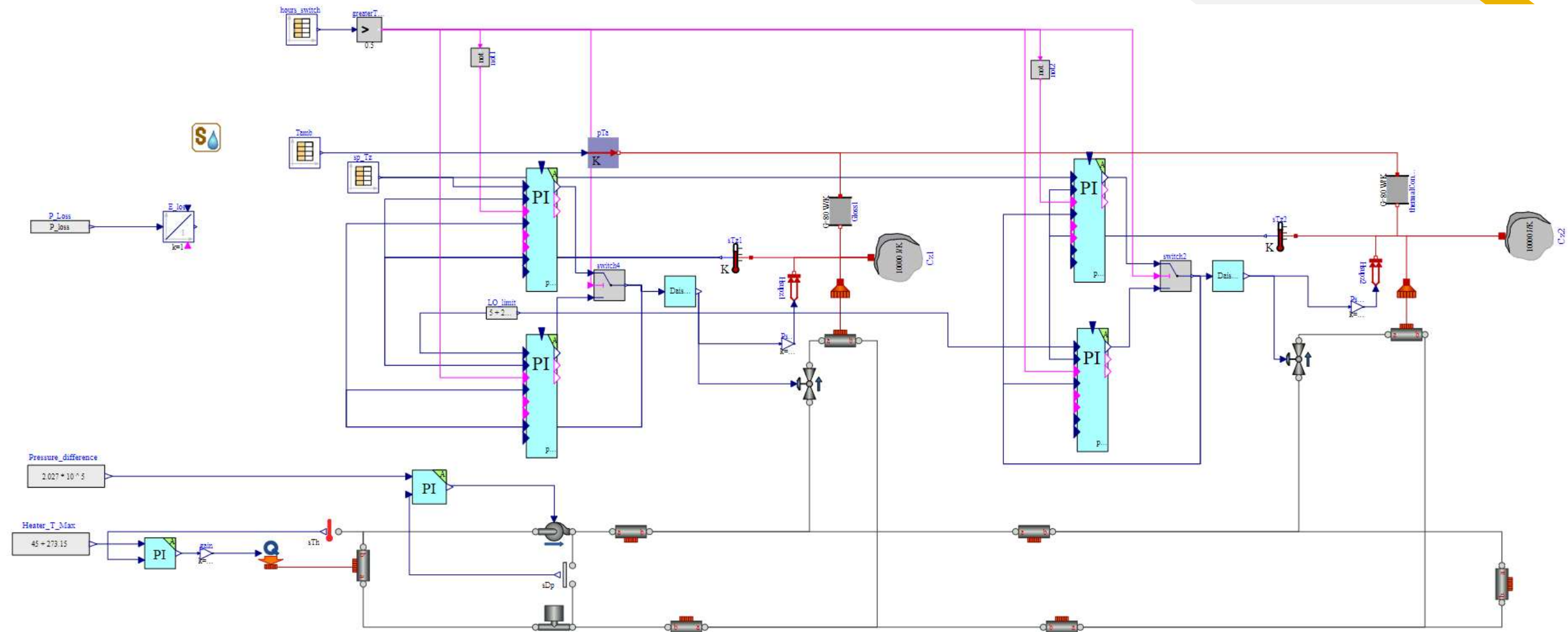
$$P_{tot} = P_{pump} + P_{heaters}$$
$$P_{average} \rightarrow 2043.9 \text{ W}$$

# Individual power consumptions



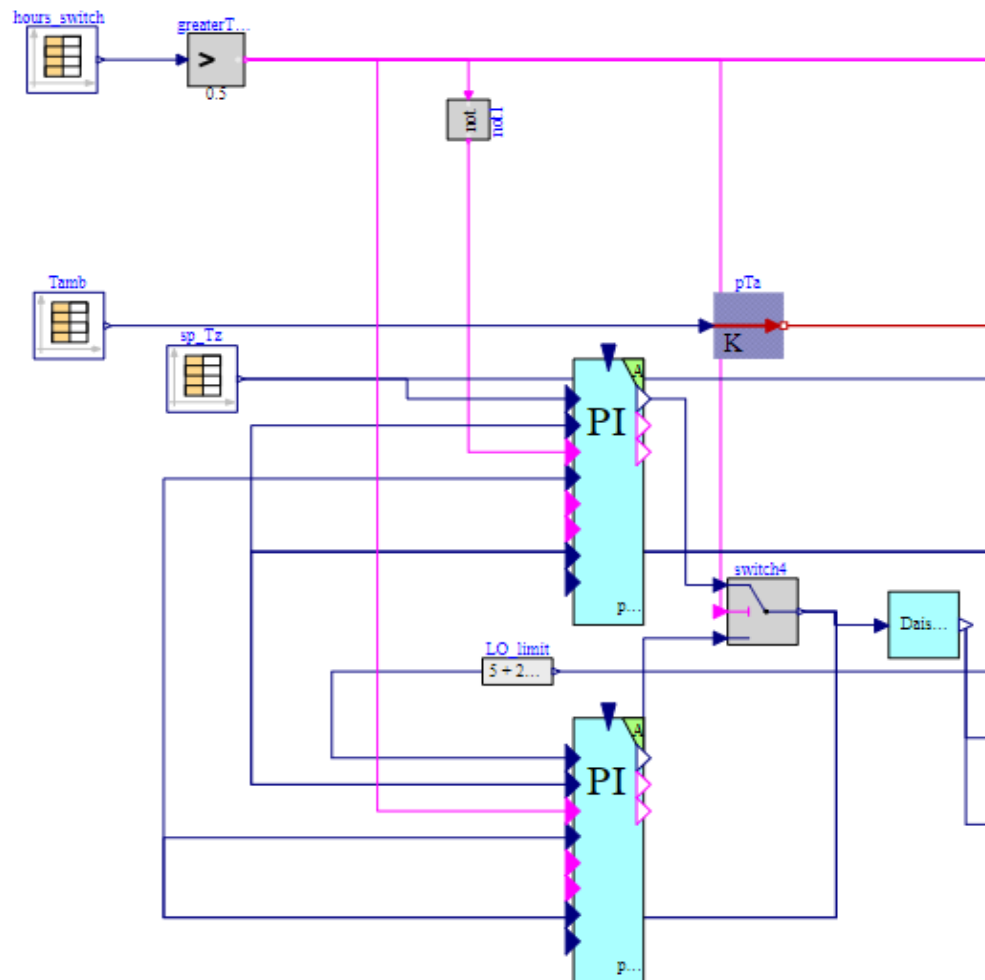
$$\begin{cases} P_{heater} = Q_{hMain} \\ P_{zones} = Q_{h1} + Q_{h2} \\ P_{pump} = w \frac{\Delta p}{\rho} \\ P_{env} = G_1(T_1 - T_{env}) + G_2(T_2 - T_{env}) \end{cases}$$

