

FLEA



bits and pieces

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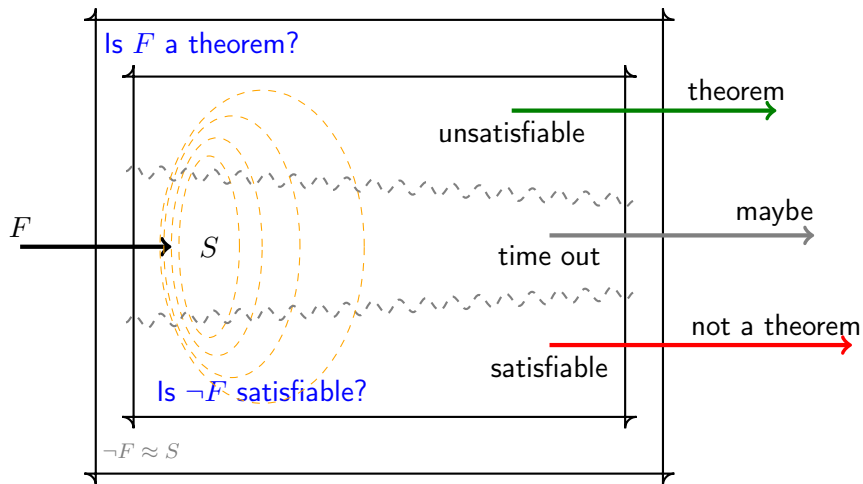
References

-  Clark Barrett, Pascal Fontaine, and Cesare Tinelli, *The Satisfiability Modulo Theories Library (SMT-LIB)*, www.SMT-LIB.org, 2016.
-  Bruno Dutertre, *Yices 2.2*, Computer-Aided Verification (CAV'2014) (Armin Biere and Roderick Bloem, eds.), Lecture Notes in Computer Science, vol. 8559, Springer, July 2014, pp. 737–744.

*Hofstadter's Law: It always takes longer than you expect,
even when you take into account Hofstadter's Law.*

— Douglas Hofstadter, Gödel, Escher, Bach: An Eternal Golden Braid

Goal



Definition (Ordered Resolution)

$$\frac{L \vee C \quad \neg L' \vee D}{(C \vee D)\sigma}$$

where

$L\sigma$ strictly maximal in $C\sigma$, $\neg L'\sigma$ maximal in $D\sigma$, $\sigma = \text{mgu}(L, L')$.

Definition (Inst-Gen)

$$\frac{L \vee C \quad \neg L' \vee D}{(L \vee C)\sigma \quad (\neg L' \vee D)\sigma}$$

where

$$\text{sel}(L \vee C) = L \quad \text{sel}(\neg L' \vee D) = \neg L' \quad \sigma = \text{mgu}(L, L')$$

Example (Resolution)

$$\frac{\frac{P(x) \vee \neg P(y) \quad \neg P(a)}{\neg P(y) \quad P(b)} \quad x \mapsto a}{\square} \quad y \mapsto b$$

Example (Inst-Gen)

$$S_0 \perp = \{P(\perp) \vee \neg P(\perp), \neg P(a), P(b)\} \quad \text{satisfiable}$$

$$\frac{P(x) \vee \neg P(y) \quad \neg P(a)}{P(a) \vee \neg P(y)} \quad x \mapsto a$$

$$S_1 \perp \supsetneq \{\neg P(a), P(b), P(a) \vee \neg P(\perp)\} \quad \text{satisfiable}$$

$$\frac{P(b) \quad P(a) \vee \neg P(y)}{P(a) \vee P(b)} \quad y \mapsto b$$

$$S_2 \perp \supsetneq \{\neg P(a), P(b), P(a) \vee \neg P(b)\} \quad \text{unsatisfiable}$$

Subsumption

$$S = \{C, D, \dots\} \quad \exists \theta \ C\theta \subseteq D \quad \text{C subsumes D}$$

$$S \text{ satisfiable} \xrightarrow{\checkmark} (S \setminus D) \text{ satisfiable}$$

$$\theta \text{ is proper, } S \perp \text{ satisfiable} \xrightarrow{\times} (S \setminus D) \perp \text{ satisfiable}$$

$$\theta \text{ is renaming, } S \perp \text{ satisfiable} \xrightarrow{\checkmark} (S \setminus D) \perp \text{ satisfiable}$$

Example

$$\begin{array}{ll} \{P(x, y), \neg P(a, z)\} & \{P(x, y), \neg P(a, z), P(a, z)\} \\ \{P(\perp, \perp), \neg P(a, \perp)\} & \{P(\perp, \perp), \neg P(a, \perp), P(a, \perp)\} \end{array}$$