

Term-Indexing

Alexander Maringele

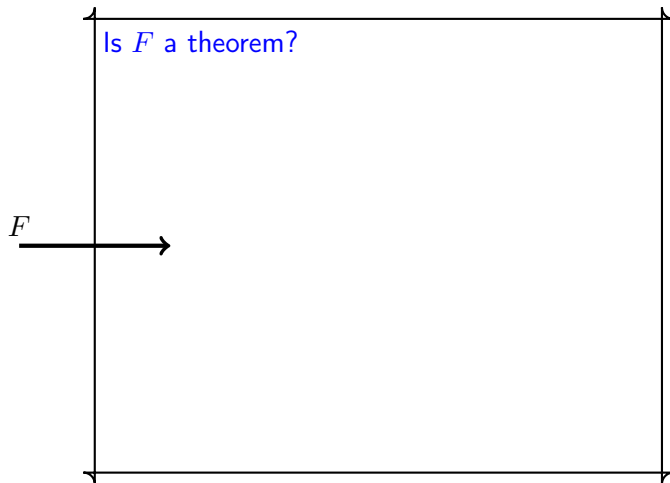
January 27th, 2016

References

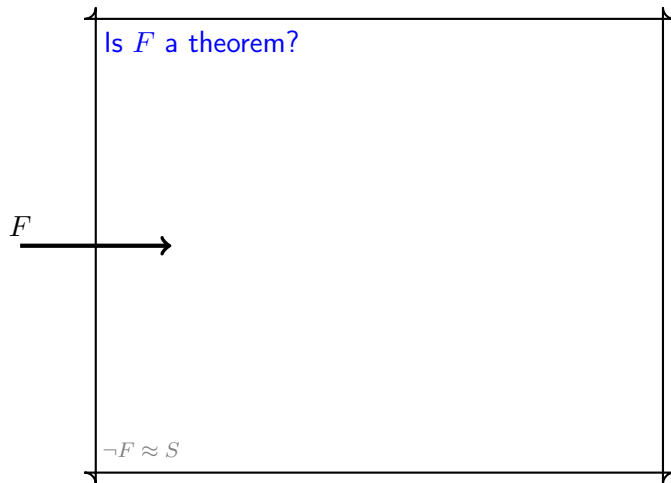
Outline

- 1 Motivation
- 2 Term Structure
- 3 Path Indexing
- 4 Discrimination Trees
- 5 Substitution Trees
- 6 Experiment

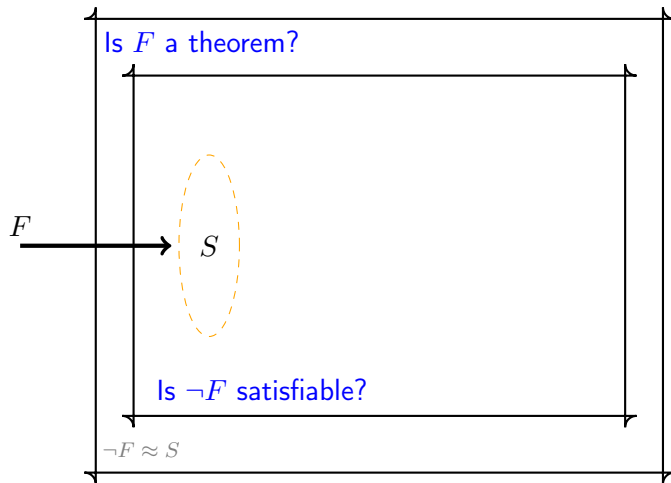
Refutation



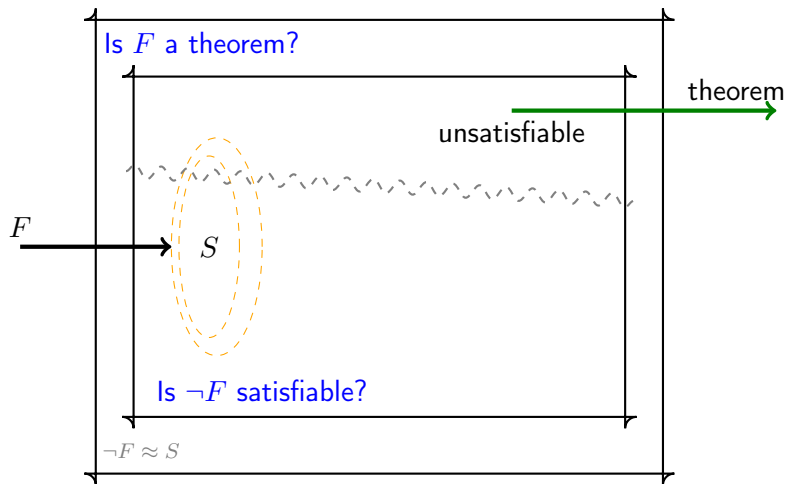
Refutation



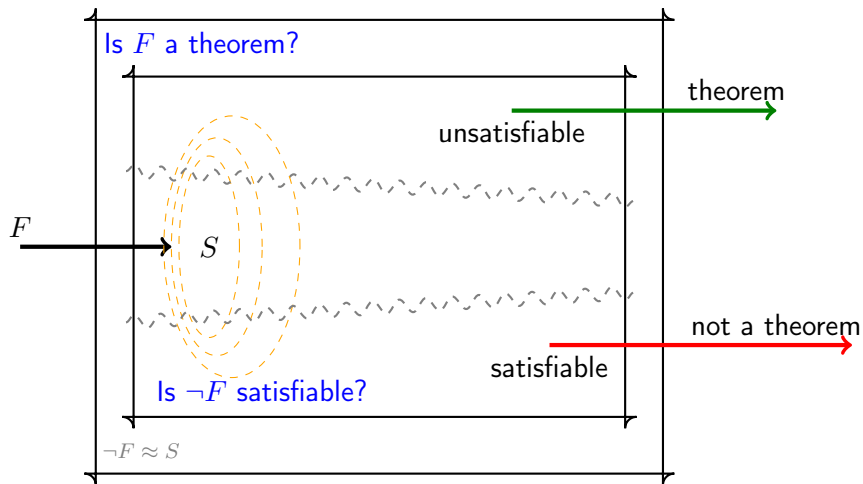
Refutation



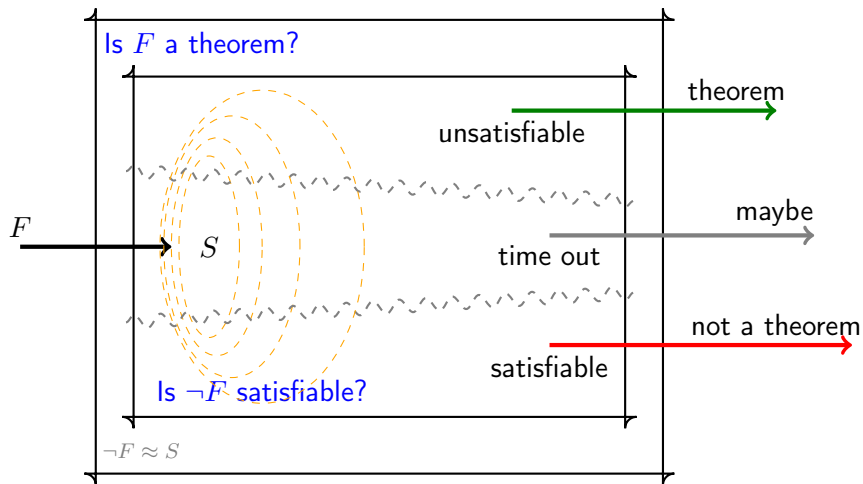
Refutation



Refutation



Refutation



Notation

Clausal form

$$\{ P(f(x)) \vee f(x) \not\approx a, g(x, y) \approx a \vee \neg Q(x, y), C_3 \}$$

Notation

Clausal form

$$\begin{aligned}
 & \{ P(f(x)) \vee f(x) \not\approx a, \ g(x, y) \approx a \vee \neg Q(x, y), \ C_3 \} \\
 & \quad \equiv \\
 & \quad \forall x (P(f(x)) \vee f(x) \not\approx a) \\
 & \quad \quad \wedge \\
 & \quad \forall xy (g(x, y) \approx a \vee \neg Q(x, y)) \\
 & \quad \quad \wedge \\
 & \quad \forall \text{Var}(C_3) (C_3)
 \end{aligned}$$

Goal

A sound and refutation complete calculus.

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Resolution (without equality)

Resolve and factor all clauses and literals in an unsatisfiable set

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$$\frac{A \vee C \quad \neg B \vee D}{(C \vee D)\sigma} (\sigma) \text{ resolution} \qquad \frac{A \vee B \vee C}{(A \vee C)\sigma} (\sigma) \text{ factoring}$$

$$\sigma = \text{mgu}(A, B)$$

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$$\frac{A \vee \mathcal{C} \quad \neg B \vee \mathcal{D}}{(\mathcal{C} \vee \mathcal{D})\sigma} (\sigma) \text{ resolution} \qquad \frac{A \vee B \vee \mathcal{C}}{(A \vee \mathcal{C})\sigma} (\sigma) \text{ factoring}$$

$$\sigma = \text{mgu}(A, B)$$

and the empty clause will be derived eventually.