# Model with the implementation of Day-Night Control



## Components of the logic switching system:

Componente	
Nome:	hours_switch
Class	
Percorso:	Modelica.Blocks.Sources.CombiTimeTable
Commento:	Table look-up with respect to time and linear/periodic extrapolation methods
Table data definition	
tableOnFile	false
table	[0, 0; 7.5, 1; 22, 0; 24, 0]
tableName	"NoName"
fileName	"NoName"
verboseRead	true
Table data interpretation	
columns	2:size(table, 2)
smoothness	Modelica.Blocks.Types.Smoothness.ConstantSegments
extrapolation	Modelica.Blocks.Types.Extrapolation.Periodic
timeScale	3600
offset	{0}
startTime	0
shiftTime	startTime
timeEvents	Modelica.Blocks.Types.TimeEvents.Always
verboseExtrapolation	false

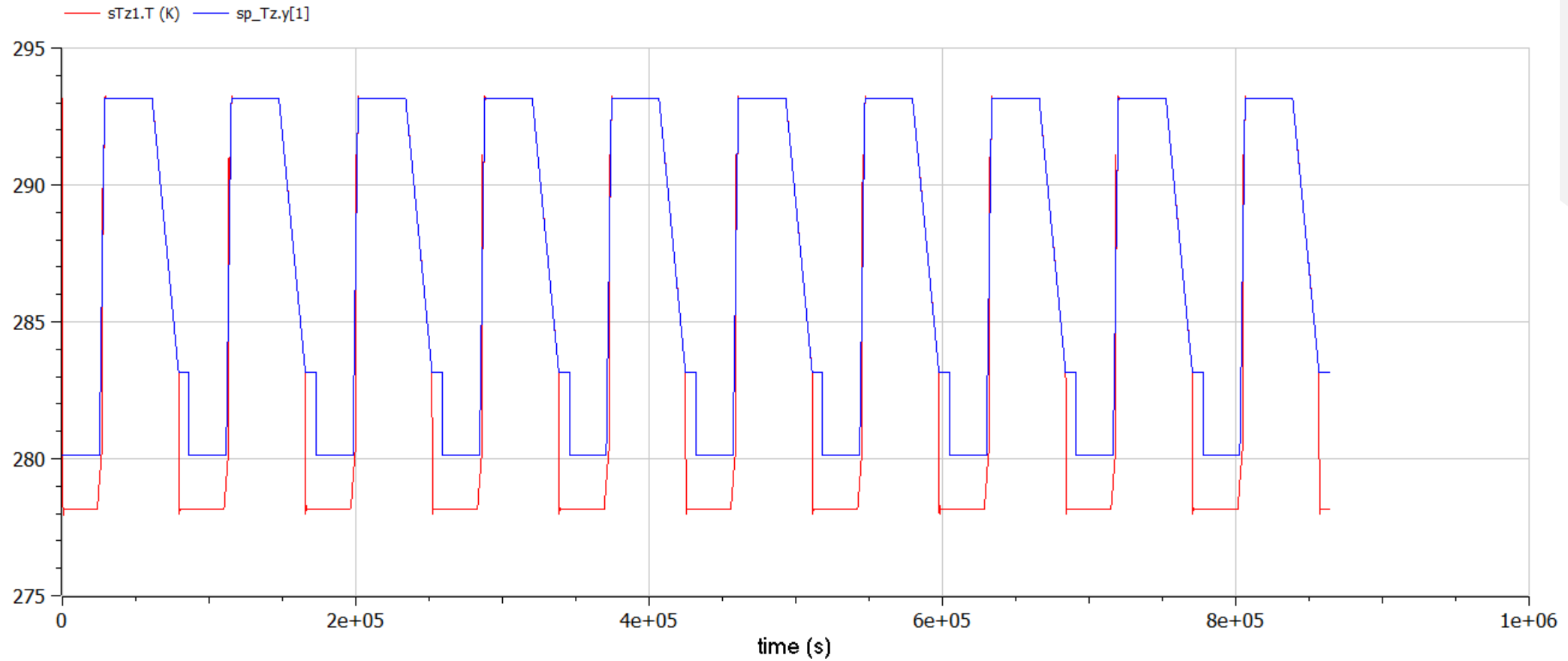


Componente	
Nome:	pI_z1D
Class	
Percorso:	AES.ControlBlocks.AnalogueControllers.PI_awfb_full
Commento:	
Parameters	
K	0.07692
Ti	76.92

