Handbook USM

Initial Setup and Definitions

```
typedef long long ll;
typedef vector< int > vi;
typedef vector< vi > vvi;
typedef pair< int, int > pii;
typedef vector< pii > vpii;
typedef vector< vpii > vvpii;
```

Fast Input ios_base::sync_with_stdio(false); cin.tie(NULL); cout.setf(ios::fixed); cout.precision(4);

#define gcd(a, b) __gcd(a, b) #define lcm(a, b) gcd(a, b) ? (a / gcd(a, b) * b) : 0 const double PI = 3.1415926535897932384626433832795; const ll PRIME_BASE = (1 << 61) - 1;

Strings

```
Rolling Hashing
class RollingHashing {
 11 p, m, ns;
 vector< 11 > pows, hash;
 RollingHashing(string s) {
   // if WA then other p and other m
   // if still WA then double hashing
   // if still WA maybe is not the answer RH
   p = 31: m = 1e9 + 7:
   ns = s.size();
   pows.resize(ns + 2):
   for(int i = 1; i < ns + 2; i++)
     pows[i] = (pows[i - 1] * p) % m;
   hash.resize(ns + 1);
   hash[0] = 0;
   for(int i = 1; i <= ns; i++) {</pre>
     11 char_to_num = S[i - 1] - 'a' + 1;
     ll prev hash = hash[i - 1]:
     hash[i] = ((char_to_num * pows[i - 1]) % m + prev_hash)
    % m;
 11 compute_hashing(ll i, ll j) {
   return (hash[j] - hash[i] + m) % m;
```

Algorithms

```
Binary Pow

11 binpow(11 a, 11 b, 11 mod) {
    a % = m;
    11 res = 1;
    while (b > 0) {
        if (b & 1)
            res = (res * a) % mod;
        a = (a * a) % mod;
        b >>= 1;
    }
    return res;
}
```

Segment Tree

```
template <class T>
stuct SegmenTree {
 int N;
  vector<T> ST;
  T (*merge)(T, T);
  void build(int n, int 1, int r, vector<T> &vs) {
    if(1 == r) ST[n] = vs[1]:
    else {
      build(n * 2, 1, (r + 1) / 2, vs);
      build(n * 2 + 1, (r + 1) / 2 + 1, vs);
      ST[n] = merge(ST[n * 2], ST[n * 2 + 1]);
  SegmentTree(vector<T> &vs, T (*m)(T a, T b)) {
    merge = m;
    N = vs.size();
    ST.resize(4 * N + 3);
    build(1, 0, N - 1, vs);
 T query(int i, int j) {
   return query(0, N - 1, 1, i, j);
 T query(int 1, int r, int n, int i, int j) {
    if(1 >= i && r <= j) return ST[n];</pre>
    int mid = (r + 1) / 2;
    if(mid < i) return query(mid + 1, r, n*2+1, i, j);</pre>
    if(mid >= j) return query(1, mid, n*2, i, j);
    return merge(query(1, mid, n * 2, i, j),
                 query(mid + 1, r, n * 2 + 1, i, j));
  void update(int pos, T val) {
    update(0, N - 1, 1, pos, val);
  void update(int 1, int r, int n, int pos, T val) {
    if(r < pos || pos < 1) return;</pre>
    if(1 == r) ST[n] = val;
    else {
      int mid = (r + 1) / 2;
      update(1, mid, n * 2, pos, val);
      update(mid + 1, r, n * 2 + 1, pos, val);
      ST[n] = merge(ST[n * 2], ST[n * 2 + 1]);
 }
};
```

Segment Tree Lazy

```
template <class T>
struct SegmentTree {
 int N; vector<T> ST, lazy;
  vector<bool> bit; T (*merge)(T, T);
  void build(int n, int 1, int r, vector<T> &vs) {
   if(1 == r) ST[n] = vs[1];
    else {
     build(2 * n, 1, (r + 1) / 2, vs):
     build(2 * n + 1, (r + 1) / 2 + 1, r, vs);
     ST[n] = merge(ST[n * 2], ST[n * 2 + 1]);
 SegmentTree(vector<T> &vs, T (*m)(T a, T b)) {
   merge = m; N = vs.size();
   ST.resize(4 * N + 3); lazy.assign(4 * N + 3, T());
   bit.assign(4 * N + 3, false); build(1, 0, N - 1, vs);
  void push(int n, int i, int j) {
   if(bit[n]) {
     ST[n] += lazv[n];
     if(i != j) {
       lazy[2 * n] += lazy[n];
       lazv[2 * n + 1] += lazv[n];
       bit[2 * n] = 1; bit[2 * n + 1] = 1;
     lazy[n] = T(); bit[n] = 0;
   }
  void apply(int n, int i, int j, T val) {
   ST[n] += val;
   if(i != j) {
     lazy[2 * n] += val;
     lazv[2 * n + 1] += val;
     bit[2 * n] = 1; bit[2 * n + 1] = 1;
 T query(int i, int j) {
   return query(0, N - 1, 1, i, j); }
 T query(int 1, int r, int n, int i, int j) {
   push(n, 1, r);
   if(i <= 1 && r <= j) return ST[n];
   int mid = (r + 1) / 2;
   if(mid<i||j<1) return query(mid + 1, r, 2 * n + 1, i, j);</pre>
   if (mid >= j \mid \mid r < i) return query(1, mid, 2 * n, i, j);
   return merge(query(1, mid, 2 * n, i, j),
                query(mid + 1, r, 2 * n + 1, i, j));
  void update(int i, int j, T val) {
   update(0, N - 1, 1, i, j, val); }
  void update(int l,int r,int n,int i,int j, T val) {
   push(n, 1, r);
    if(r < i || j < 1) return;</pre>
   if(i <= 1 && r <= j) {
     apply(n, 1, r, val); return;
   int mid = (r + 1) / 2;
   update(1, mid, 2 * n, i, j, val);
   update(mid + 1, r, 2 * n + 1, i, j, val);
   ST[n] = merge(ST[2 * n], ST[2 * n + 1]);
```

Union Find struct UnionFind { vector<int> p, r; UnionFind(int n) { r.assign(n+1, 0); p.assign(n+1, 0); for(int i=1; i<=n; i++) p[i] = i;</pre> int findSet(int i) { return (p[i] == i)? i:(p[i] = findSet(p[i])); bool isSameSet(int i, int j) { return findSet(i) == findSet(j); void unionSet(int i, int j) { if (!isSameSet(i, j)) { int x = findSet(i), y = findSet(j); if (r[x] > r[y]) p[y] = x;else { p[x] = y;if (r[x] == r[y]) r[y]++;

Maths

```
struct Fraction {
    11 numerator, denominator;
    Fraction(11 a, 11 b){
        numerator = a, denominator = b;
    }
    Fraction simplify(Fraction f){
        11 g = gcd(f.numerator, f.denominator);
        return Fraction(f.numerator/g, f.denominator/g);
    }
    Fraction add(Fraction f){
        11 1 = 1cm(denominator, f.denominator);
        numerator *= (1/denominator);
        numerator += f.numerator * (1/f.denominator);
        return simplify(Fraction(numerator, 1));
    }
};
```