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and the empty clause will be derived eventually.

Observation

Usually the set grows too fast to obtain a result.

Goal

A sound, refutation complete, and

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A sound, refutation complete, and *effective* calculus.

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- 1 *Reduce* search space

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 - Ordered Resolution, Strategies, ...

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- ...with selection functions for clauses and literals

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- 2 *Reduce* redundancy

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 - e.g. discard clauses that are subsumed by other clauses

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A sound, refutation complete, and *effective* calculus.

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 - ... depending on the calculus

Example (forward subsumption)

$$S = \{^1P(x, y), ^2\neg P(a, z)\} \cup \{^3P(a, z')\}$$

t_1 subsumes t_3

$$\frac{P(x, y) \quad \neg P(a, z)}{\square} \quad \{x \mapsto a, y \mapsto z\}$$

Resolution

$$S \perp = \{P(\perp, \perp), \neg P(a, \perp), P(a, \perp)\}$$

InstGen / SMT

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- 3 Quickly find

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3 Quickly find

- *variants*

variant removal

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- *variants*
- *instances*

variant removal
backward subsumption

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A sound, refutation complete, and effective calculus.

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- *unifiable terms*

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backward subsumption

forward subsumption

resolution, demodulation

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of a query term in a given set of terms.

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of a query term in a given set of terms.

Observation

Deduction rate drops quickly with sequential search.

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Term Indexing

Data structures and algorithms for fast retrieval of matching terms.

Position Strings

Definition

$$\mathcal{Pos}^{\Sigma}(t) = \left\{ \right.$$

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$$\mathcal{Pos}^{\Sigma}(t) = \begin{cases} \{\langle \epsilon, x \rangle\} & \text{if } t = x \in \mathcal{V} \\ \{\langle \epsilon, f \rangle\} \cup \{\langle ip, s \rangle \mid \langle p, s \rangle \in \mathcal{Pos}^{\Sigma}(t_i)\} & \text{if } t = f(t_1, \dots, t_n) \end{cases}$$

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Term traversals

$$\mathcal{Pos}^{\Sigma}(h(f(a, y))) = \{ \quad \quad \quad \}$$

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Term traversals

$$\begin{array}{l} \langle \epsilon, h \rangle \\ \langle 1, f \rangle \end{array} \quad \mathcal{Pos}^{\Sigma}(h(f(a, y))) = \{ \langle \epsilon, h \rangle, \langle 1, f \rangle, \quad \}$$

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$$\langle 1, f \rangle$$

$$\langle 11, a \rangle$$

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Term traversals

$$\langle \epsilon, h \rangle \quad \mathcal{Pos}^{\Sigma}(h(f(a, y))) = \{\langle \epsilon, h \rangle, \langle 1, f \rangle, \langle 11, a \rangle, \langle 12, y \rangle\}$$

$$\langle 1, f \rangle$$

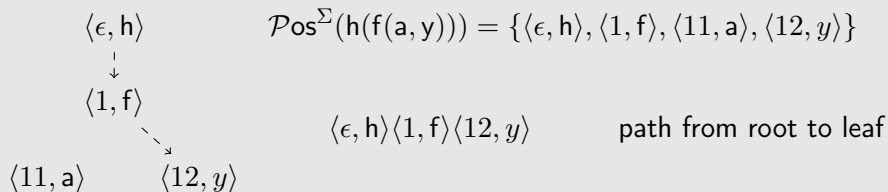
$$\langle 11, a \rangle \quad \langle 12, y \rangle$$

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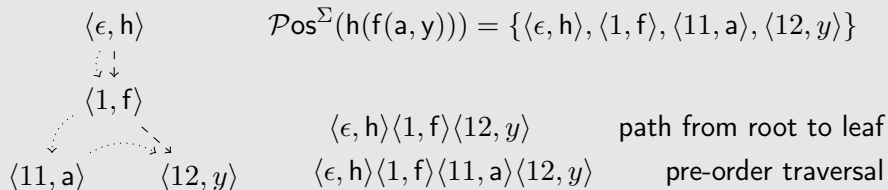


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Term traversals



Variables

Variants of terms generate the same position strings

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- if variable names are ignored

$$f(y, z) \Rightarrow \langle \epsilon, f \rangle \langle 1, * \rangle \langle 2, * \rangle$$

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In the first case even non-variants of terms generate the same strings.

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- path strings $\langle \epsilon, h \rangle \langle 1, f \rangle \langle 12, * \rangle$

$h.1.f.2.*$

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- and pre-order traversal strings $\langle \epsilon, h \rangle \langle 1, f \rangle \langle 11, * \rangle \langle 12, * \rangle$ h.f.a.*

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when the arities of function symbols are fixed.

Path Indexing

Build

$$^{t_1:} h(f(x, y)), ^{t_2:} h(f(x, a)), ^{t_3:} h(f(a, a))$$

$$t_1 \Rightarrow \{h.1.f.1.*, h.1.f.2.*\}$$

$$t_2 \Rightarrow \{h.1.f.1.*, h.1.f.2.a\}$$

$$t_3 \Rightarrow \{h.1.f.1.a, h.1.f.2.a\}$$

Path Indexing

Build

·
h
·

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h
↓
1
↓
.

Path Indexing

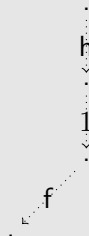
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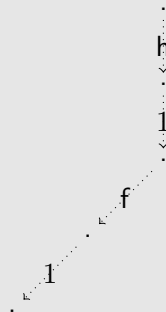
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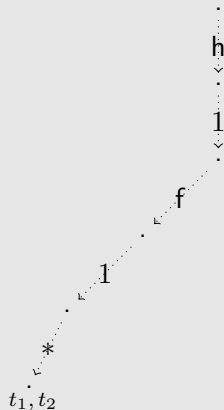
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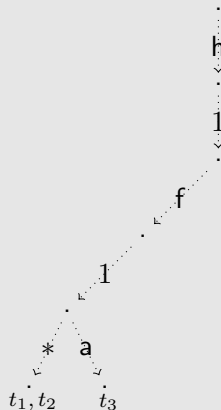
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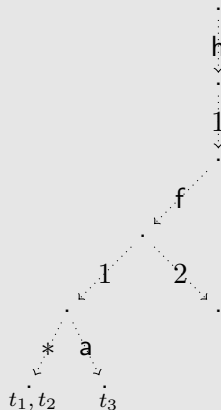
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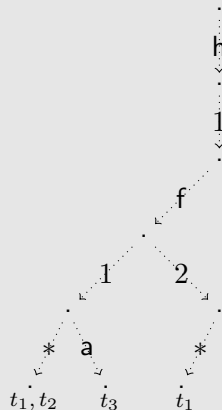
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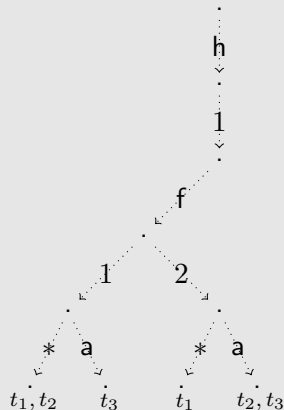
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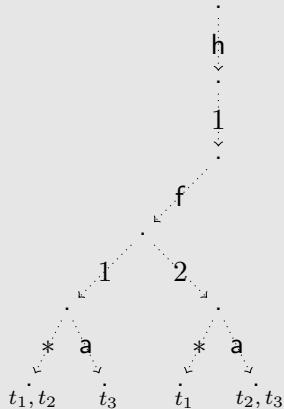


Retrieve

$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, a)), ^{t_3}h(f(a, a))$$

$$h(f(z, b)) \Rightarrow \{h.1.f.1.*, h.1.f.2.b\}$$

$$u : h(f(\textcolor{blue}{z}, \textcolor{green}{b})) \mapsto$$

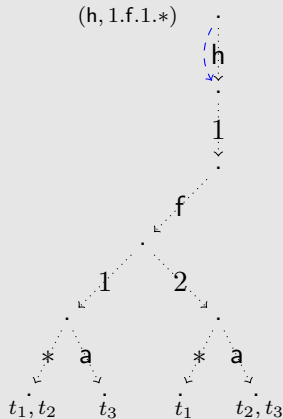


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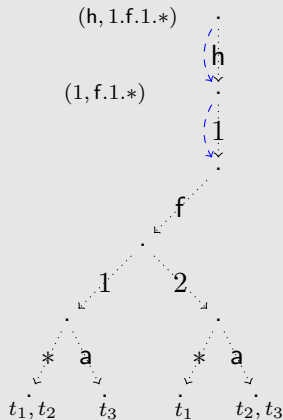