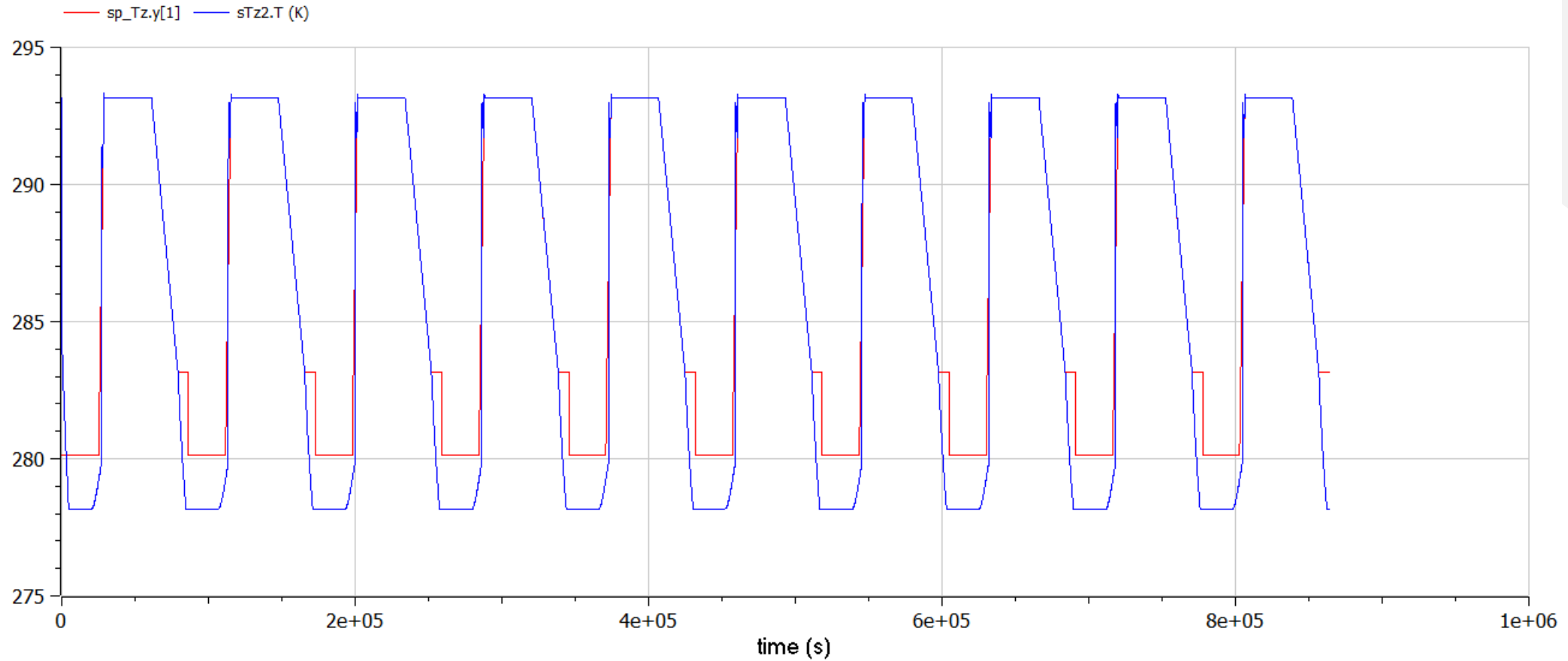
Componente	
Nome:	pI_z2D
Class	
Percorso:	AES.ControlBlocks.AnalogueControllers.PI_awfb_full
Commento:	
Parameters	
K	0.3846
Ti	76.92



