

Assignment 8

Due Tuesday, June 23rd, before class.

Prof. Dr. Sven Behnke Endenicher Allee 19a

- 8.1) Consider a frictionless pendulum with point-mass $m = 4$ kg and length $l = 3$ m. The state shall be described by angle θ (deviation from upright) and angular speed ω . Gravity will act on the pendulum. Control actions produce a torque around the pendulum hinge joint. Model the system behavior as a discrete-time system with a step size of 0.01 s! Compute the evolution of the state over 1 s for an initial state of $\theta_0 = 0.3$ rad and $\omega_0 = -1$ rad/s with zero control input.
- 4 points
- 8.2) Linearize the system around the standing still upright state ($\theta = 0, \omega = 0$). Compare the evolution of the state for this linearized system for the same initial state of $\theta_0 = 0.3$ rad and $\omega_0 = -1$ rad/s with zero control input.
- 4 points
- 8.3) Define a cost function which penalizes deviation from the standing still upright state and costs of control actions in a quadratic way.
- 2 points
- 8.4) Use the method of Linear Quadratic Regulation (LQR) to design a state-feedback policy which optimizes your cost function from 8.3) over a time horizon of 0.5 s, starting from the initial condition $\theta_0 = 0.3$ rad and $\omega_0 = -1$ rad/s.
- Show how the state evolves when the policy is applied.
- 8 points
- 8.5) Add zero-mean Gaussian noise with covariance matrix $\Sigma = \text{diag}(0.01, 0.04)$ to the state after each transition and compare how the state evolves when above policy is applied from the same initial conditions.
- 2 points