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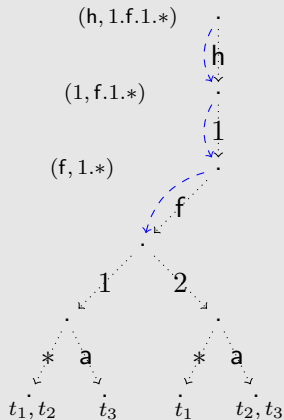


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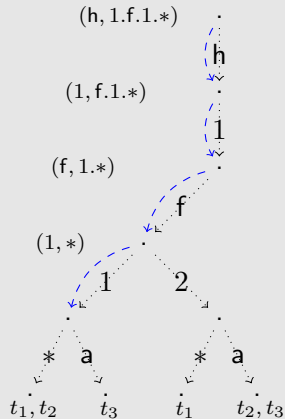


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$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, a)), ^{t_3}h(f(a, a))$$

$$h(f(z, b)) \Rightarrow \{h.1.f.1.*, h.1.f.2.b\}$$

$$u : h(f(z, b)) \mapsto$$

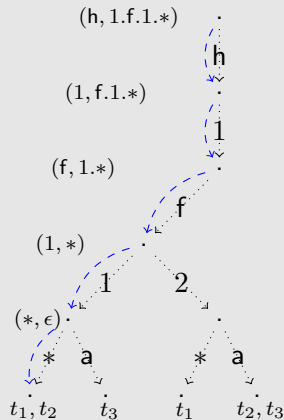


Retrieve

$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, a)), ^{t_3}h(f(a, a))$$

$$h(f(z, b)) \Rightarrow \{h.1.f.1.*, h.1.f.2.b\}$$

$$u : h(f(z, b)) \mapsto \{t_1, t_2, \quad \}$$

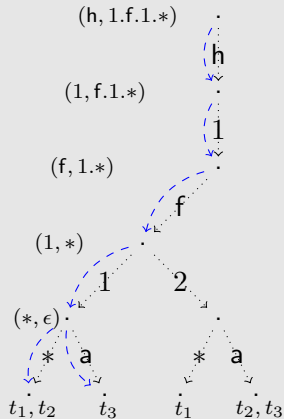


Retrieve

$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, a)), ^{t_3}h(f(a, a))$$

$$h(f(z, b)) \Rightarrow \{h.1.f.1.*, h.1.f.2.b\}$$

$$u : h(f(z, b)) \mapsto \{t_1, t_2, t_3\}$$

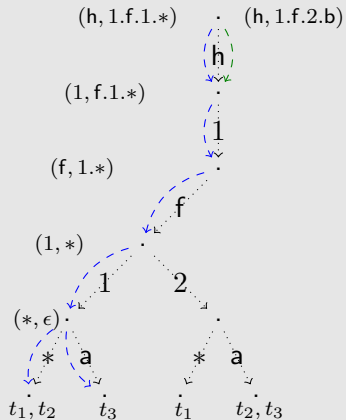


Retrieve

$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, a)), ^{t_3}h(f(a, a))$$

$$h(f(z, b)) \Rightarrow \{h.1.f.1.*, h.1.f.2.b\}$$

$$u : h(f(z, b)) \mapsto \{t_1, t_2, t_3\}$$

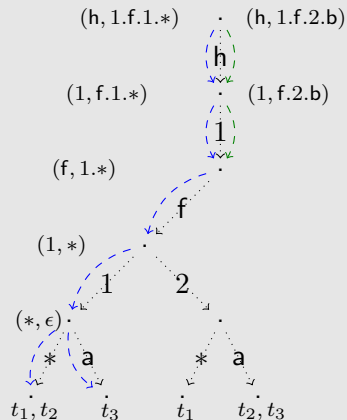


Retrieve

$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, a)), ^{t_3}h(f(a, a))$$

$$h(f(z, b)) \Rightarrow \{h.1.f.1.*, h.1.f.2.b\}$$

$$u : h(f(z, b)) \mapsto \{t_1, t_2, t_3\}$$

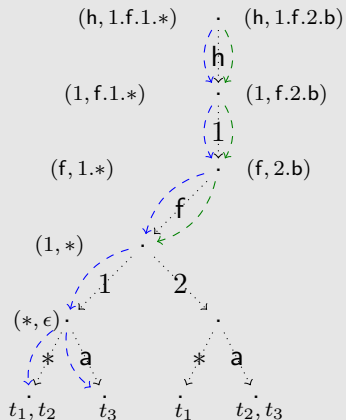


Retrieve

$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, a)), ^{t_3}h(f(a, a))$$

$$h(f(z, b)) \Rightarrow \{h.1.f.1.*, h.1.f.2.b\}$$

$$u : h(f(z, b)) \mapsto \{t_1, t_2, t_3\}$$

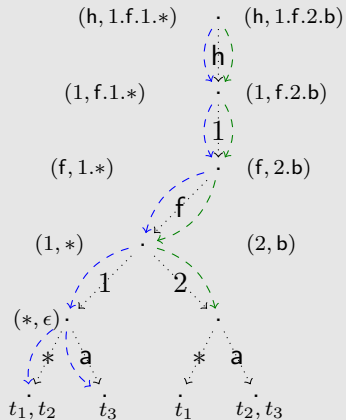


Retrieve

$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, a)), ^{t_3}h(f(a, a))$$

$$h(f(z, b)) \Rightarrow \{h.1.f.1.*, h.1.f.2.b\}$$

$$u : h(f(z, b)) \mapsto \{t_1, t_2, t_3\}$$

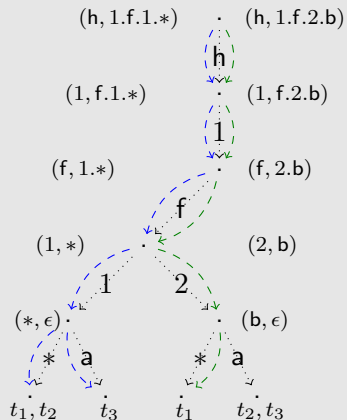


Retrieve

$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, a)), ^{t_3}h(f(a, a))$$

$$h(f(z, b)) \Rightarrow \{h.1.f.1.*, h.1.f.2.b\}$$

$$u : h(f(z, b)) \mapsto \{t_1, t_2, t_3\} \cap \{t_1\}$$



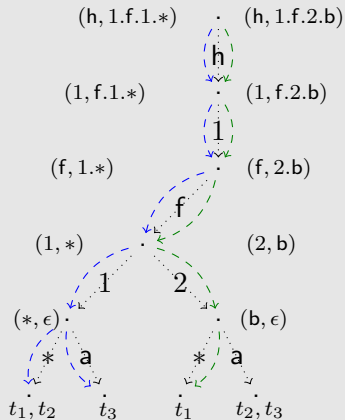
Retrieve

$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, a)), ^{t_3}h(f(a, a))$$

$$h(f(z, b)) \Rightarrow \{h.1.f.1.*, h.1.f.2.b\}$$

$$u : h(f(z, b)) \mapsto \{t_1, t_2, t_3\} \cap \{t_1\}$$

$$i : h(f(z, b)) \mapsto \{t_1, t_2, t_3\} \cap \{\}$$



Retrieve

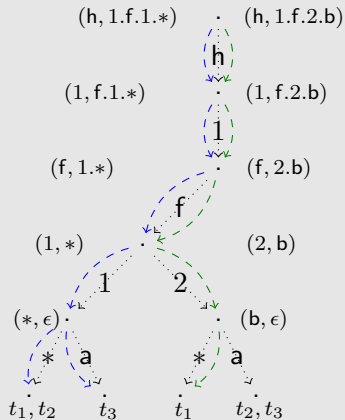
$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, a)), ^{t_3}h(f(a, a))$$

$$h(f(z, b))) \Rightarrow \{h.1.f.1.*, h.1.f.2.b\}$$

$$u : h(f(z, b)) \mapsto \{t_1, t_2, t_3\} \cap \{t_1\}$$

$$i : h(f(z, \mathbf{b})) \mapsto \{t_1, t_2, t_3\} \cap \{$$

$$g : h(f(z, \mathbf{b})) \mapsto \{t_1, t_2\} \cap \{t_1\}$$



Retrieve

$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, a)), ^{t_3}h(f(a, a))$$

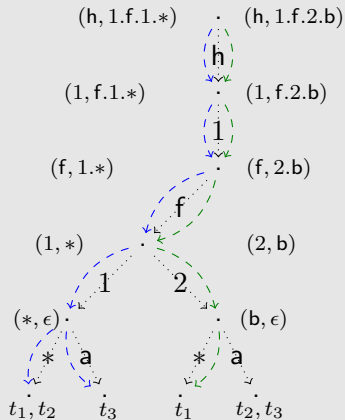
$$h(f(z, b)) \Rightarrow \{h.1.f.1.*, h.1.f.2.b\}$$