# Temperature tracking of zone 1

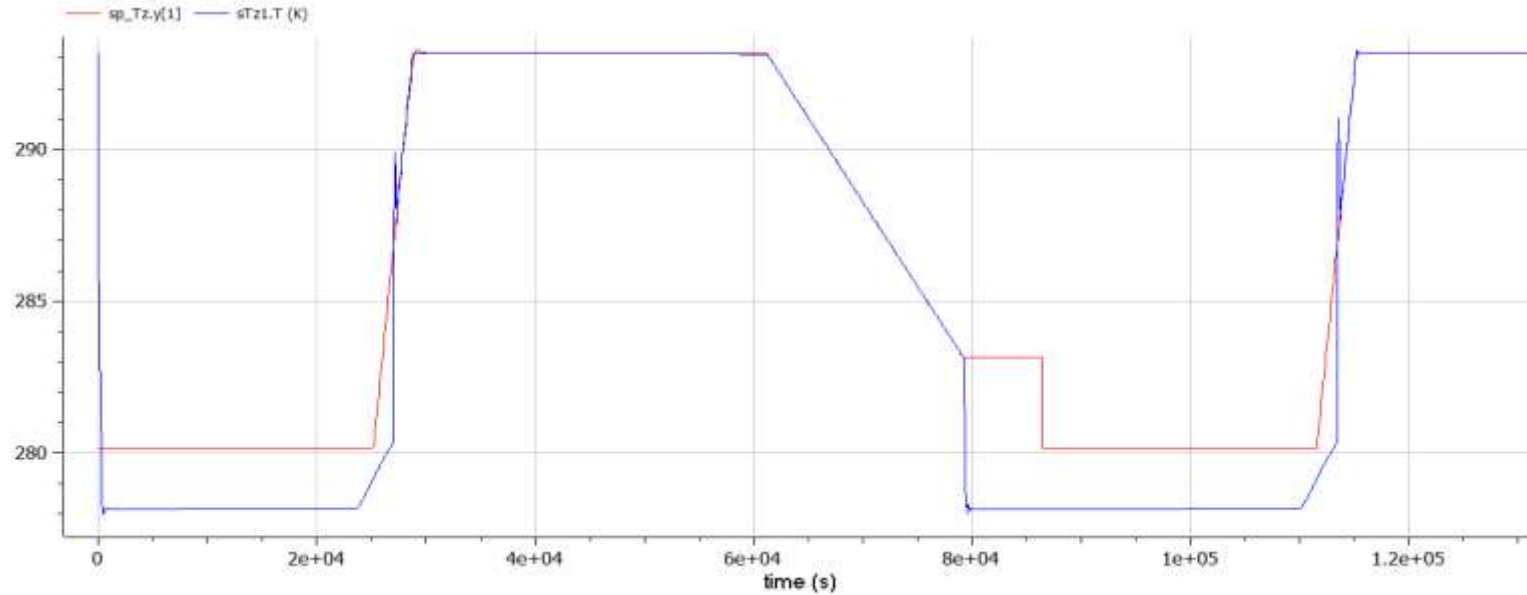


# Temperature tracking of zone 2

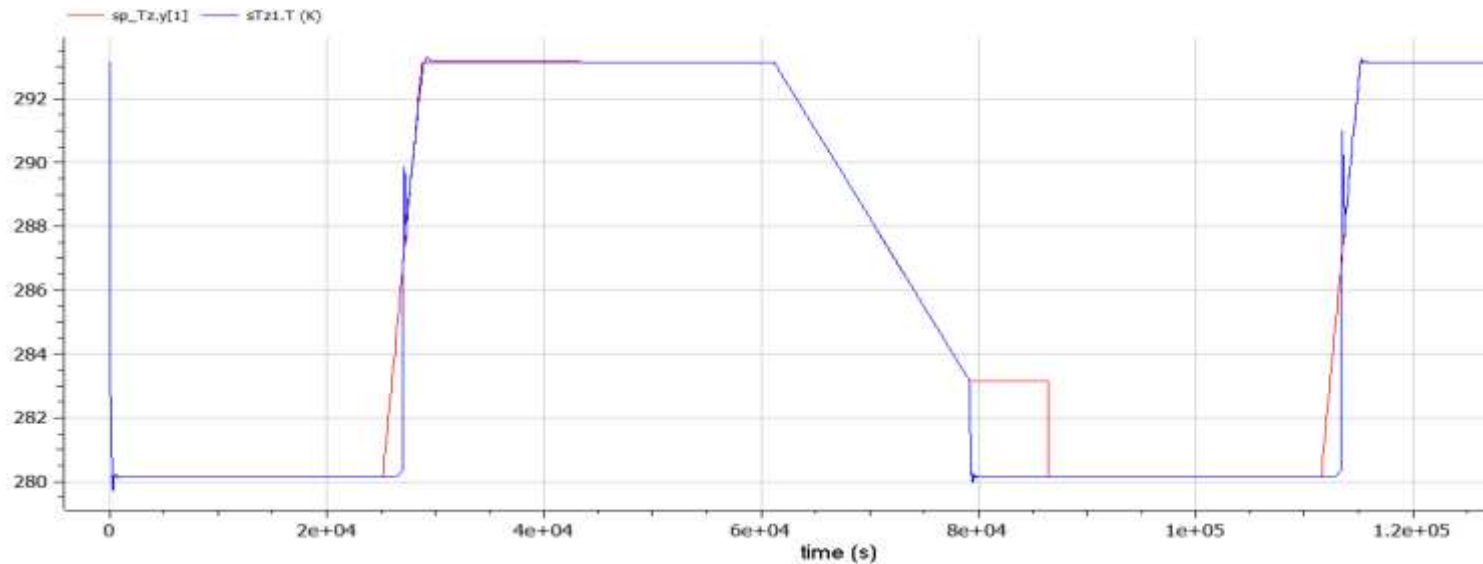


# Zone 1 Temperature tracking with different low limits

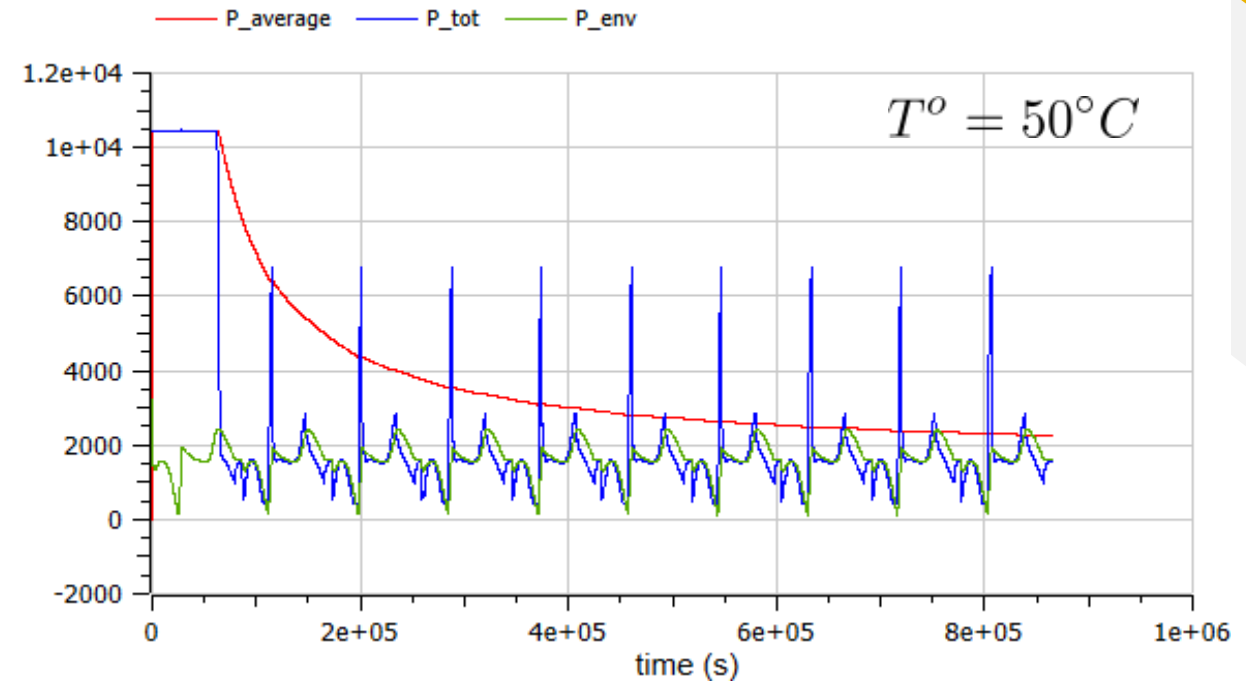
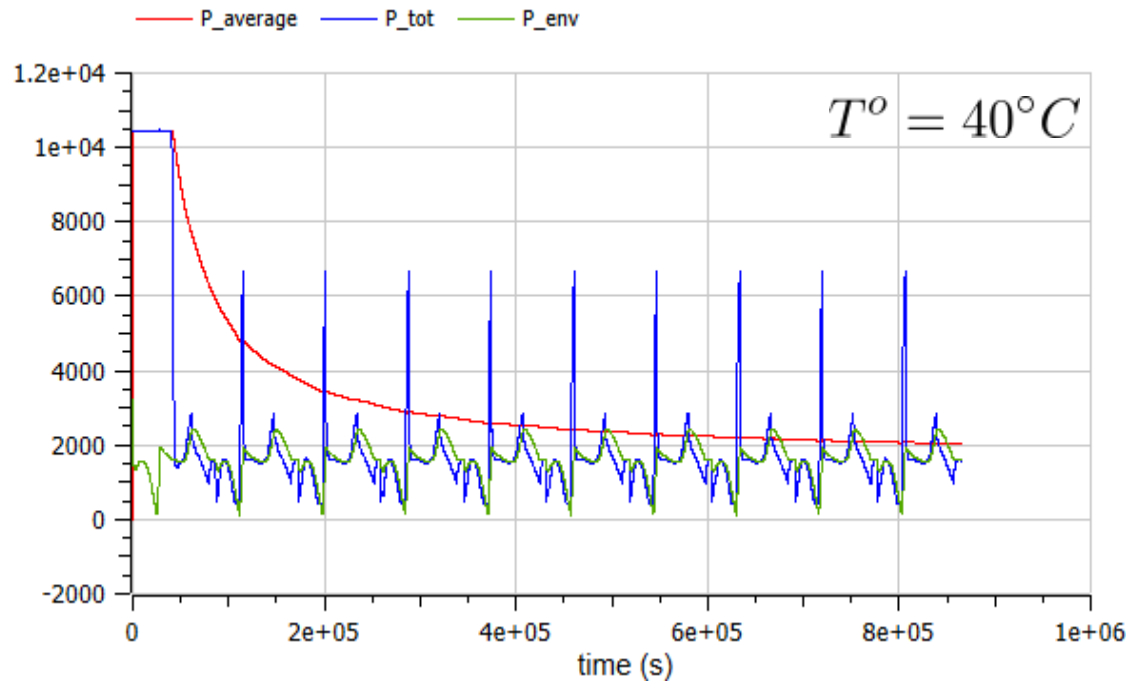
Low limit=  $5+273,15\text{K}$



