

**Control of Mobile Robots**  
**Project work**  
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## Instructions

Each student should upload the project to WeBeep folder “Assignments/Project work”, at least 3 working days before the date of the exam call, as a compressed zip file named “studentID\_surname.name.zip”, including:

- a PDF file, written in English or in Italian, answering to the questions (see below);
- a ROS workspace including all the code used to answer the questions.

If running a launch file or a script no results, or results that are different from the ones reported in the PDF file are generated, the project work gets zero points (projects are verified using ROS Melodic).

The project work can be submitted only once for each academic year. The mark obtained with the first submission is valid for all the academic year and cannot be changed submitting another solution (even in the case of zero points).

## Problem

Consider a car-like robot simulated using its single-track dynamic model, with linear or Fiala tyre model. The parameters that characterise the robot are:

- mass  $m$ , given in the parameter table;
- distance of the center of gravity from the front axle  $a$ , 0.14 m;
- distance of the center of gravity from the rear axle  $b$ , 0.12 m;
- ground friction coefficient  $\mu$ , 0.385;
- front wheel cornering stiffness  $C_{\alpha_f}$ , 50 N/rad;
- rear wheel cornering stiffness  $C_{\alpha_r}$ , 120 N/rad;
- yaw inertia  $I_z$ , given in the parameter table.

Set up a ROS package “car\_simulator”, based on Boost Odeint library, to simulate the robot.

The package should include:

- a ROS node that simulates the robot;
- a ROS node that allows to feed the simulator with simple (e.g., step) commands to test the model behaviour;
- a yaml file including model parameters;
- a launch file to run the simulator and the test node;
- a Python or MATLAB script to plot the test results starting from a bag file.

Set up a ROS package “car\_traj\_ctrl”, implementing a trajectory tracking controller.

The controller is composed of a feedback linearisation law, based on the bicycle kinematic model, and a PI trajectory tracking controller with velocity feed-forward (PI controller can be implemented using Forward Euler discretisation). The trajectory tracking controller should be tested using an 8-shaped trajectory, generated according to the following equations:

$$x = a \sin\left(\frac{2\pi}{T}t\right)$$
$$y = a \sin\left(\frac{2\pi}{T}t\right) \cos\left(\frac{2\pi}{T}t\right)$$

where  $a = 2$  m, and the value of  $T$  is given in the parameter table.

The package should include:

- a ROS node that implements the trajectory tracking controller, including reference trajectory generation;
- a yaml file including model parameters;
- a launch file to run the simulator and the trajectory tracking controller;
- a Python or MATLAB script to plot the test results starting from a bag file.

## Questions

1. Tune the trajectory tracking controller, selecting in an appropriate way the PI parameters and the sampling time, in order to achieve the best performance in terms of tracking error. Follow two steps: first use standard tools from control theory, then verify running simulations and varying the controller parameters if you can improve the first tuning. Report the values of:

- (a) the proportional gains  $K_{P_x}$ ,  $K_{P_y}$ ;
- (b) the integral time constants  $T_{I_x}$ ,  $T_{I_y}$ ;
- (c) the sampling time  $T_s$ ;

for both tuning steps, explaining the procedures you have followed to determine the controller requirements (crossover frequency, zero steady-state error, disturbance rejection, actuator effort limitation, etc.), and to tune the controller.

2. Report the results of a test of the trajectory tracking controller with the bicycle kinematic model. In particular, the following pictures should be reported:

- (a) a figure showing the reference and actual robot trajectory;
- (b) a figure showing the  $x$  and  $y$  components of the tracking error;
- (c) a figure showing the two control signals (velocity and steering);

together with the value of the maximum tracking error in the  $x$  and  $y$  directions.

Clearly and thoroughly comment the quality of the results, with particular reference to your tuning procedure or tuning requirements (are the results in accordance with the requirements? if no, why?).

3. Report the results of a test of the trajectory tracking controller with the single-track dynamic model, using a linear tyre model. In particular, the following pictures should be reported:

- (a) a figure showing the reference and actual robot trajectory;
- (b) a figure showing the  $x$  and  $y$  components of the tracking error;
- (c) a figure showing the two control signals (velocity and steering);

together with the value of the maximum tracking error in the  $x$  and  $y$  directions.

Clearly and thoroughly comment the quality of the results, with particular reference to your tuning procedure or tuning requirements (are the results in accordance with the requirements? if no, why?).

4. Report the results of a test of the trajectory tracking controller with the single-track dynamic model, using a Fiala tyre model and reducing of 25 % the value of  $T$ . In particular, the following pictures should be reported:

- (a) a figure showing the reference and actual robot trajectory;
- (b) a figure showing the  $x$  and  $y$  components of the tracking error;
- (c) a figure showing the two control signals (velocity and steering);
- (d) a figure showing the front and rear lateral tyre forces, and their maximum values;

together with the value of the maximum tracking error in the  $x$  and  $y$  directions.

Clearly and thoroughly compare these results with the ones you obtained in the previous question.

5. Report:

- (a) the values of the parameters  $m$ ,  $I_z$ , and  $T$ ;
- (b) the names of the launch files and Python or MATLAB scripts one have to run in order to generate the results required in questions 2, 3 and 4.

## Evaluation

The project work is evaluated in this way.

First, a check is done on the solution to verify that all the questions have been answered, and the instructions have been fulfilled. Second, the solution is evaluated considering:

- the correctness of the requirements, and how they are explained and motivated;
- the correctness of the tuning procedure, and how it is explained and motivated;
- the coherence between the requirements and the results.

Note that, the aim is not to necessarily achieve the best possible tuning, but a good tuning supported by reasonable and well-motivated requirements.

Every choice in the design and tuning process should be thoroughly motivated.