$$u : h(f(z, b)) \mapsto \{t_1, t_2, t_3\} \cap \{t_1\}$$

$$i : h(f(z, b)) \mapsto \{t_1, t_2, t_3\} \cap \{\}$$

$$g : h(f(z, b)) \mapsto \{t_1, t_2\} \cap \{t_1\}$$

$$v : h(f(z, b)) \mapsto \{t_1, t_2\} \cap \{\}$$



Retrieve

$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, a)), ^{t_3}h(f(a, a))$$

$$h(f(z, b)) \Rightarrow \{h.1.f.1.*, h.1.f.2.b\}$$

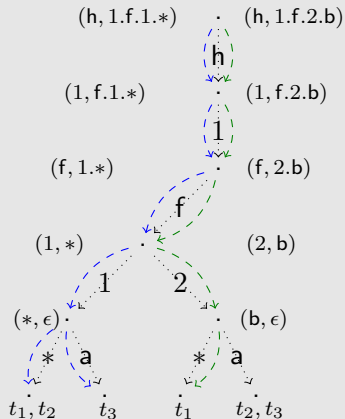
$$u : h(f(z, b)) \mapsto \{t_1, t_2, t_3\} \cap \{t_1\}$$

$$i : h(f(z, b)) \mapsto \{t_1, t_2, t_3\} \cap \{\}$$

$$g : h(f(z, b)) \mapsto \{t_1, t_2\} \cap \{t_1\}$$

$$v : h(f(z, b)) \mapsto \{t_1, t_2\} \cap \{\}$$

$$v : h(f(z, z)) \mapsto \{t_1, t_2\} \cap \{t_1\}$$



Unit Superposition Inference Rules

$$\frac{s \approx t \quad L[s']}{(L[t]) \cdot \sigma} \quad \begin{array}{l} \text{unit} \\ \text{paramodulation} \end{array}$$

where $\sigma = \text{mgu}(s, s')$, $s' \notin \mathcal{V}$, $t\sigma \neq s\sigma$

$$\frac{s \approx t \quad u[s'] \not\approx v}{(u[t] \not\approx v) \cdot \sigma} \quad \begin{array}{l} \text{unit} \\ \text{superposition} \end{array} \quad \frac{s \approx t \quad u[s'] \approx v}{(u[t] \approx v) \cdot \sigma}$$

where $\sigma = \text{mgu}(s, s')$, $s' \notin \mathcal{V}$, $t\sigma \neq s\sigma$, $v\sigma \neq u[s']\sigma$

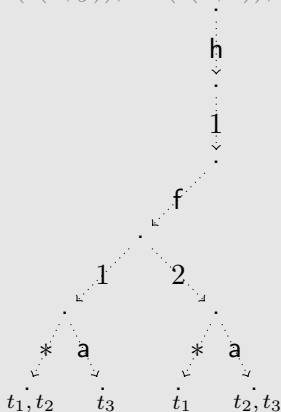
$$\frac{s \not\approx t}{\square} \quad \begin{array}{l} \text{unit equality} \\ \text{resolution} \end{array}$$

$$\frac{A \quad \neg B}{\square} \quad \begin{array}{l} \text{unit} \\ \text{resolution} \end{array}$$

where s and t (A and B respectively) are unifiable

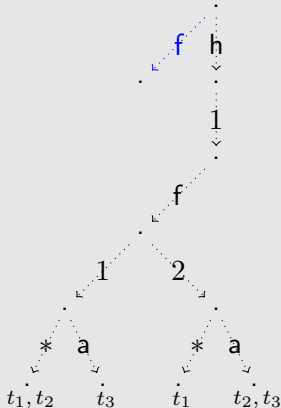
Demodulation

$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, a)), ^{t_3}h(f(a, a)), \dots, f(x, a) \approx x$$



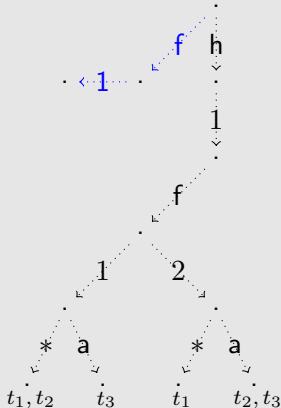
Demodulation

$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, a)), ^{t_3}h(f(a, a)), \dots, f(x, a) \approx x$$



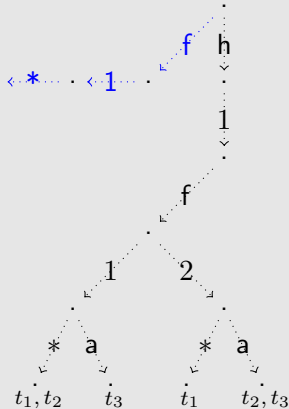
Demodulation

$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, a)), ^{t_3}h(f(a, a)), \dots, f(x, a) \approx x$$



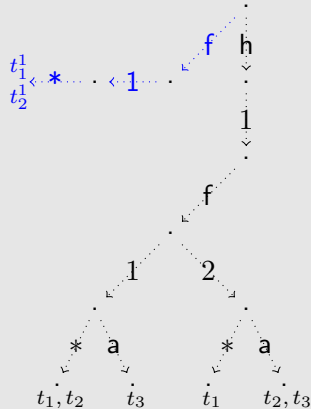
Demodulation

$${}^{t_1}h(f(x, y)), {}^{t_2}h(f(x, a)), {}^{t_3}h(f(a, a)), \dots, f(x, a) \approx x$$



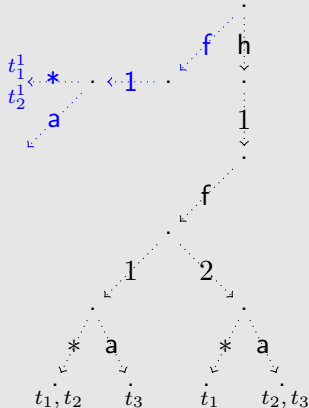
Demodulation

$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, a)), ^{t_3}h(f(a, a)), \dots, f(x, a) \approx x$$



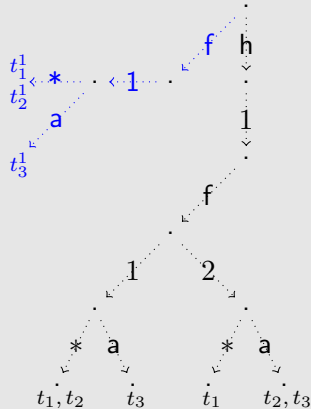
Demodulation

$${}^{t_1}h(f(x, y)), {}^{t_2}h(f(x, a)), {}^{t_3}h(f(a, a)), \dots, f(x, a) \approx x$$



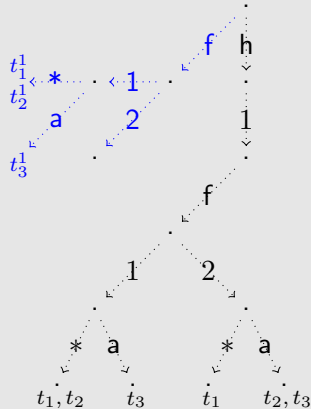
Demodulation

$${}^{t_1}h(f(x, y)), {}^{t_2}h(f(x, a)), {}^{t_3}h(f(a, a)), \dots, f(x, a) \approx x$$



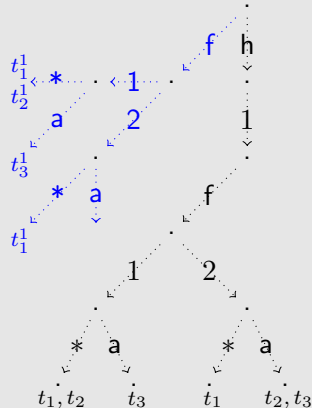
Demodulation

$${}^{t_1}h(f(x, y)), {}^{t_2}h(f(x, a)), {}^{t_3}h(f(a, a)), \dots, f(x, a) \approx x$$



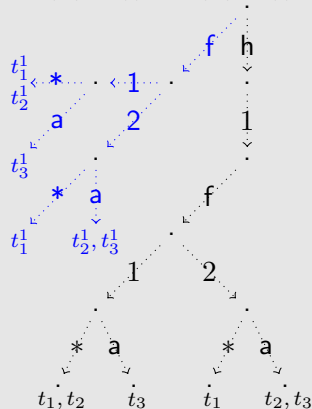
Demodulation

$${}^{t_1}\mathbf{h}(\mathbf{f}(x, y)), {}^{t_2}\mathbf{h}(\mathbf{f}(x, \mathbf{a})), {}^{t_3}\mathbf{h}(\mathbf{f}(\mathbf{a}, \mathbf{a})), \dots, \mathbf{f}(x, \mathbf{a}) \approx x$$