Low limit=  $7+273,15\text{K}$



# Power consumption with different outlet temperatures in day mode

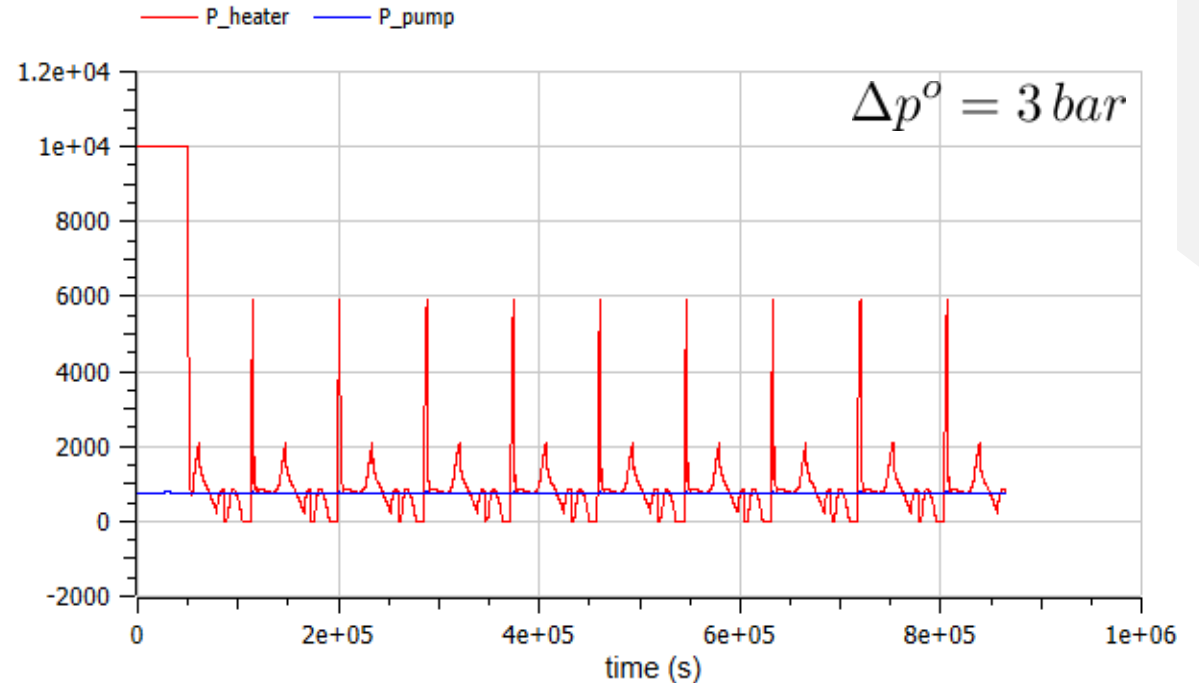
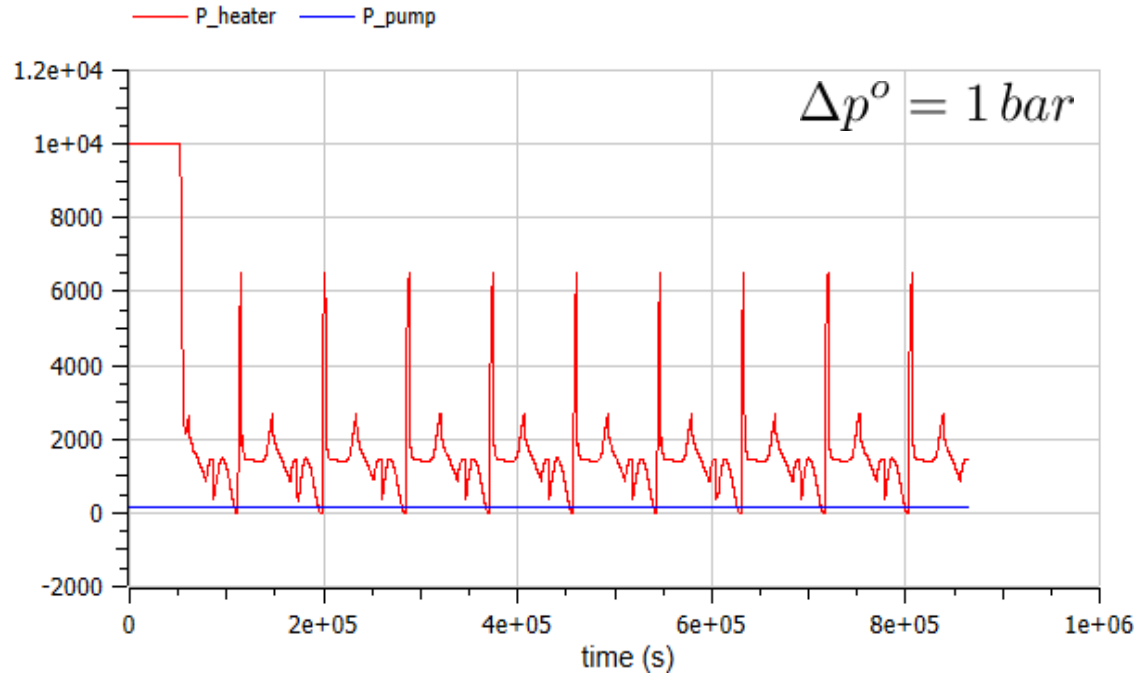