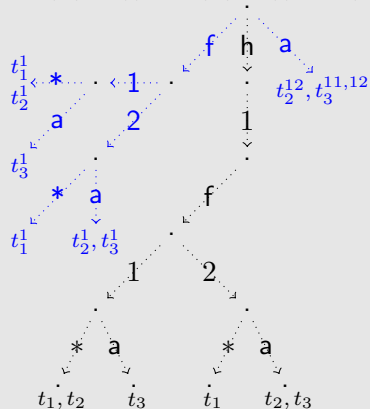
Demodulation

$${}^{t_1}\mathbf{h}(\mathbf{f}(x, y)), {}^{t_2}\mathbf{h}(\mathbf{f}(x, \mathbf{a})), {}^{t_3}\mathbf{h}(\mathbf{f}(\mathbf{a}, \mathbf{a})), \dots, \mathbf{f}(x, \mathbf{a}) \approx x$$



Demodulation

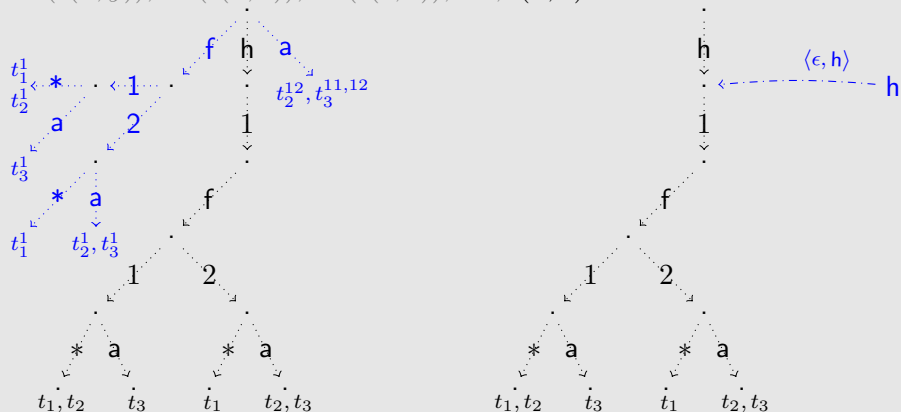
$${}^{t_1}h(f(x, y)), {}^{t_2}h(f(x, a)), {}^{t_3}h(f(a, a)), \dots, f(x, a) \approx x$$



Demodulation

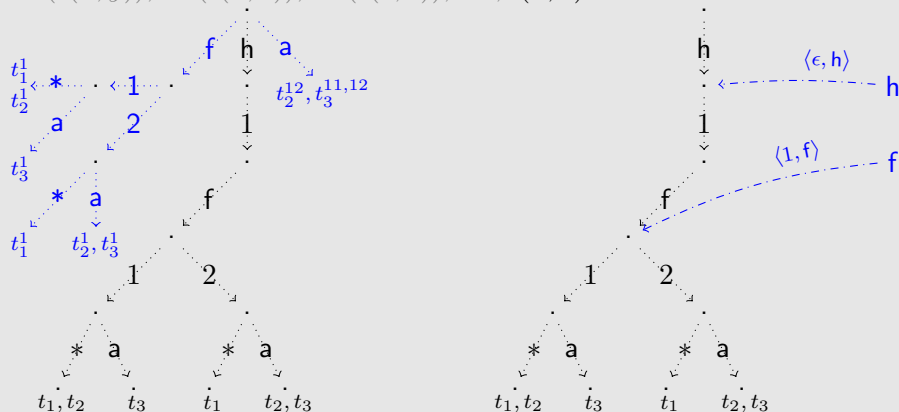
$${}^{t_1}h(f(x, y)), {}^{t_2}h(f(x, a)), {}^{t_3}h(f(a, a)), \dots, f(x, a) \approx x$$



$${}^{t_1}\mathbf{h}(\mathbf{f}(x, y)), {}^{t_2}\mathbf{h}(\mathbf{f}(x, \mathbf{a})), {}^{t_3}\mathbf{h}(\mathbf{f}(\mathbf{a}, \mathbf{a})), \dots, \mathbf{f}(x, \mathbf{a}) \approx x$$


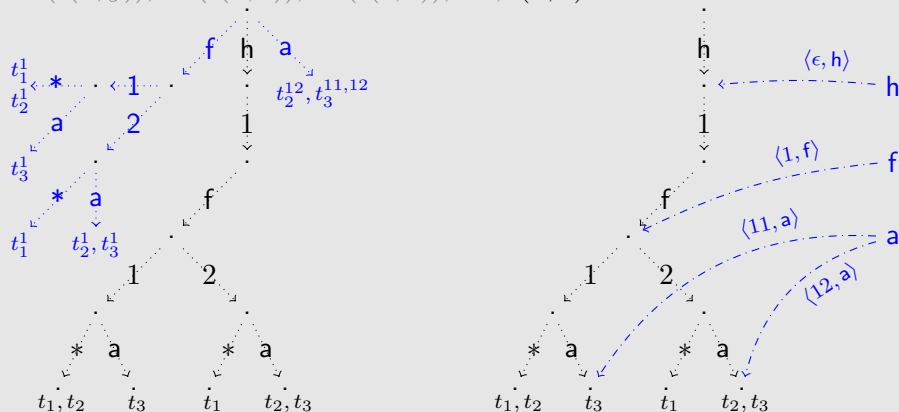
Demodulation

$${}^{t_1}h(f(x, y)), {}^{t_2}h(f(x, a)), {}^{t_3}h(f(a, a)), \dots, f(x, a) \approx x$$



Demodulation

$${}^{t_1}h(f(x, y)), {}^{t_2}h(f(x, a)), {}^{t_3}h(f(a, a)), \dots, f(x, a) \approx x$$



Discrimination Trees

Insert

$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, h(a))), ^{t_3}h(f(h(a), a))$$

$$t_1 \Rightarrow h.f.*.*$$

$$t_2 \Rightarrow h.f.*.h.a$$

$$t_3 \Rightarrow h.f.h.a.a$$

Discrimination Trees

Insert



$t_1: h(f(x, y)), t_2: h(f(x, h(a))), t_3: h(f(h(a), a))$

$t_1 \Rightarrow h.f.*.*$

$t_2 \Rightarrow h.f.*.h.a$

$t_3 \Rightarrow h.f.h.a.a$

Discrimination Trees

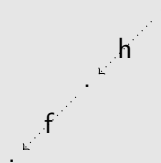
Insert

$t_1: h(f(x, y)), t_2: h(f(x, h(a))), t_3: h(f(h(a), a))$

$t_1 \Rightarrow h.f.*.*$

$t_2 \Rightarrow h.f.*.h.a$

$t_3 \Rightarrow h.f.h.a.a$



Discrimination Trees

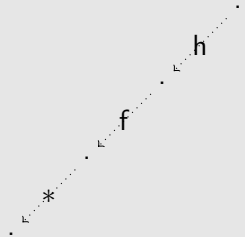
Insert

$t_1: h(f(x, y)), t_2: h(f(x, h(a))), t_3: h(f(h(a), a))$

$t_1 \Rightarrow h.f.*.*$

$t_2 \Rightarrow h.f.*.h.a$

$t_3 \Rightarrow h.f.h.a.a$



Discrimination Trees

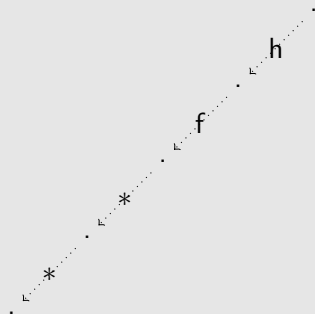
Insert

$t_1: h(f(x, y)), t_2: h(f(x, h(a))), t_3: h(f(h(a), a))$

$t_1 \Rightarrow h.f.*.*$

$t_2 \Rightarrow h.f.*.h.a$

$t_3 \Rightarrow h.f.h.a.a$



Discrimination Trees

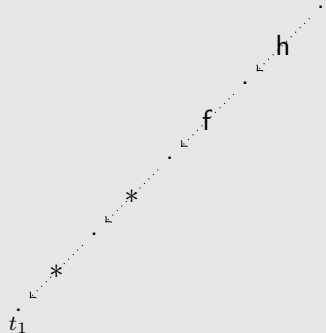
Insert

$t_1: h(f(x, y)), t_2: h(f(x, h(a))), t_3: h(f(h(a), a))$

$t_1 \Rightarrow h.f.*.*$

$t_2 \Rightarrow h.f.*.h.a$

$t_3 \Rightarrow h.f.h.a.a$



Discrimination Trees

Insert

$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, h(a))), ^{t_3}h(f(h(a), a))$$
$$t_1 \Rightarrow \text{h.f.*.*}$$
$$t_2 \Rightarrow \text{h.f.} * \text{h.a}$$
$$t_3 \Rightarrow \text{h.f.h.a.a}$$