If I change the reference outlet temperature of the heater, while keeping the reference pressure constant, I get the following power consumption diagrams,

where  $P_{average} = \frac{\int_0^t P_{tot}}{t}$ .

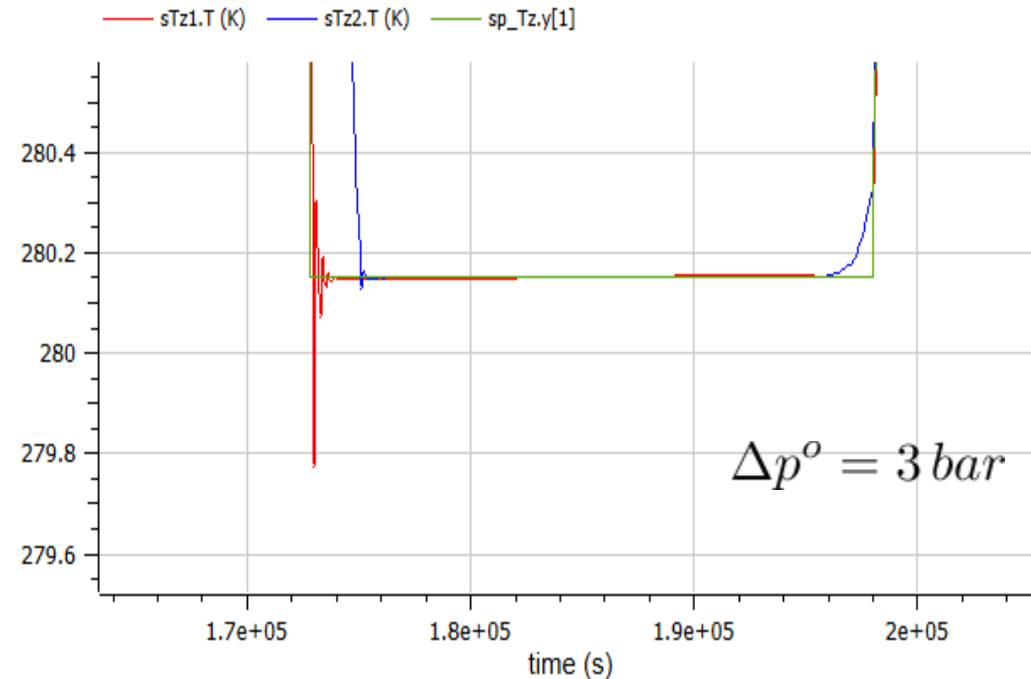
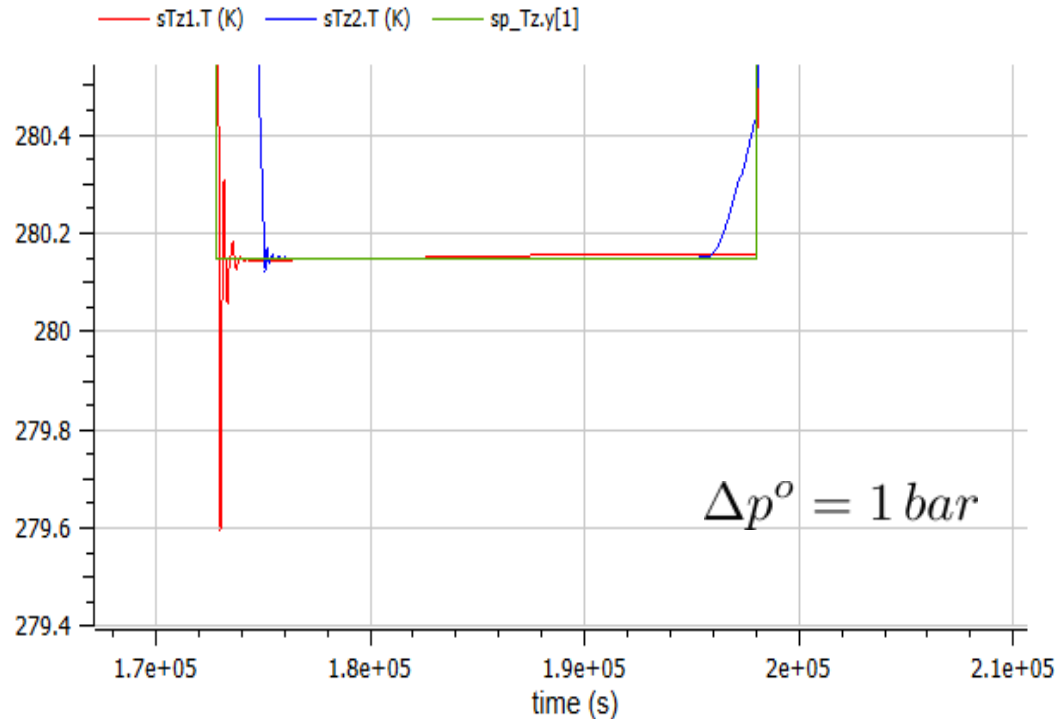
$$T^o \uparrow \Rightarrow P_{average} \uparrow$$