Discrimination Trees

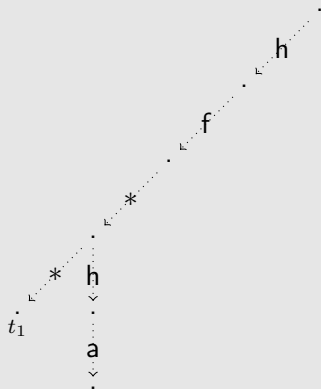
Insert

$t_1: h(f(x, y)), t_2: h(f(x, h(a))), t_3: h(f(h(a), a))$

$t_1 \Rightarrow h.f.*.*$

$t_2 \Rightarrow h.f.*.h.a$

$t_3 \Rightarrow h.f.h.a.a$



Discrimination Trees

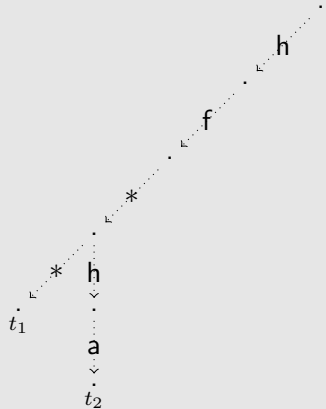
Insert

$t_1: h(f(x, y)), t_2: h(f(x, h(a))), t_3: h(f(h(a), a))$

$t_1 \Rightarrow h.f.*.*$

$t_2 \Rightarrow h.f.*.h.a$

$t_3 \Rightarrow h.f.h.a.a$



Discrimination Trees

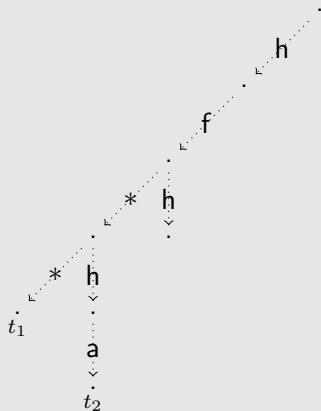
Insert

$t_1: h(f(x, y)), t_2: h(f(x, h(a))), t_3: h(f(h(a), a))$

$t_1 \Rightarrow h.f.*.*$

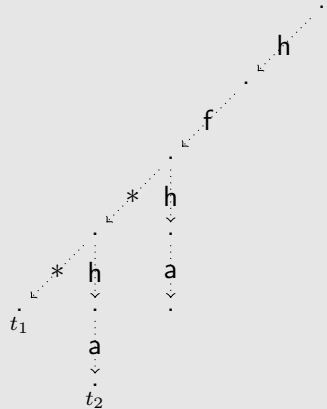
$t_2 \Rightarrow h.f.*.h.a$

$t_3 \Rightarrow h.f.h.a.a$



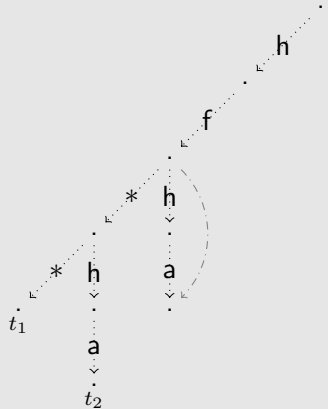
Discrimination Trees

Insert

$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, h(a))), ^{t_3}h(f(h(a), a))$$
$$t_1 \Rightarrow \text{h.f.*.*}$$
$$t_2 \Rightarrow \text{h.f.} * \text{h.a}$$
$$t_3 \Rightarrow \text{h.f.h.a.a}$$


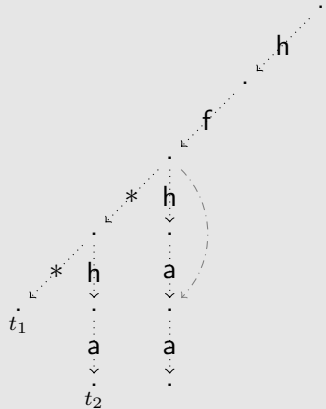
Discrimination Trees

Insert

$$^{t_1:}h(f(x, y)), ^{t_2:}h(f(x, h(a))), ^{t_3:}h(f(h(a), a))$$
$$t_1 \Rightarrow \text{h.f.}.*.*$$
$$t_2 \Rightarrow \text{h.f.} * \text{h.a}$$
$$t_3 \Rightarrow \text{h.f.h.a.a}$$


Discrimination Trees

Insert

$$^{t_1:}h(f(x, y)), ^{t_2:}h(f(x, h(a))), ^{t_3:}h(f(h(a), a))$$
$$t_1 \Rightarrow \text{h.f.*.*}$$
$$t_2 \Rightarrow \text{h.f.} * \text{h.a}$$
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Discrimination Trees

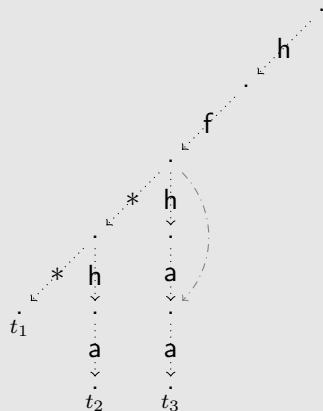
Insert

$t_1: h(f(x, y)), t_2: h(f(x, h(a))), t_3: h(f(h(a), a))$

$t_1 \Rightarrow h.f.*.*$

$t_2 \Rightarrow h.f.*.h.a$

$t_3 \Rightarrow h.f.h.a.a$

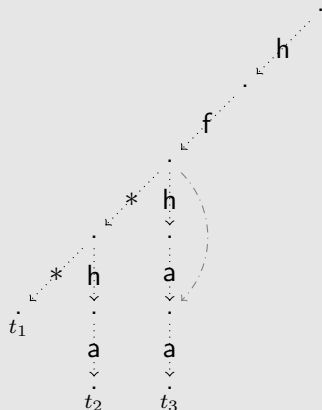


Retrieve

$$t_1: h(f(x, y)), t_2: h(f(x, h(a))), t_3: h(f(h(a), a))$$

$$h(f(x', a)) \Rightarrow h.f.*.a$$

$$u : h(f(x', a)) \mapsto \{ \quad \}$$

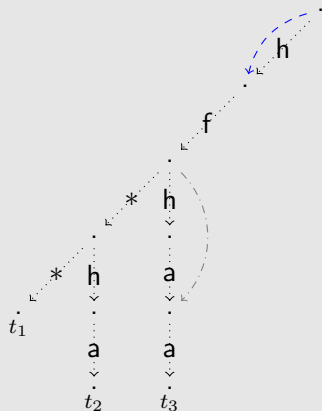


Retrieve

$$t_1: h(f(x, y)), t_2: h(f(x, h(a))), t_3: h(f(h(a), a))$$

$$h(f(x', a)) \Rightarrow h.f.*.a$$

$$u : h(f(x', a)) \mapsto \{ \quad \}$$

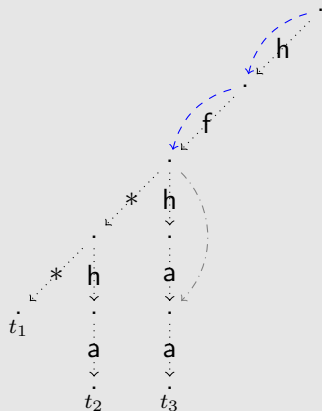


Retrieve

$$t_1: h(f(x, y)), t_2: h(f(x, h(a))), t_3: h(f(h(a), a))$$

$$h(f(x', a)) \Rightarrow h.f.*.a$$

$$u : h(f(x', a)) \mapsto \{ \quad \}$$

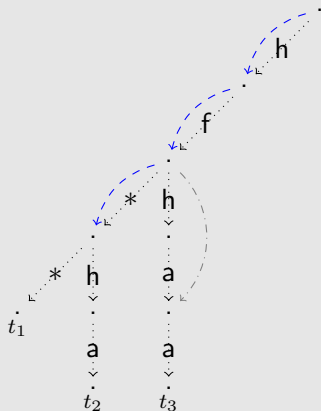


Retrieve

$$t_1: h(f(x, y)), t_2: h(f(x, h(a))), t_3: h(f(h(a), a))$$

$$h(f(x', a)) \Rightarrow h.f.*.a$$

$$u : h(f(x', a)) \mapsto \{ \quad \}$$

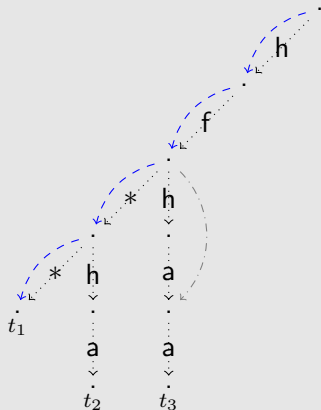


Retrieve

$$^{t_1:}h(f(x, y)), ^{t_2:}h(f(x, h(a))), ^{t_3:}h(f(h(a), a))$$

$$h(f(x', a)) \Rightarrow h.f.*.a$$

$$u : h(f(x', \mathbf{a})) \mapsto \{t_1, \quad \}$$

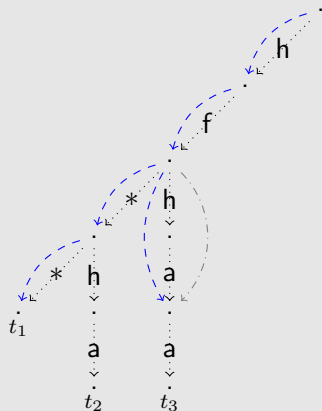


Retrieve

$$t_1: h(f(x, y)), t_2: h(f(x, h(a))), t_3: h(f(h(a), a))$$

$$h(f(x', a)) \Rightarrow h.f.*.a$$

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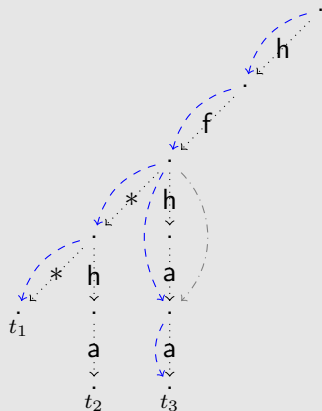


Retrieve

$$t_1: h(f(x, y)), t_2: h(f(x, h(a))), t_3: h(f(h(a), a))$$

$$h(f(x', a)) \Rightarrow h.f.*.a$$

$$u : h(f(x', a)) \mapsto \{t_1, t_3\}$$



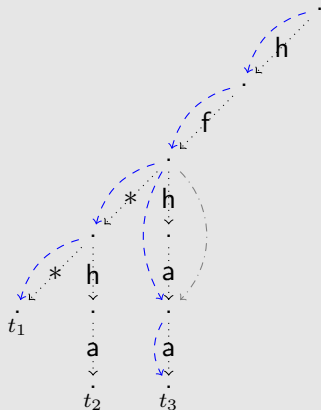
Retrieve

$$^{t_1:}h(f(x, y)), ^{t_2:}h(f(x, h(a))), ^{t_3:}h(f(h(a), a))$$

$$h(f(x', a)) \Rightarrow h.f.*.a$$

$$u : h(f(x', \mathbf{a})) \mapsto \{t_1, t_3\}$$

$$i : \mathbf{h}(\mathbf{f}(x', \mathbf{a})) \mapsto \{t_3\}$$



Retrieve

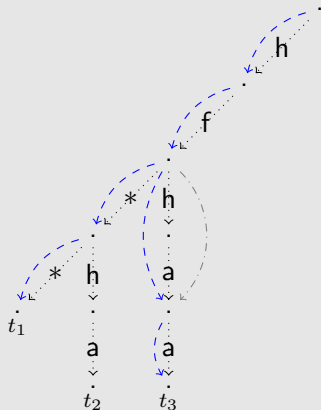
$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, h(a))), ^{t_3}h(f(h(a), a))$$

$$h(f(x', a)) \Rightarrow h.f.*.a$$

$$u : h(f(x', a)) \mapsto \{t_1, t_3\}$$

$$i : h(f(x', a)) \mapsto \{t_3\}$$

$$g : h(f(x', a)) \mapsto \{t_1\}$$



Retrieve

$$^{t_1:}h(f(x, y)), ^{t_2:}h(f(x, h(a))), ^{t_3:}h(f(h(a), a))$$

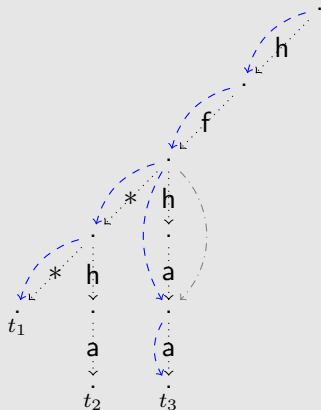
$$h(f(x', a)) \Rightarrow h.f.*.a$$

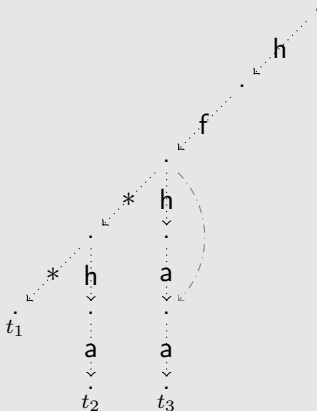
$$u : h(f(x', \mathbf{a})) \mapsto \{t_1, t_3\}$$

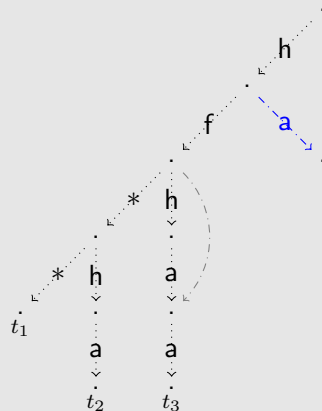
$$i : h(f(x', \mathbf{a})) \mapsto \{t_3\}$$

$$g : h(f(x', a)) \mapsto \{t_1\}$$

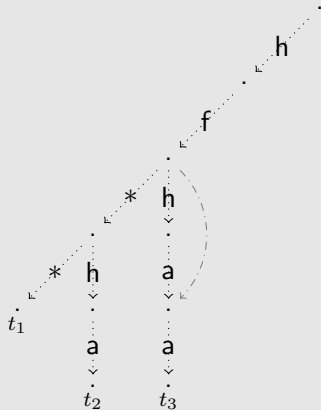
$$v : \mathbf{h}(\mathbf{f}(x', \mathbf{a})) \mapsto \{ \}$$

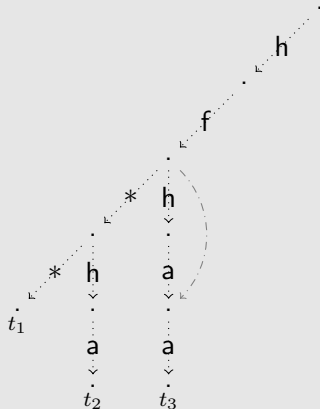
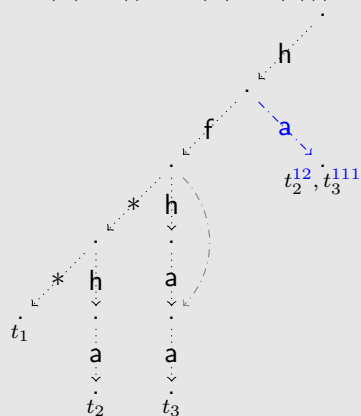


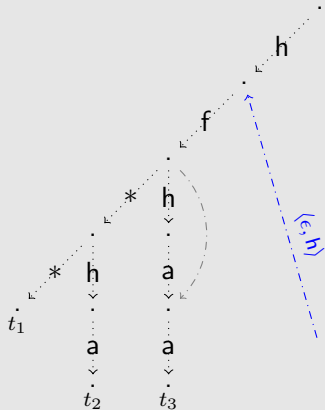
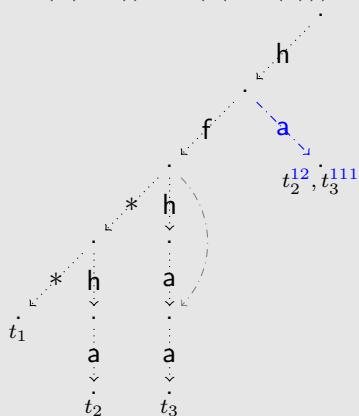
$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, h(a))), ^{t_3}h(f(h(a), a))$$


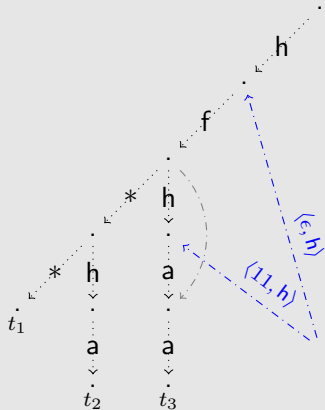
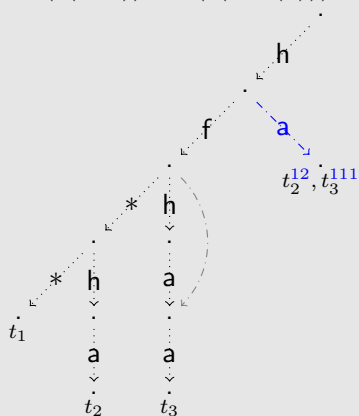
$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, h(a))), ^{t_3}h(f(h(a), a))$$