# Power consumption with different outlet pressure in day mode



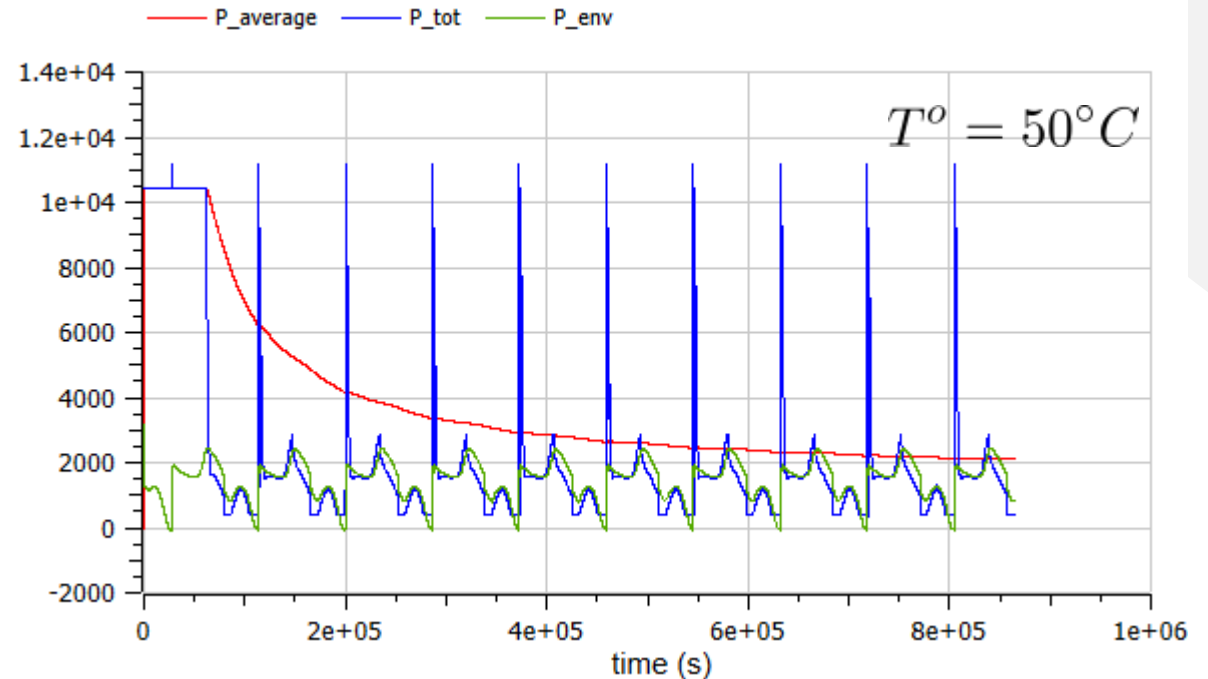
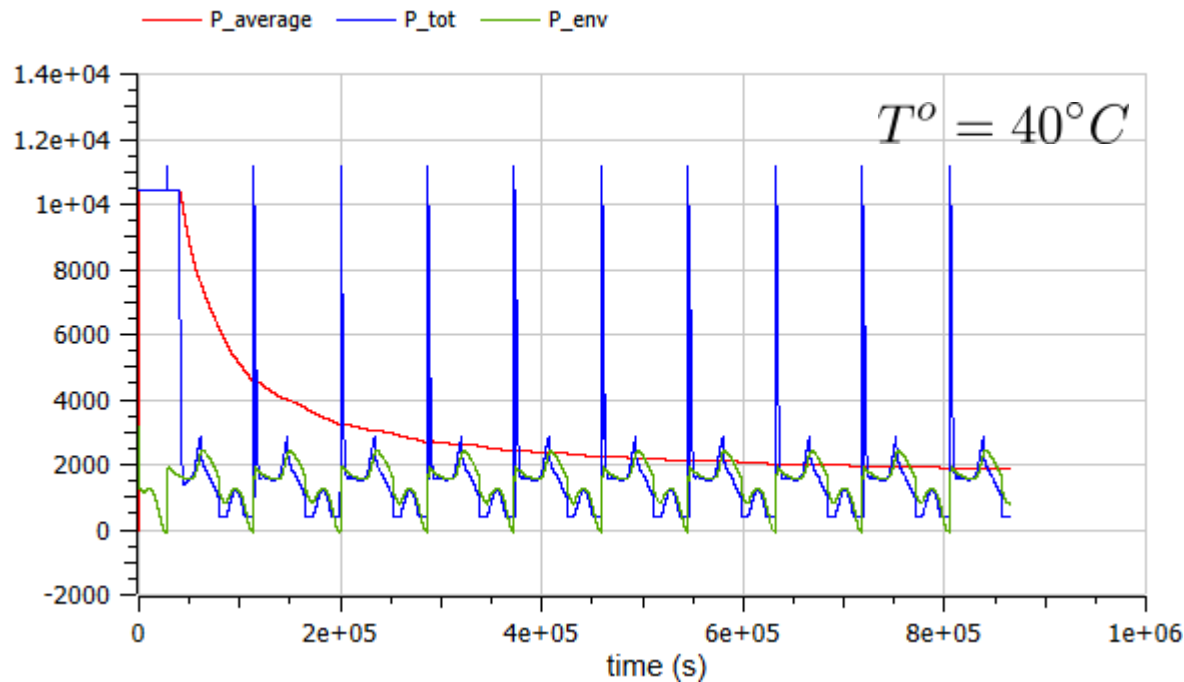
The higher the reference pressure, the more the pump will be used. As the overall consumption remains the same, I can decrease or increase the pressure reference based on the efficiency of the heater and the pump. In this case I change the pressure keeping the temperature at 45°C.