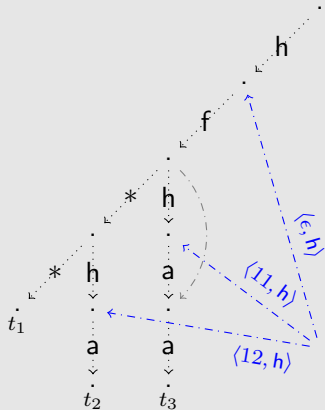
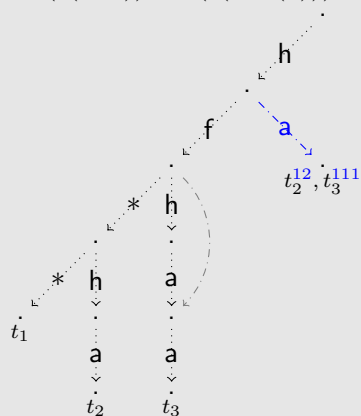
$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, h(a))), ^{t_3}h(f(h(a), a))$$


$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, h(a))), ^{t_3}h(f(h(a), a))$$


$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, h(a))), ^{t_3}h(f(h(a), a))$$


$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, h(a))), ^{t_3}h(f(h(a), a))$$


$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, h(a))), ^{t_3}h(f(h(a), a))$$


$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, h(a))), ^{t_3}h(f(h(a), a))$$


Substitution Trees

Build

$t_1: h(f(x, y)), t_2: h(f(x, h(a))), t_3: h(f(h(a), a)), t_4: h(f(a, a))$

Substitution Trees

Build

$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, h(a))), ^{t_3}h(f(h(a), a)), ^{t_4}h(f(a, a)))$$


$$*_0 \mapsto h(*_1)$$

Substitution Trees

Build

$t_1: h(f(x, y)), t_2: h(f(x, h(a))), t_3: h(f(h(a), a)), t_4: h(f(a, a))$

↓

$*_0 \mapsto h(*_1)$

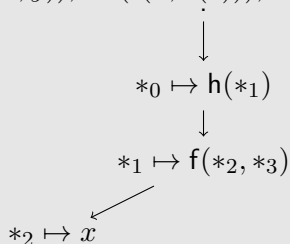
↓

$*_1 \mapsto f(*_2, *_3)$

Substitution Trees

Build

$t_1: h(f(x, y)), t_2: h(f(x, h(a))), t_3: h(f(h(a), a)), t_4: h(f(a, a))$



Substitution Trees

Build

$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, h(a))), ^{t_3}h(f(h(a), a)), ^{t_4}h(f(a, a)))$$

$$\downarrow$$

$$*_0 \mapsto h(*_1)$$

$$\downarrow$$

$$*_1 \mapsto f(*_2, *_3)$$

$$\swarrow$$

$$*_2 \mapsto x$$

$$\swarrow$$

$$*_3 \mapsto y$$

$$t_1$$

Substitution Trees

Build

$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, h(a))), ^{t_3}h(f(h(a), a)), ^{t_4}h(f(a, a)))$$

$$\downarrow$$

$$*0 \mapsto h(*1)$$

$$\downarrow$$

$$*1 \mapsto f(*2, *3)$$

$$\swarrow \searrow$$

$$*2 \mapsto x$$

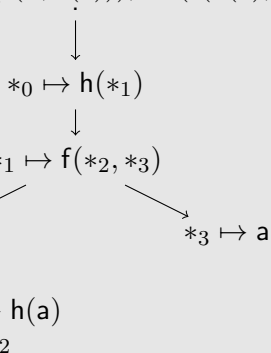
$$\swarrow \searrow$$

$$*3 \mapsto y \quad *3 \mapsto h(a)$$

$$t_1 \quad t_2$$

Substitution Trees

Build

$$^{t_1}h(f(x, y)), ^{t_2}h(f(x, h(a))), ^{t_3}h(f(h(a), a)), ^{t_4}h(f(a, a)))$$


Substitution Trees

Build

$$t_1: h(f(x, y)), t_2: h(f(x, h(a))), t_3: h(f(h(a), a)), t_4: h(f(a, a))$$

$$\downarrow$$

$$*0 \mapsto h(*1)$$

$$\downarrow$$

$$*1 \mapsto f(*2, *3)$$

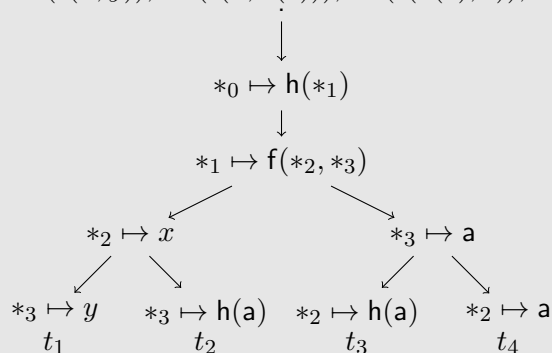
$$\swarrow \quad \searrow$$

$$*2 \mapsto x \quad *3 \mapsto a$$

$$\begin{array}{ccc} \swarrow & \searrow & \swarrow \\ *3 \mapsto y & *3 \mapsto h(a) & *2 \mapsto h(a) \\ t_1 & t_2 & t_3 \end{array}$$

Substitution Trees

Build

$$t_1: h(f(x, y)), t_2: h(f(x, h(a))), t_3: h(f(h(a), a)), t_4: h(f(a, a))$$


TPTP/Problems/HWV/HWV134-1.p

2 332 428 formulae, 6 570 884 literals

TPTP/Problems/HWV/HWV134-1.p

2 332 428 formulae, 6 570 884 literals

checking 1000 new literals	sequential	path	speed
afterwards	search	index	up
(ℓ_1, ℓ_2)			
$A, \neg B$			

TPTP/Problems/HWV/HWV134-1.p

2 332 428 formulae, 6 570 884 literals

checking 1000 new literals	sequential	path	speed
afterwards (ℓ_1, ℓ_2) $A, \neg B$	search	index	up
1 000 500 000 761	726ms	70ms	10

TPTP/Problems/HWV/HWV134-1.p

2 332 428 formulae, 6 570 884 literals

checking afterwards	1000 new literals (ℓ_1, ℓ_2)	$A, \neg B$	sequential search	path index	speed up
1 000	500 000	761	726ms	70ms	10
2 000	1 500 000	812	2s	69ms	29

TPTP/Problems/HWV/HWV134-1.p

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1 000	500 000	761	726ms	70ms	10
2 000	1 500 000	812	2s	69ms	29
4 000	3 500 000	723	4s	75ms	53

TPTP/Problems/HWV/HWV134-1.p

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checking 1000 new literals afterwards	(ℓ_1, ℓ_2)	$A, \neg B$	sequential search	path index	speed up
1 000	500 000	761	726ms	70ms	10
2 000	1 500 000	812	2s	69ms	29
4 000	3 500 000	723	4s	75ms	53
8 000	7 500 000	433	9s	125ms	72

TPTP/Problems/HWV/HWV134-1.p

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1 000	500 000	761	726ms	70ms	10
2 000	1 500 000	812	2s	69ms	29
4 000	3 500 000	723	4s	75ms	53
8 000	7 500 000	433	9s	125ms	72
16 000	15 500 000	742	21s	221ms	95

TPTP/Problems/HWV/HWV134-1.p

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1 000	500 000	761	726ms	70ms	10
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4 000	3 500 000	723	4s	75ms	53
8 000	7 500 000	433	9s	125ms	72
16 000	15 500 000	742	21s	221ms	95
32 000	31 500 000	592	40s	489ms	81

TPTP/Problems/HWV/HWV134-1.p

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8 000	7 500 000	433	9s	125ms	72
16 000	15 500 000	742	21s	221ms	95
32 000	31 500 000	592	40s	489ms	81
64 000	63 500 000	1 167	80s	697ms	114

TPTP/Problems/HWV/HWV134-1.p

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1 000	500 000	761	726ms	70ms	10
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4 000	3 500 000	723	4s	75ms	53
8 000	7 500 000	433	9s	125ms	72
16 000	15 500 000	742	21s	221ms	95
32 000	31 500 000	592	40s	489ms	81
64 000	63 500 000	1 167	80s	697ms	114
128 000	127 500 000	1 479	160s	13s	12

TPTP/Problems/HWV/HWV134-1.p

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16 000	15 500 000	742	21s	221ms	95
32 000	31 500 000	592	40s	489ms	81
64 000	63 500 000	1 167	80s	697ms	114
128 000	127 500 000	1 479	160s	13s	12
256 000	255 500 000	1 097	320s	440s	<1

TPTP/Problems/HWV/HWV134-1.p

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64 000	63 500 000	1 167	80s	697ms	114
128 000	127 500 000	1 479	160s	13s	12
256 000	255 500 000	1 097	320s	440s	<1
512 000	511 500 000	1 440	640s	348s	<2

TPTP/Problems/HWV/HWV134-1.p

2 332 428 formulae, 6 570 884 literals

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64 000	63 500 000	1 167	80s	697ms	114
128 000	127 500 000	1 479	160s	13s	12
256 000	255 500 000	1 097	320s	440s	<1
512 000	511 500 000	1 440	640s	348s	<2
1 024 000	1023 500 000	1 534	1280s	330s	<4