# Comparison of different reference values in day mode



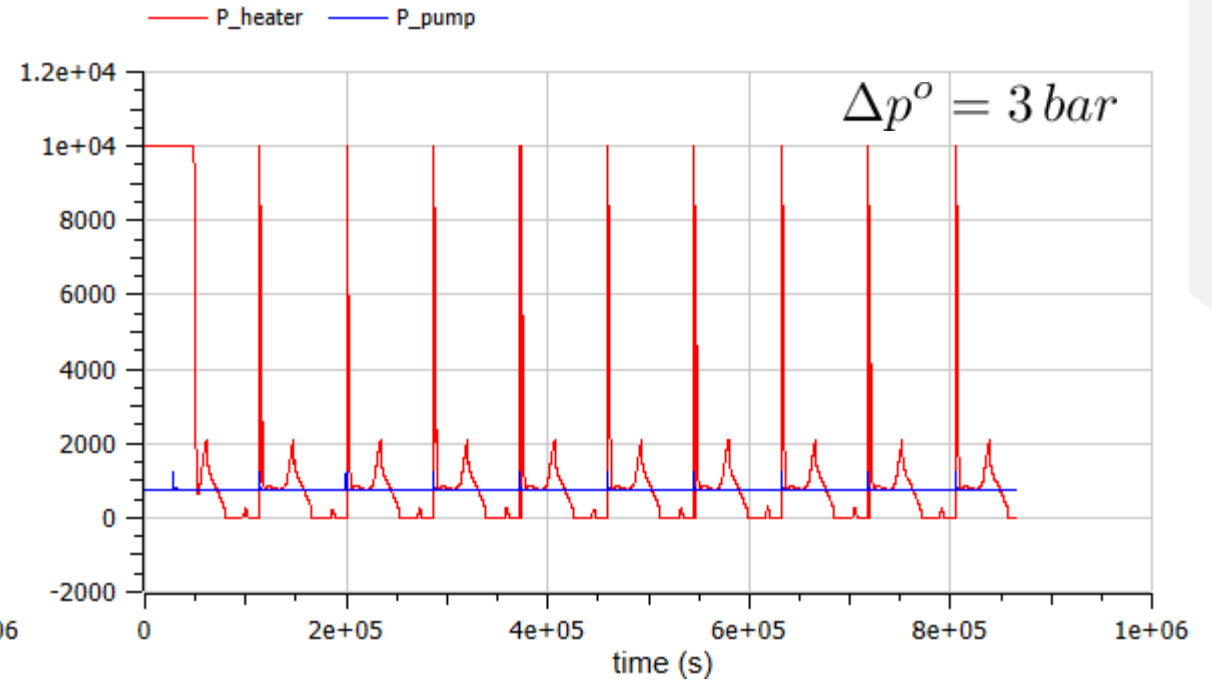
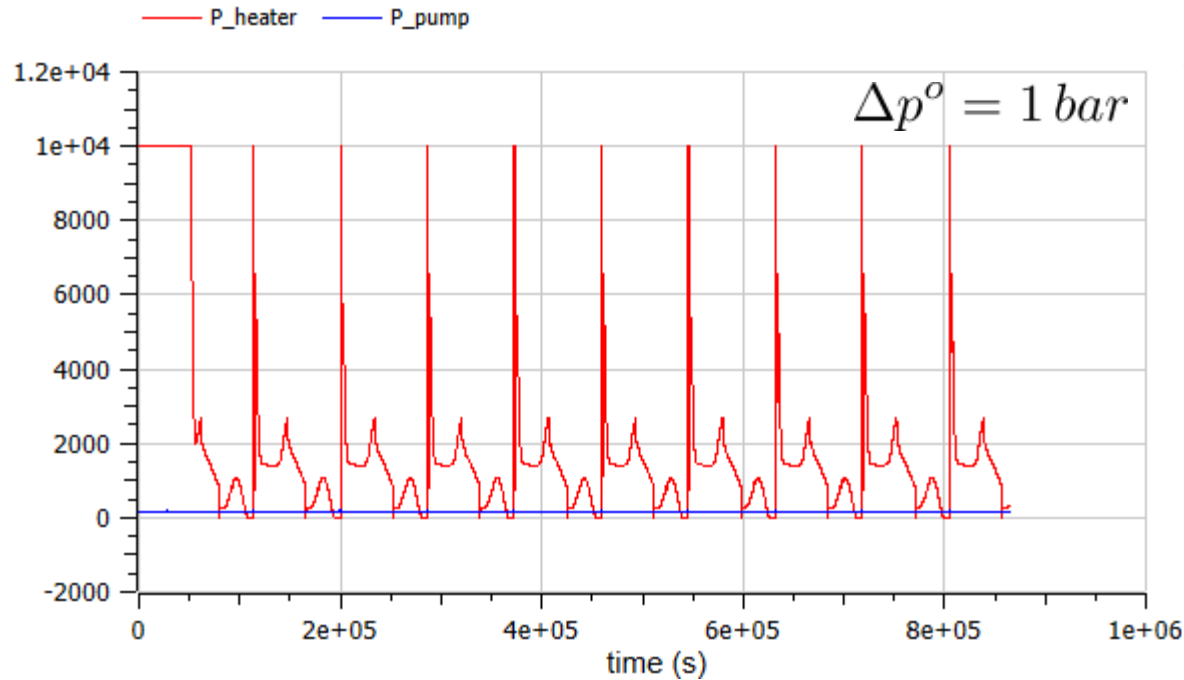
Modifying the pressure and outlet temperature references I don't change the room temperature dynamics. I only have a small reduction of the amplitude of oscillations in the case I operate at higher pressure. It is not advisable therefore to operate at higher fluid temperatures because I don't have consistent advantages.

# Power consumption with different outlet temperatures in day/night mode



The same behavior can also be observed in the day/night mode. The only difference with the previous case is that the same increment of the fluid temperature produces now a higher average power increase: 12% compared to a 10.7% increase in the day mode.

# Power consumption with different outlet pressure in day/night mode



As in the other case, higher pressure references mean more utilization of the pump instead of the heater. As during the night one of our objectives is to minimize the heater usage, we are more inclined to consider the second option.